



# CSCI/ECEN 3302

## Introduction to Robotics

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# Administrivia

- Grades
  - Lab 2 is out
  - HW1 is out
  - Lab 3 will be out soon
  - Next in line is Lab 4
- Lab 5 and HW2 are going on

# Future Outlook

- Many extra-credit opportunities
  - Mid-semester review up later this week and open for one week
    - Entirely ANONYMOUS
    - If 90% of the enrolled students fill it out, everyone in the class will be awarded an **extra 10 points to their final cumulative homework score!!!**
- Maja Mataric AMA
- Robotics AMA
- After next week
  - We will start delving deeper in final project work!
  - You should start thinking about it – assignment coming up soon!



# Maja Mataric AMA

- Maja Mataric AMA
  - Video recording
  - Piazza discussion – extra credit for participating
  - Live AMA over Zoom



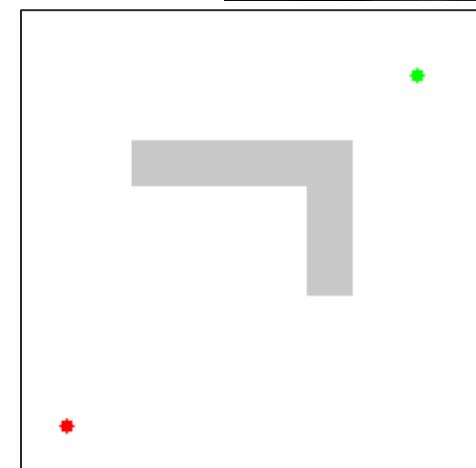
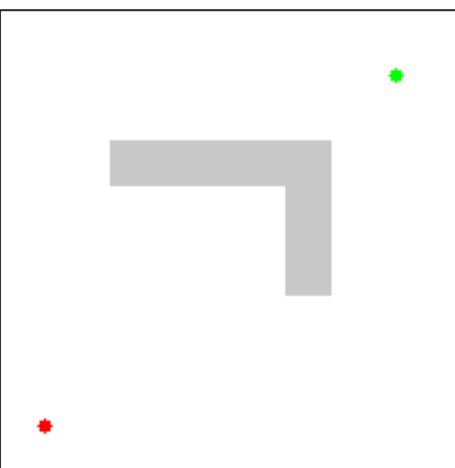
# Robotics AMA

- Not mandatory
- Not recorded
- Loosely structured – I may have some slides or not
- I (we) will happily answer any questions you might have about robotics, in particular how to chart your path to a robotics career

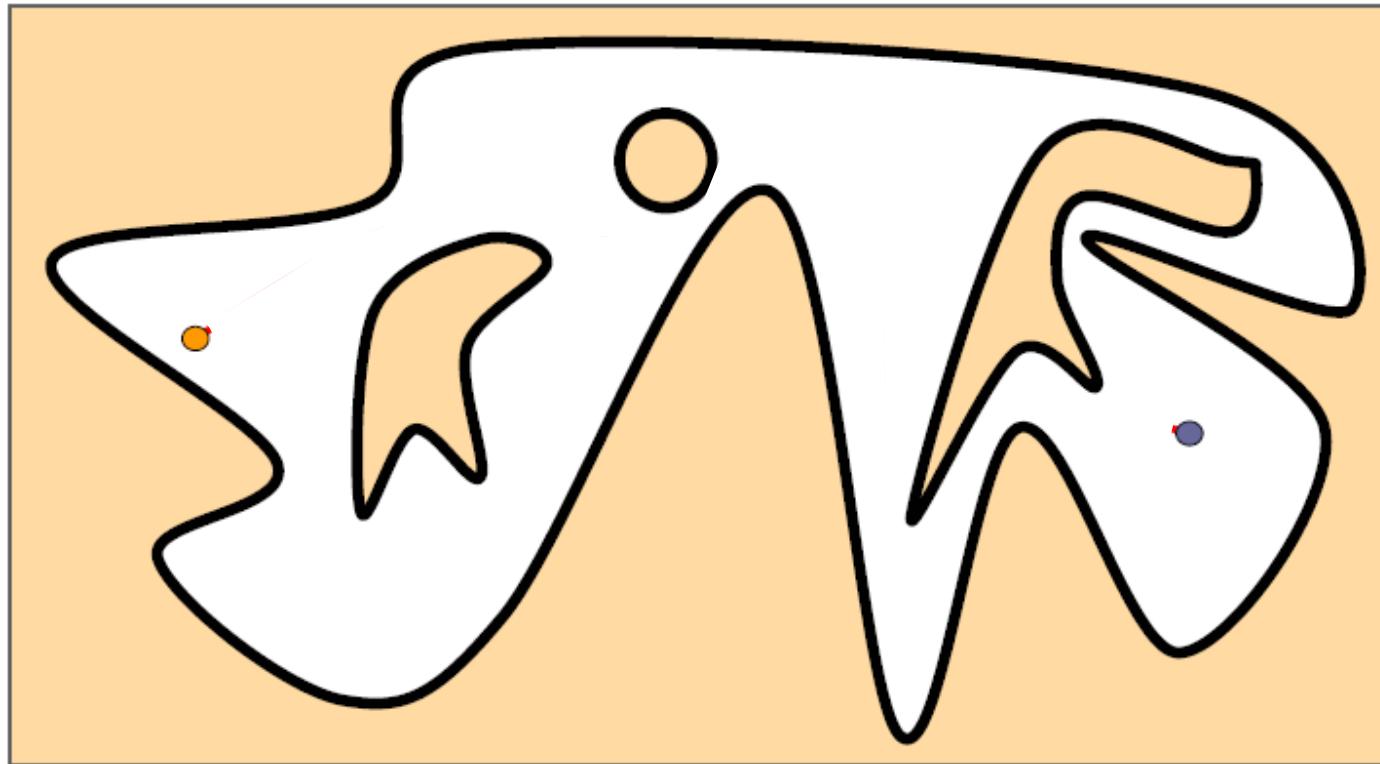
# Chapter 13

## RECAP

### Search Algorithms



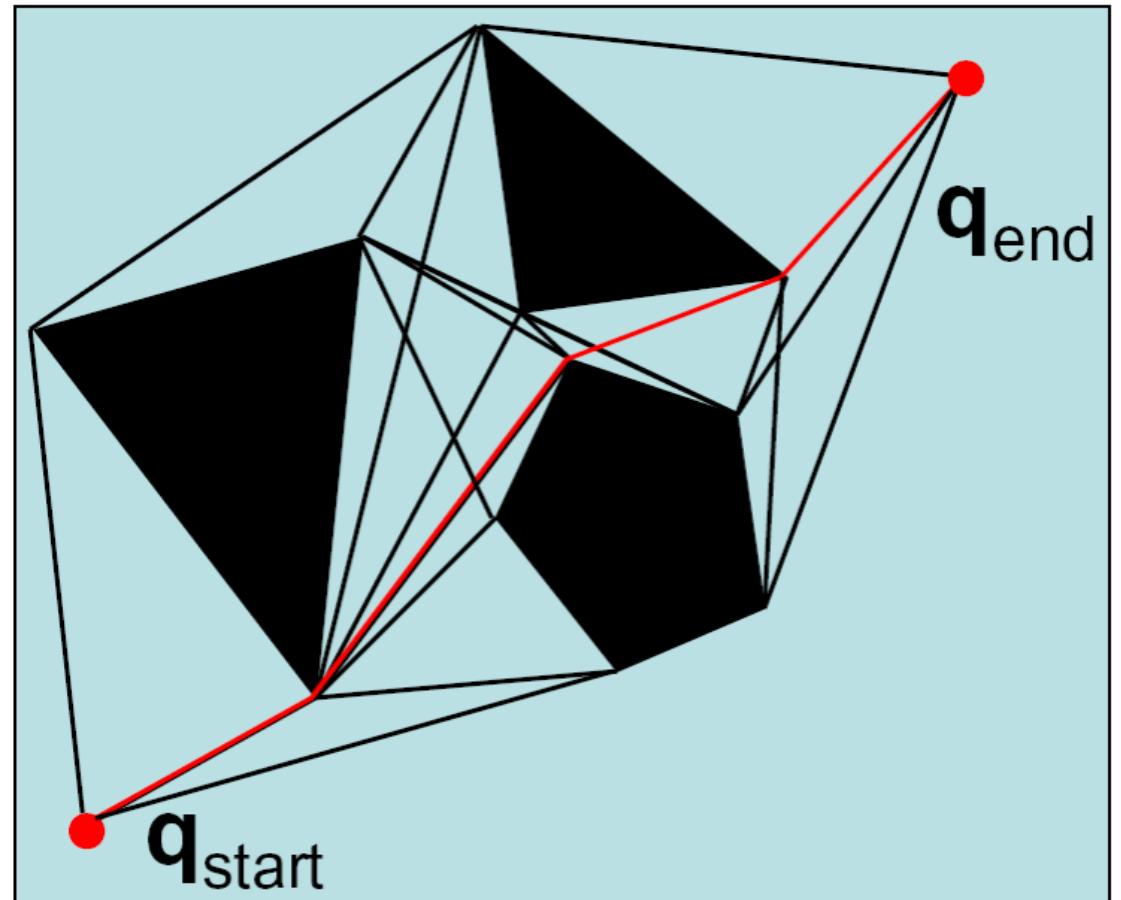
# Moving from Start to Goal state



- General **approach**: Reduce what amounts to an intractable problem in continuous C-space to a tractable problem in a discrete space.
- **Tools**:
  - Environment Representations
  - Search Algorithms

# Some Well-Known Representations

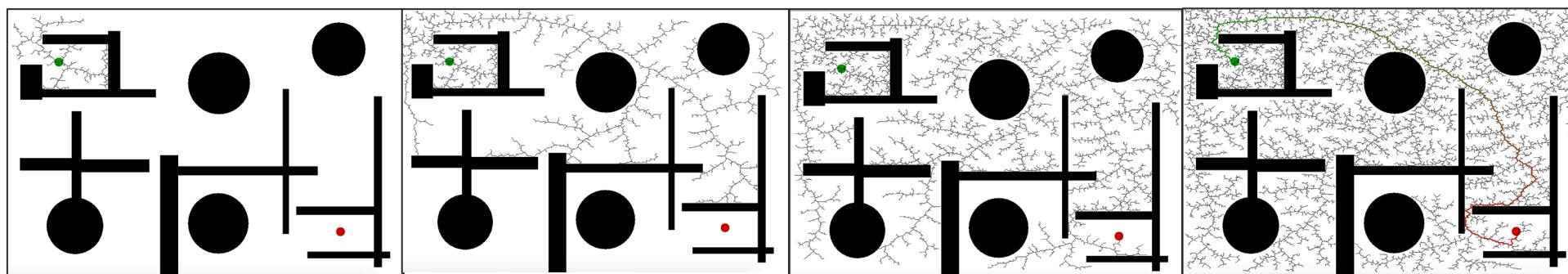
- Visibility Graphs
- Roadmap
- Cell Decomposition
- Potential Field



# How to sample points?

- Uniformly vs randomly
- Sample more near places with few neighbors
- Bias samples to exist near obstacles
- Use human-provided waypoints
- Something better?

Rapidly-exploring Random Trees (RRT)



# Rapidly Exploring Random Trees [RRT]

Basic idea:

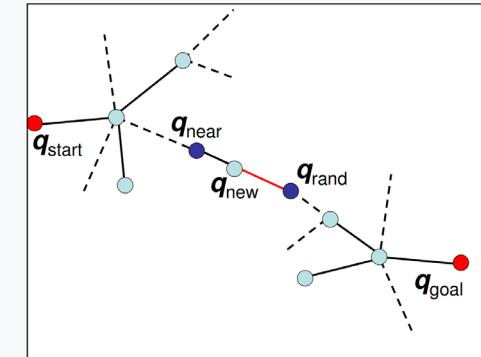
- Build up a tree through generating “next states” in the tree by executing **random controls**
- However: to ensure good coverage, we need something better than the above!!

# Rapidly-exploring Random Trees

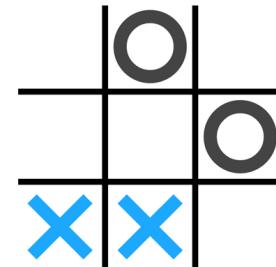
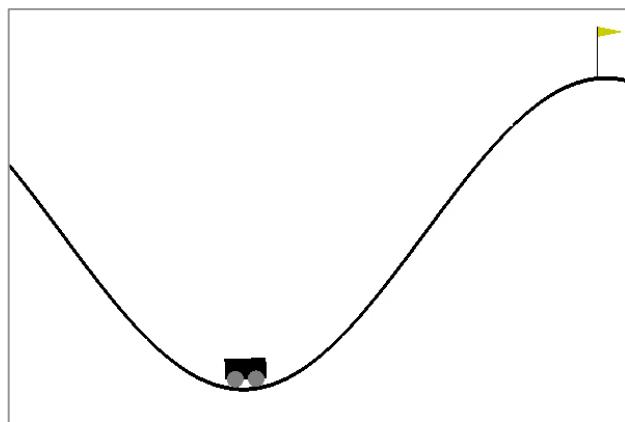
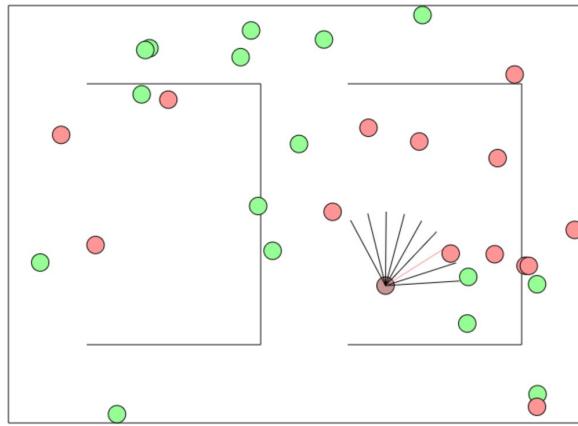
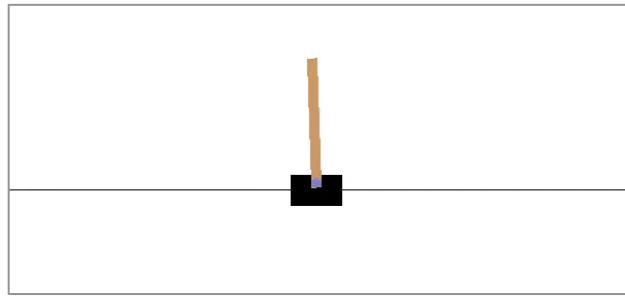
**Algorithm BuildRRT**

Input: Initial configuration  $q_{init}$ , number of vertices in RRT  $K$ , incremental distance  $\Delta q$   
Output: RRT graph  $G$

```
G.init( $q_{init}$ )
for  $k = 1$  to  $K$ 
     $q_{rand} \leftarrow \text{RAND\_CONF}()$ 
     $q_{near} \leftarrow \text{NEAREST\_VERTEX}(q_{rand}, G)$ 
     $q_{new} \leftarrow \text{NEW\_CONF}(q_{near}, q_{rand}, \Delta q)$ 
    G.add_vertex( $q_{new}$ )
    G.add_edge( $q_{near}$ ,  $q_{new}$ )
return G
```



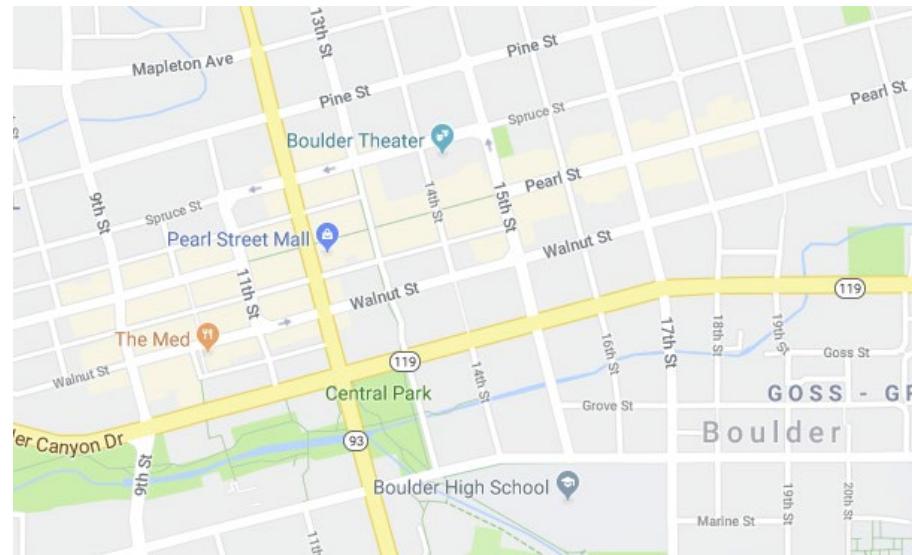
# State Representation is Critical



# Exercise: Building an Autonomous Car

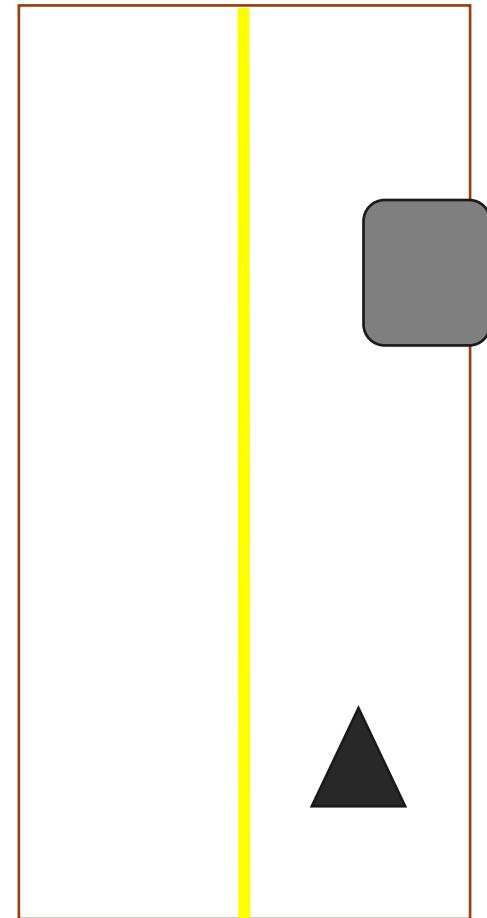
What do we need?

- World Representation
- Planning System



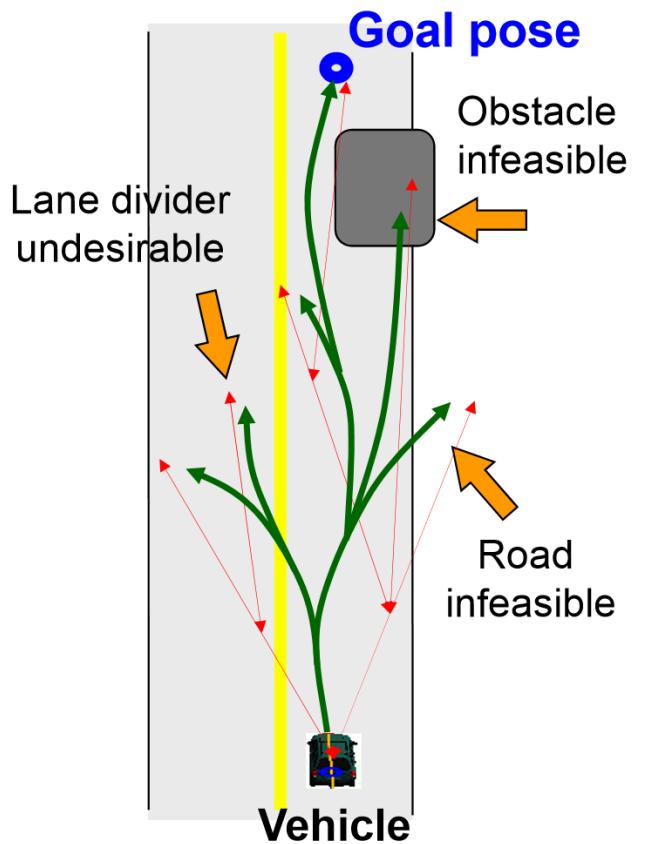
# Exercise: Building an Autonomous Car

How can we get our agent to  
accommodate obstacles?



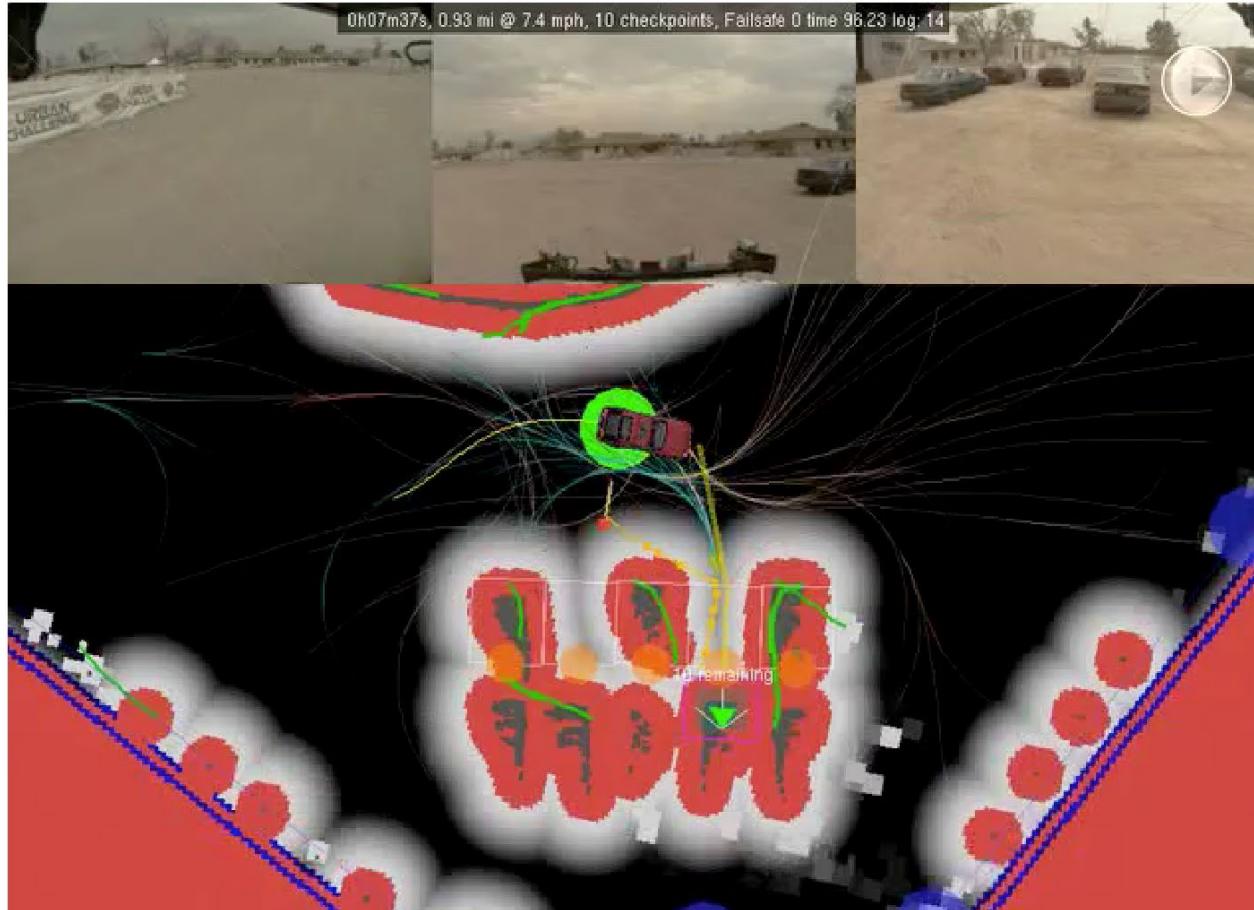
# Exercise: Building an Autonomous Car

- Tree of trajectories is grown by sampling configurations randomly
- Rapidly explores several configurations that the robot can reach
  - Many test trajectories generated (10k/s)
- Safety of any trajectory is “guaranteed” as of instantaneous world state at the time of trajectory generation
- Choose best one that reaches the goal, e.g.:
  - Maximizes minimum distance to obstacles
  - Minimizes path length
- Supports dynamic replanning; if traj becomes infeasible:
  - Choose another that is feasible
  - If none remain, then e-stop



# RRT for Autonomous Parking

[http://acl.mit.edu/papers/Kuwata\\_IROS08.pdf](http://acl.mit.edu/papers/Kuwata_IROS08.pdf)



**How can we make use of these representations?  
Search algorithms provide a way to find a path!**

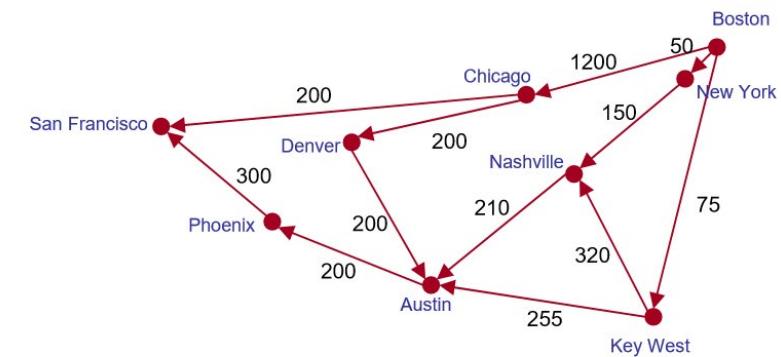
# Search Algorithms

Allow us to **use** the world representations:

- Basics
- Uniform Cost
- Informed Search

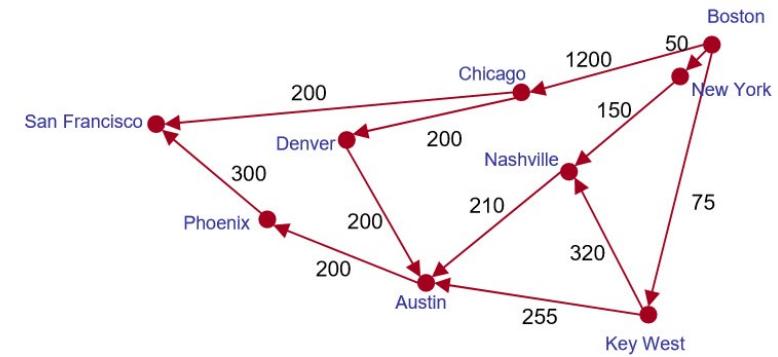
# Goal Formulation

- Well defined function that identifies both the **goal states** and the **conditions** under which to achieve it
  - E.g. “Fly from Boston to San Francisco”
- **Metrics** for optimality may depend on:
  - Least amount of money
  - Fewest number of transfers
  - Shortest amount of time in the air
  - Shortest amount of time in airports

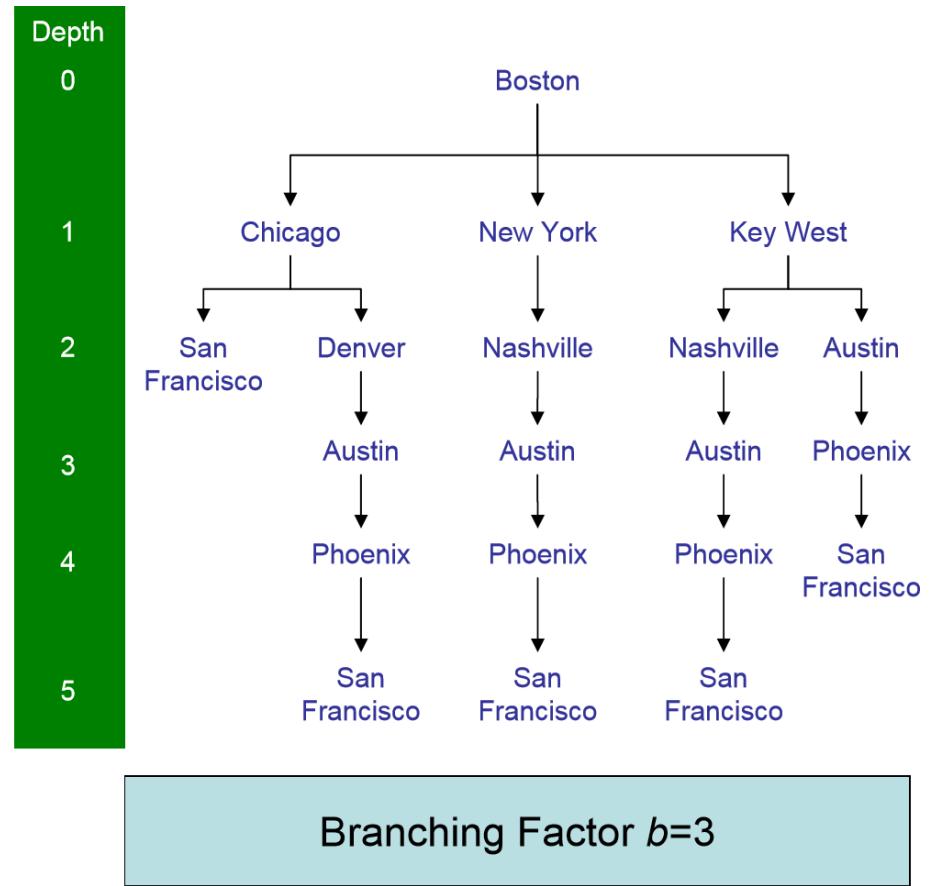
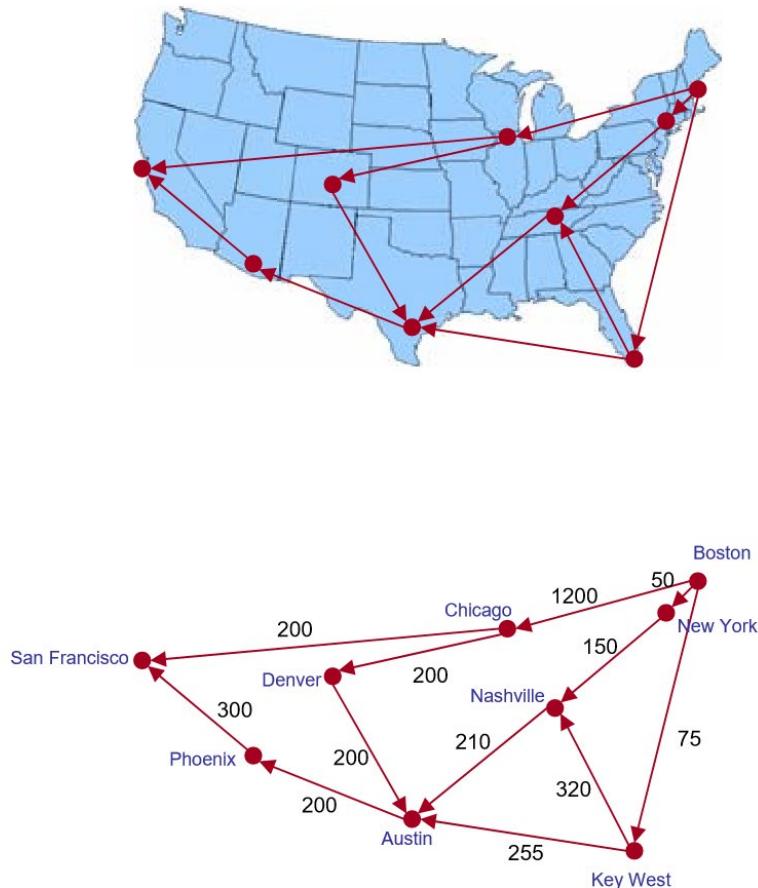


# Problem formulation

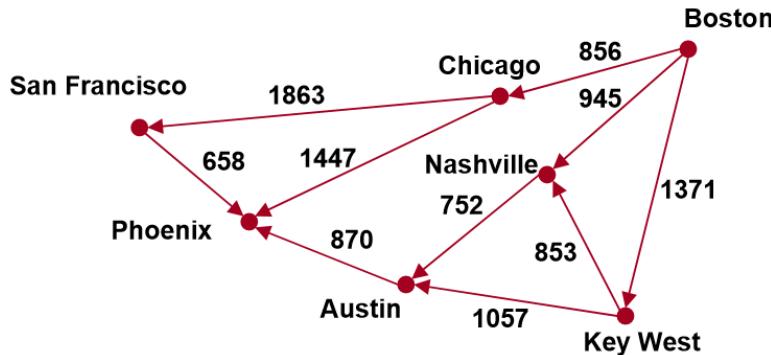
- **Well defined** problems
  - Fully observable
  - Deterministic
  - Discrete Set of possible actions
- **State Space:** the set of all states that are reachable from an initial state by any sequence of actions
- **Path:** sequence of actions leading from one state to another



# Search as a problem solving technique!!

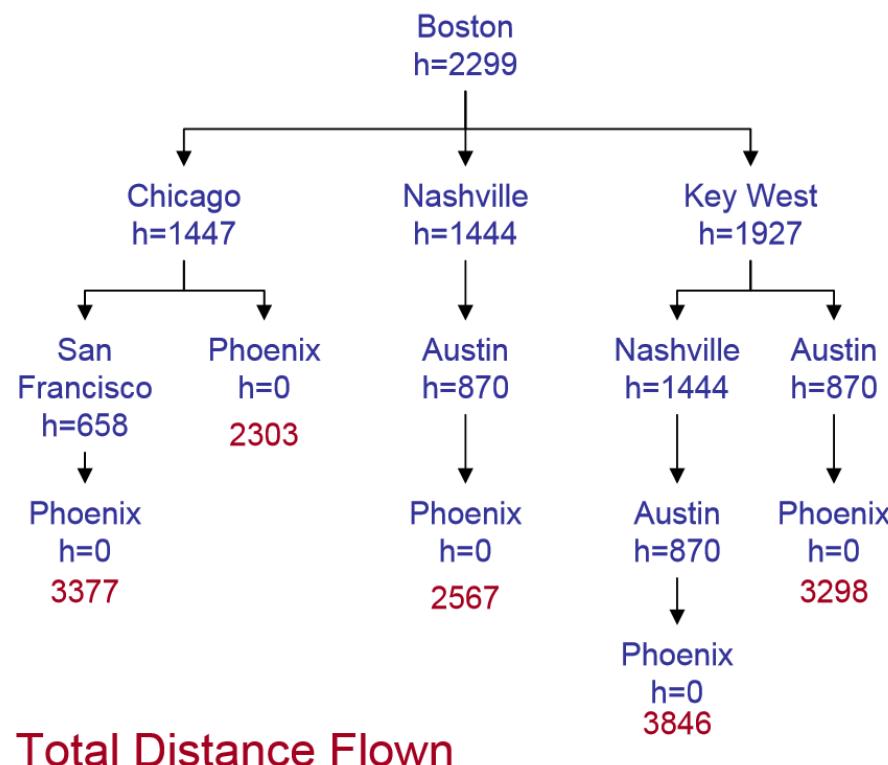


# Greedy Best-First-Search



	Straight Line Distance to Phoenix
Boston	2299
Chicago	1447
Nashville	1444
Key West	1927
Austin	870
San Francisco	658

- Minimize estimated cost to reach a goal (in this case, the distance to Phoenix)



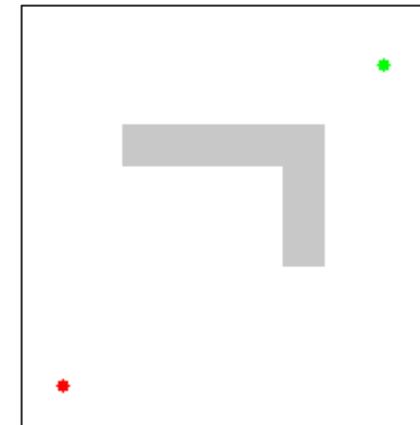
# Search Algorithms: Uniform Cost

## Dijkstra's Algorithm:

```
1 function Dijkstra(Graph, source):
2
3     create vertex set Q
4
5     for each vertex v in Graph:           // Initialization
6         dist[v] ← INFINITY               // Unknown distance from source to v
7         prev[v] ← UNDEFINED              // Previous node in optimal path from source
8         add v to Q                      // All nodes initially in Q (unvisited nodes)
9
10    dist[source] ← 0                   // Distance from source to source
11
12    while Q is not empty:
13        u ← vertex in Q with min dist[u] // Node with the least distance
14                                // will be selected first
15        remove u from Q
16
17        for each neighbor v of u:       // where v is still in Q.
18            alt ← dist[u] + length(u, v)
19            if alt < dist[v]:           // A shorter path to v has been found
20                dist[v] ← alt
21                prev[v] ← u
22
23    return dist[], prev[]
```

```
1 S ← empty sequence
2 u ← target
3 if prev[u] is defined or u = source:
4     while u is defined:
5         insert u at the beginning of S
6         u ← prev[u]
7
8     // Do something only if the vertex is reachable
9     // Construct the shortest path with a stack S
10    // Push the vertex onto the stack
11    // Traverse from target to source
```

Finds shortest paths  
between nodes in a graph



# Informed Search

- Dijkstra's Algorithm:
- Lots of wasted exploration!
- We usually know which two nodes we want to find a path between:
  - Why compute all distances from source?
- **Heuristic**: A function that ranks choices in a search algorithm to help choose how to branch/explore.

Finds shortest path  
between two nodes in  
a graph



# A\* Search Algorithm

Finds shortest path  
between two nodes in  
a graph

- Adds heuristic to Dijkstra's Algorithm

to **bias exploration!**

- Insight:

$$f(n) = g(n) + h(n)$$

- $f(n)$  = Cost so far + Est. cost to go

Admissible Heuristic: An **underestimate** of the shortest possible path from node n to the goal.

# A\* Search Algorithm

- Complete: Yes

(If an answer exists, this will find it)

- Optimal: Yes

(Returned answer will be the best possible)

- Optimally Efficient: Yes

(No algorithm with same heuristic will expand fewer nodes)

- Finding good admissible heuristics is challenging!

```
function reconstruct_path(cameFrom, current)
    total_path := [current]
    while current in cameFrom.Keys:
        current := cameFrom[current]
        total_path.append(current)
    return total_path
```

```
function A*(start, goal)
    // The set of nodes already evaluated
    closedSet := {}

    // The set of currently discovered nodes that are not evaluated yet.
    // Initially, only the start node is known.
    openSet := {start}

    // For each node, which node it can most efficiently be reached from.
    // If a node can be reached from many nodes, cameFrom will eventually contain the
    // most efficient previous step.
    cameFrom := the empty map

    // For each node, the cost of getting from the start node to that node.
    gScore := map with default value of Infinity
    gScore[start] := 0

    // For each node, the total cost of getting from the start node to the goal
    // by passing by that node. That value is partly known, partly heuristic.
    fScore := map with default value of Infinity
    fScore[start] := heuristic_cost_estimate(start, goal)

    while openSet is not empty
        current := the node in openSet having the lowest fScore[] value
        if current = goal
            return reconstruct_path(cameFrom, current)

        openSet.Remove(current)
        closedSet.Add(current)

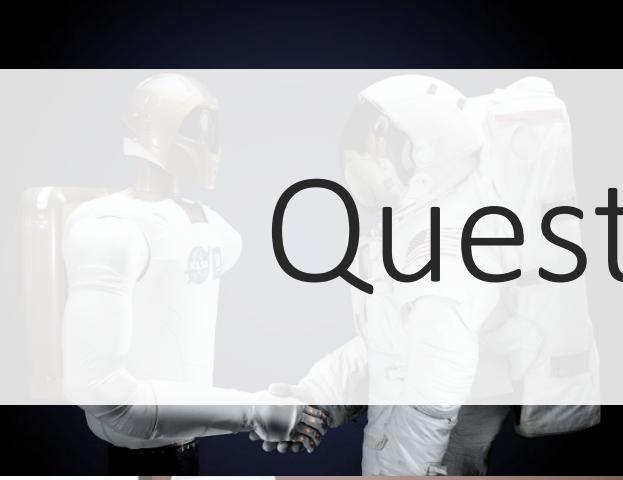
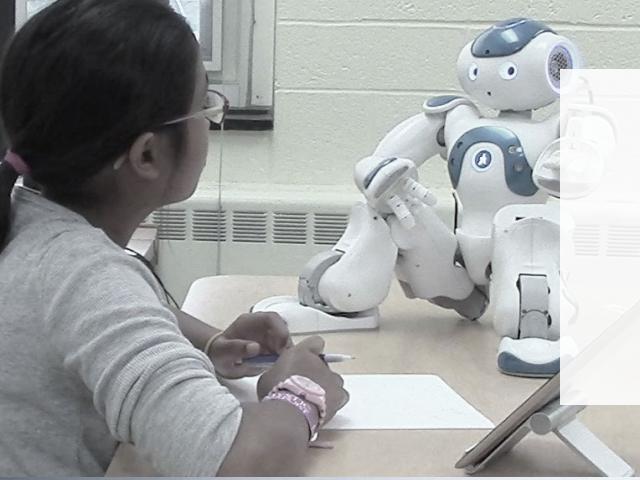
        for each neighbor of current
            if neighbor in closedSet
                continue      // Ignore the neighbor which is already evaluated.

            if neighbor not in openSet // Discover a new node
                openSet.Add(neighbor)

            // The distance from start to a neighbor
            tentative_gScore := gScore[current] + dist_between(current, neighbor)
            if tentative_gScore >= gScore[neighbor]
                continue      // This is not a better path.

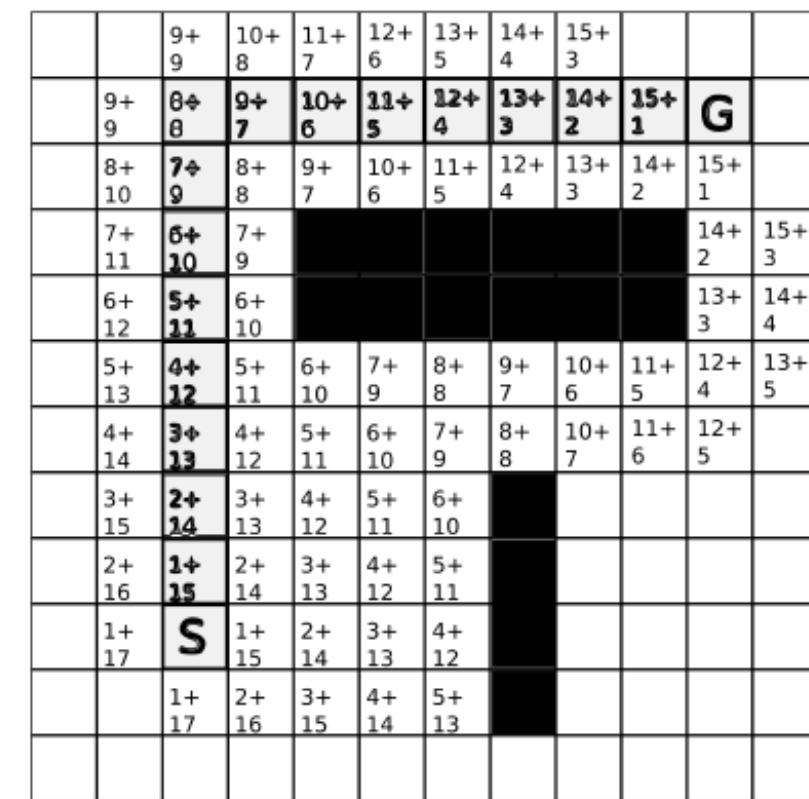
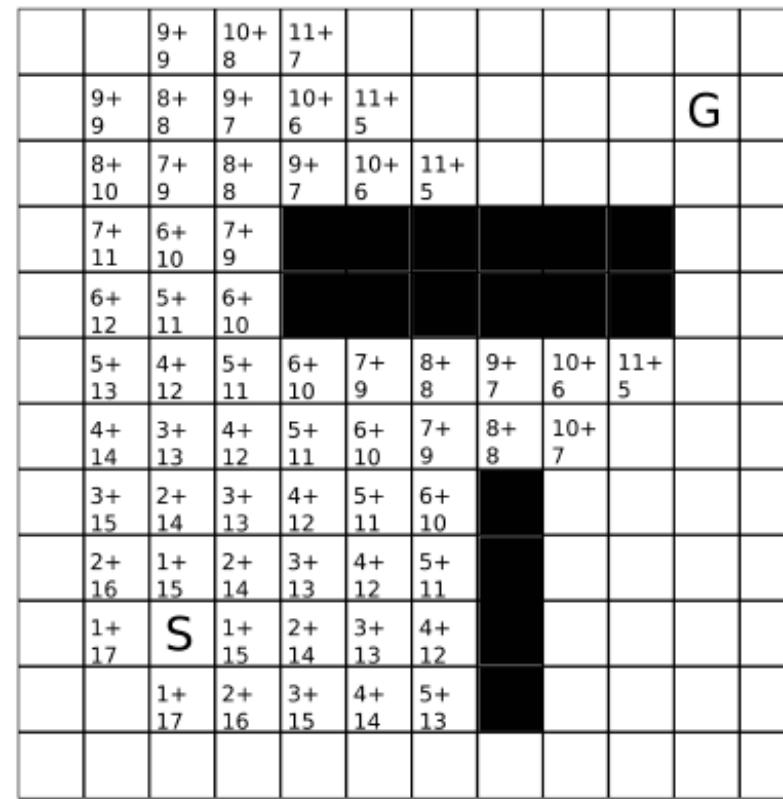
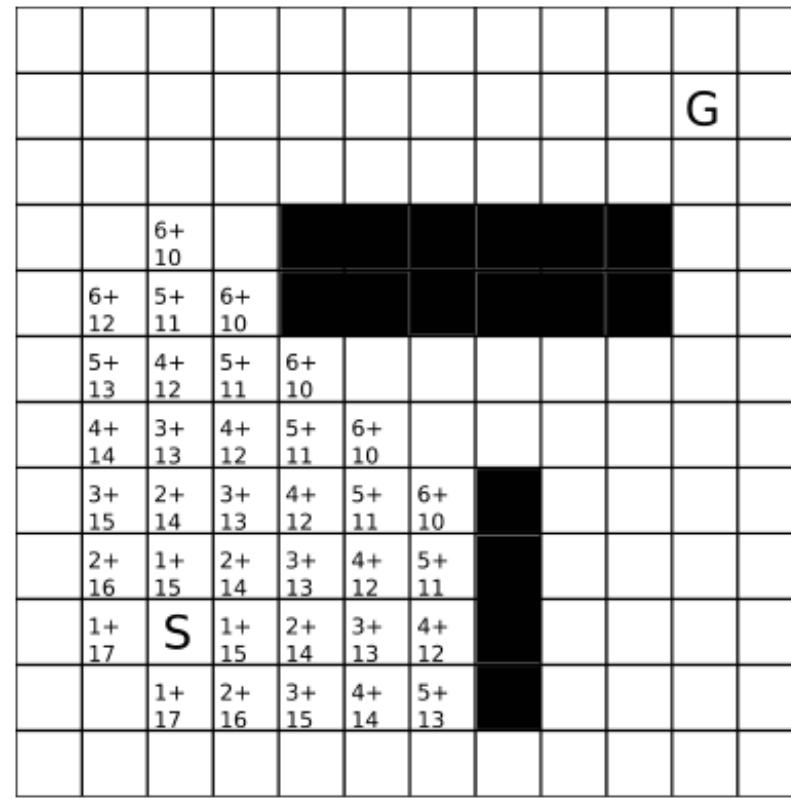
            // This path is the best until now. Record it!
            cameFrom[neighbor] := current
            gScore[neighbor] := tentative_gScore
            fScore[neighbor] := gScore[neighbor] + heuristic_cost_estimate(neighbor, goal)

    return failure
```

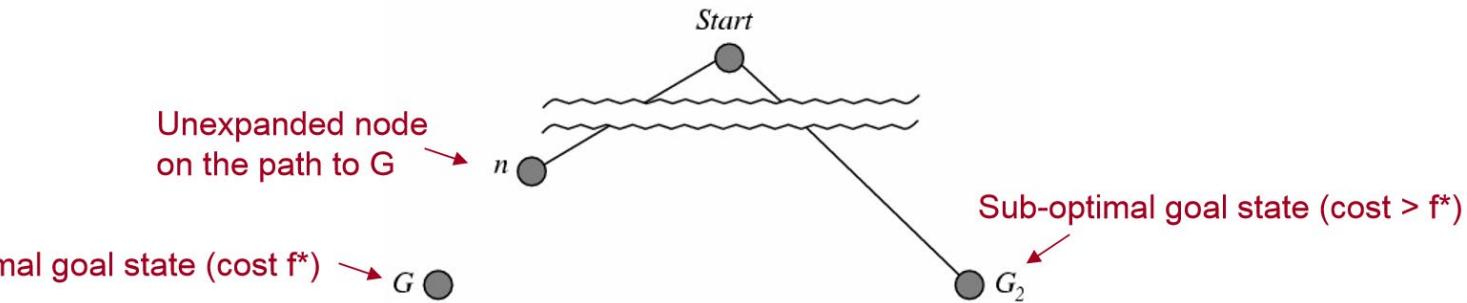


# Questions?

# Dijkstra plus directional heuristic: A\*



# Optimality of A\*



- Assume that  $G_2$  has been chosen for expansion over  $n$
- Because  $h$  is admissible:

$$f^* \geq f(n)$$

- If  $n$  is not chosen for expansion over  $G_2$ , we must have:

$$f(n) \geq f(G_2)$$

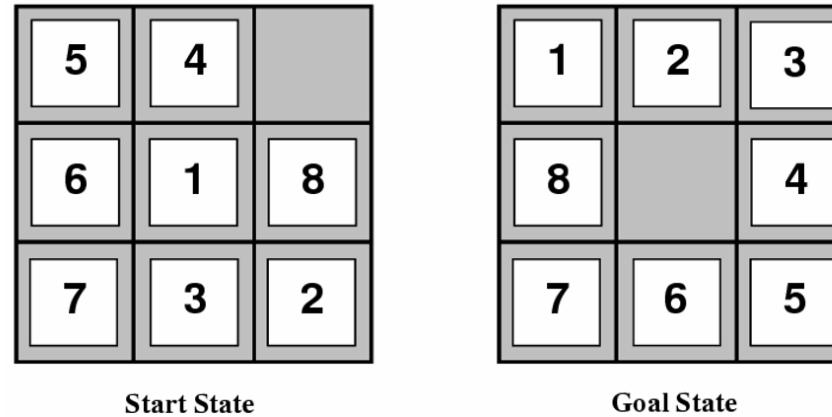
- Combining these, we get:

$$f^* \geq f(G_2)$$

- However, this violates the assertion that  $G_2$  is sub-optimal! Therefore,  $A^*$  never selects a sub-optimal goal for expansion



# Heuristic Selection



- Must be admissible (never over-estimate)
- Heuristics for the 8-Puzzle

# Heuristic Selection Effects

d	Search Cost			Effective Branching Factor		
	IDS	A*( $h_1$ )	A*( $h_2$ )	IDS	A*( $h_1$ )	A*( $h_2$ )
2	10	6	6	2.45	1.79	1.79
4	112	13	12	2.87	1.48	1.45
6	680	20	18	2.73	1.34	1.30
8	6384	39	25	2.80	1.33	1.24
10	47127	93	39	2.79	1.38	1.22
12	364404	227	73	2.78	1.42	1.24
14	3473941	539	113	2.83	1.44	1.23
16	-	1301	211	-	1.45	1.25
18	-	3056	363	-	1.46	1.26
20	-	7276	676	-	1.47	1.27
22	-	18094	1219	-	1.48	1.28
24	-	39135	1641	-	1.48	1.26

- Compare iterative-deepening with A\* using  $h_1$  (# misplaced tiles) and  $h_2$  (city block distance)
- Effective branching factor  $b^*$ 
  - Number of expanded nodes =  $1 + b^* + (b^*)^2 + \dots + (b^*)^{\text{depth}}$
  - $b^*$  remains relatively constant across many measurements

How do humans solve the path/motion  
planning problem?

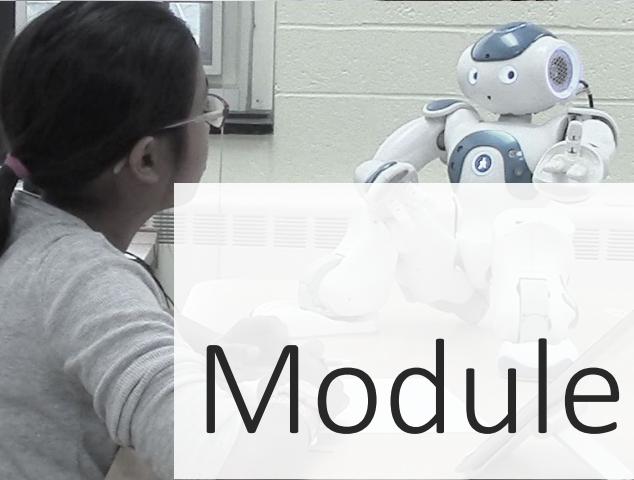
# Wrap-up

	Completeness	Computational Complexity
Exact Cell Decomposition	Complete	Exponential time
Potential Fields	Not complete	Polynomial time
Discretization and A* search	Resolution complete	Exponential time
Probabilistic RoadMap (PRM)	Probabilistically complete	Hard to characterize!

# Take-home lessons

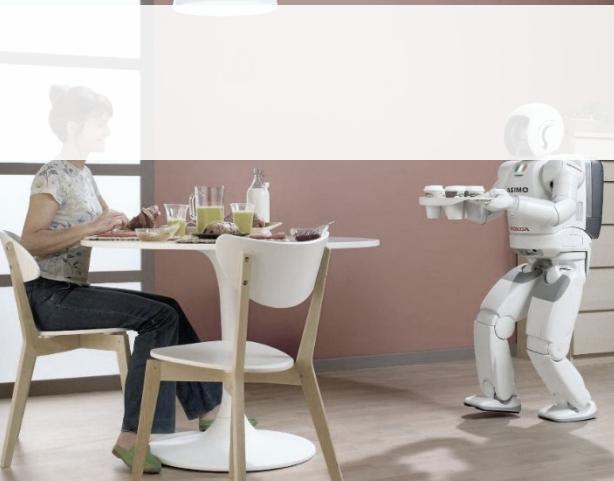
- First step in addressing a planning problem is choosing a **suitable map representation**
- Reduce robot to a **point-mass** by inflating obstacles
- Grid-based algorithms are complete, **sampling-based** ones probabilistically complete, but usually faster
- Most real planning problems require **combination** of multiple algorithms

# Chapter 5

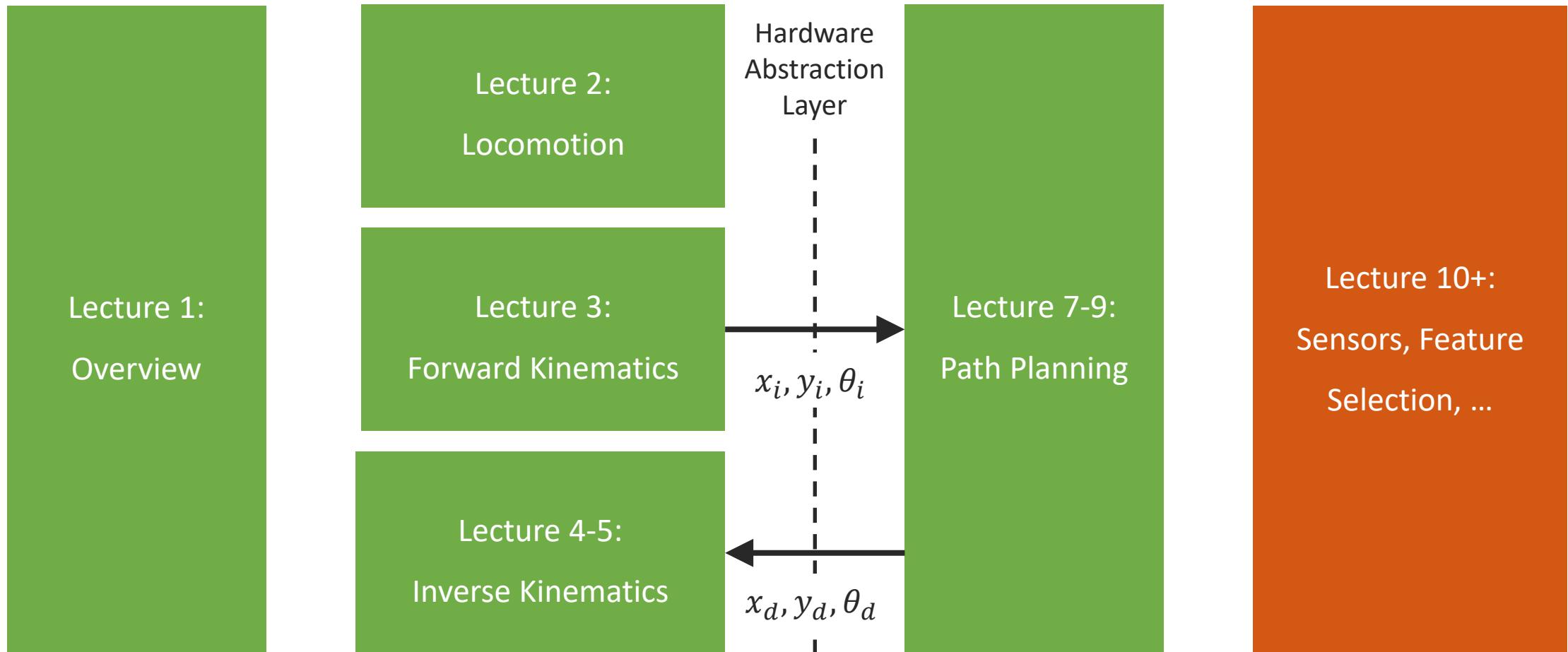


## Module 3 – SENSING AND ACTUATION

### Part I – Sensors

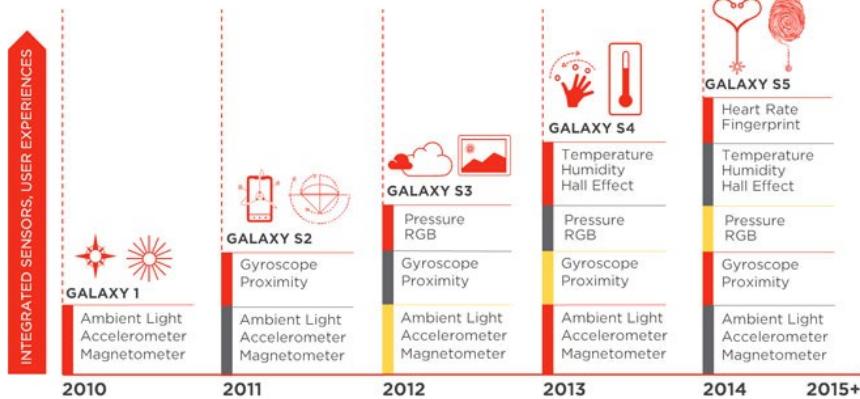


# Roadmap



# Sample of everyday sensors

## SENSOR GROWTH IN SMARTPHONES



US (ultrasonic)



3D



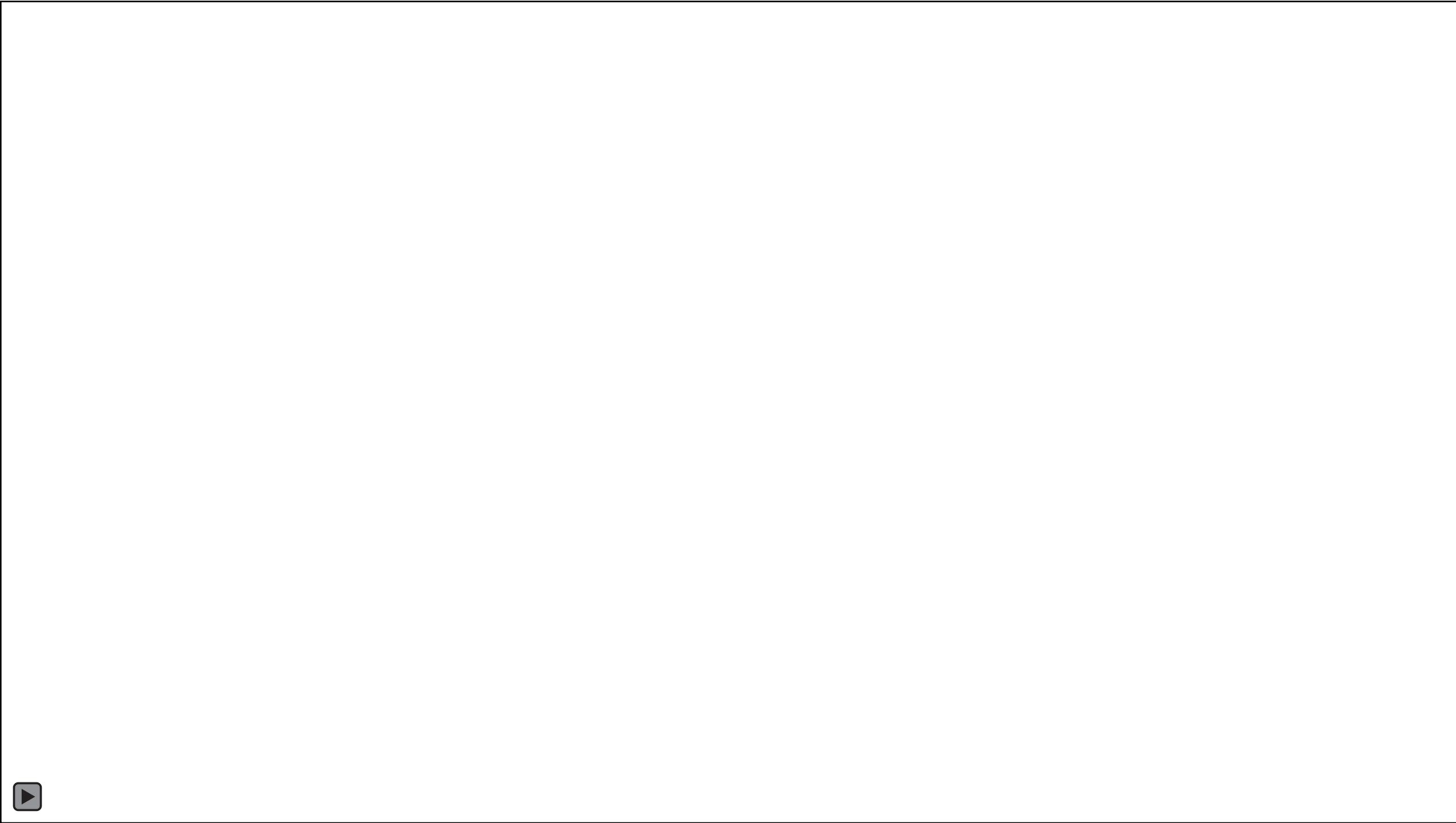
PIR  
(passive infrared)



Radar



So far: Robotics always benefits, never drives sensor development





# Sensors on Sparki e-puck

- Accelerometer
- Gyroscope
- Floor sensor
- Ultrasound sensor
- IR receiver
- Light sensor
- NO Encoders due to Stepper Motor

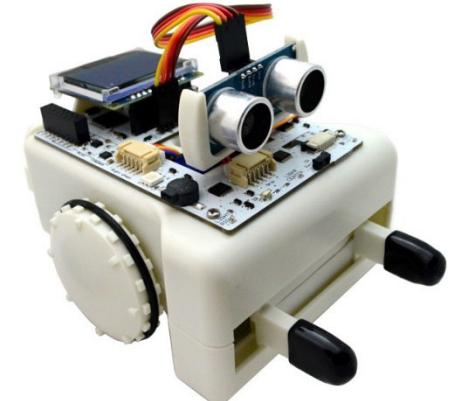
Which of these sensors can be used to reduce odometry error?



# Improving Sparki's Odometry

- Accelerometer:
- Magnetometer:
- Floor sensor:
- Ultrasound sensor:
- IR receiver:
- ...

Few (any?) sensors have specific applications, but most problems benefit from as much information as possible.



# Classifying sensors

- Type of information
- Physical Principle
- Absolute vs. derivative
- Amount of information (Bandwidth)
- Low and high reading (Dynamic range)
- Accuracy and Precision

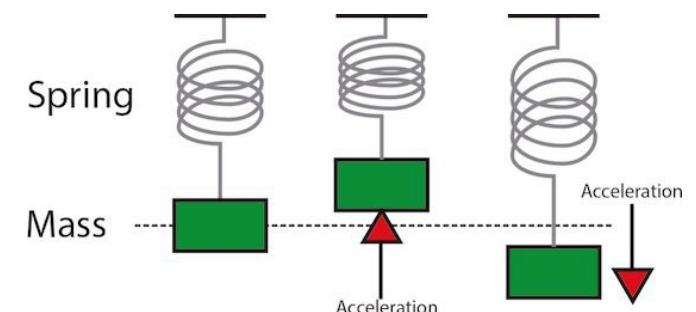
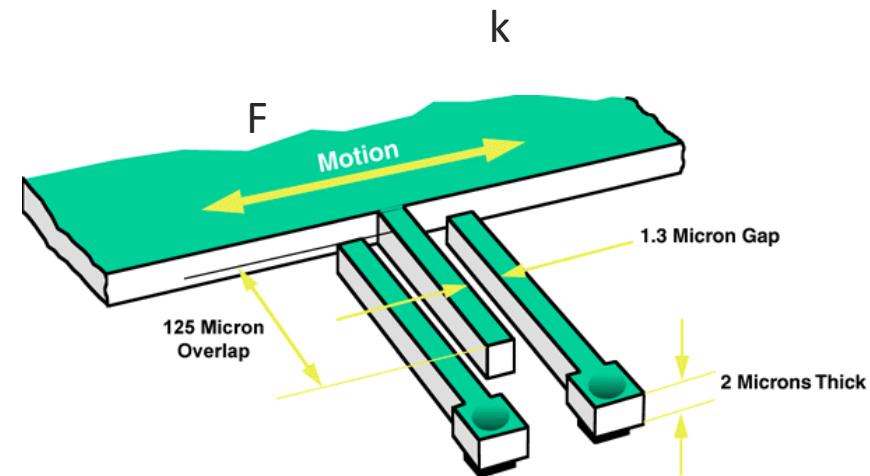
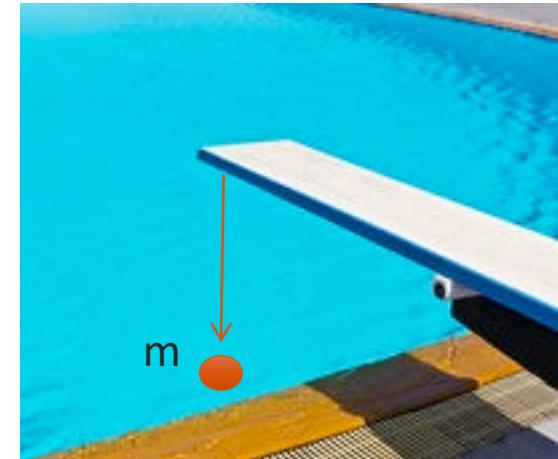
Specification	URG-04LX
Power source	Regulated 5V ±5%
Interface	RS232, USB
Detection Distance	20 to 4000 (mm)
Guaranteed Accuracy (min to 1m)	±10mm
Guaranteed Accuracy (1m to max)	1% of detected distance

Specifications	
Power source	5V +/-5%
Current consumption	0.5A (Rush current 0.8A)
Detection range	0.02 to approximately 4m
Laser wavelength	785nm, Class 1
Scan angle	240°
Scan time	100msec/scan (10.0Hz)
Resolution	1mm
Angular Resolution	0.36°
Interface	USB 2.0, RS232
Weight	5.0 oz (141 gm)

# Accelerometer

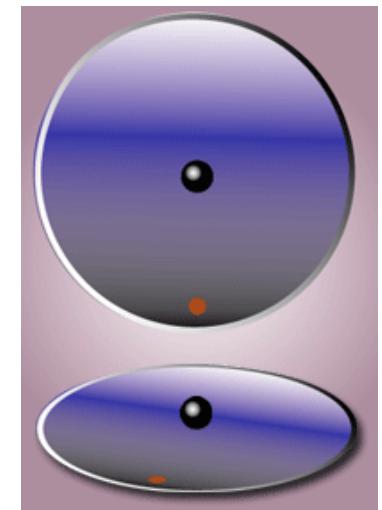
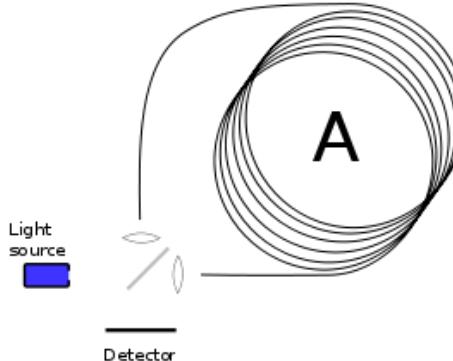
$$F = kx = ma$$

- Very cheap and small
- Measures acceleration
- Integrate for speed and distance
- Applications
  - Tell the pose of an object from the direction of gravity
  - Tell when robot hits an object

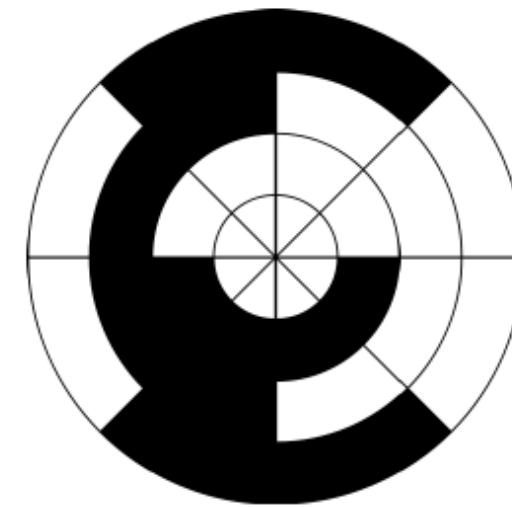
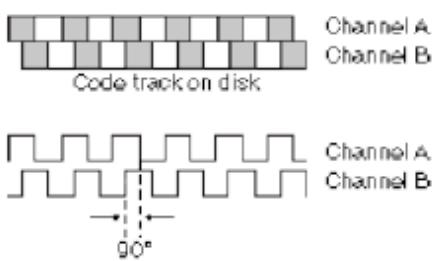
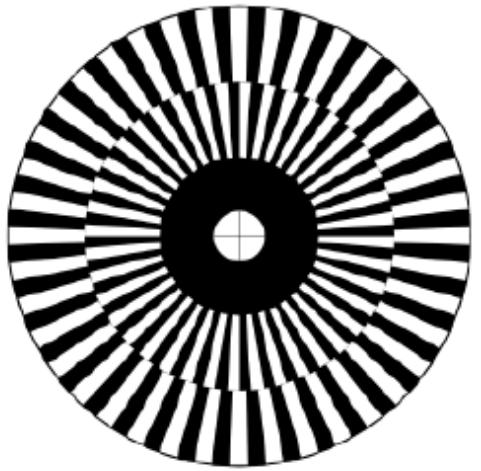
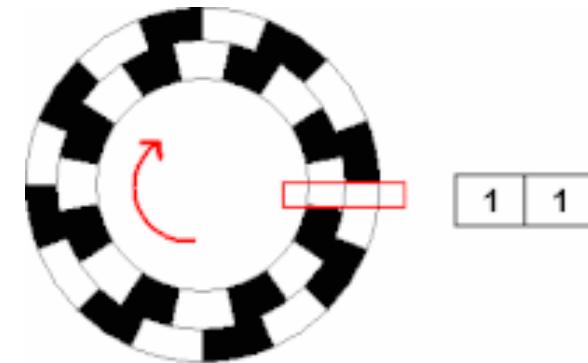


# Gyroscopes

- Measures orientation
- Very expensive, infeasible to miniaturize
- Rate gyroscopes measure rotational speed
- Implemented using MEMS vibration devices, measure Coriolis force on two proof masses vibrating in plane
- Applications
  - Correct heading

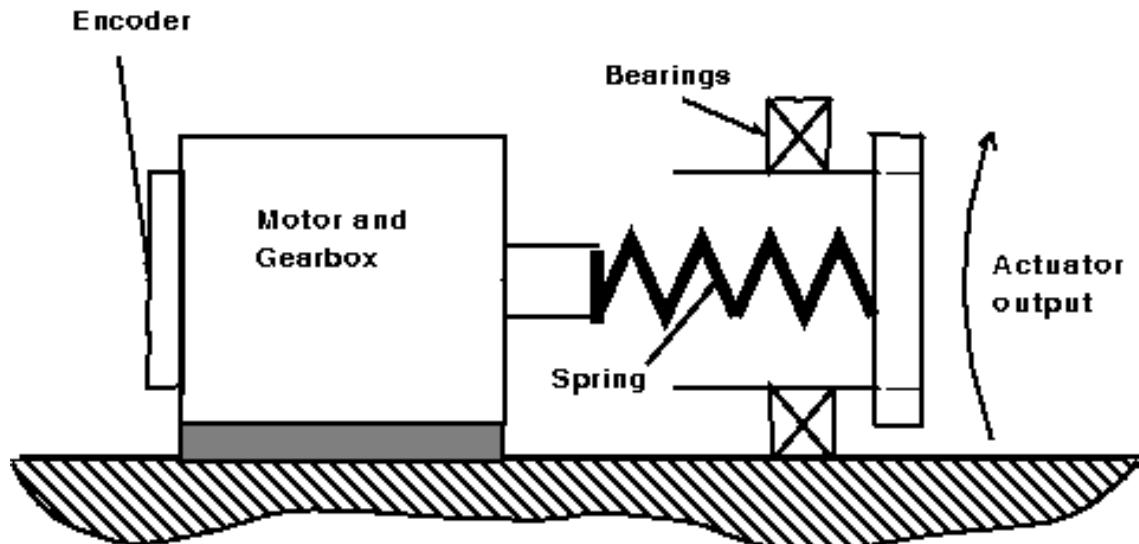


# Wheel/Joint encoder



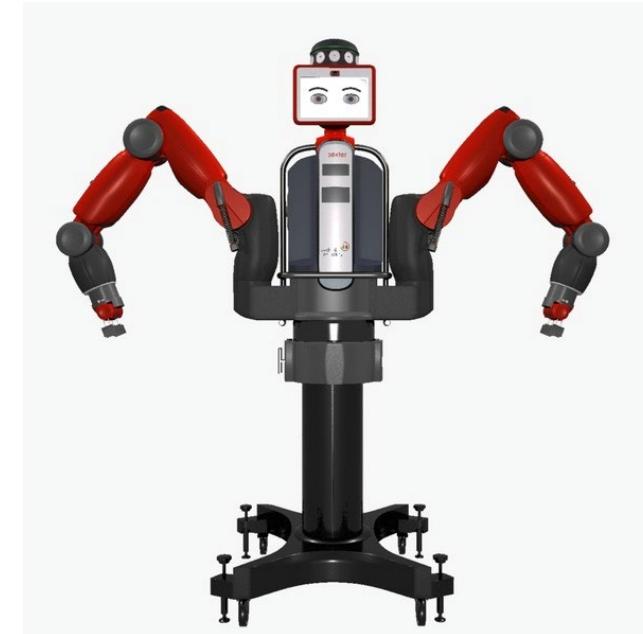
Can also be implemented magnetically or electrically (same principle). Main stream technology: CNC machines and RC servos.

# Series Elastic Actuator



$$F = kx \text{ (Hooke's law)}$$

Measure distance using  
potentiometer

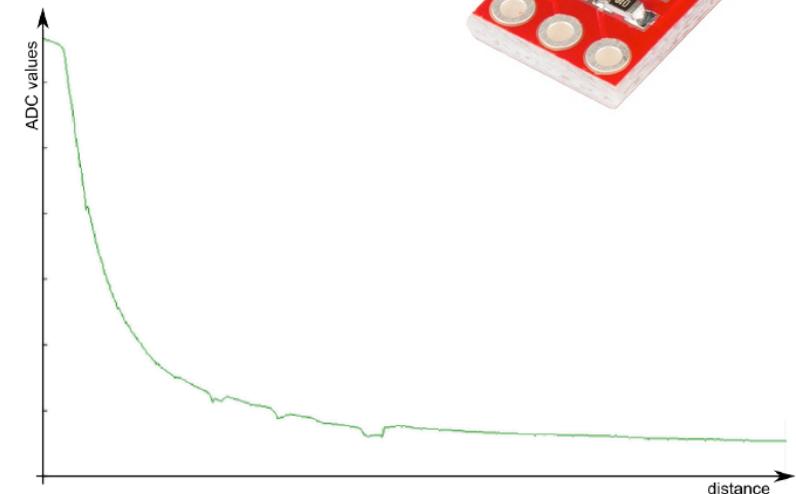


# Series Elastic Actuator

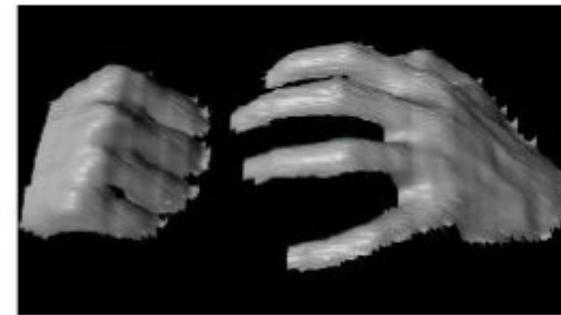
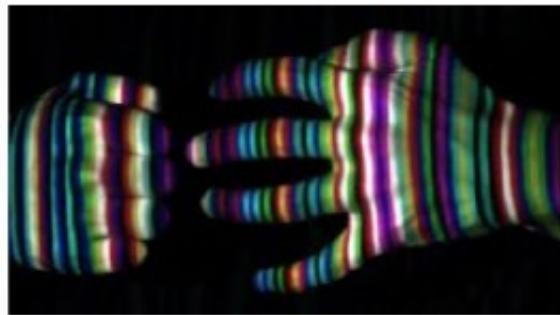


# Distance from light intensity

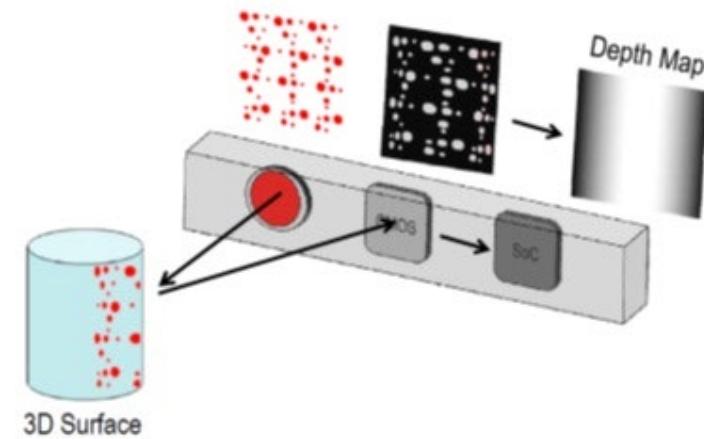
- Emitter/receiver pair
- Highly non-linear
- Depends on surface color
- Confuses emissions from other sensors
- Requires a lot of energy



# Distance from structure



Zhang et al. (2002)



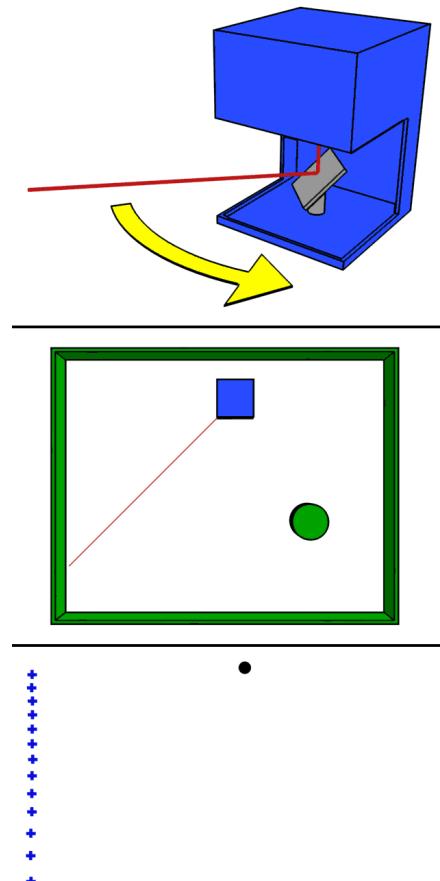
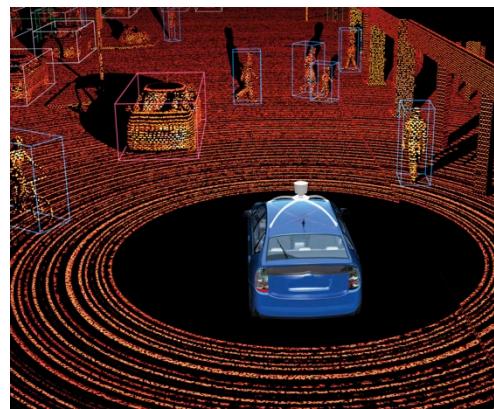
<http://www.depthbiomechanics.co.uk/?p=100>

# Distance from Sound

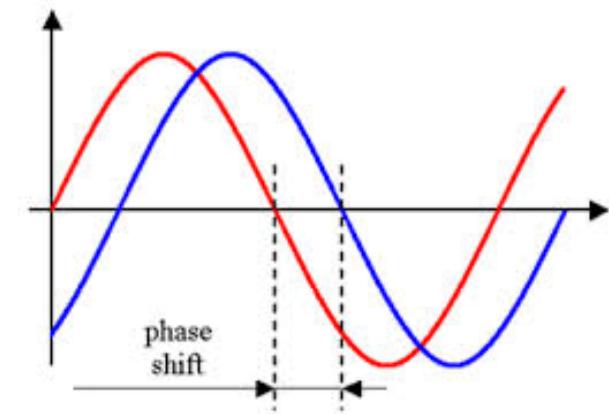
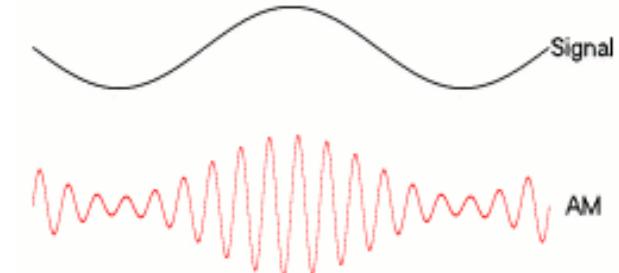
- Emitter/receiver pair
- Algorithm
  - Emit ping
  - Measure time until it returns
  - Calculate distance based on 300m/s
- Requires large objects
- Quality of result depends on object size



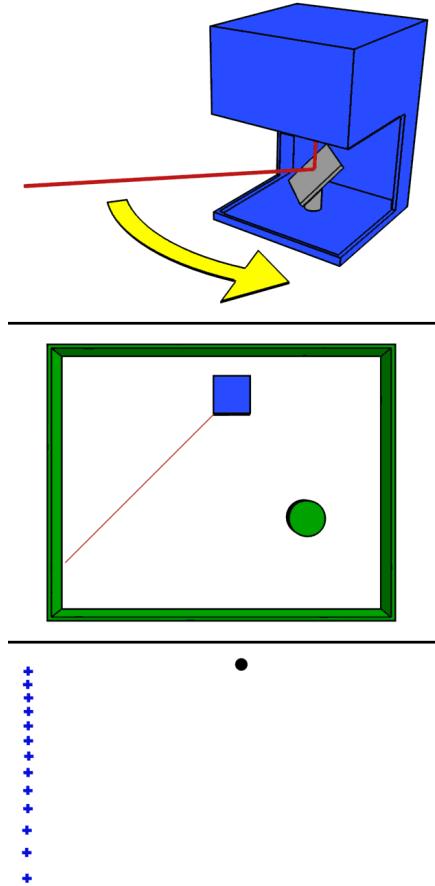
# Distance from phase shift



5 Mhz ~ 60m



# How much data does a laser scanner produce?



Specifications	
Power source	5V +/-5%
Current consumption	0.5A (Rush current 0.8A)
Detection range	0.02 to approximately 4m
Laser wavelength	785nm, Class 1
Scan angle	240°
Scan time	100msec/scan (10.0Hz)
Resolution	1mm
Angular Resolution	0.36°
Interface	USB 2.0, RS232
Weight	5.0 oz (141 gm)

Specification	URG-04LX
Power source	Regulated 5V ±5%
Interface	RS232, USB
Detection Distance	20 to 4000 (mm)
Guaranteed Accuracy (min to 1m)	±10mm
Guaranteed Accuracy (1m to max)	1% of detected distance



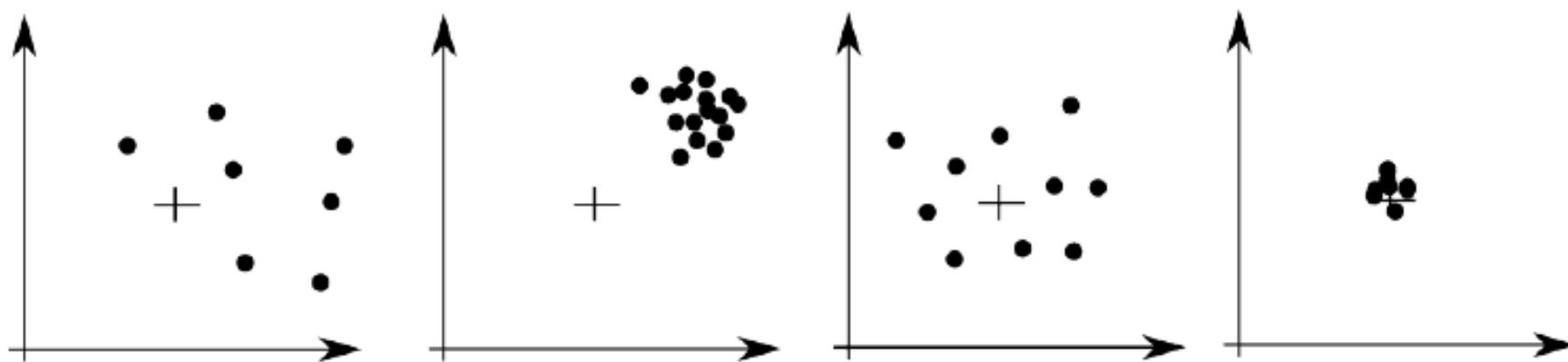
Hokuyo URG

What to do with so  
much data? (Cameras  
are even worse!)

# Sensor characteristics

- Active and passive
- Resolution
- Accuracy
- Precision
- Bandwidth
- Range
- Dynamic Range
- Cross-sensitivity

# Precision vs. Accuracy



Neither precise nor accurate, precise and not accurate, accurate and not precise, precise and accurate

# Performance of a laser scanner

- Range: difference between highest and lowest reading
- Dynamic range: ratio of lowest and highest reading
- Resolution: minimum difference between values
- Linearity: variation of output as function of input
- Bandwidth: speed with which measurements are delivered
- Cross-Sensitivity: sensitivity to environment
- Accuracy: difference between measured and true value
- Precision: reproducibility of results



Hokuyo URG

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Resolution	1mm
Angular Resolution	0.36°
Interface	USB 2.0, RS232
Weight	5.0 oz (141 gm)

# Performance of an ultrasonic sensor

- Range: difference between highest and lowest reading
- Dynamic range: ratio of lowest and highest reading
- Resolution: minimum difference between values
- Linearity: variation of output as function of input
- Bandwidth: speed with which measurements are delivered
- Cross-Sensitivity: sensitivity to environment
- Accuracy: difference between measured and true value
- Precision: reproducibility of results



- Power Supply :+5V DC
- Quiescent Current : <2mA
- Working Current: 15mA
- Effectual Angle: <15°
- Ranging Distance : 2cm – 400 cm/1" - 13ft
- Resolution : 0.3 cm
- Measuring Angle: 30 degree
- Trigger Input Pulse width: 10uS
- Dimension: 45mm x 20mm x 15mm

# Summary

- Sensors do not serve specific applications and no sensor solves a problem completely
- Many sensors observe the same phenomenon using different physical principles
- Different sensors have different trade-offs qualified in their different precision, accuracy, bandwidth, dynamic range and resolution
- There are smart ways to extract the desired information from a set of sensors and fuse them

[Sensor Fusion]