



# Introduction to Programming

## CS101

Fall 2011

Lecture #12



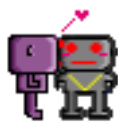
Did you like CS101 so far? Would you like to learn more about programming?

Starting next spring, the CS department is offering CS109 "Programming Practice". It is especially meant for students who did NOT learn programming in high school and who want to learn and practice more programming than we can teach in CS101.

If you consider majoring computer science but did not learn programming in high school, then CS109 is highly recommended, as the second year computer science courses assume you are familiar with the material taught in CS109.

Please visit the CS109 homepage, if you're interested:

<http://tclab.kaist.ac.kr/~otfried/cs109/>



## Course Evaluation

- When: December 1, 10AM – December 14, 5PM
- Where: KAIPA (<http://kaipa.kaist.ac.kr>)



---

In the first half of the semester we covered

- Why we learn programming
- Boolean values / conditionals / loops
- Objects / types / variables / methods / operators / expressions / tuples
- Functions / Function parameters / Lists
- Local and global variables / modules / graphics
- String methods / Image manipulation



---

In the first half of the semester we covered

- Why we learn programming
- Boolean values / conditionals / loops
- Objects / types / variables / methods / operators / expressions / tuples
- Functions / Function parameters / Lists
- Local and global variables / modules / graphics
- String methods / Image manipulation

In the second half of the semester we are covering

- Object creation
- File I/O
- How to control a system
- Object constructors / User interface programming
- Interpreters vs compilers / Recursion



---

Why is Photoshop so much faster for image processing than our `cs1media` programs?



---

Why is Photoshop so much faster for image processing than our `cs1media` programs?

Because computers do not speak Python...



---

Why is Photoshop so much faster for image processing than our `cs1media` programs?

Because computers do not speak Python...

A computer directly understands only one kind of language—its `machine language`. This language is different for different CPUs.





Why is Photoshop so much faster for image processing than our `cs1media` programs?

Because computers do not speak Python...

A computer directly understands only one kind of language—its `machine language`. This language is different for different CPUs.

Machine language is just numbers in the memory:

21 37 158 228 255 10 49 26 88 250 12 ...



Why is Photoshop so much faster for image processing than our `cs1media` programs?

Because computers do not speak Python...

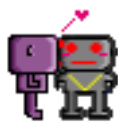
A computer directly understands only one kind of language—its `machine language`. This language is different for different CPUs.

Machine language is just numbers in the memory:

21 37 158 228 255 10 49 26 88 250 12 ...

Each number means some instruction:

- Load value from memory to CPU register
- Add two register values
- Store register value to memory
- Compare two numbers
- Jump to a new memory address



---

Machine language instructions are very fast: A 2 GHz processor executes 2,000,000,000 instructions per second!



Machine language instructions are very fast: A 2 GHz processor executes 2,000,000,000 instructions per second!

But machine instructions are very primitive, and nobody programs in machine language anymore.



Machine language instructions are very fast: A 2 GHz processor executes 2,000,000,000 instructions per second!

But machine instructions are very primitive, and nobody programs in machine language anymore.

Python uses an **interpreter**: An interpreter is a program that reads your Python code and executes its instructions one after another.



Machine language instructions are very fast: A 2 GHz processor executes 2,000,000,000 instructions per second!

But machine instructions are very primitive, and nobody programs in machine language anymore.

Python uses an **interpreter**: An interpreter is a program that reads your Python code and executes its instructions one after another.

Other interpreted languages are Scheme, MATLAB, or Flash.



Machine language instructions are very fast: A 2 GHz processor executes 2,000,000,000 instructions per second!

But machine instructions are very primitive, and nobody programs in machine language anymore.

Python uses an **interpreter**: An interpreter is a program that reads your Python code and executes its instructions one after another.

Other interpreted languages are Scheme, MATLAB, or Flash.

Languages such as C, C++, Java, or FORTRAN are **compiled**. The input program (source code) is converted to a numeric format that contains machine instructions.



Using an interpreter is like making a dish using a cooking book in a foreign language that you cannot read well. You need to look up many words, and you execute the recipe slowly.

### Fondant au chocolat

par Crevette

Pour 6 personnes :  
Préparation : 20 min  
Cuisson : 30 min

#### Ingrédients :

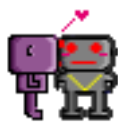
200 g de chocolat pâtissier  
60 g de beurre  
4 cuillerées à soupe de farine  
4 œufs  
150 g de sucre



#### Préparation :

Faire fondre le chocolat au **bain-marie**. Séparer les jaunes d'œufs des blancs.  
Ajouter le beurre ramolli au chocolat fondu, ensuite les jaunes d'œufs, le sucre et la farine.  
  
Montez les blancs d'œufs en neige bien ferme. Incorporez-les délicatement au mélange.  
Cuire au four à 180°C (th.6) pendant environ 30 minutes.





Using an interpreter is like making a dish using a cooking book in a foreign language that you cannot read well. You need to look up many words, and you execute the recipe slowly.

When we have to cook the same dish many times, it is more efficient to first translate the recipe and to write it down in your mother tongue. This is what a compiler does.



---

Using an interpreter is like making a dish using a cooking book in a foreign language that you cannot read well. You need to look up many words, and you execute the recipe slowly.

When we have to cook the same dish many times, it is more efficient to first translate the recipe and to write it down in your mother tongue. This is what a compiler does.

It takes time and effort to do the translation and to write it down. It is not worth doing that if we only cook the dish once. But now we can cook the dish many times quickly.



---

The Python shell interactively executes our instructions, so we can experiment with objects of different types and test their behavior.



---

The Python shell interactively executes our instructions, so we can experiment with objects of different types and test their behavior.

We can also interactively explore data, or perform mathematical analysis (try symbolic differentiation in C++!).



---

The Python shell interactively executes our instructions, so we can experiment with objects of different types and test their behavior.

We can also interactively explore data, or perform mathematical analysis (try symbolic differentiation in C++!).

An interpreter makes it easier to debug a program, because changing the program is fast. We can also look at the objects created in the program.



---

The Python shell interactively executes our instructions, so we can experiment with objects of different types and test their behavior.

We can also interactively explore data, or perform mathematical analysis (try symbolic differentiation in C++!).

An interpreter makes it easier to debug a program, because changing the program is fast. We can also look at the objects created in the program.

Memory-management is done automatically by the interpreter.



---

Why is Photoshop faster than our 'posterize' function?

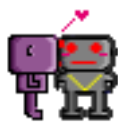


---

Why is Photoshop faster than our 'posterize' function?

- Photoshop is written in C++ and compiled to machine language.





---

Why is Photoshop faster than our 'posterize' function?

- Photoshop is written in C++ and compiled to machine language.
- Photoshop uses smarter algorithms.

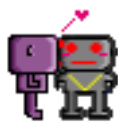


---

Why is Photoshop faster than our 'posterize' function?

- Photoshop is written in C++ and compiled to machine language.
- Photoshop uses smarter algorithms.

A smart algorithm in an interpreted language can easily beat a simple algorithm in a compiled language.



Here is a simple algorithm to sort a list **a**:

```
for i in range(len(a) - 1):  
    for j in range(len(a) - 1):  
        if a[j] > a[j+1]:  
            a[j], a[j+1] = a[j+1], a[j]
```



Here is a simple algorithm to sort a list **a**:

```
for i in range(len(a) - 1):  
    for j in range(len(a) - 1):  
        if a[j] > a[j+1]:  
            a[j], a[j+1] = a[j+1], a[j]
```

If the list **a** has  $n$  elements, then the **if** statement is executed  $(n - 1)^2$  times.

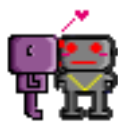


Here is a simple algorithm to sort a list **a**:

```
for i in range(len(a) - 1):  
    for j in range(len(a) - 1):  
        if a[j] > a[j+1]:  
            a[j], a[j+1] = a[j+1], a[j]
```

If the list **a** has  $n$  elements, then the **if** statement is executed  $(n - 1)^2$  times.

On a 2.8 GHz desktop, sorting 10000 numbers takes 20 seconds.



# Merge Sort: a smarter algorithm

---

We partition the list into small pieces of one element.

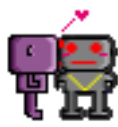


# Merge Sort: a smarter algorithm

---

We partition the list into small pieces of one element.

Then we **merge** pieces together in pairs, until the whole list is sorted.



# Merge Sort: a smarter algorithm

---

We partition the list into small pieces of one element.

Then we **merge** pieces together in pairs, until the whole list is sorted.

Merging two sorted lists **a** and **b** is easy, as in each step we only need to select an element from either **a** or **b**.





# Merge Sort: a smarter algorithm

---

We partition the list into small pieces of one element.

Then we **merge** pieces together in pairs, until the whole list is sorted.

Merging two sorted lists **a** and **b** is easy, as in each step we only need to select an element from either **a** or **b**.

We can show that this algorithm compares two list elements only  $n \log_2 n$  times.



# Merge Sort: a smarter algorithm

---

We partition the list into small pieces of one element.

Then we **merge** pieces together in pairs, until the whole list is sorted.

Merging two sorted lists **a** and **b** is easy, as in each step we only need to select an element from either **a** or **b**.

We can show that this algorithm compares two list elements only  $n \log_2 n$  times.

Sorting 10000 numbers on the same desktop computer takes 0.1 seconds. One million numbers can be sorted in 11 seconds.



---

Designing **efficient** algorithms for a problem is a fundamental branch of computer science.



---

Designing **efficient** algorithms for a problem is a fundamental branch of computer science.

Here, “efficient” means that we can prove that the number of operations made by the algorithm is bounded by some function of the problem size  $n$ .



---

Designing **efficient** algorithms for a problem is a fundamental branch of computer science.

Here, “efficient” means that we can prove that the number of operations made by the algorithm is bounded by some function of the problem size  $n$ .

An algorithm is **optimal** if we can prove that no algorithm can possibly solve the problem with a smaller number of operations (asymptotically).



---

Designing **efficient** algorithms for a problem is a fundamental branch of computer science.

Here, “efficient” means that we can prove that the number of operations made by the algorithm is bounded by some function of the problem size  $n$ .

An algorithm is **optimal** if we can prove that no algorithm can possibly solve the problem with a smaller number of operations (asymptotically).

We can prove that it is impossible to sort  $n$  numbers with less than  $n \log_2 n$  comparisons, and therefore Merge Sort is optimal.



“Recursion” means to define something in terms of itself.



“Recursion” means to define something in terms of itself.

A folder is a collection of files and folders.





“Recursion” means to define something in terms of itself.

A folder is a collection of files and folders.

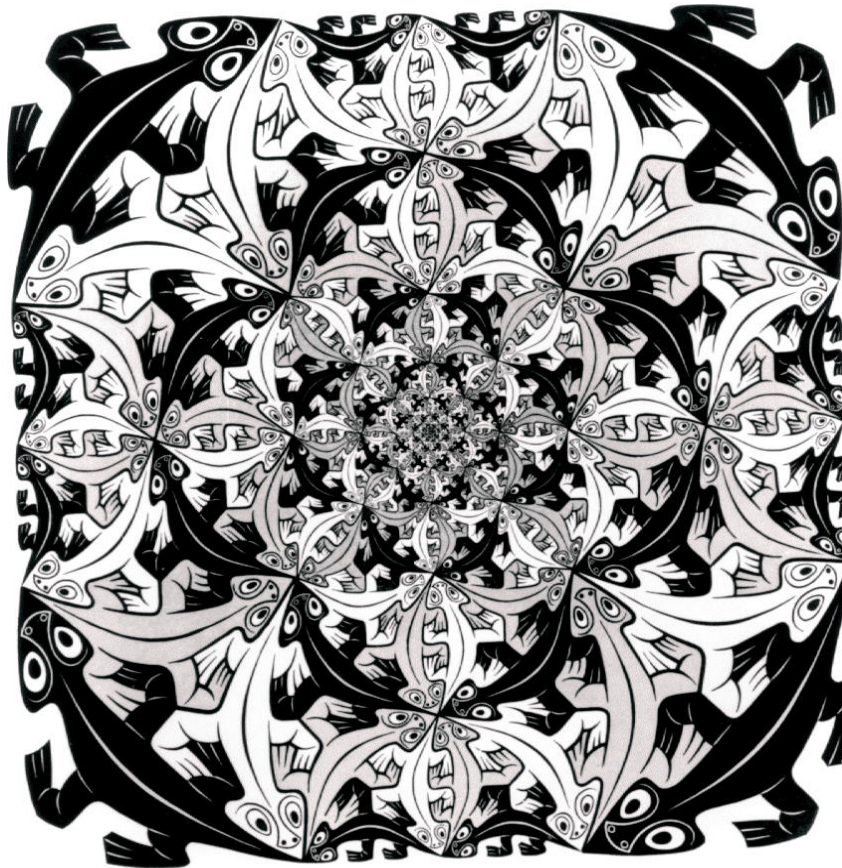
Words in dictionaries are defined in terms of other words.



“Recursion” means to define something in terms of itself.

A folder is a collection of files and folders.

Words in dictionaries are defined in terms of other words.





Factorial

$$n! = \begin{cases} 1 & \text{if } n = 0 \\ (n - 1)! \times n & \text{if } n > 0 \end{cases}$$



---

How would you implement this function?

```
>>> downup("Hello")
```

```
Hello
```

```
Hell
```

```
Hel
```

```
He
```

```
H
```

```
He
```

```
Hel
```

```
Hell
```

```
Hello
```



How would you implement this function?

```
>>> downup("Hello")
```

```
Hello
```

```
Hell
```

```
Hel
```

```
He
```

```
H
```

```
He
```

```
Hel
```

```
Hell
```

```
Hello
```

My solution:

```
def downup(w):  
    print w  
    if len(w) <= 1:  
        return  
    downup(w[::-1])  
    print w
```



How would you implement this function?

```
>>> downup("Hello")
```

```
Hello
```

```
Hell
```

```
Hel
```

```
He
```

```
H
```

```
He
```

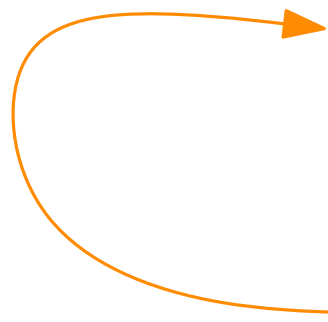
```
Hel
```

```
Hell
```

```
Hello
```

My solution:

```
def downup(w):  
    print w  
    if len(w) <= 1:  
        return  
    downup(w[::-1])  
    print w
```



recursive call



---

How do you print a number in binary? Or in base 8?



---

How do you print a number in binary? Or in base 8?

The last digit of number  $n$  in base  $b$  is easy:  $n \% b$





How do you print a number in binary? Or in base 8?

The last digit of number  $n$  in base  $b$  is easy:  $n \% b$

The remaining digits are the representation of  $n / b$  in base  $b$ :

```
def to_radix(n, b):  
    if n < b:  
        return str(n)  
    s = to_radix(n / b, b)  
    return s + str(n % b)
```



Merge Sort is an example of a more interesting recursive algorithm: it uses **two** recursive calls:

```
def merge_sort(a):  
    if len(a) <= 1:  
        return  
    m = len(a)/2  
    a1 = a[:m]  
    a2 = a[m:]  
    merge_sort(a1)  
    merge_sort(a2)  
    merge(a, a1, a2)
```



Merge Sort is an example of a more interesting recursive algorithm: it uses **two** recursive calls:

```
def merge_sort(a):  
    if len(a) <= 1:  
        return  
    m = len(a)/2  
    a1 = a[:m]  
    a2 = a[m:]  
    merge_sort(a1)  
    merge_sort(a2)  
    merge(a, a1, a2)
```

**Divide & Conquer:** Divide a problem into two smaller problems. Solve the smaller problems, and combine the solutions.

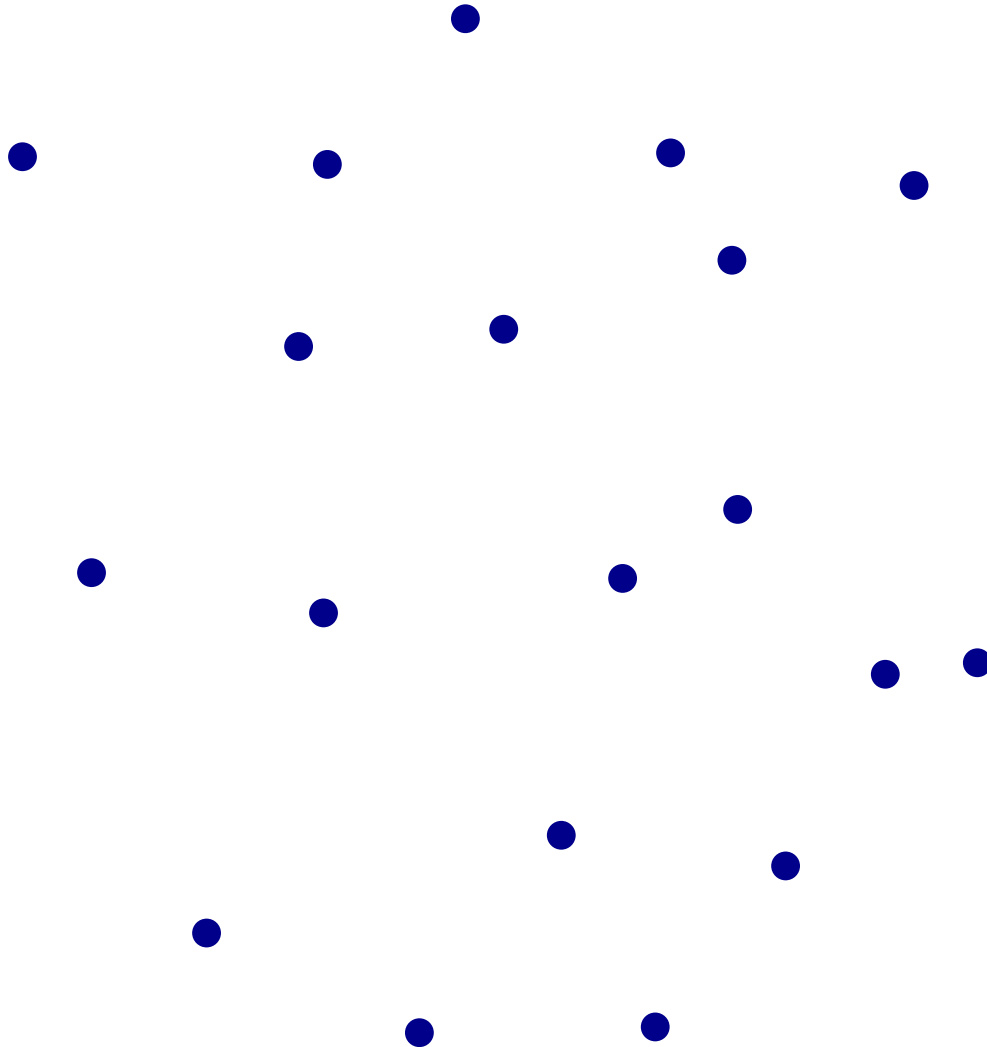


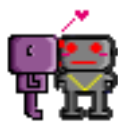
---

**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.

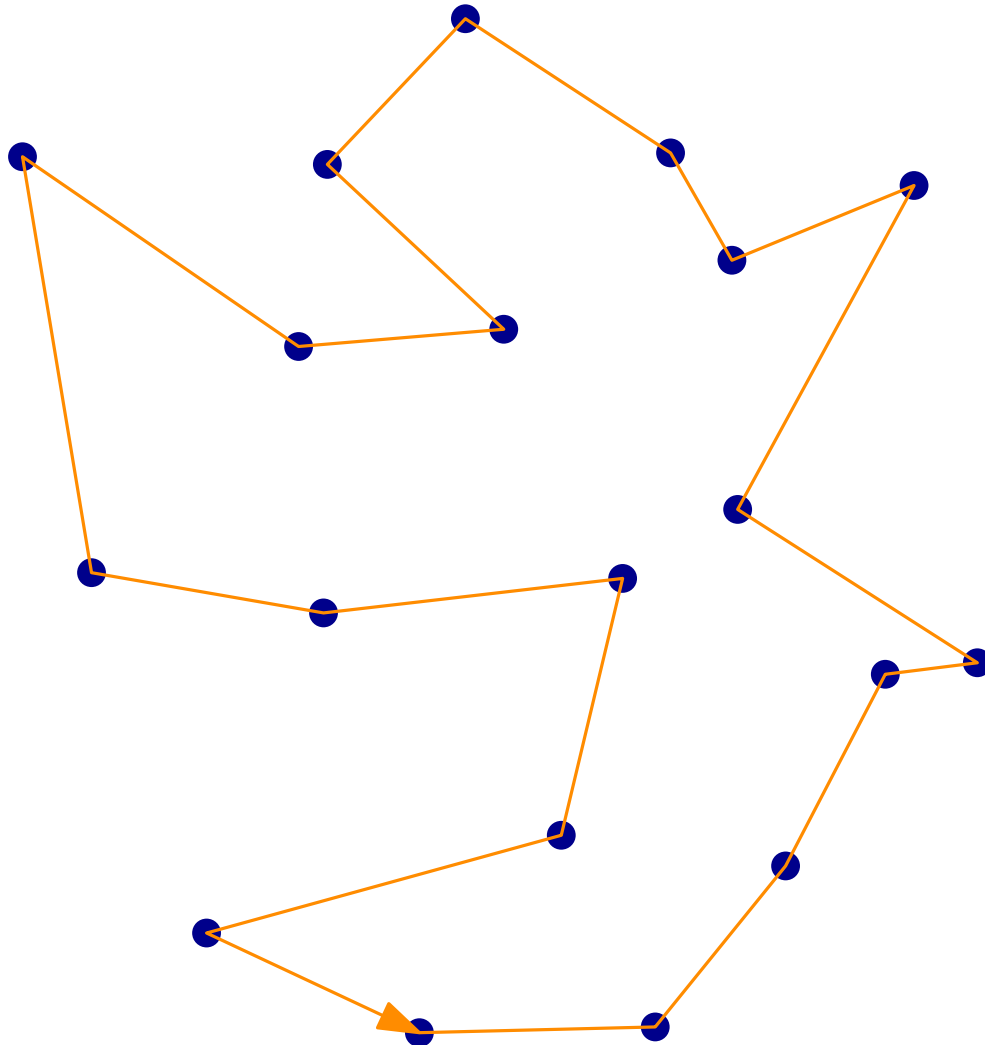


**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.





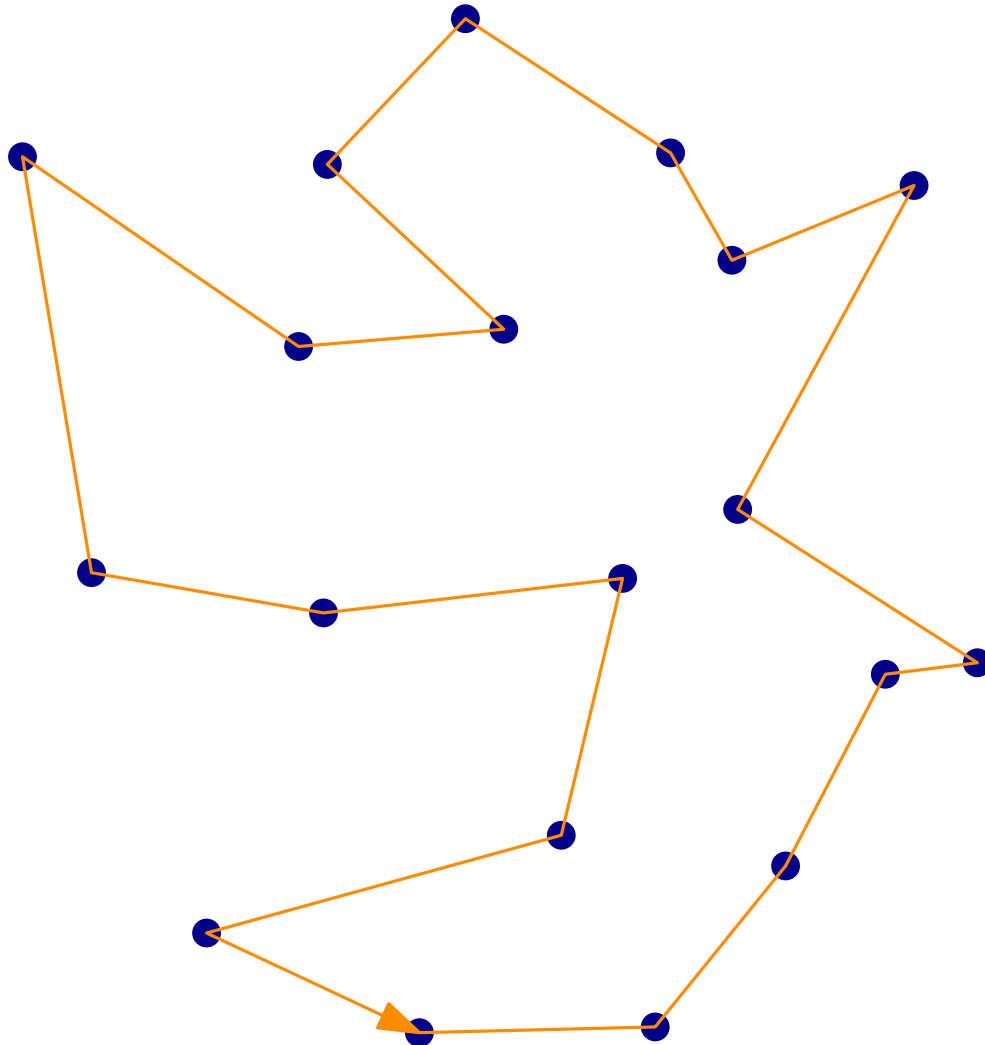
**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.





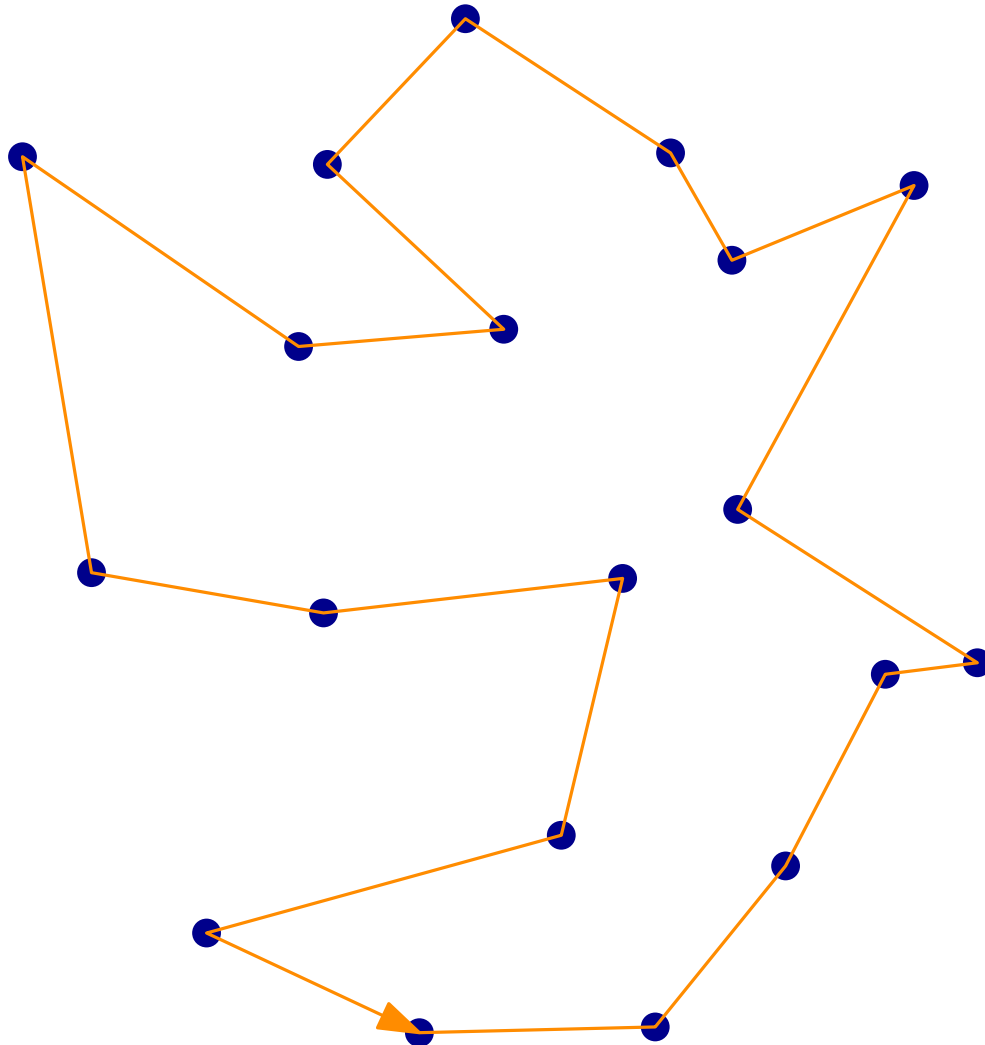
**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.

Best known algorithm  
needs roughly  $2^n$   
operations.





**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.



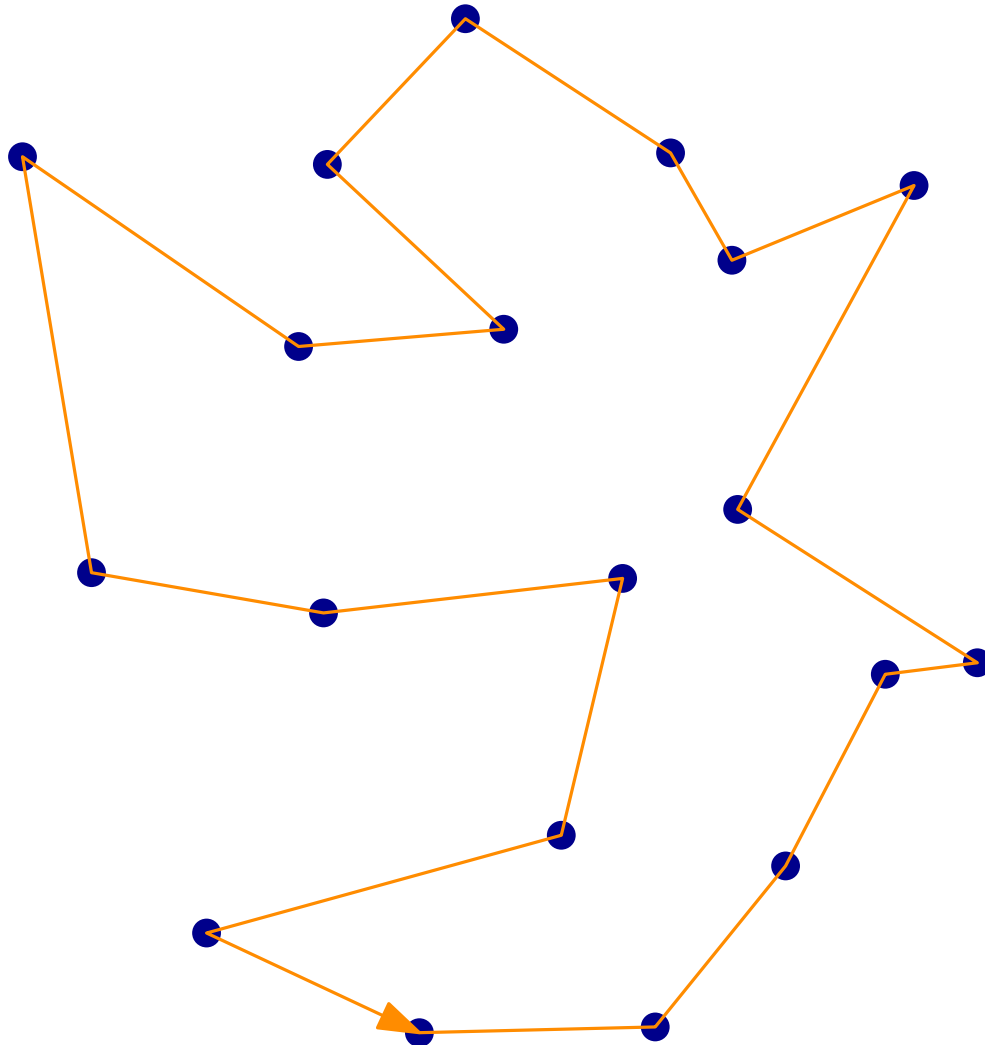
Best known algorithm  
needs roughly  $2^n$   
operations.

Nobody can prove that  
 $n^2$  operations is  
impossible.





**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.



Best known algorithm  
needs roughly  $2^n$   
operations.

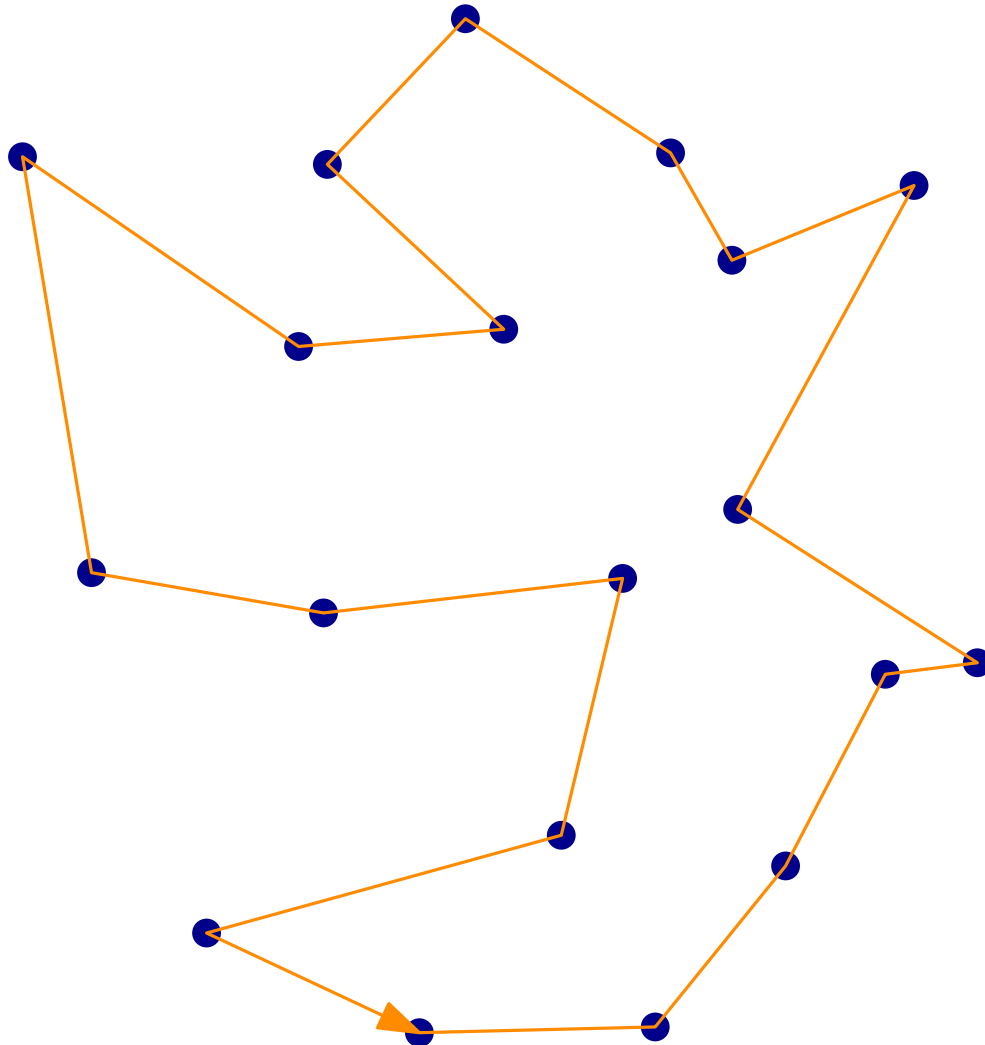
Nobody can prove that  
 $n^2$  operations is  
impossible.

Million-dollar question:

$$P = NP ?$$



**Travelling Salesman:** Given  $n$  points in the plane, find the shortest tour that visits all the points.



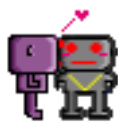
Best known algorithm needs roughly  $2^n$  operations.

Nobody can prove that  $n^2$  operations is impossible.

Million-dollar question:

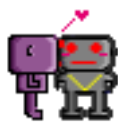
$$P = NP ?$$

There are problems for which we can prove that no algorithm exists.



---

We learnt a language for expressing computations (Python).



---

We learnt a language for expressing computations (Python).

We learnt about the process of writing and debugging a program.

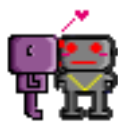


---

We learnt a language for expressing computations (Python).

We learnt about the process of writing and debugging a program.

We learnt about abstractions (data and functions).



---

We learnt a language for expressing computations (Python).

We learnt about the process of writing and debugging a program.

We learnt about abstractions (data and functions).

We learnt about breaking problems into smaller pieces, and testing parts of a program one-by-one.



---

We learnt a language for expressing computations (Python).

We learnt about the process of writing and debugging a program.

We learnt about abstractions (data and functions).

We learnt about breaking problems into smaller pieces, and testing parts of a program one-by-one.

Remember that you can program to find answers to questions.



---

We learnt a language for expressing computations (Python).

We learnt about the process of writing and debugging a program.

We learnt about abstractions (data and functions).

We learnt about breaking problems into smaller pieces, and testing parts of a program one-by-one.

Remember that you can program to find answers to questions.

THE END