

A Gemcitabine Intracellular Model, Parameter Estimation and ML workflow Sample Work

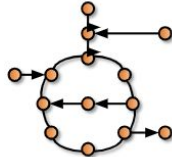
Christian D. Basile, MS - Last Updated July 20, 2022

GEMCITABINE PATHWAY: MODELING RATIONALE

- ❑ How Well understood is Gemcitabine pathway?
- ❑ Is it possible to build a generalized model that can explain different cell line's behavior?



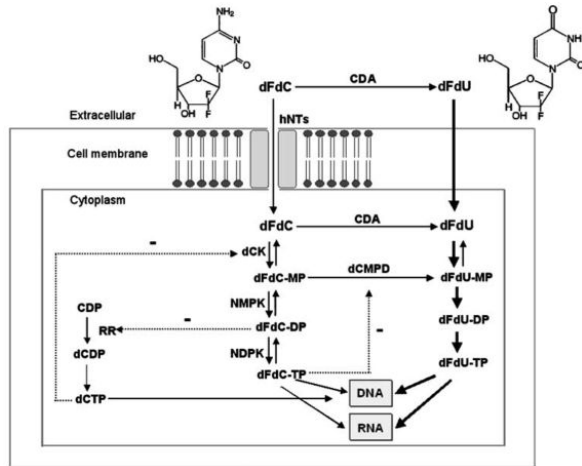
Integrated



Comprehensive

MODELING RATIONALE

- ❑ Gemcitabine strong In vitro and in vivo antitumor activity.
- ❑ Inhibition of DNA Synthesis, specifically it inhibits ribonucleotide reductase and it inhenders DNA synthesis and thus cell dies.
- ❑ Typically is given weekly for 3 weeks



Enzymes:

dCK(Deoxycytidine kinase)
RR(Ribonucleotide Reductase)
dCMPD(Deoxycytidylate Deaminase)
5'-NT(5'-Nucleotidase)
CDA(Cytidine Deaminase)
NDPK(ucleoside Diphosphate Kinase)
NMPK(Nucleoside Monophosphate Kinase)

Metabolites:

- **dCTP**(Deoxycytidine triphosphate)
- **CDP**(Cytidine Diphosphate)
- **dCTP**(Deoxycytidine diphosphate)

DATA 1 Heinemann V, 1(1992)

CCRF-CEM Human T- Lymphoblast cell line dFdCTP and its metabolites.

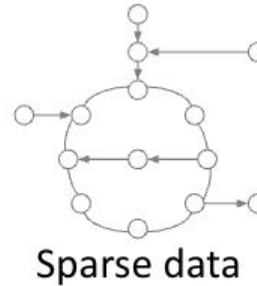
- ❑ **dFdC** was incubated in vitro for 2 hrs. in RPMI at (uM) = [0.1 0.3 1 10].
- ❑ Cells washed in drug free medium after 2hrs.
- ❑ Intracellular and Extracellular Concentrations are measured after 2hrs.

Physical Properties of the experiment:

Mean Cell Volume = 9.43×10^{-11} L/cell

Number of Cells Incubated = 2×10^6 Cells

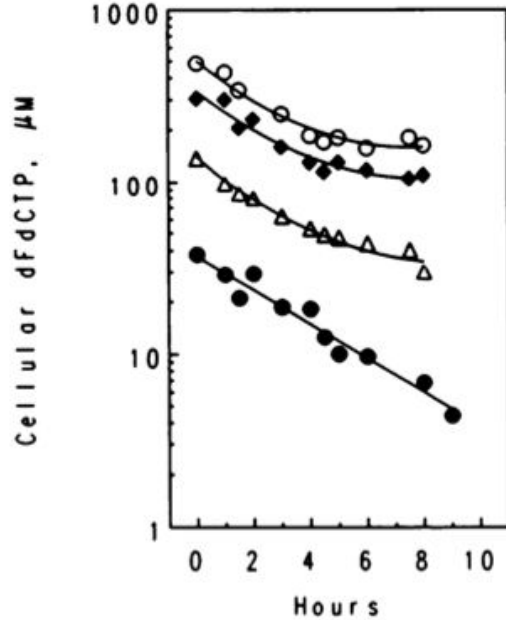
Volume medium = Unknown(Extracellular)



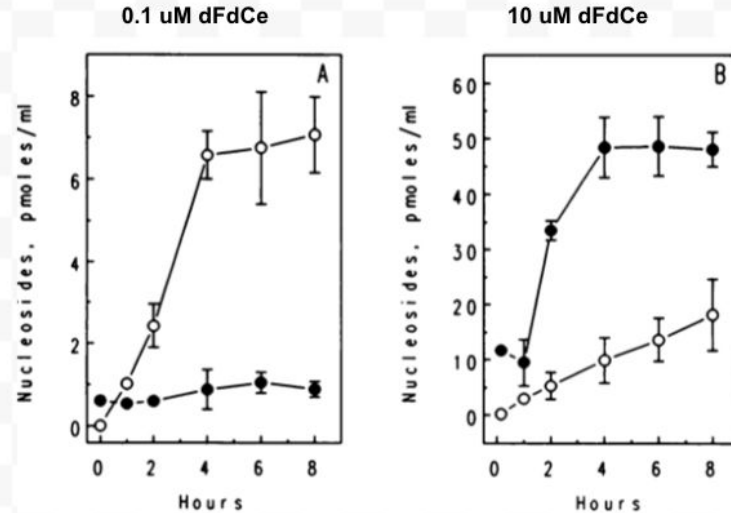
DATA 1 continued

Heinemann V, 1(1992)

Intracellular uM dFdCTP after 2 hrs



Extracellular dFdU(White) and dFdC(Black) after 2 hrs



dFdCe incubation

[0.1, 0.3, 1.0 or 10 µM] after 2hrs.

DATA 2: VELTKMAN Study_(Veltkamp 2008)

HepG2, A549, and MDCK cells were incubated with dFdC or dFdU

HepG2 cells :

- ☐ 5 nmol/L dFdC + THU,
- ☐ dFdC 0.5 μ M + THU
- ☐ dFdU 500 μ M and
- ☐ 0.5 μ M dFdU for 24 hr.

Physical Properties of Experiment:

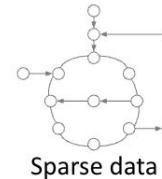
Tetrahydrouridine (THU) is a CDA competitive inhibitor $K_i \sim 110$ nM

HepG2 (12×10^6 cells) 1 mg protein activity $\rightarrow \mu\text{M} = \text{pmol/mg} \times 4.90$

HepG2 Volume ~ 17 fL

Parameter “a” ($V_{\text{medium}}/V_{\text{cells}}$) in the in vitro study experiment $\rightarrow a = 49000$ ($V_{\text{m}}/V_{\text{cells}}$)

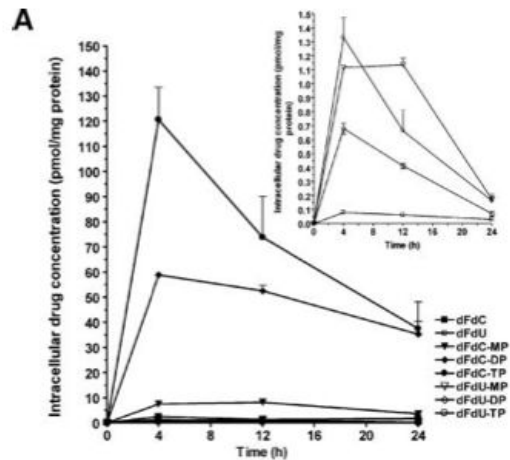
Note: “a” for Heinemann study is not known because V_{medium} is not known



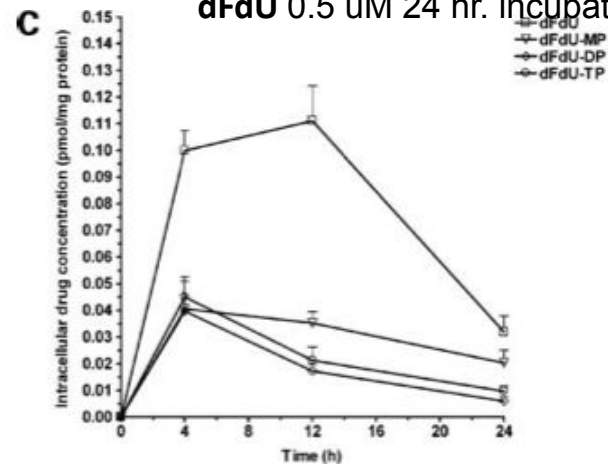
DATA 2: VELTKMAN STUDY_{Veltkamp 2008)}

Metabolite Concentrations (pmol/mg protein). Decoupling the system.

dFdC 0.5 μ M 24 hr incubation + THU



dFdU 0.5 μ M 24 hr. incubation.



DATA 2: VELTKMAN STUDY

	dFdC	dFdU	dFdC-MP	dFdC-DP	dFdC-TP	dFdU-MP	dFdU-DP	dFdU-TP
HepG2								
5 nmol/L dFdC + THU								
C_{\max} (pmol/mg protein)	0.2 ± 0.01	0.03 ± 0.01	0.5 ± 0.05	1.4 ± 0.2	2.1 ± 0.1	0.3 ± 0.1	0.2 ± 0.04	0.3 ± 0.03
AUC (h pmol/mg protein)	6.3 ± 0.5	1.0 ± 0.1	14 ± 0.7	44 ± 5.4	45 ± 5.4	6.7 ± 1.4	4.0 ± 0.7	5.0 ± 0.4
0.5 μ mol/L dFdC + THU								
C_{\max} (pmol/mg protein)	2.5 ± 0.4	0.1 ± 0.01	8.2 ± 0.3	59 ± 1.0	121 ± 13	1.1 ± 0.04	0.7 ± 0.04	1.3 ± 0.1
AUC (h pmol/mg protein)	38 ± 0.2	1.2 ± 0.2	148 ± 2.3	$1,090 \pm 64$	$1,687 \pm 253$	19 ± 0.7	8.6 ± 0.4	16 ± 2.2
$t_{1/2}$ (h)	n.d.	13 ± 1.9	10 ± 2.1	33 ± 18	12 ± 0.7	6.0 ± 0.5	6.0 ± 0.6	7.0 ± 0.9
DNA (pmol/ μ mol)	n.a.	n.a.	n.a.	n.a.	$1,600 \pm 300$	n.a.	n.a.	20 ± 1.0
RNA (pmol/ μ mol)	n.a.	n.a.	n.a.	n.a.	400 ± 30	n.a.	n.a.	10 ± 2.0
0.5 μ mol/L dFdU								
C_{\max} (pmol/mg protein)	n.d.	0.1 ± 0.01	n.d.	n.d.	n.d.	0.04 ± 0.01	0.04 ± 0.01	0.05 ± 0.01
AUC ₀₋₂₄ (h pmol/mg protein)	n.d.	1.9 ± 0.2	n.d.	n.d.	n.d.	0.7 ± 0.1	0.5 ± 0.1	0.5 ± 0.1
$t_{1/2}$ (h)	n.d.	10 ± 0.9	n.d.	n.d.	n.d.	21 ± 7.0	8.0 ± 0.8	9.0 ± 2.0
DNA (pmol/ μ mol)	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	10 ± 2.0
RNA (pmol/ μ mol)	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	n.a.	6.0 ± 1.0
500 μ mol/L dFdU								
C_{\max} (pmol/mg protein)	n.d.	74 ± 9.0	n.d.	n.d.	n.d.	45 ± 3.0	21 ± 2.6	15 ± 3.4
AUC ₀₋₂₄ (h pmol/mg protein)	n.d.	$2,090 \pm 167$	n.d.	n.d.	n.d.	$1,098 \pm 58$	557 ± 45	309 ± 63
A549								
0.5 μ mol/L dFdC + THU								
C_{\max} (pmol/mg protein)	0.8 ± 0.1	0.3 ± 0.1	4.6 ± 1.0	26 ± 4.6	64 ± 13	0.1 ± 0.03	0.2 ± 0.06	0.3 ± 0.03

CELL ENTRY

1 Cell Entry

$$uM = \frac{pmol}{mg} * \frac{(CellsIncubated)(1mg)}{12 * 10^6} * \left(\frac{1umol}{10^6 pmol} \right) * \left(\frac{1cell}{17 * 10^{-15}} \right)$$

$$uM \approx \frac{pmol}{mg} * 4.90$$

$$a = \frac{V_{medium}}{V_{Cell}} \approx 49000$$

$$\frac{dFdC_e}{dt} = -\frac{1}{a} * \frac{V_{max}dFdC_e \frac{dFdC_e}{K_{mdFdC_e}}}{\left(1 + \frac{dFdC_e}{K_{mdFdC_e}} + \frac{dFdC}{K_{mdFdC}} + \frac{dFdU_e}{K_{mdFdU_e}} + \frac{dFdU}{K_{mdFdU}} \right)}$$

$$\frac{dFdC}{dt} = \frac{a}{1} * \frac{V_{max}dFdC * \frac{dFdC}{K_{mdFdC}}}{\left(1 + \frac{dFdC_e}{K_{mdFdC_e}} + \frac{dFdC}{K_{mdFdC}} + \frac{dFdU_e}{K_{mdFdU_e}} + \frac{dFdU}{K_{mdFdU}} \right)} + (P_{cflux})$$

$$\frac{dFdU_e}{dt} = -\frac{1}{a} * \frac{V_{max}dFdU_e * \frac{dFdU_e}{K_{mdFdU_e}}}{\left(1 + \frac{dFdC_e}{K_{mdFdC_e}} + \frac{dFdC}{K_{mdFdC}} + \frac{dFdU_e}{K_{mdFdU_e}} + \frac{dFdU}{K_{mdFdU}} \right)}$$

$$\frac{dFdU}{dt} = \frac{a}{1} * \frac{V_{max}dFdU * \frac{dFdU}{K_{mdFdU}}}{\left(1 + \frac{dFdC_e}{K_{mdFdC_e}} + \frac{dFdC}{K_{mdFdC}} + \frac{dFdU_e}{K_{mdFdU_e}} + \frac{dFdU}{K_{mdFdU}} \right)} + (P_{uflux})$$

Vmaxcda	360 uM/hr
Kmcda	95.7 uM
VdCK	8.94 uM/hr
KmdCK	4.2 uM
Km dFdCMP to dFdCDP	581 uM
Ki dFdCTP on dCMPD	460 uM
Ki dCTP on dCK	2 to 5 uM
Ki dFdCDP on RR	0.3 to 4 uM

dFdCTP elimination

2 DNA Elimination

$$\frac{dFdCTP}{dt} = (FluxdFdCTP) - \frac{\frac{VmaxdFdCTP*dFdCTP}{KmdFdCTP}}{\left(1 + \frac{dFdCTP}{KmdFdCTP} + \frac{dFdUTP}{KmdFdUTP} + \frac{dCTP}{KmdCTP}\right)}$$

$$\frac{dFdUTP}{dt} = (FluxdFdUTP) - \frac{\frac{VmaxdFdUTP*dFdUTP}{KmdFdUTP}}{\left(1 + \frac{dFdCTP}{KmdFdCTP} + \frac{dFdUTP}{KmdFdUTP} + \frac{dCTP}{KmdCTP}\right)}$$

CELL ENTRY

```
#state dfdce lpositive 1 negative
dx[4] = ( (1/a)*((vmhout*x[5]/kmhout)/(1.0 + x[4]/kmhin + x[5]/kmhout + x[10]/kmuhout + x[9]/kmuhin ) ) - #dfdce
( (vmhin*x[4]/kmhin) / (1.0 + x[4]/kmhin + x[5]/kmhout + x[10]/kmuhout + x[9]/kmuhin ) ) ); #dfdce -> dfc

#state dfdc 2positive 3 negative
dx[5] = ( a*( (vmhin*x[4]/kmhin) / (1.0 + x[4]/kmhin + x[5]/kmhout + x[10]/kmuhout + x[9]/kmuhin ) ) + #dfdce -> dfc
( (vmaxdfdc2dfdc*x[6]) / (kmdfdcp2dfdc + x[6]) ) - #dfdc -> dfc
( (vmhout*x[5]/kmhout) / (1.0 + x[4]/kmhin + x[5]/kmhout + x[10]/kmuhout + x[9]/kmuhin ) ) - #dfdc->dfdce
( (vmaxdfdc2dfdc*x[5]) / (kmdfdcp2dfdc*(1.0 + x[3]/kinhdctp) + x[5]) ) - #dfdc -> dfdc
( (vmaxdfdc2dfdu*x[5]) / (kmdfdcp2dfdu*(1.0 + x[10]/kinhdctu) + x[5]) ) ) #dfdc-> dfdu
); #dfdc-> dfc

#state dfdcmp 2positive 3 negative
dx[6] = ( ( (vmaxdfdc2dfc*x[5]) / (kmdfdcp2dfc*(1.0 + x[3]/kinhdctp) + x[5]) ) + #dfdc -> dfc
( (vmaxdfdc2dfdc*x[7]) / (kmdfdcp2dfdc + x[7]) ) - #dfdc -> dfc
( (vmaxdfdc2dfdc*x[6]) / (kmdfdcp2dfdc + x[6]) ) - #dfdc -> dfc
( (vmaxdfdc2dfdu*x[6]) / (kmdfdcp2dfdu*(kinhdctu/(kinhdctu + x[8]))) ) - #dfdc -> dfdu
( (vmaxdfdc2dfdc*x[6]) / (kmdfdcp2dfdc + x[6]) ) ) #dfdc -> dfc

#state dfdcdp 2positive 2 negative
```

2 DNA Elimination

$$\frac{dFdCTP}{dt} = (FluxdFdCTP) - \frac{\frac{VmaxdFdCTP \cdot dFdCTP}{KmdFdCTP}}{(1 + \frac{dFdCTP}{KmdFdCTP} + \frac{dFdUTP}{KmdFdUTP} + \frac{dCTP}{KmdCTP})}$$

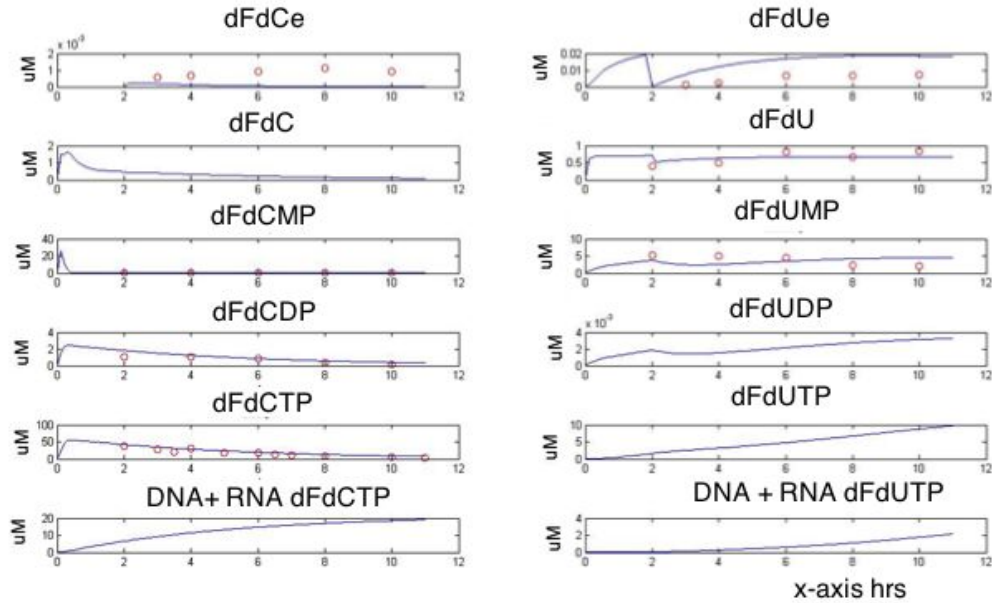
$$\frac{dFdUTP}{dt} = (FluxdFdUTP) - \frac{\frac{VmaxdFdUTP \cdot dFdUTP}{KmdFdUTP}}{(1 + \frac{dFdCTP}{KmdFdCTP} + \frac{dFdUTP}{KmdFdUTP} + \frac{dCTP}{KmdCTP})}$$

Julia
Representation

dFdCTP, dCTP, dFdCTP ELIMINATION

```
#state dfdcdp 2positive 2 negative
dx[7] = ( ( (vmaxdfdc2dfdc*x[6]) / (kmdfdcp2dfdc + x[6]) ) + #dfdc -> dfc
( (vmaxdfdc2dfdc*x[8]) / (kmdfdcp2dfdc + x[8]) ) - #dfdc -> dfc
( (vmaxdfdc2dfdc*x[7]) / (kmdfdcp2dfdc + x[7]) ) - #dfdc -> dfc
( (vmaxdfdc2dfdc*x[7]) / (kmdfdcp2dfdc + x[7]) ) ) ); #dfdc -> dfc
```

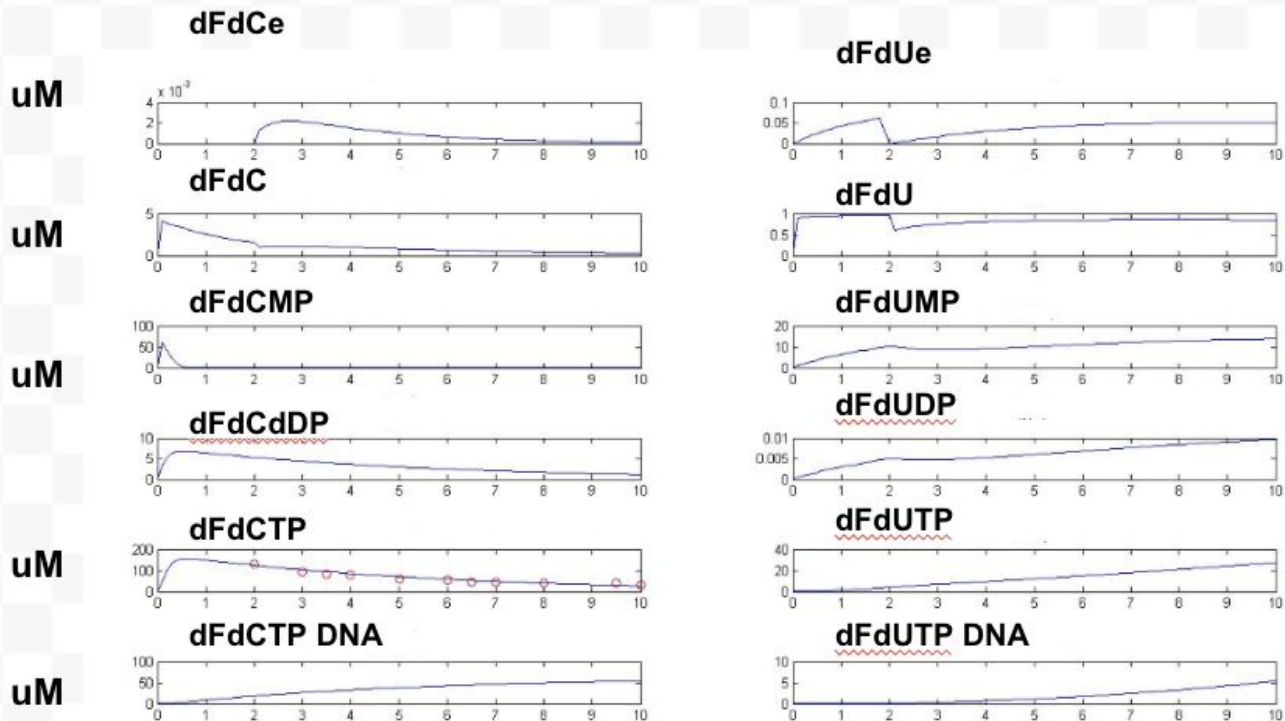
DATA 1: 0.1 μM dFdC incubation



x-axis = hours

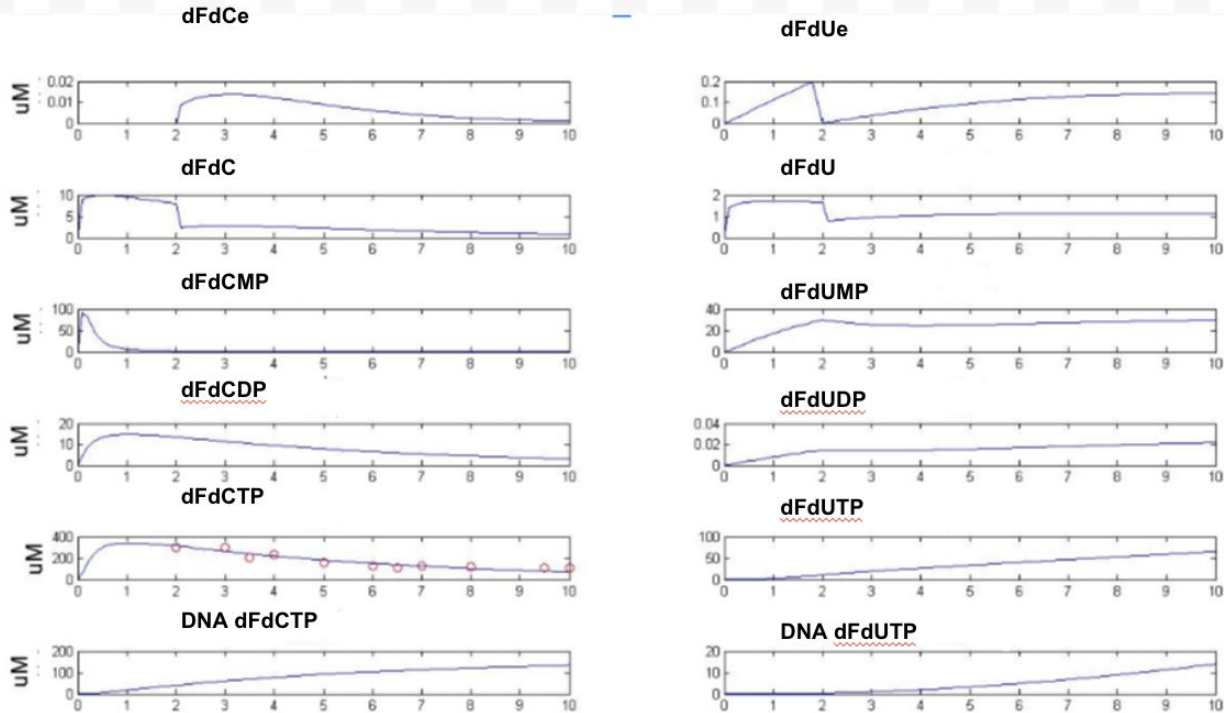
dFdCe decrement explains Maximum Concentration reached before 2 hrs(incubation time)

DATA 1: 0.3 μ M dFdC incubation



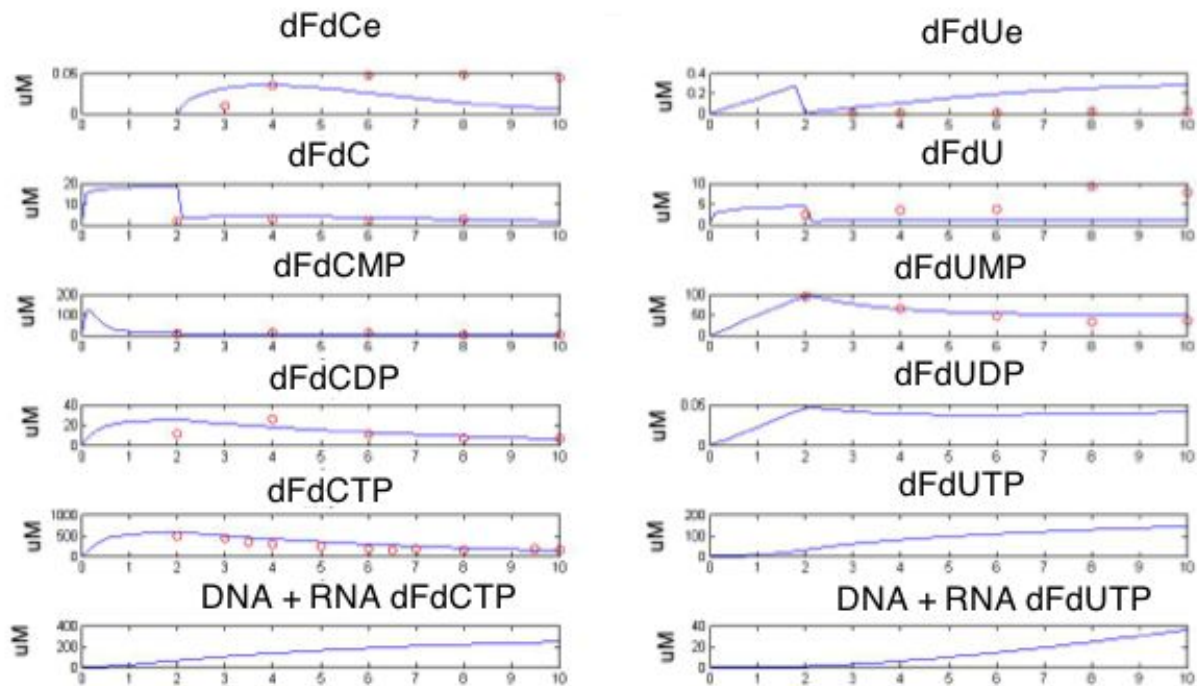
x-axis = hours

DATA 1: 1 uM dFdC incubation



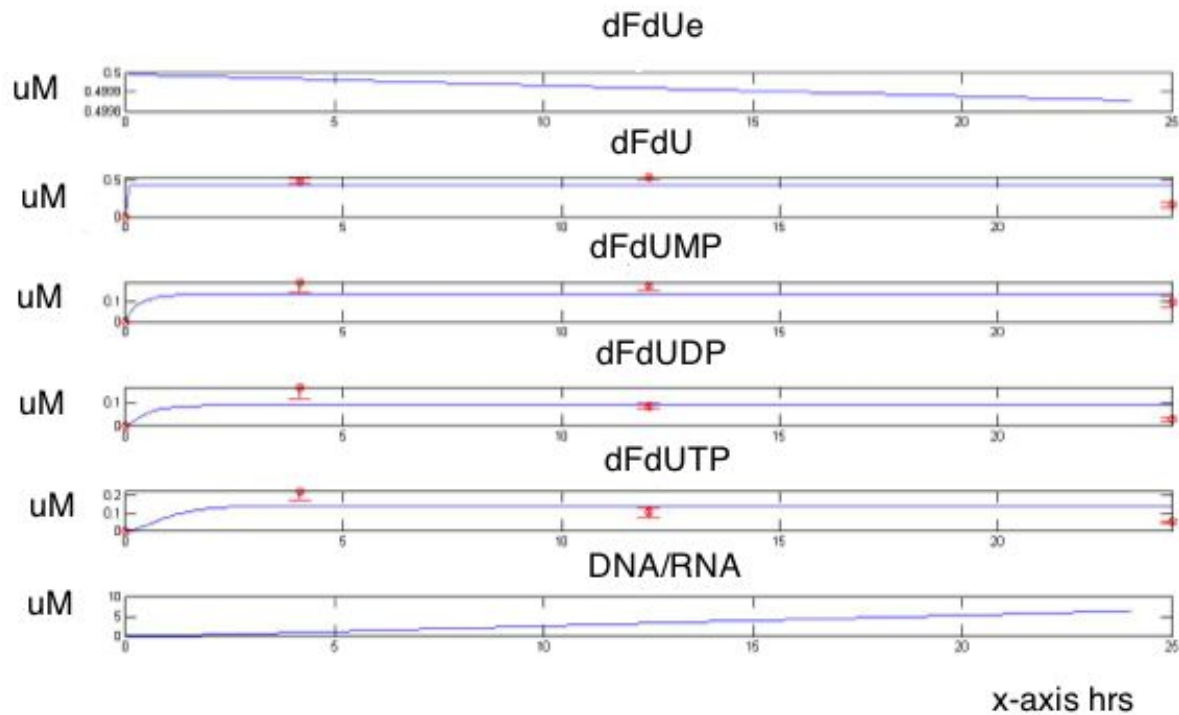
x-axis = hours

DATA 1: 10 μM dFdC incubation

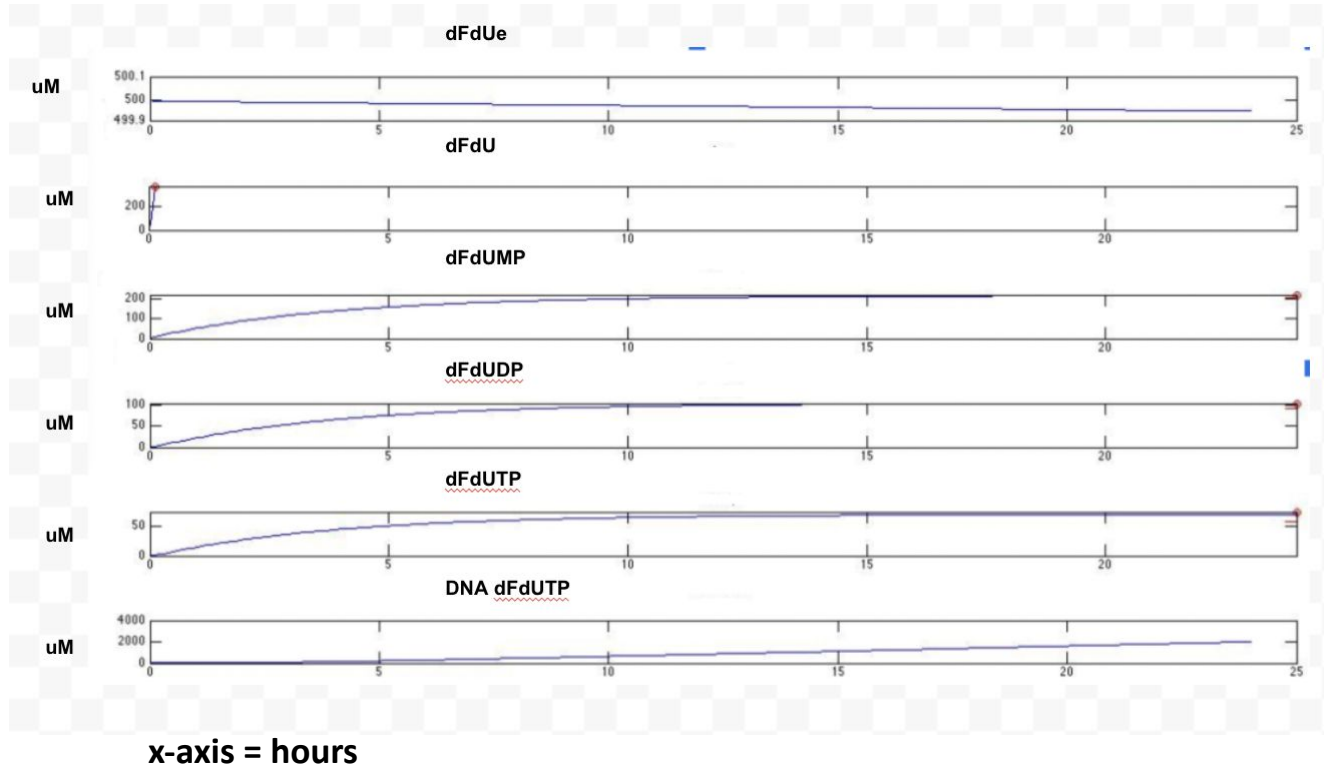


x-axis = hours

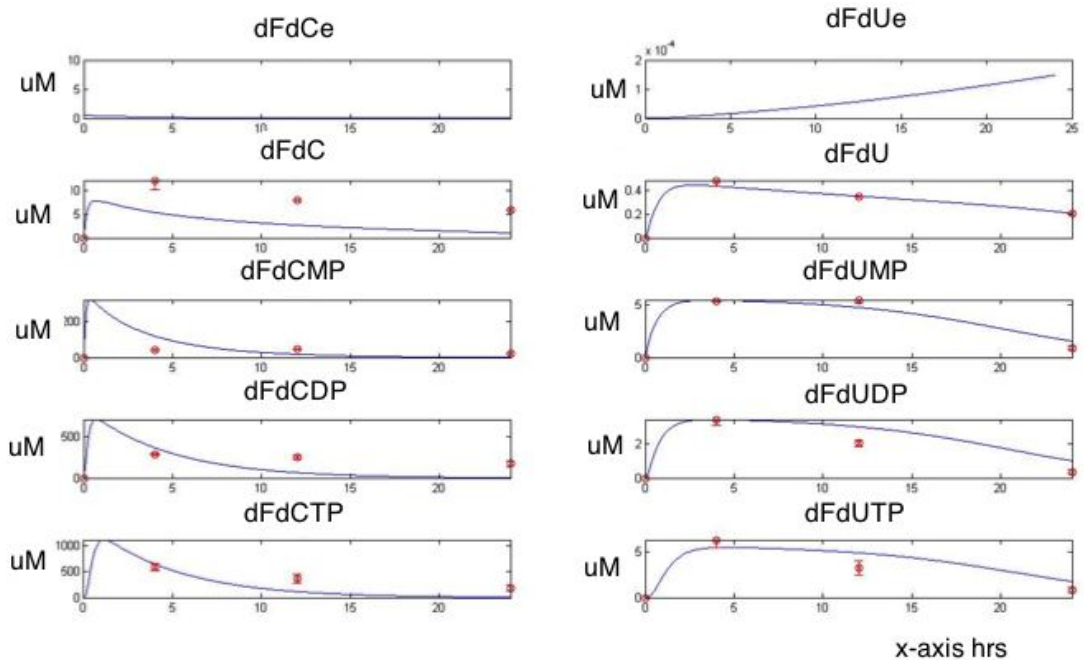
DATA 2: dFdU 0.5 μ M



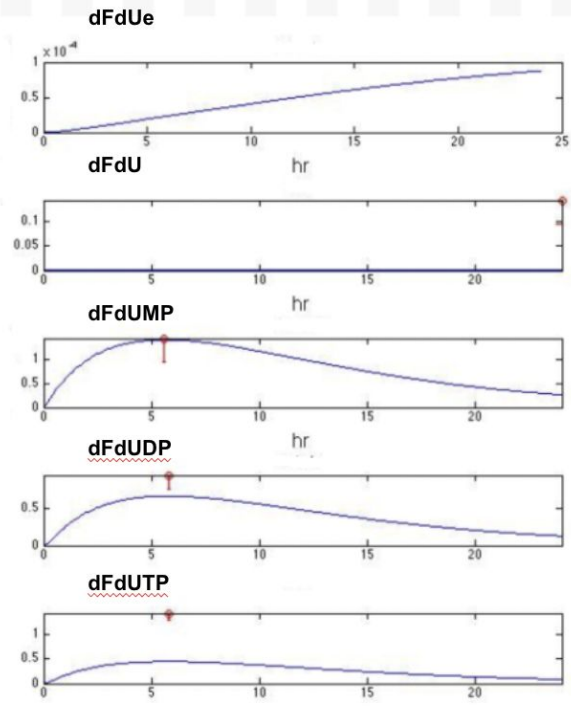
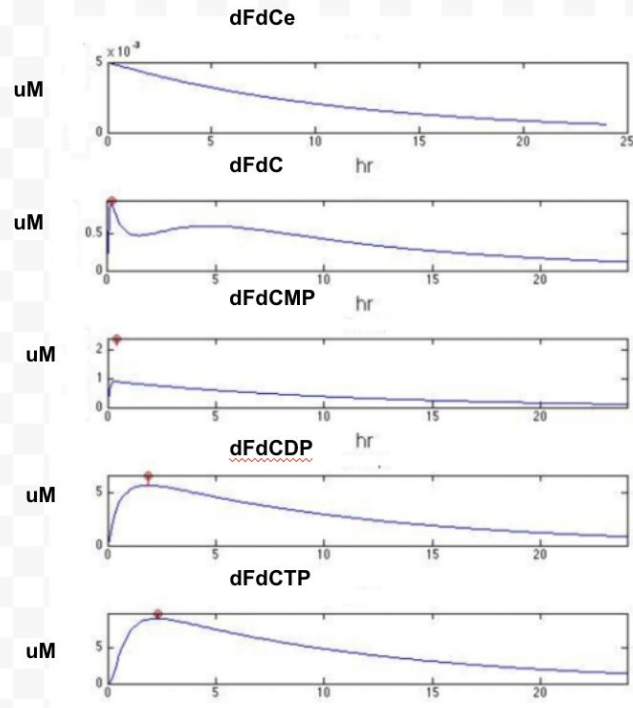
DATA 2: 500 μM dFdU



DATA 2: dFdCe 0.5 uM



DATA 2: 5 nM dFdC



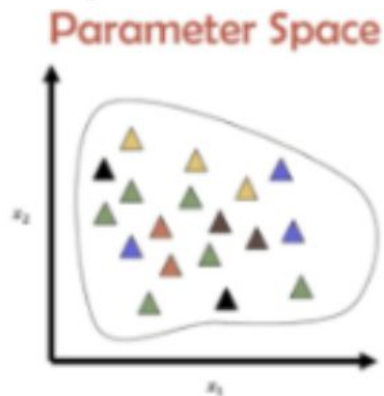
x-axis = hours



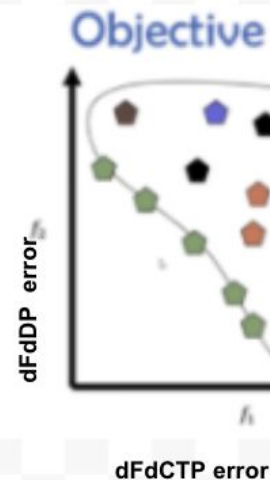


Good Solutions

	Y65I	Y73I	B
	Float64	Float64	String
1	49000.0	49000.0	a
2	0.005	0.0001	kcdp2dcdp
3	0.01	0.0100767	kinhbydfdcdp
4	0.1	1.97201	kcdp2dctp
5	0.0001	10.0	kcdtpelim
6	505.857	0.793568	vmhin
7	290.76	852.684	vmhout
8	686.142	709.147	kmhin
9	2.0	476.271	kmhout
10	964.366	1047.57	vmuhin
11	1000.0	259.096	vmuhout
12	329.446	387.285	kmuhin
13	900.0	917.727	kmuhout
14	806.652	638.749	vmaxdfdcmp2dfdcv
15	564.806	855.233	kmdfdcmp2dfdc
16	928.309	1000.0	vmaxdfdc2dfdcmp
17	5.0	5.0	kmdfdc2dfdcmp
18	500.0	5.0	kinhdctp
19	0.01224	400.0	vmaxdfdc2dfdu
20	95.7	95.7	kmdfdc2dfdu
21	343.436	573.129	kinhdfdu
22	561.647	1000.0	vmaxdfdc2dfcmp
23	0.235061	0.119926	vmaxdfdcdp2dfdcmp
24	400.0	400.0	kmdfdcdp2dfdcmp
25	998.497	1000.0	vmaxdfdcmp2dfdcdp
26	100.18	580.365	kmdfdcmp2dfdcdp



Pareto optimal front
projection
return me your
pareto solution set



$$\mathbf{J} = \begin{bmatrix} \frac{\partial \mathbf{f}}{\partial x_1} & \cdots & \frac{\partial \mathbf{f}}{\partial x_n} \end{bmatrix} = \begin{bmatrix} \nabla^T f_1 \\ \vdots \\ \nabla^T f_m \end{bmatrix} = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \cdots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial x_1} & \cdots & \frac{\partial f_m}{\partial x_n} \end{bmatrix}$$

Subject/Item	MATLAB	SciPy	differential	DifferentiaEquations.jl	Sundials
Language	MATLAB	Python	C++	Julia	C++ and Fortran
Selection of Methods for ODEs	Fair	Poor	Fair	Excellent	Good
Efficiency*	Poor	Poor****	Poor***	Excellent	Excellent
Tweakability	Fair	Good	Good	Excellent	Excellent
Event Handling	Good	Good	Fair	Excellent	Good**
Symbolic Calculation of Jacobians and AutoDifferentiation	None	None	None	Excellent	None
Complex Numbers	Excellent	Good	Fair	Good	None
Arbitrary Precision Numbers	None	None	None	Excellent	None
Control Over Linear/Nonlinear Solvers	None	Poor	None	Excellent	Excellent
Built-in Parallelism	None	None	None	Excellent	Excellent

$$\begin{array}{l}
27 \quad \mathbf{F.jacobian}([y1, y2]) \\
28 \\
29 \quad \mathbf{dFdCTP} \qquad \qquad \qquad \mathbf{DNA}
\end{array}$$

$$\mathbf{dFdCTP/dt} : \left[\begin{array}{l} \frac{vmaxd\text{fdct}p2d\text{fdcd}p y_1}{(kmd\text{fdct}p2d\text{fdcd}p + y_1)^2} - \frac{vmaxd\text{fdct}p2d\text{fdcd}p}{kmd\text{fdct}p2d\text{fdcd}p + y_1} - \frac{vmaxd\text{fdct}pelim}{kmd\text{fdct}pelim \left(\frac{dCTP}{kmdCTP} + 1.0 + \frac{y_1}{kmd\text{fdct}pelim} \right)} + \frac{vmaxd\text{fdct}pelim y_1}{kmd\text{fdct}pelim^2 \left(\frac{dCTP}{kmdCTP} + 1.0 + \frac{y_1}{kmd\text{fdct}pelim} \right)^2} \\ \frac{vmaxd\text{fdct}pelim}{kmd\text{fdct}pelim \left(\frac{dCTP}{kmdCTP} + 1.0 + \frac{y_1}{kmd\text{fdct}pelim} \right)} - \frac{vmaxd\text{fdct}pelim y_1}{kmd\text{fdct}pelim^2 \left(\frac{dCTP}{kmdCTP} + 1.0 + \frac{y_1}{kmd\text{fdct}pelim} \right)^2} \end{array} \right] \begin{array}{l} 0 \\ 0 \end{array}$$

$$\mathbf{dFdCTP} \\
\mathbf{DNA/dt}$$

$$y1 = \mathbf{dFdCTP}$$

- ❑ SIMULATION FAILS DUE TO PARAMETER CHOSEN
- ❑ ODE OPTION /studying cases.

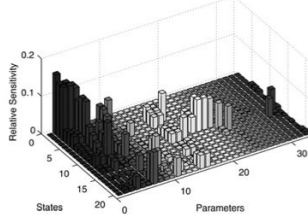
SymPy in Python outputs the Jacobian; Similarly Modeling ToolKit in Julia can as well

PROPOSED FRAMEWORK

1. Mechanistic models vs less Complex Models
2. Parameter Sampling
3. Local Sensitivity Analysis vs. Global Sensitivity analysis (i.e Variance Methods)

Multiple inputs can affect a state different than other

Collect states data that is sensitive



Model defined in terms of ODEs

$$\frac{dy}{dt} = f(y, p)$$

$y \in \mathbb{R}^n$ state vector
 $p \in \mathbb{R}^m$ parameter vector

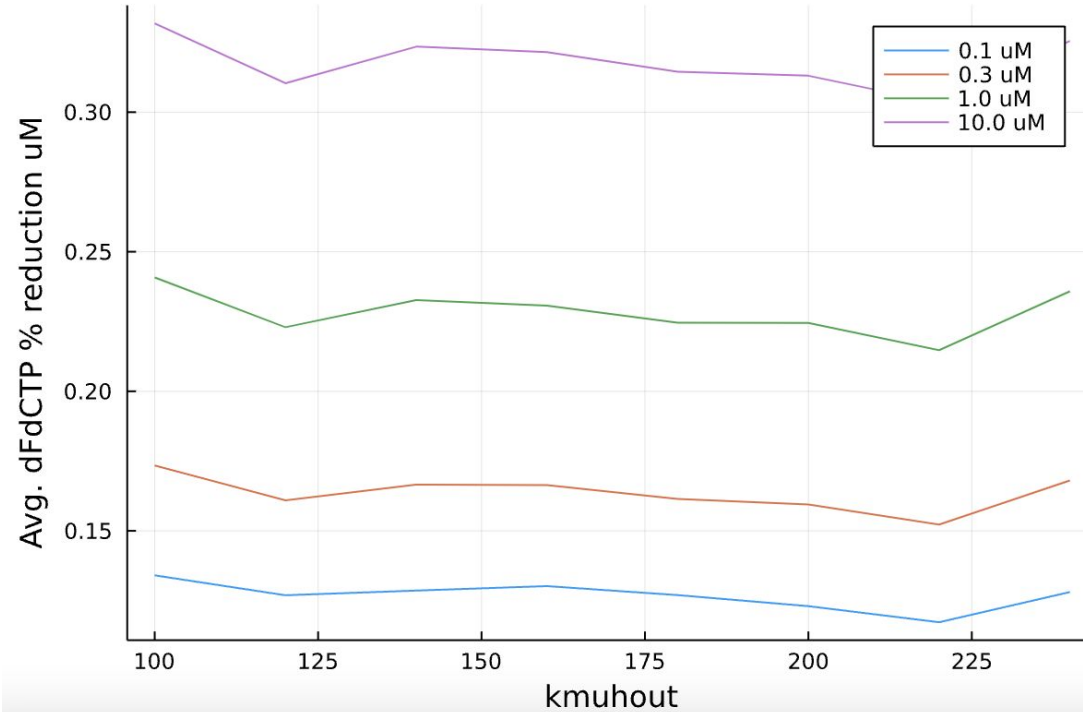
dose-response relationship (drr): change in **output** as a function of a **parameter**

$y_i(p_k)$ $\begin{cases} \text{keep remaining parameters at a fixed value } p_{j \neq k} \text{ (local drr)} \\ \text{average over remaining parameters} \longrightarrow \text{conditional expectation } E_{p_{j \neq k}}(y_i | p_k) \end{cases}$



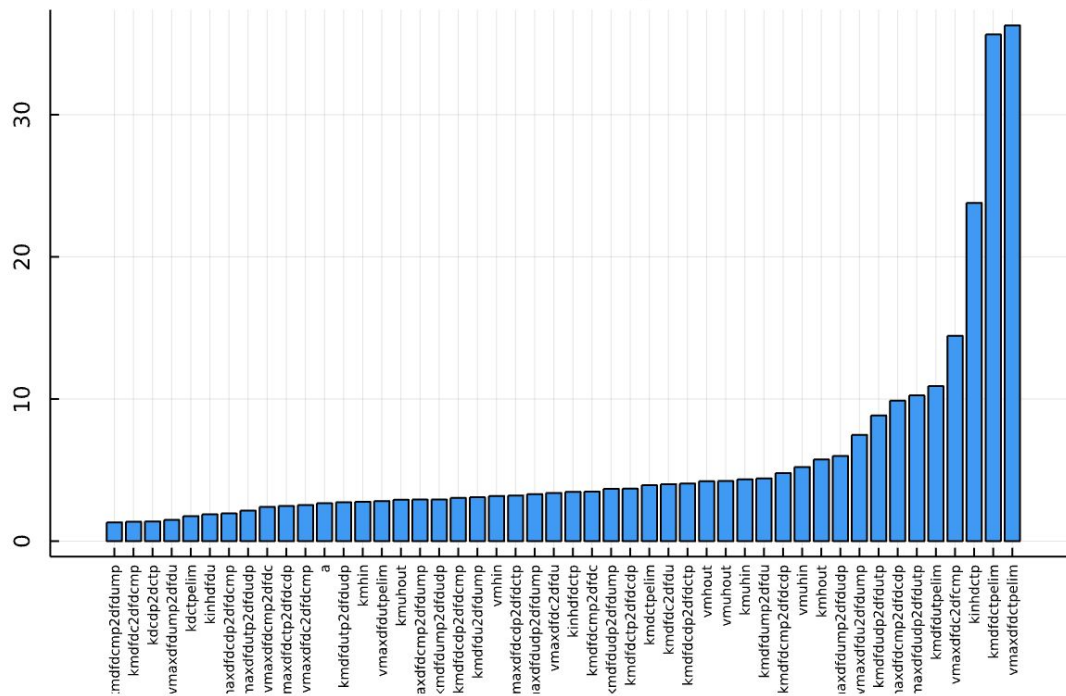


DOSE RESPONSE % dFdCTP Reduction



N = 2000 Samples

Coefficient of Variation of Dose Response sorted at 10 uM

Coefficient of Variation σ/μ at 10.0 μM 

N = 2000 Samples