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# THE FESTINA LENTE BOUND AND ITS PHENO IMPLICATIONS

Based on 2106.07650 with C.Vafa, T.Van Riet, G.Venken

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Miguel Montero

Harvard

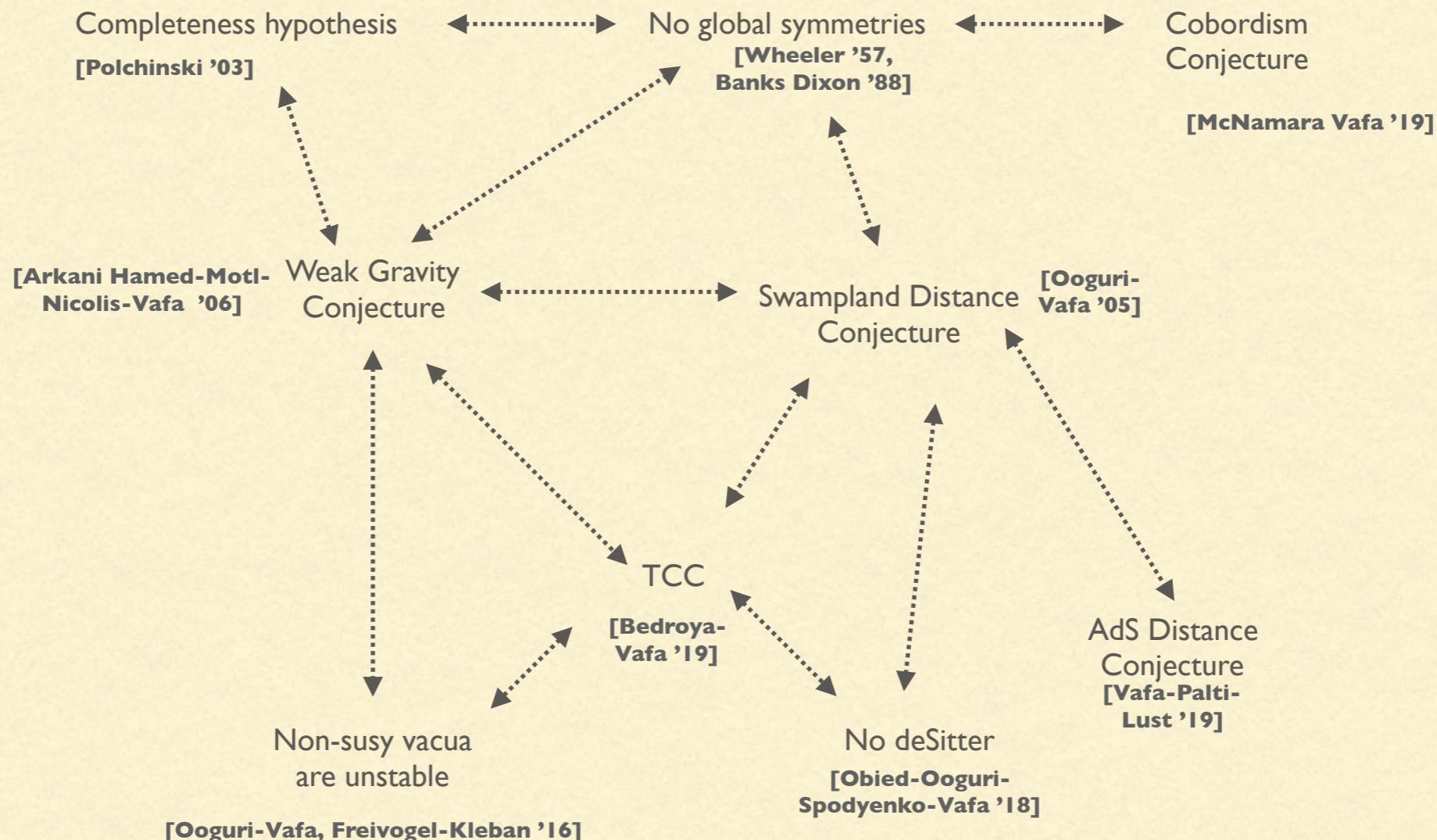
StringPheno seminars

July 6st 2021



# Main Swampland Idea: Ascertain **universal** features of quantum gravity

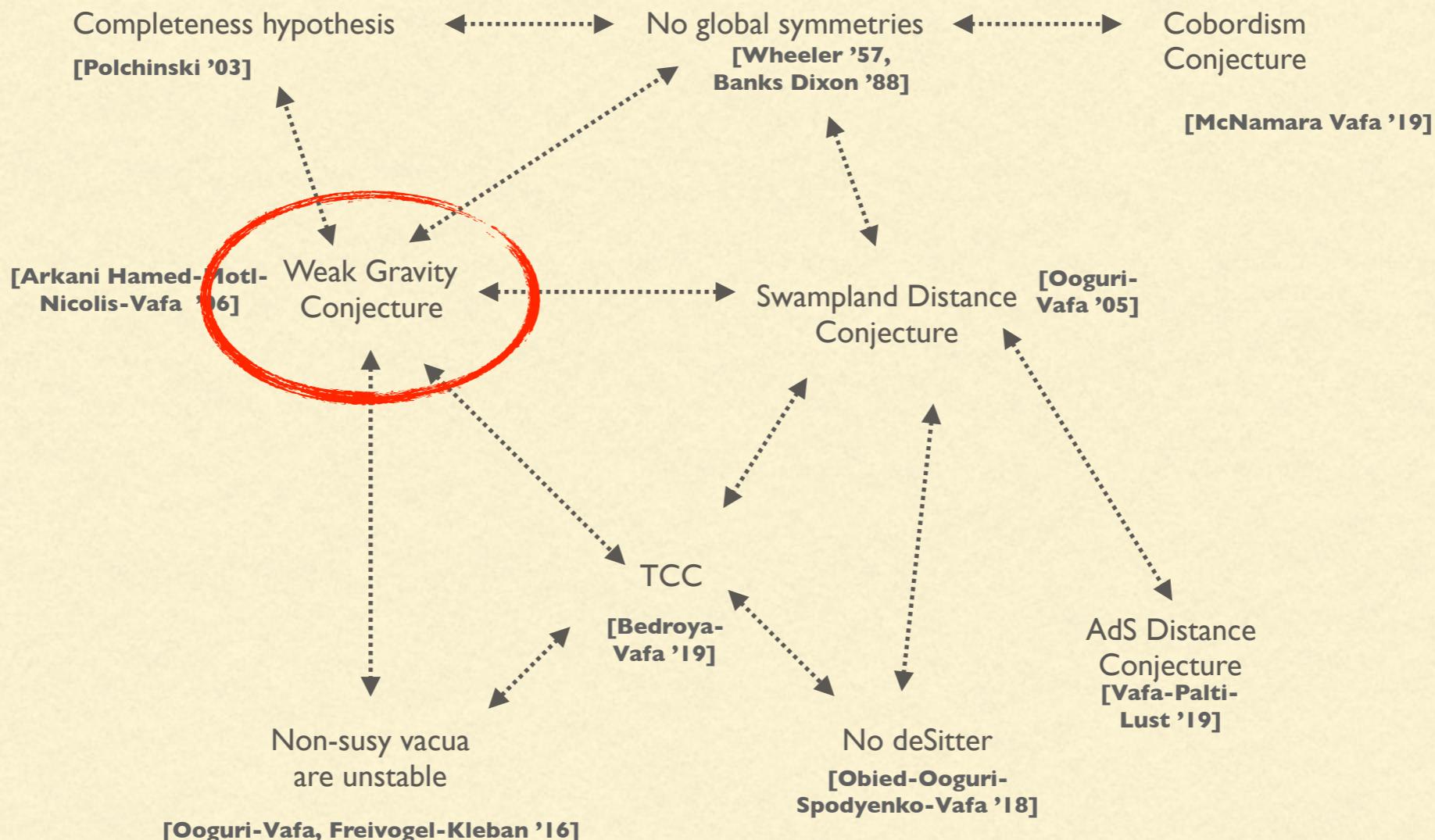
We organize this in a web of interconnected **conjectures**



[See e.g. 2102.01111 by van Beest, Calderon Infante, Mirfendereski, Valenzuela '21 for the most recent review]

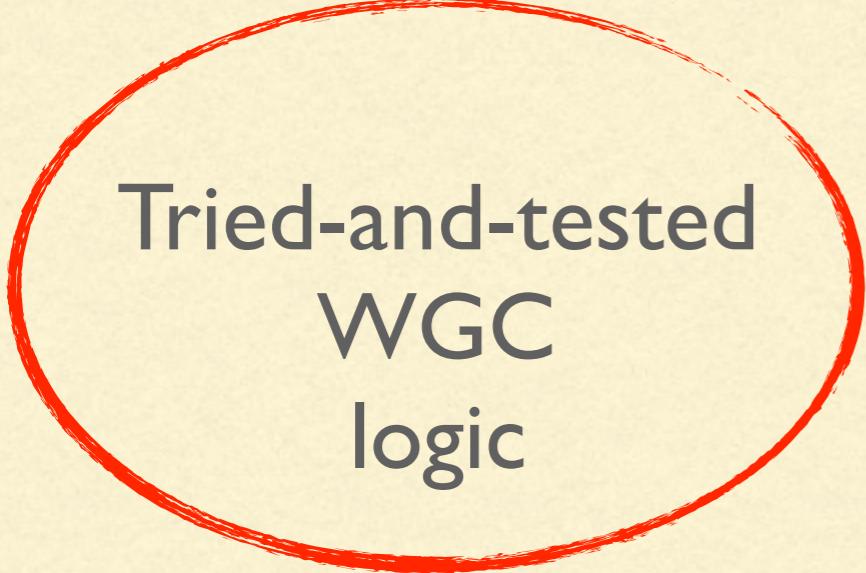
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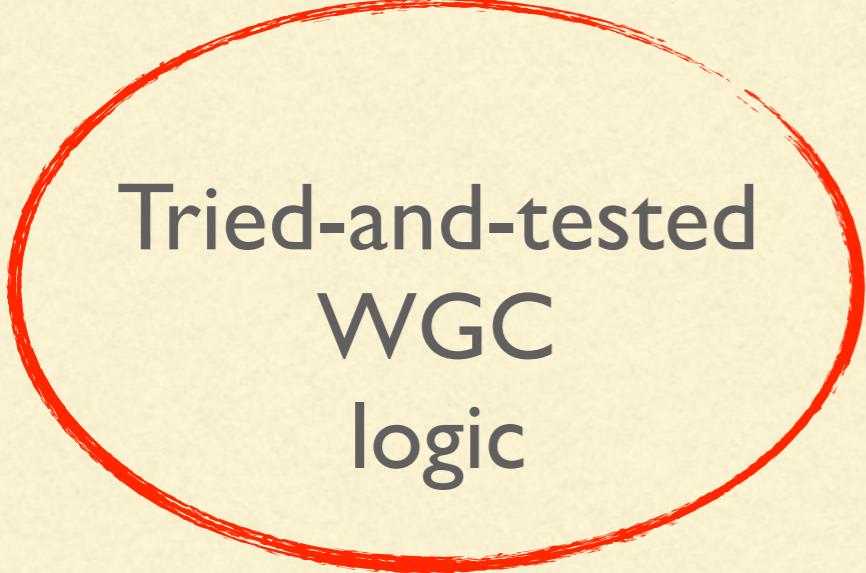
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Tried-and-tested  
WGC  
logic

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Tried-and-tested  
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Black Holes  
w. positive vacuum  
energy

Tried-and-tested  
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+

Black Holes  
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==

Festina Lente

[MM-Thomas Van Riet- Gerben Venken '19, MM-  
Cumrun Vafa-Thomas Van Riet- Gerben Venken]

## WGC:

[Arkani-Hamed, Motl, Nicolis, Vafa '06]

Any consistent QG with a  $U(1)$  **must** have charged states satisfying

$$m < \sqrt{2} q g M_P$$

We have **extensive** evidence for this in String Theory.

[Heidenreich-Reece-Rudelius '15,'16, MM-Shiu-Soler '16, Grimm-Palti-Valenzuela '18, Valenzuela-Gendler '20]

**Why?** Black holes decay **without becoming superextremal**

(No global syms, connection to cosmic censorship, ER=EPR)

[Santos-Horowitz '17,18, MM'18]

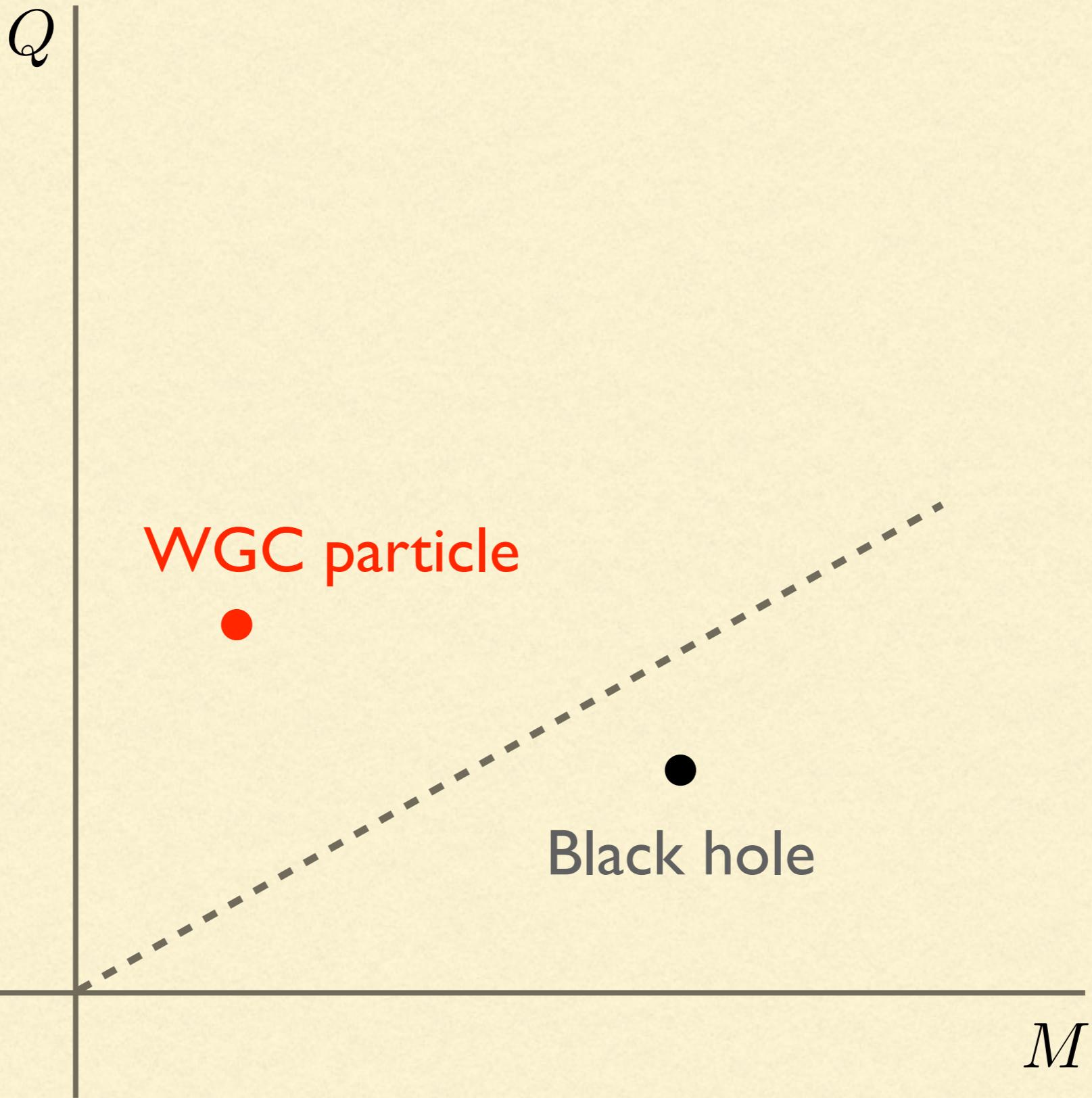
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$Q$



$M$





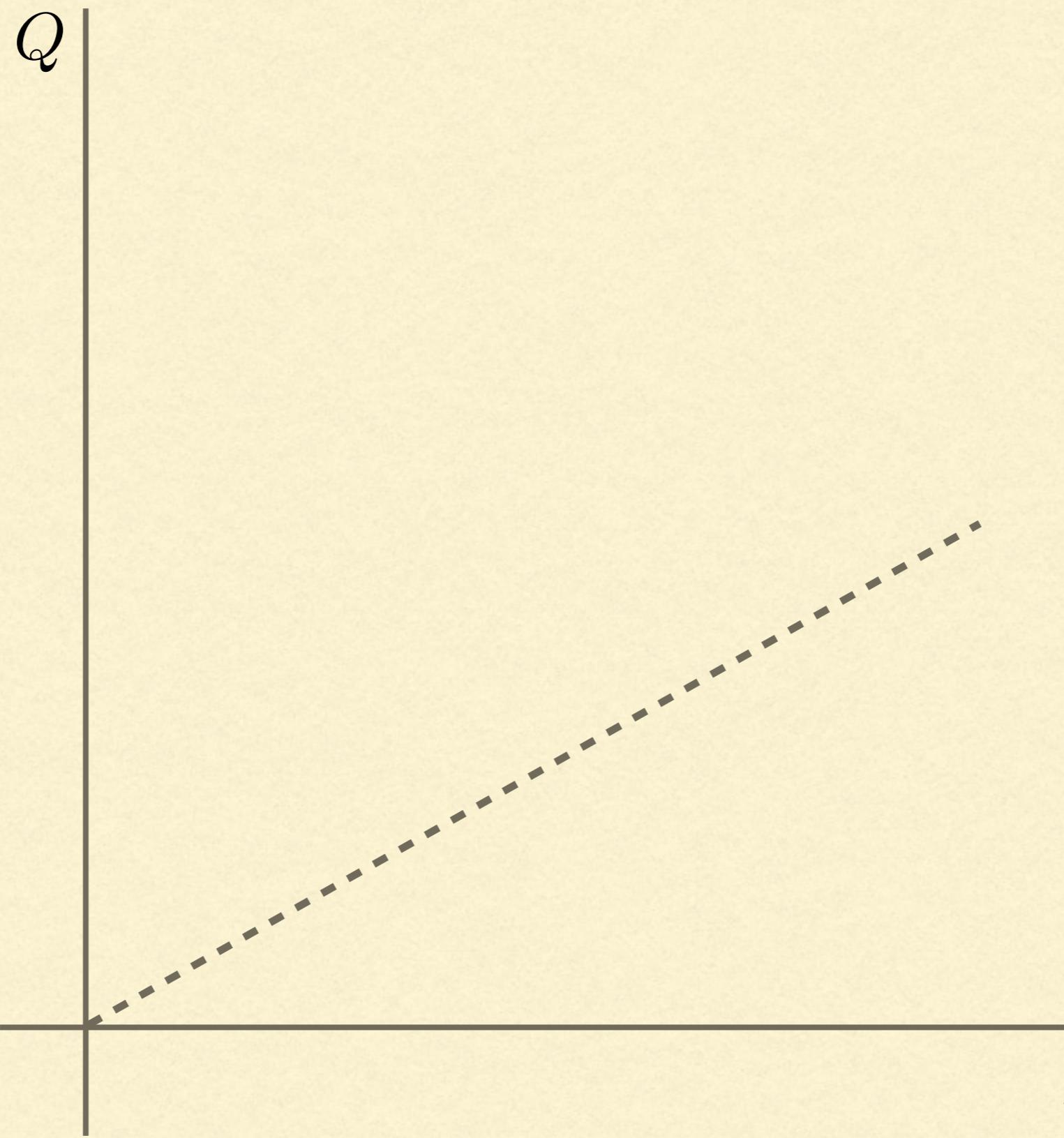
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So let's just do the same  
for **charged black**  
**holes in dS**

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$Q$

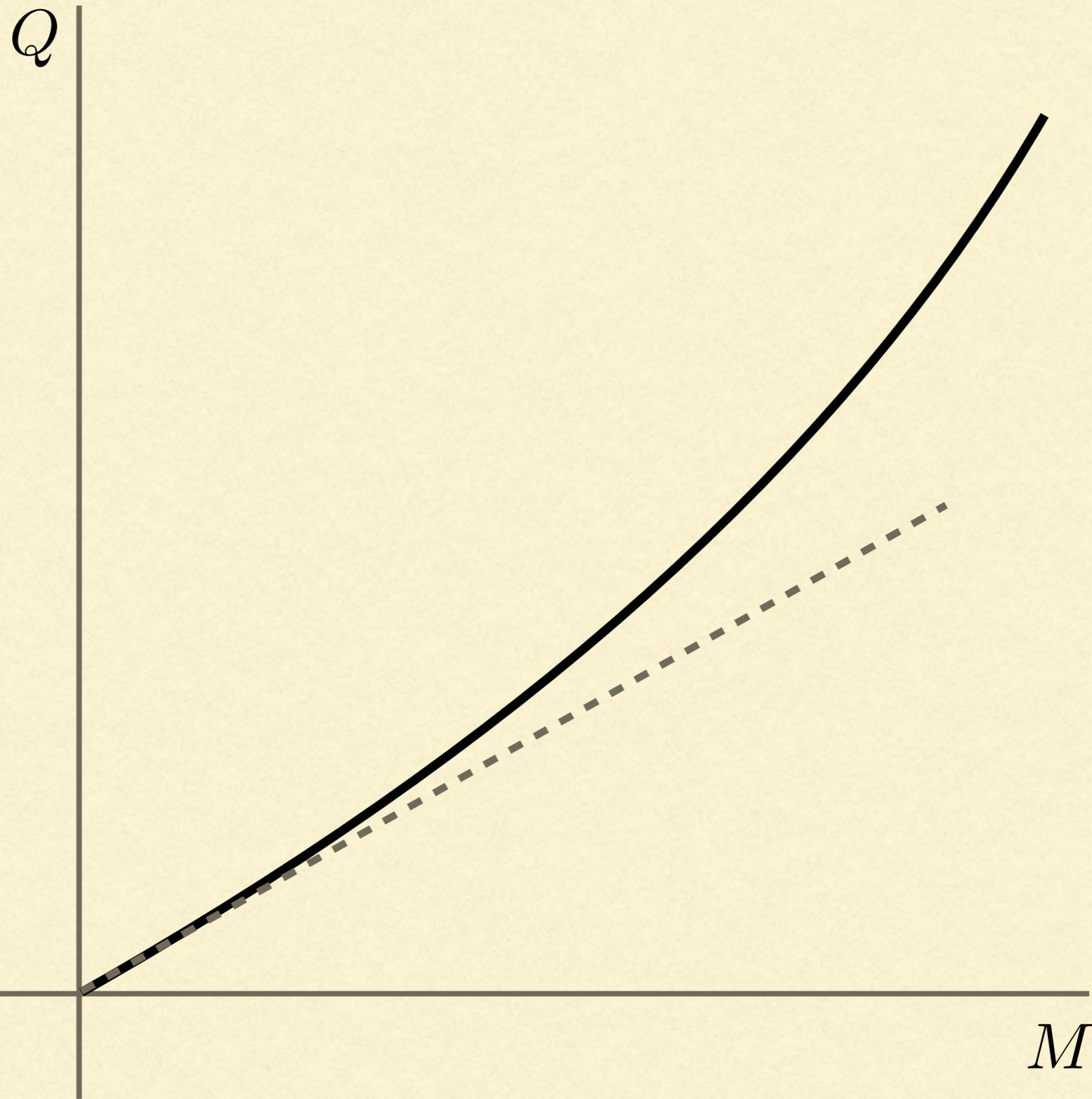


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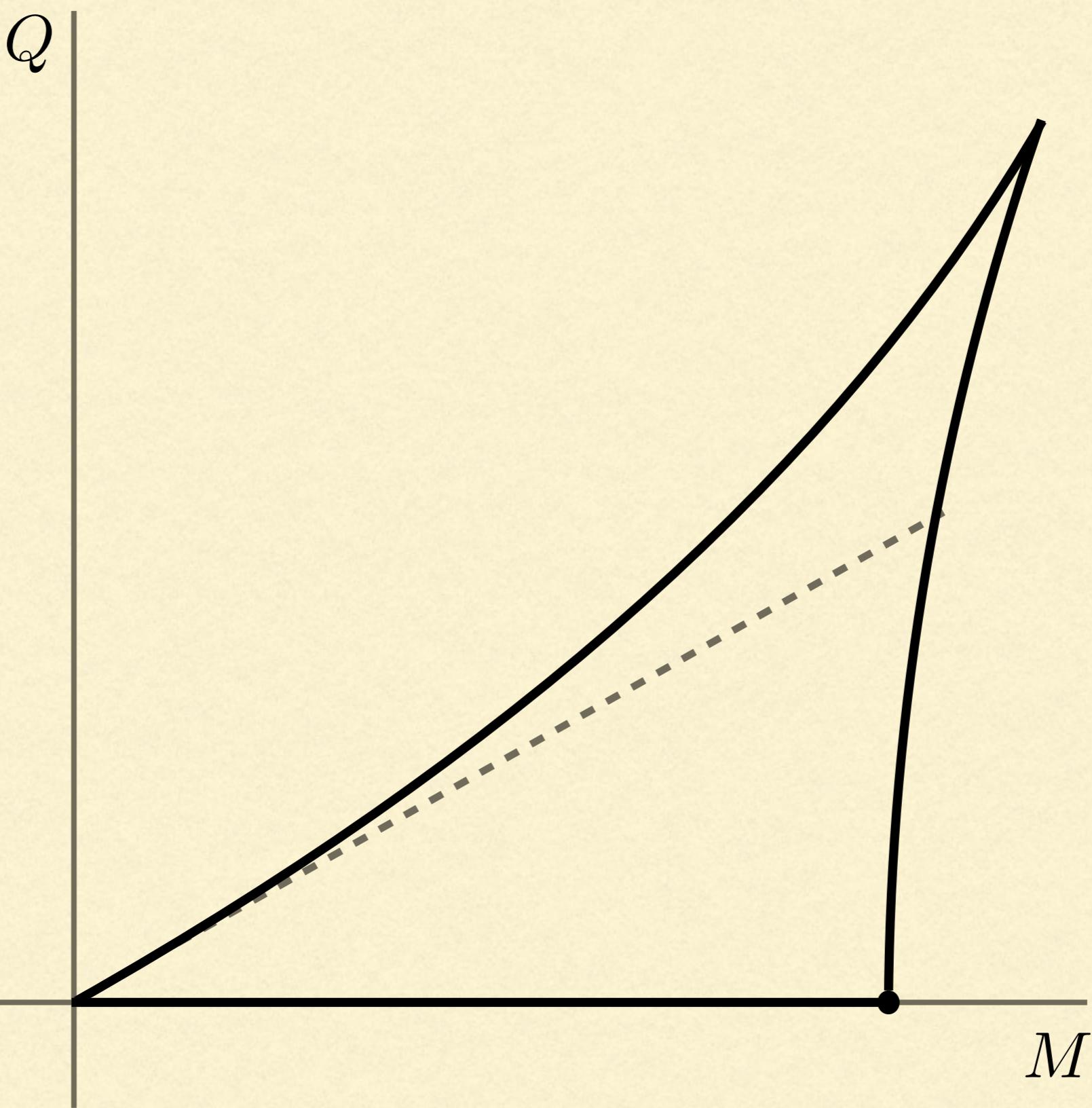
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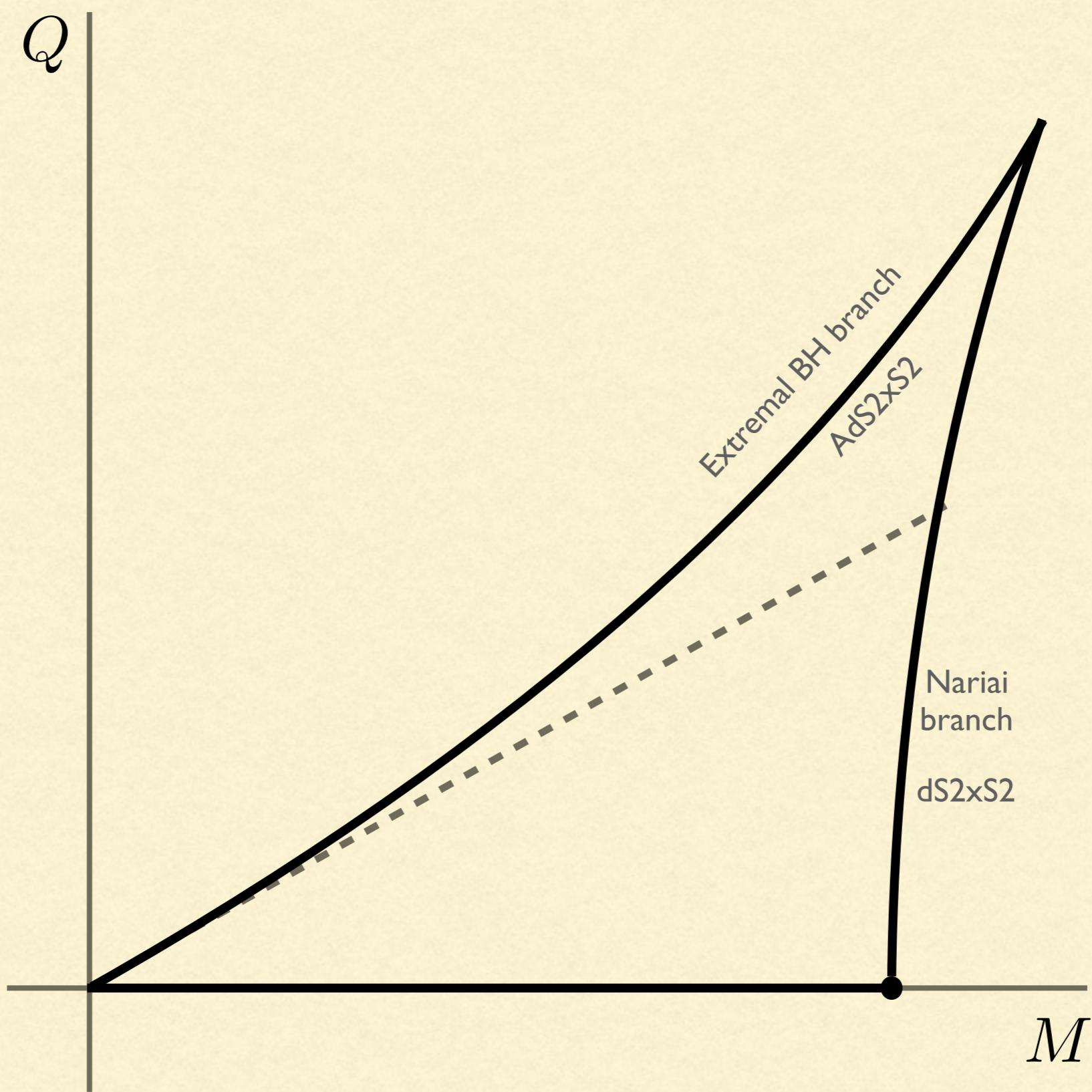
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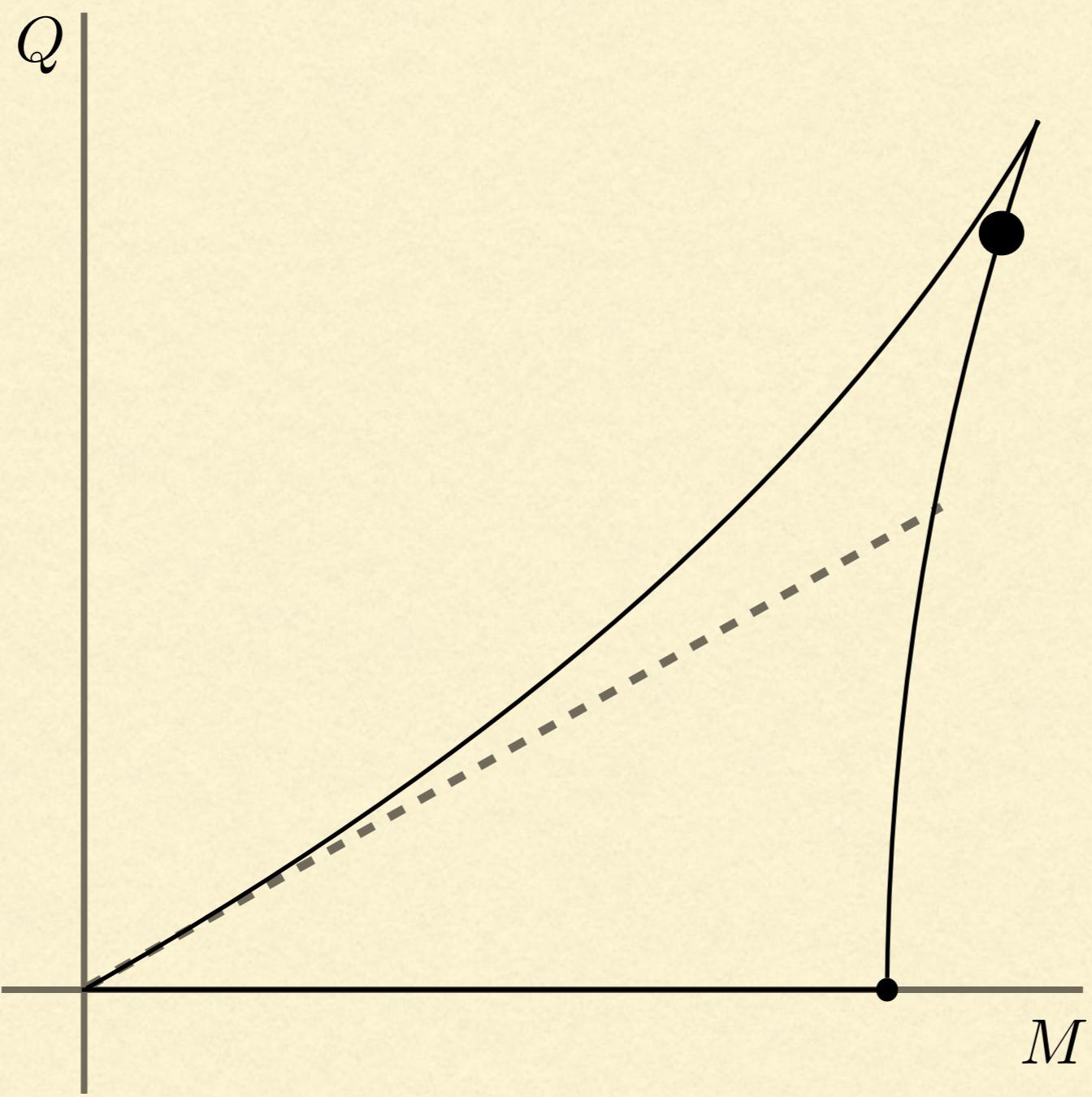


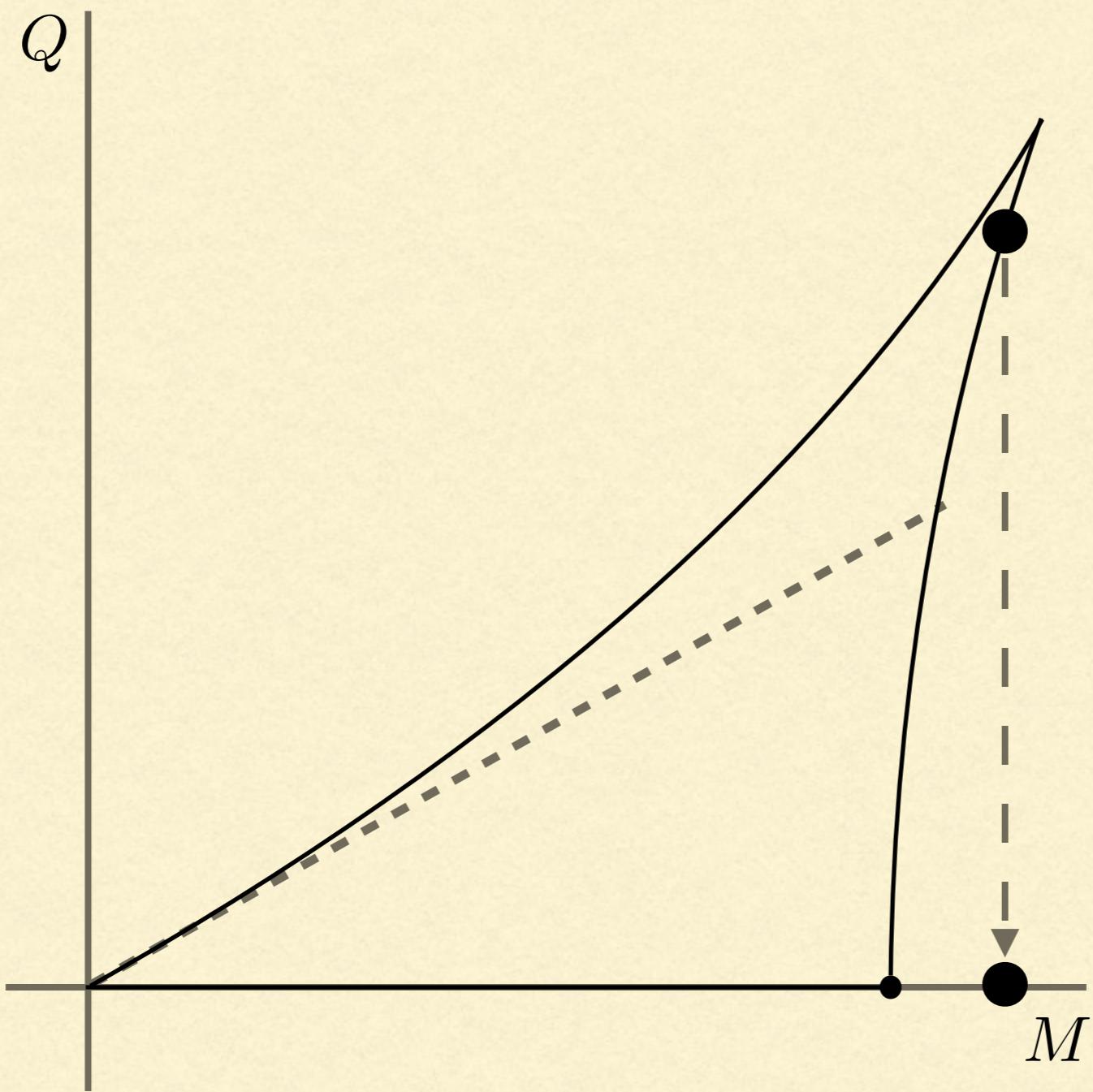
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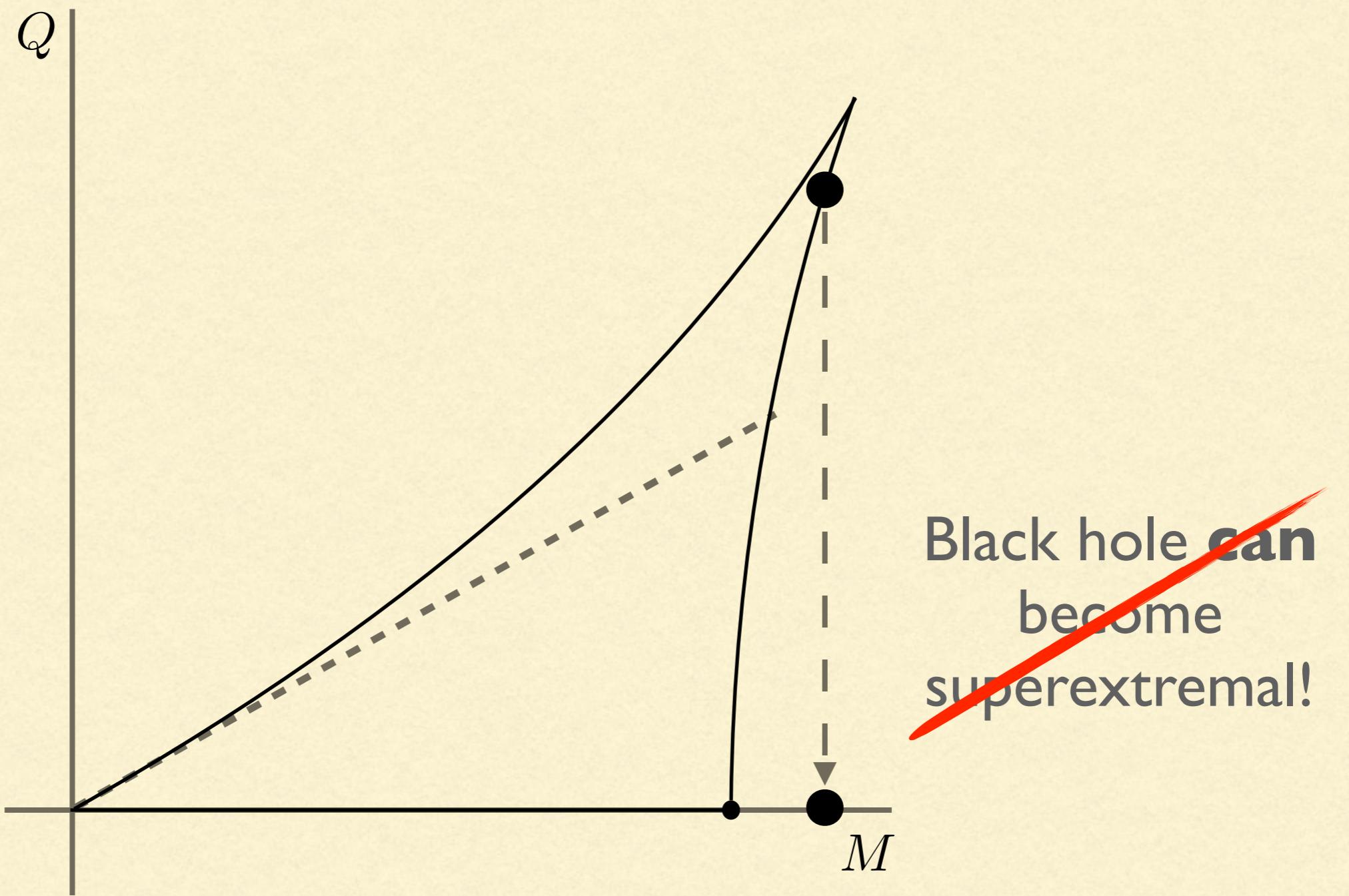








Black hole **can**  
become  
superextremal!



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To avoid overextremal decay of largest Nariai, we must impose

$$m^4 \gtrsim 2 g^2 V$$

for **every** particle in the theory.

This is the **Festina Lente** proposal (FL)  
(latin phrase that translates to “Hurry up, but do it calmly”)

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$$V = V(\phi), \quad g = g(\phi)$$

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but can be satisfied (in principle) in the bulk

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Rest of the talk: **consequences** and checks of the FL bound

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together imply

$$g^2 > \frac{3}{2} \left( \frac{H}{M_P} \right)^2$$

which also **follows** from a **magnetic FL argument**

[Huang, Li, Song '06, Antoniadis-Benakli '20]

(just demand  $q=1$  monopole is inside cosmo horizon)

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It also behaves well under **dimensional reduction**

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We find FL is satisfied **at large radius** and also on a stabilized minimum provided that

$$M_{\text{KK}} > V^{1/2}$$

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More generalizations (tower version, multi-U(1) fields) in the paper

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$$\Lambda \lesssim \frac{m^4}{24\pi\alpha M_P}$$

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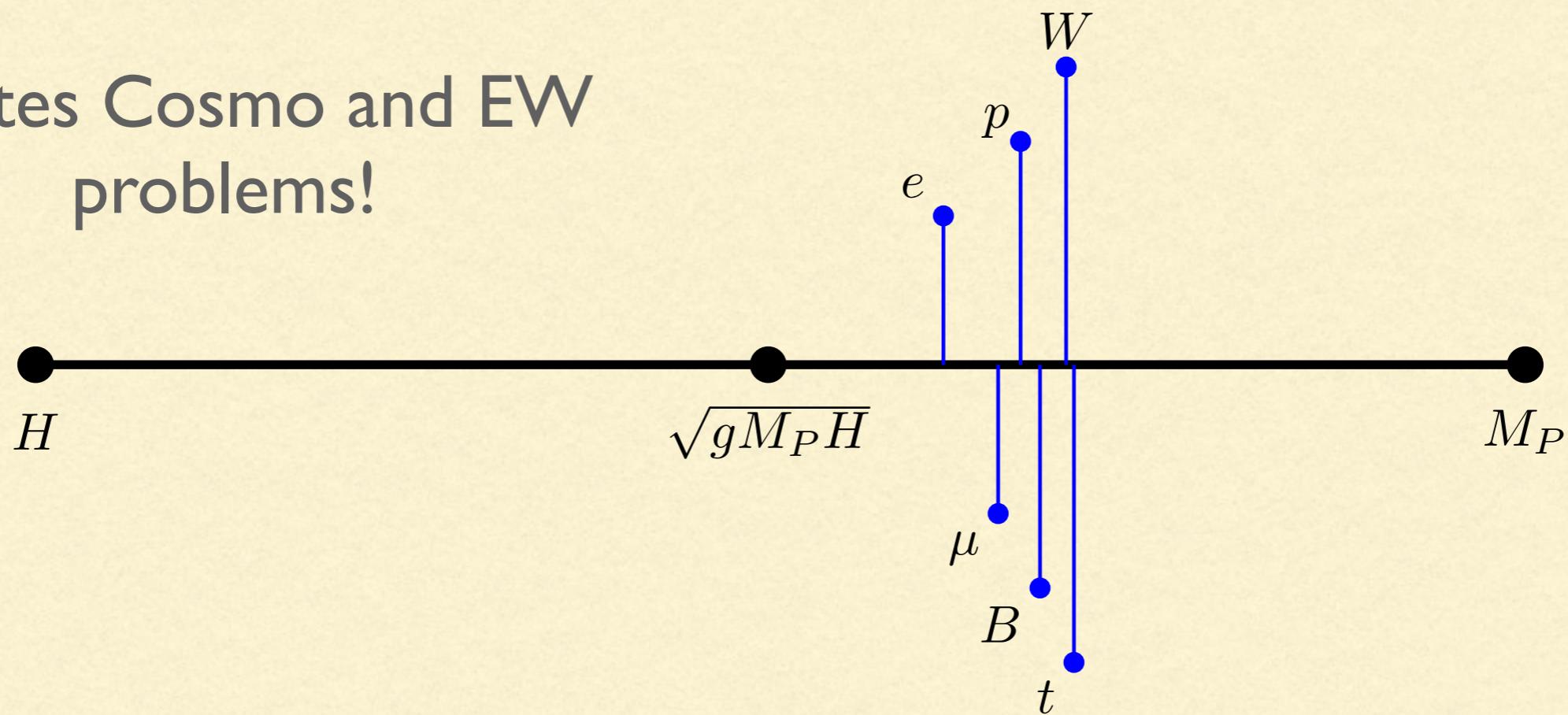
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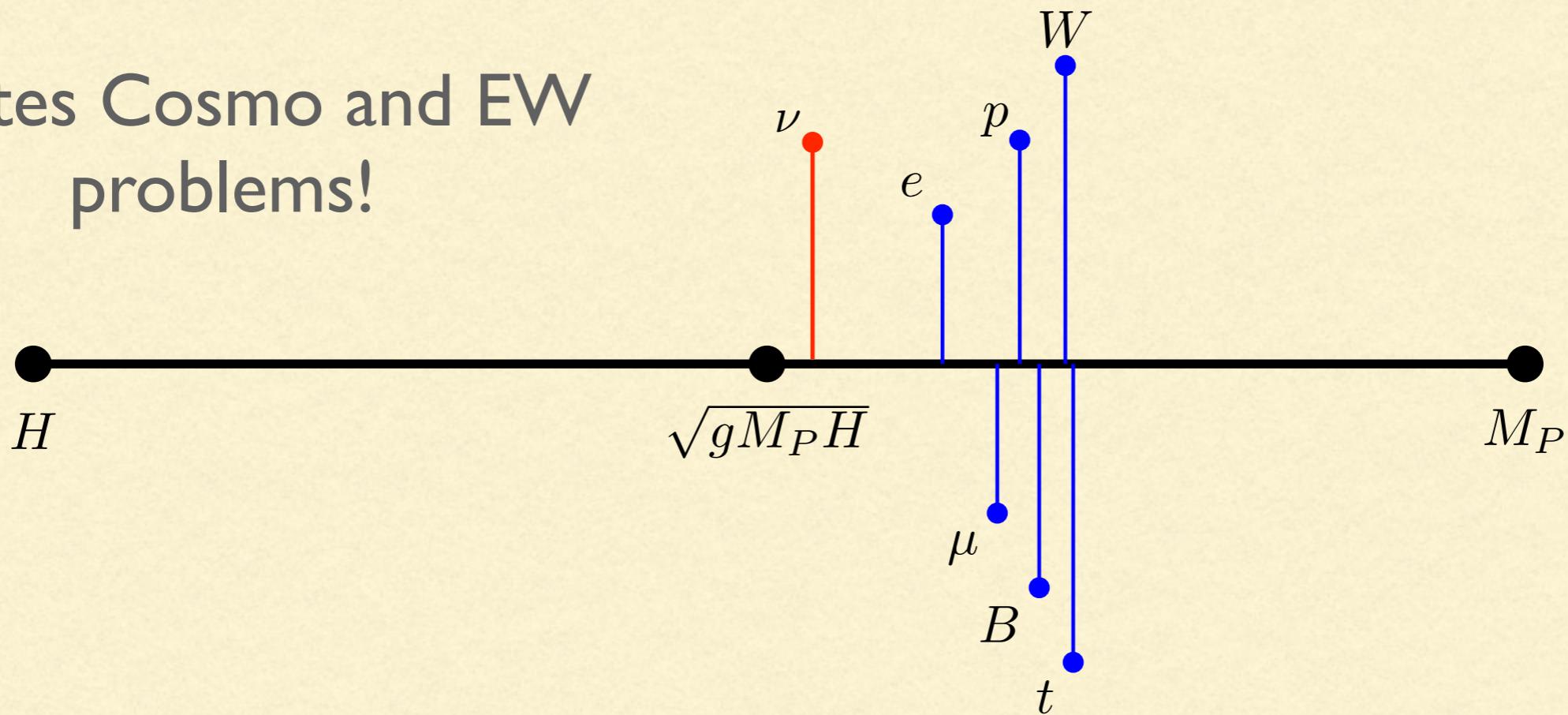
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Neutrinos **almost** saturate the bound, but uncharged.  
Coincidence?

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**Scenario** for FL microphysics that may also get neutrinos:

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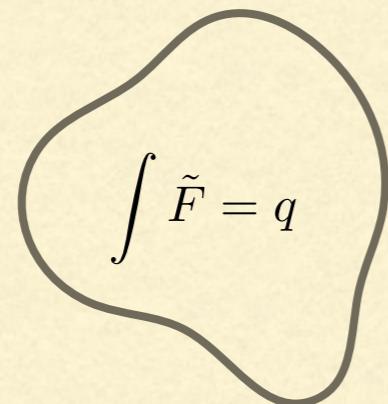
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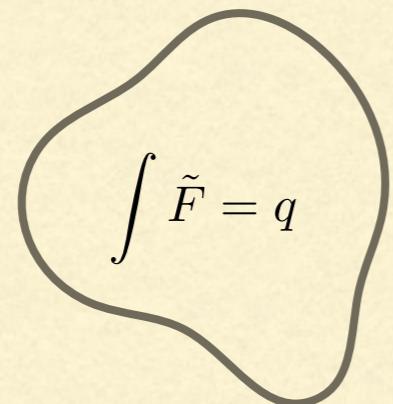


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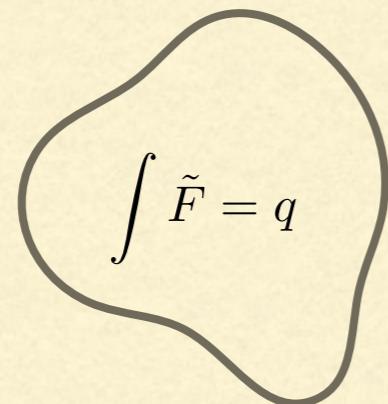
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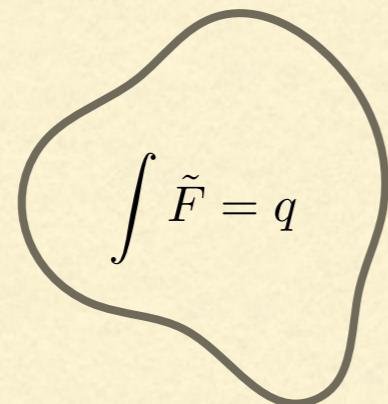
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$$T^{4/3} \gtrsim \Delta V > V$$

$$\frac{m^4}{V} \gtrsim g^\alpha$$

$$\int \tilde{F} = 0$$

this scenario also leads to **neutral states** of similar mass

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FL is also **in tension** with non-abelian gauge fields with

$$m \lesssim H$$

Predicts gauge fields must be **confined** or **Higgsed** above Hubble scale

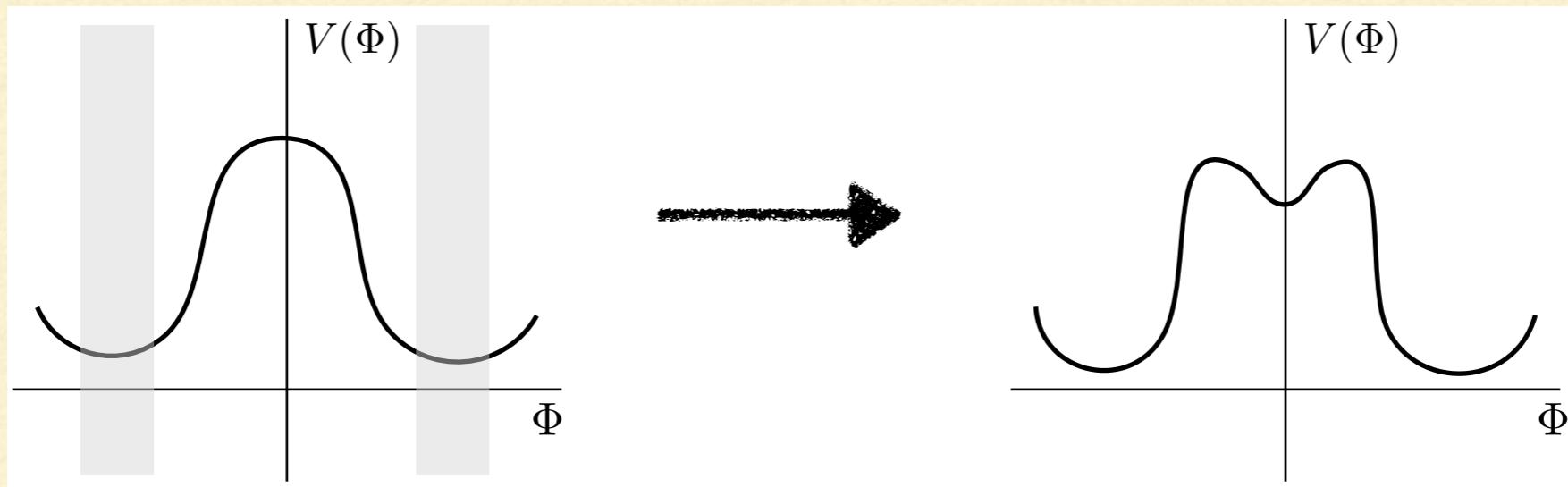
$$\Lambda_{QCD} \sim 150 \text{ MeV}$$

$$m_W \sim 80 \text{ GeV}$$

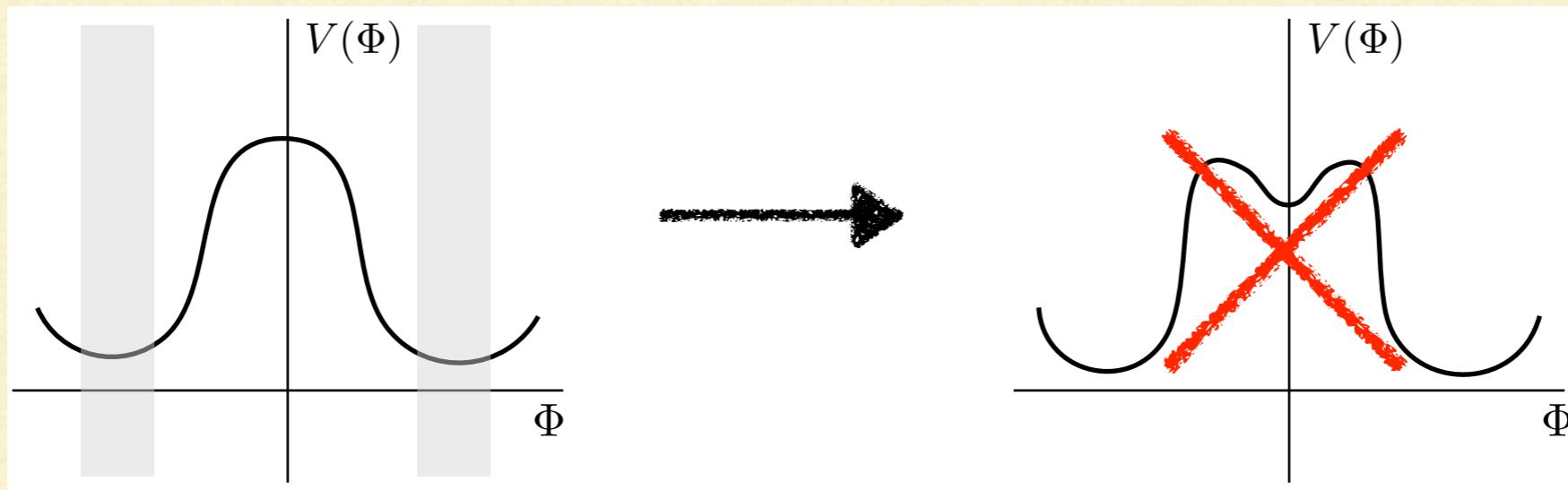
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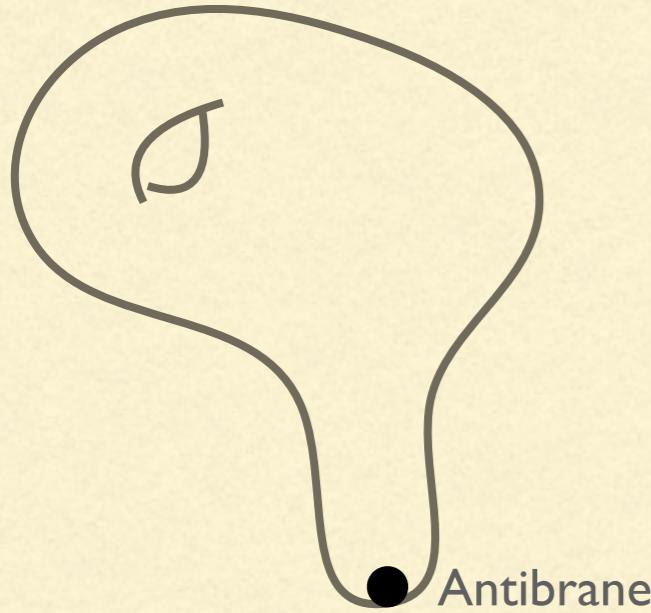


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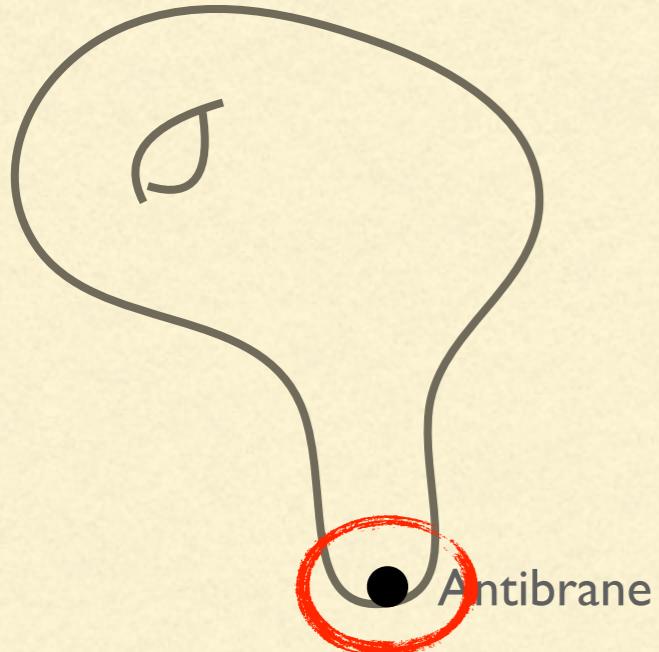


FL puts **bounds on the Higgs potential**

(Results compatible w. Ibañez, Gonzalo '18 from compactification of SM without Higgs to AdS3)



Finally, a few words about **antibrane uplift scenarios**

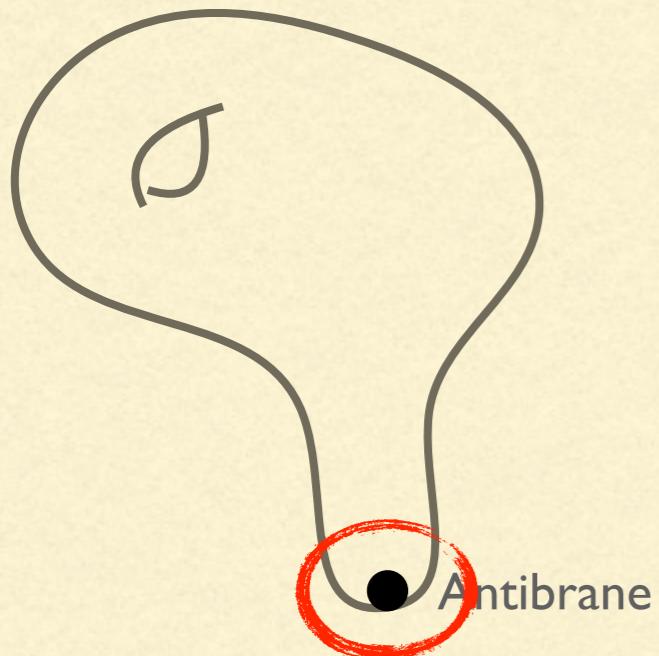


## Finally, a few words about **antibrane uplift scenarios**

Decoupled from the rest of the world

$$m^4 \gtrsim 2 g^2 V \quad \text{No } M_p \text{ in the formula!}$$

(with some assumptions) there is a **flat-space** version of FL



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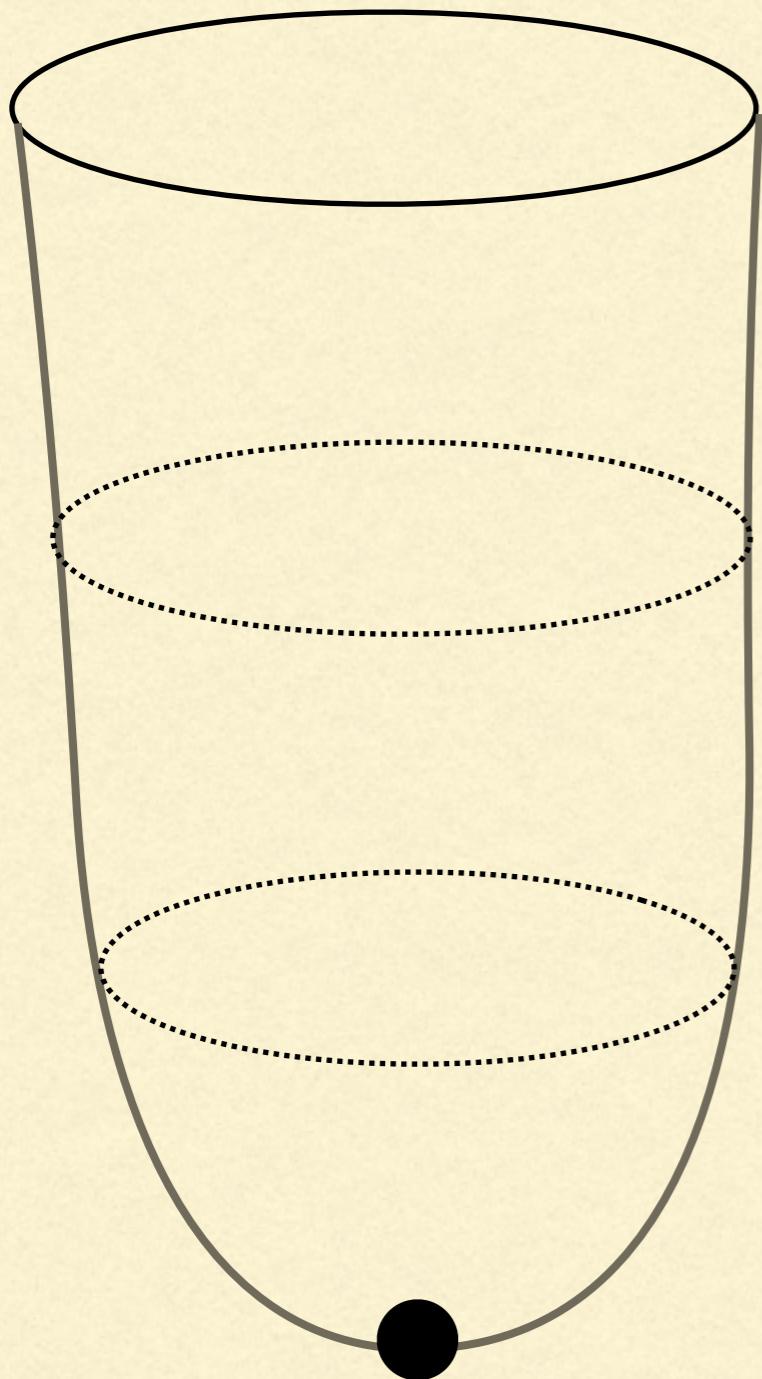
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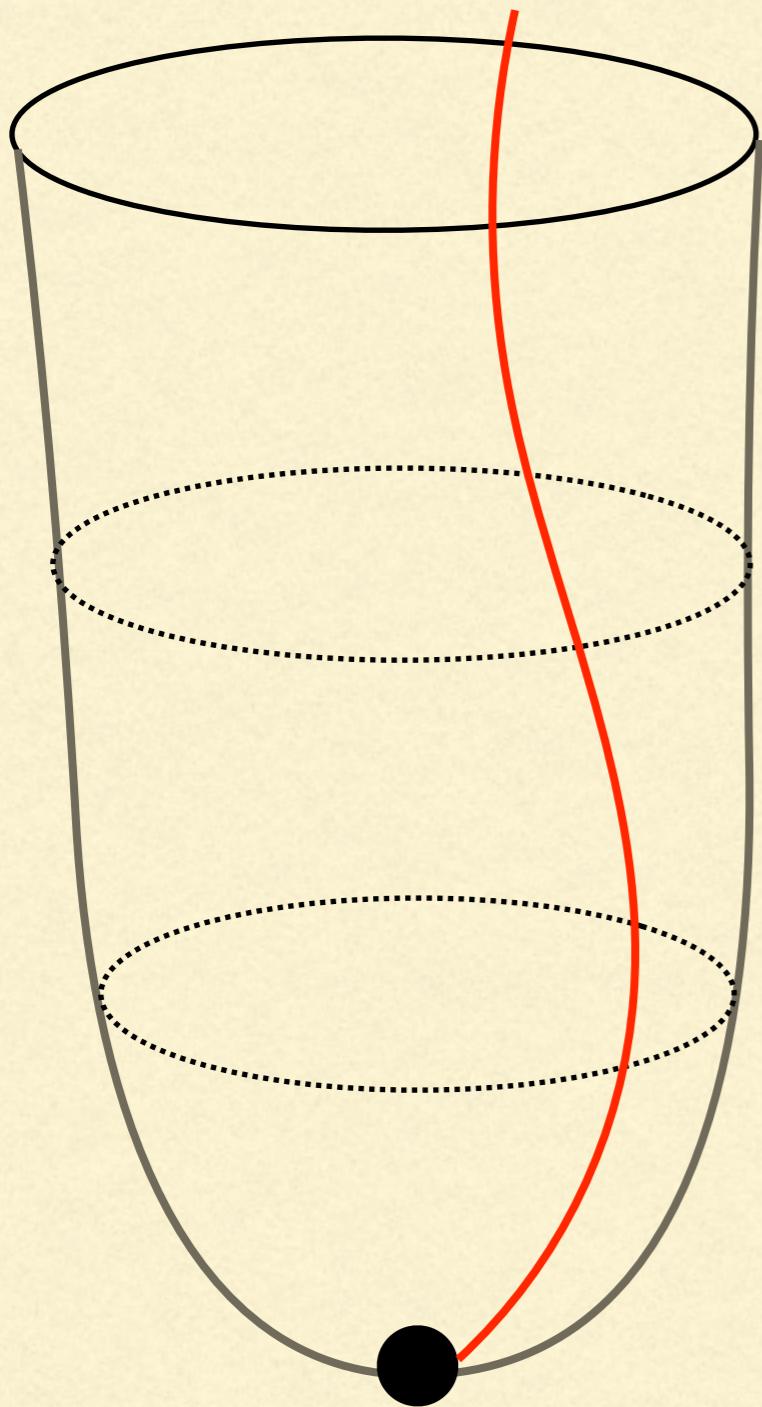
$$\mathcal{L}_{\text{DBI}} \supset \int \frac{1}{2} |F - B|^2$$

Projected out by orientifold



There are **two kinds** of charged states

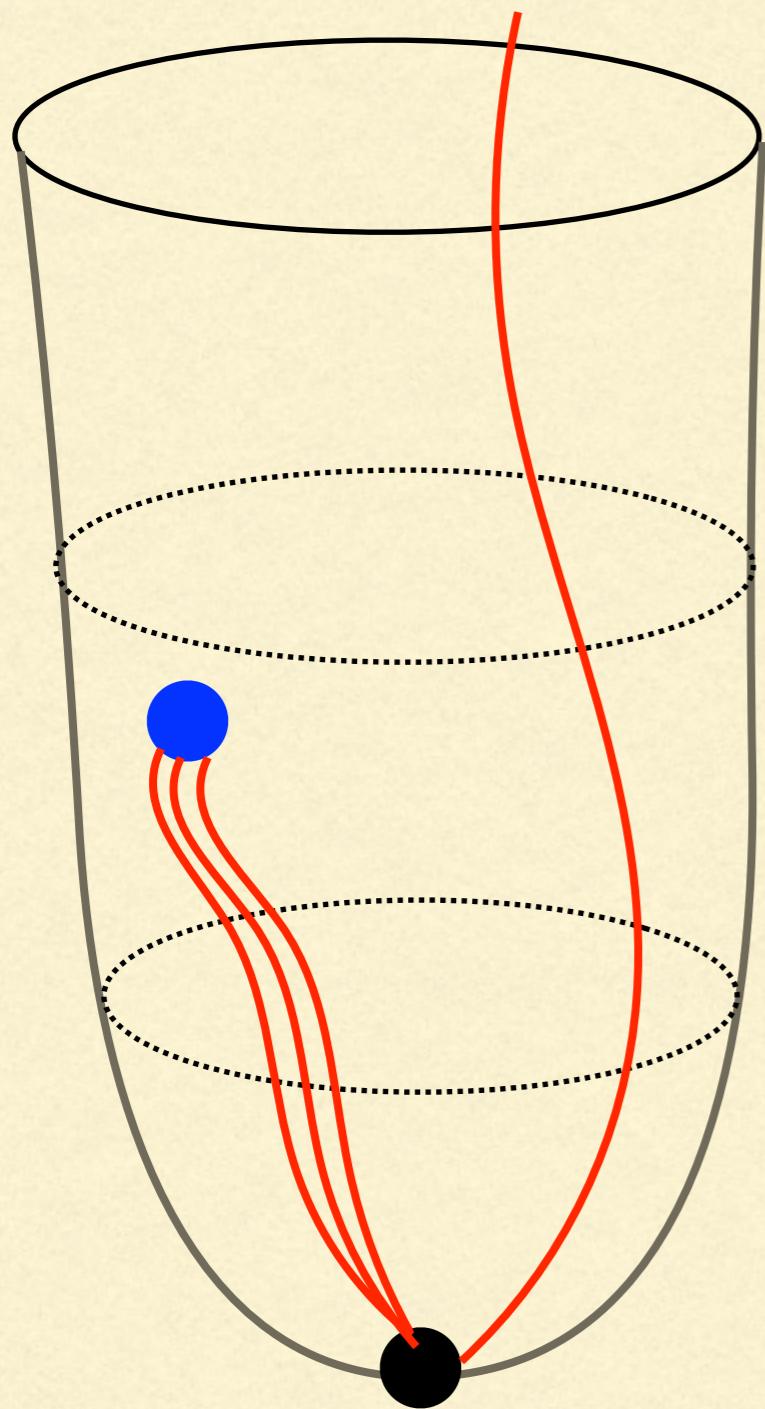
$$\int_A F_3 = M, \int_B H_3 = K$$



There are **two kinds** of charged states

FI strings that leave the throat

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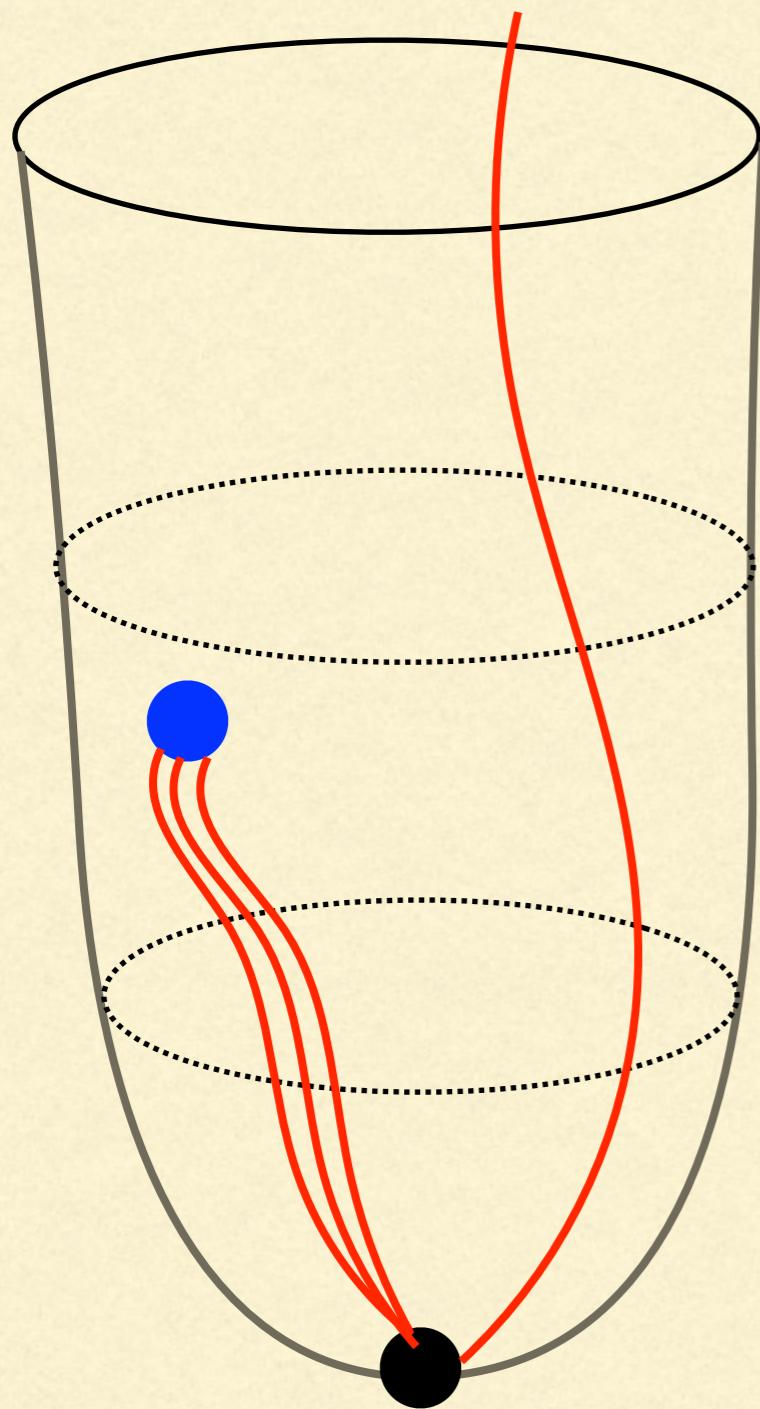


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FL and WGC amount to:

$$\sqrt{\frac{g_s}{\sigma}} L_t < 1.$$

$$e^{-\frac{2\pi K}{3g_s M}} < \sqrt{\frac{4\pi\sigma}{g_s}}$$

$$\frac{r_0^4}{g_s} e^{-\frac{r_0^4}{g_s}} < 1$$

$$(g_s M) K^{1/2} \gg 1$$

**All these** are satisfied!

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**So antibrane uplift** complies with both constraints.

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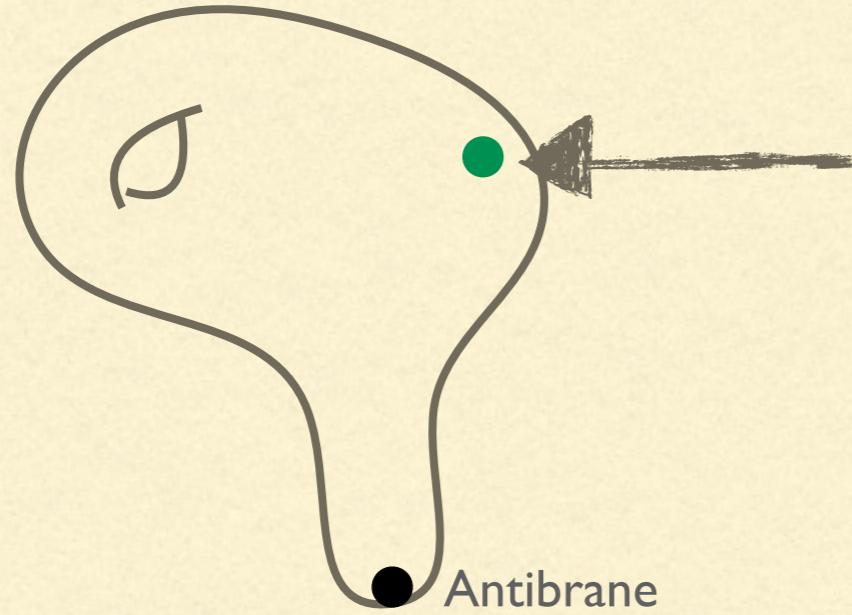
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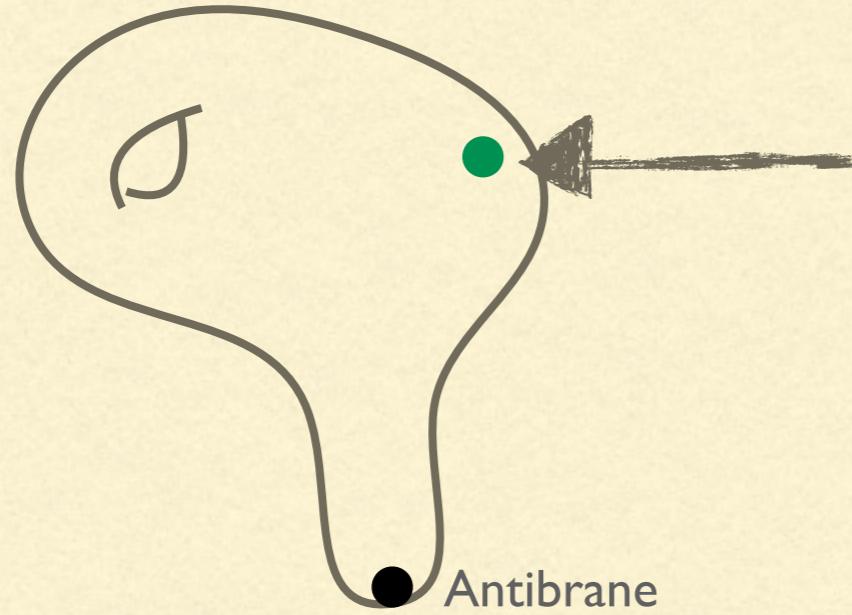
(for instance, a brane which doesn't confine)

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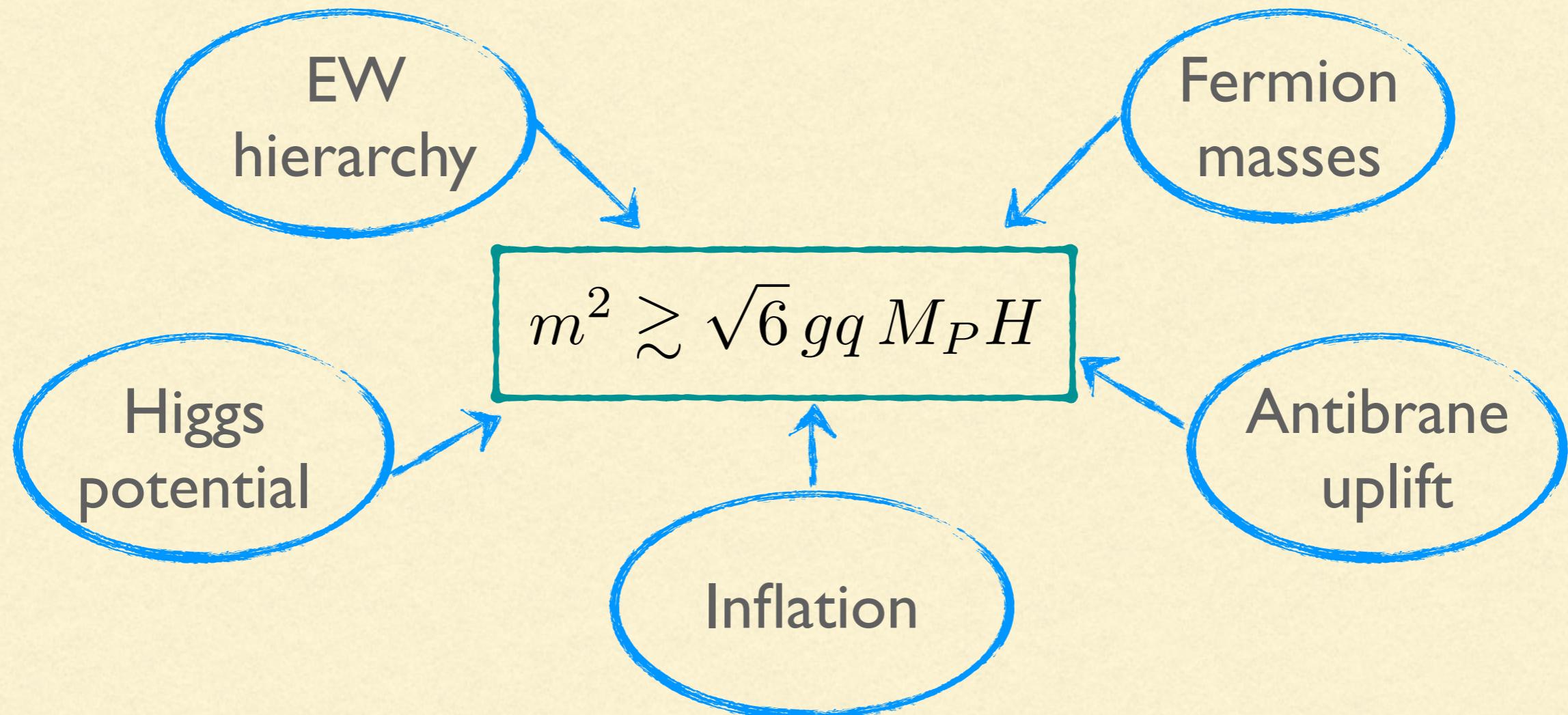
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FL incorporates Swampland **intuition**: Stuff in the throat  
cannot fully **decouple**

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# TO WRAP UP



- Working out several of these connections
- Is it correct? More checks/arguments? Counterexamples?

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**Thank you very much!**

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