

# Dynamical Tadpoles, Stringy Cobordism and the SM from Spontaneous Compactification



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*Seminar Series on String Phenomenology, 27th April 2021*

# Plan of the talk

- Introduction and motivation

Dynamical tadpoles and the swampland cobordism conjecture

- Two tadpole lessons from string theory examples

Conifold

3-form flux models

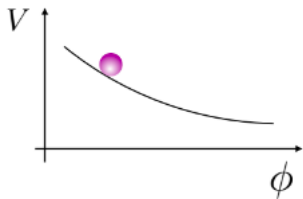
Magnetized branes

non susy 10d  $USp(32)$  theory

SM from spontaneous compactification

- Conclusions

# Dynamical tadpoles

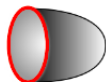


- theories sitting on the **slope** of some scalar potential  
⇒ dynamical tadpoles (as opposed to topological tadpoles)
- properties of the resulting **spacetime-dependent** solutions?

# Cobordism defects

- n-dim manifold can/cannot be the boundary of (n+1)-dim manifold

$S^1$  is trivial

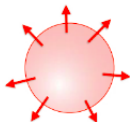


Point is non-trivial

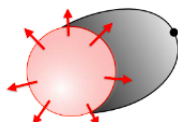
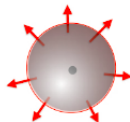


- cobordism charge can be removed by localized sources

$S^2$  with a U(1)  $F_2$  flux can't just shrink



Flux removed by monopole



# Cobordism defects

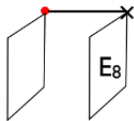
- swampland cobordism conjecture

[McNamara Vafa]

$\Omega_{QG} = 0$  related to no global symmetries

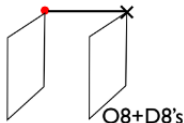
- examples

I I dM-theory



Horava-Witten  
boundary

Type IIA



Type I'

Type IIB on  $S^1$   
With -1  $SL(2, Z)$  WL



Half  $T^2/Z_2$

O7+D7s

Etc...

- not all defects are known

# Two lessons

## Finite Distance:

The running solution extends at most a distance  $\Delta$  scaling as

$$\Delta^{-n} \sim \mathcal{T}$$

with the strength of the tadpole  $\mathcal{T}$ .

## Dynamical Cobordism:

Spacetime is cut off at this distance by the cobordism defect of the swampland cobordism conjecture.

# $AdS_5 \times T^{1,1}$

- $AdS_5 \times T^{1,1}$  with **N** units of RR 5-form flux

[Klebanov Witten]

near horizon limit of N D3's at conifold singularity  
 $T^{1,1} = S^2 \times S^3$  is 5d base of 6d cone

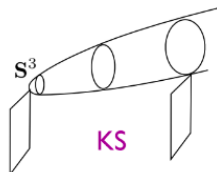
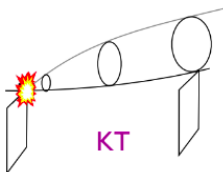
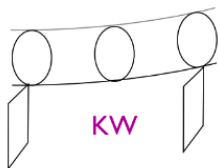
- Add **M** units of RR 3-form flux on  $S^3$

[Klebanov Tseytlin]

running  $T^{1,1}$  geometry and singularity at finite distance  $r_0$

- Smooth out the singularity by finite size  $S^3$

[Klebanov Strassler]

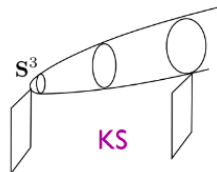
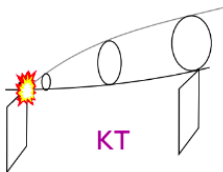
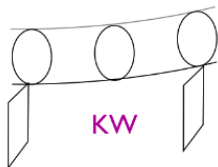


# $\text{AdS}_5 \times \mathbb{T}^{1,1}$

- dilaton tadpole  $V(\phi) \sim M^2 e^\phi$        $\nabla^2 \phi = -e^{-6q-\phi}(\partial\Phi)^2 + e^{-14q+\phi} M^2$
- solved by running NSNS axion  $\Phi = 3g_s M \log(r/r_0)$

**Finite Distance**     $\Delta^{-1} \sim M^2 e^\phi \sim \mathcal{T}$

**Dynamical Cobordism**





# 3-form flux models

- type IIB on  $T^5$  with RR 3-form flux  $F_3 = N dx^1 dx^2 dx^3$
- dilaton tadpole  $\nabla^2 \phi \sim e^\phi (F_3)^2 - e^{-\phi} (H_3)^2$   
solved by  $H_3 = N dy^1 dy^2 dy^3 \Rightarrow \Phi \sim Ny$

## Finite Distance

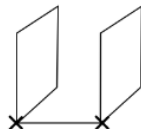
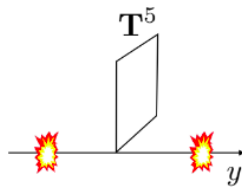
$$ds_{10}^2 = Z^{-\frac{1}{2}} ds_4^2 + Z^{\frac{1}{2}} R^2 (dz^1 d\bar{z}^1 + dz^2 d\bar{z}^2 + dz^3 d\bar{z}^3)$$

$$\text{with } -\tilde{\nabla}^2 Z = \frac{g_s}{6} (F_3)^2 \Rightarrow Z = 1 - \frac{g_s}{12} (F_3)^2 y^2$$

$$\text{singularities at } y^{-2} = \frac{1}{12} g_s (F_3)^2 \Rightarrow \Delta^{-2} \sim \mathcal{T}$$

## Dynamical Cobordism

singularities removed by O3's (possibly with D3's)



# Magnetized branes

- type IIB on  $T^2_{(1)} \times T^2_{(2)}$  with O7's and D7's transverse to  $T^2_{(1)}$
- Add  $\mathbf{M}$  units of D7 worldvolume magnetic flux on  $T^2_{(2)}$   
susy breaking and tadpole for dilaton and  $T^2_{(2)}$  Kähler modulus
- Solve by magnetic field  $F_2 = F(dz_2 d\bar{z}_2 - dz_3 d\bar{z}_3)$

## Finite Distance

lift to F-theory  $G_4 \sim F_2 \wedge \omega_2$  singular warp factor  $\Delta^{-2} \sim (F_2)^2 \sim \mathcal{T}$

## Dynamical Cobordism

compactification on extra  $T_2/Z_2$  with additional O7's and D7's

# 10d non susy $USp(32)$ string

- orientifold of IIB with  $O9^+$  and  $32 \overline{D9}$ 's

[Sugimoto]

- dilaton tadpole

$$S_E = \frac{1}{2\kappa^2} \int d^{10}x \sqrt{-G} \left[ R - \frac{1}{2}(\partial\phi)^2 \right] - T_9^E \int d^{10}x \sqrt{-G} \quad 64 e^{\frac{3\phi}{2}}$$

- running solution  $\phi = \frac{3}{4}\alpha_E y^2 + \frac{2}{3} \log |\sqrt{\alpha_E} y| + \phi_0$  [Dudas Mourad]

$$ds_E^2 = |\sqrt{\alpha_E} y|^{\frac{1}{9}} e^{-\frac{\alpha_E y^2}{8}} \eta_{\mu\nu} dx^\mu dx^\nu + |\sqrt{\alpha_E} y|^{-1} e^{-\frac{3\phi_0}{2}} e^{-\frac{9\alpha_E y^2}{8}} dy^2$$

singularities at  $y = 0, \infty$  separated by

**Finite Distance**  $\Delta \sim \int_0^\infty \sqrt{g_{yy}} dy \sim e^{-\frac{3\phi_0}{4}} \alpha_E^{-\frac{1}{2}} \Rightarrow \Delta^{-2} \sim \mathcal{T}$

# 10d non susy $USp(32)$ string

## Dynamical Cobordism

strong coupling defect, that is able to gap chiral non anomalous content

- Solve by magnetization:  $T^6/(Z^2 \times Z^2)$  with  $O9^+$  and 8  $O5_i^-$

obj.	$N_\alpha$	$(n_\alpha^1, m_\alpha^1)$	$(n_\alpha^2, m_\alpha^2)$	$(n_\alpha^3, m_\alpha^3)$
$O9^+$	32	(1, 0)	(1, 0)	(1, 0)
$O5_1^-$	-32	(1, 0)	(0, 1)	(0, -1)
$O5_2^-$	-32	(0, 1)	(1, 0)	(0, -1)
$O5_3^-$	-32	(0, 1)	(0, -1)	(1, 0)
D9	16	(-1, 1)	(-1, 1)	(-1, 1)
D9'	16	(-1, -1)	(-1, -1)	(-1, -1)

$n_\alpha^i$  wrapping on  $T_i^2$

$m_\alpha^i$  magnetic flux  
on  $T_i^2$

# SM from spontaneous compactification

- type I on  $(T^2 \times T^2)/Z^2$  with 32 magnetized D9's and O9, O5's

$N_\alpha$	$(n_\alpha^1, m_\alpha^1)$	$(n_\alpha^2, m_\alpha^2)$
$N_{a+d} = 6 + 2$	$(1, 3)$	$(1, -3)$
$N_{h_1} = 4$	$(1, -3)$	$(1, -4)$
$N_{h_2} = 4$	$(1, -4)$	$(1, -3)$
40	$(0, 1)$	$(0, -1)$

$n_\alpha^i$  wrapping on  $T_i^2$

$m_\alpha^i$  magnetic flux on  $T_i^2$

T dual to intersecting D7's

RR tadpoles  $\sum_\alpha N_\alpha n_\alpha^2 n_\alpha^3 = 16 \quad \sum_\alpha N_\alpha m_\alpha^2 m_\alpha^3 = -16$

non susy  $\Rightarrow$  dynamical tadpoles for inverse areas of  $T^2$ 's

# SM from spontaneous compactification

- Solve by magnetization along two of the 6d spacetime dimensions

$$\Rightarrow (T^2 \times T^2 \times T^2) / (Z^2 \times Z^2) \quad \text{with extra O5's, D5's}$$

$N_\alpha$	$(n_\alpha^1, m_\alpha^1)$	$(n_\alpha^2, m_\alpha^2)$	$(n_\alpha^3, m_\alpha^3)$
$N_{a+d} = 6 + 2$	(1, 3)	(1, -3)	(1, 0)
$N_b = 2$	(0, 1)	(1, 0)	(0, 1)
$N_c = 2$	(-1, 0)	(0, -1)	(0, 1)
$N_{h_1} = 2$	(1, -3)	(1, -4)	(2, -1)
$N_{h_2} = 2$	(1, -4)	(1, -3)	(2, -1)
40	(0, 1)	(0, -1)	(0, 1)

RR tadpoles

$$\sum_\alpha N_\alpha n_\alpha^1 n_\alpha^2 n_\alpha^3 = 16$$

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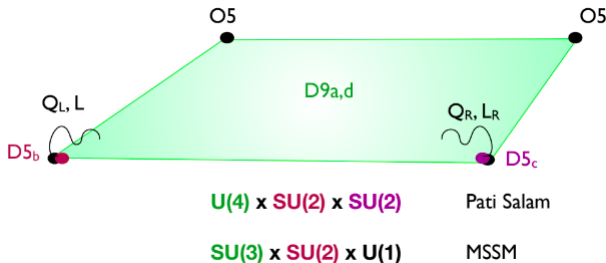
$$\sum_\alpha N_\alpha m_\alpha^1 m_\alpha^2 n_\alpha^3 = -16$$

$$\text{susy} \quad \chi_1 = \chi_2 \quad \chi_3 = \frac{14\chi_1}{1-12\chi_1^2} \quad \Rightarrow \quad \text{no dynamical tadpoles}$$

# SM from spontaneous compactification

3-family MSSM-like spectrum

[Marchesano Shiu]



Note that all MSSM but gluons/inos arise from cobordism branes

# Conclusions

- We have studied the properties of space-dependent solutions in theories with dynamical tadpoles
- Two lessons: Finite Distance and Dynamical Cobordism
- Many open questions
  - Time-dependent backgrounds
  - More non susy examples
  - Links to other swampland conjectures
  - ...