

# The Gravitino and the Swampland

based on arXiv 2104.08288 in collaboration with Niccolò Cribiori and Dieter Lüst

### **Marco Scalisi**



# DISCLAIMER!

Our work is **does not directly contribute** to the discussion of

recent investigations about gravitino physics on de Sitter backgrounds:

- 2x Kolb, Long, McDonough 2021 ----- Evan's talk on Apr 13

- Dudas, Garcia, Mambrini, Olive, Peloso, Verner 2021
- ▶ Terada 2021

### **Outline**

- **Motivations**
- > The Gravitino Mass Conjecture
- Tests of the GMC
- Phenomenological implications of the GMC
- **Conclusions**

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Vafa 2006 Ooguri, Vafa 2006

(reviews)

Palti 2019

Beest, Calderon-Infante, Mirfendereski, Valenzuela



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The limit of small gravitino mass

$$m_{3/2} \to 0$$

always corresponds to the massless limit of an infinite tower of states and to the breakdown of the effective field theory.

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Evidences of infinite tower mass related to  $m_{3/2}$ 

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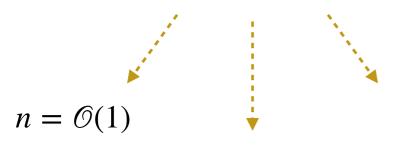


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$$m \sim \left(m_{3/2}\right)^n$$



$$n = 1$$

Strong GMC

Corrections to this simple scaling might be possible but still satisfying the GMC

e.g. for log corrections

Blumenhagen, Brinkmann, Makridou 2019

#### AdS Distance Conjecture (ADC)

Lüst, Palti, Vafa 2019

The limit of small AdS cosmological constant

$$|\Lambda| \to 0$$

is accompanied by a light infinite tower with mass

$$m \sim |\Lambda|^a$$

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for non-SUSY AdS vacua

$$m_{3/2}^2 > -\frac{\Lambda}{3}$$

 $GMC \neq ADC$ 

however

$$m_{3/2} \rightarrow 0$$
 implies  $\Lambda \rightarrow 0$  i.e. GMC  $\rightarrow$  ADC (in AdS space!)

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$$GMC = ADC$$

$$n = 2a$$



No EFT with finite number of fields interpolating AdS, Minkowski and dS



Extension of the **ADC** to **de Sitter space** implies that there should be a tower with mass

$$m \sim 10^{-120a}$$

for non-SUSY AdS vacua

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 $GMC \neq ADC$ 

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#### The scalar potential is given by

Cremmer, Ferrara, Girardello, Van Proeyen 1983

$$V = V_F + V_D - 3m_{3/2}^2$$

with 
$$m_{3/2} = e^{K(\phi,\bar{\phi})/2} |W(\phi)|$$

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$$m_{3/2}^2 \ge -\frac{V}{3}$$

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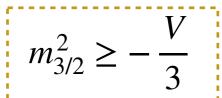
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trivially follows

with  $\,V_{\!F}\,$  and  $\,V_{\!D}\,$  being the supersymmetry breaking terms



it looks like the analogous of the Higuchi bound

Higuchi 1987

it follows also from requiring **unitarity propagation** and hold more generally than  ${\cal N}=1~{\rm SUGRA}$ 

Deser, Waldron 2001 Zinoviev 2007

We identify the tower with the Kaluza-Klein (KK) states, with mass

$$m_{KK} = \left(\frac{1}{\mathcal{V}}\right)^{2/3}$$

for **isotropic** manifolds

with  $\ensuremath{\mathscr{V}}$  being the internal 6-dimensional volume

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Kähler potential and super-potential

$$K(\phi, \bar{\phi}) = -\alpha \log \mathcal{V}(\phi, \bar{\phi}) + K'$$

remaining part dependent on the complex structure moduli and on the dilaton

$$\langle W \rangle \sim \mathcal{V}^{\beta/2}$$

scaling at the minimum of the potential

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**Gravitino mass** 

$$m_{3/2} \sim \left(\frac{1}{\mathcal{V}}\right)^{\frac{\alpha-\beta}{2}} \qquad \cdots \qquad m \sim \left(m_{3/2}\right)^n \longrightarrow \qquad n = \frac{4}{3(\alpha-\beta)}$$

$$\cdots m \sim (m_{3/2})^n \cdots \rightarrow$$

$$n = \frac{4}{3(\alpha - \beta)}$$

$$\mathcal{N} = 1$$
  $D = 4$  Examples

**Anti-de Sitter** 

▶ For background 
$$AdS_d \times S^{d'}$$
 -----  $n = 1$ 

# $\mathcal{N}=1$ D=4 Examples

#### **Anti-de Sitter**

- For background  $AdS_d \times S^{d'} \longrightarrow n = 1$
- Supersymmetric IIB AdS vacua (KKLT)

Kachru, Kallosh Linde, Trivedi 2003

$$K = -3\log(T + \bar{T}) + \dots = -2\log\mathcal{V} + \dots$$

$$\mathcal{V} = (\text{Re}T)^{3/2}$$

$$\alpha = 2 \qquad \beta = 4/3 \qquad n = 2$$

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$$\downarrow \qquad \qquad \langle W \rangle \sim Te^{-cT}$$

$$\downarrow \qquad \qquad \qquad \mathcal{V} = (\mathrm{Re}T)^{3/2}$$

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isotropic scaling of the KK masses not valid! -----→

$$m \sim \left(m_{3/2}\right)^{1/3} \times \log \text{ corrections}$$

Blumenhagen, Brinkmann, Makridou 2019 Bena, Dudas, Grana, Lüst 2018 Blumenhagen, Kläwer, Schlechter 2019

$$n = 1/3$$

# $\mathcal{N}=1$ D=4 Examples

**Anti-de Sitter** 

Non-SUSY IIB AdS vacuum (Large Volume Scenario)

Balasubramanian, Berglund, Conlon, Quevedo 2005

$$K = -2\log(\mathcal{V} + \xi/2) \qquad \qquad W \sim W_0 + \text{non-perturbative terms}$$
 can be order one

$$\alpha = 2 \qquad \beta = 0 \qquad n = 2/3$$

$$m_{3/2} \sim \frac{1}{\mathcal{V}}$$



non-perturbative contributions to W leads to log-corrections in the KK masses in terms of the cosmological constant

Blumenhagen, Brinkmann, Makridou 2019

# $\mathcal{N} = 1$ D = 4 Examples

#### Minkowski

No-scale models

Cremmer, Ferrara, Kounnas, Nanopoulos 1983 Ellis, Kounnas, Nanopoulos 1984

$$K = -3\log(T + \bar{T})$$
  $W = \text{const}$ 

$$\alpha = 1 \qquad \beta = 0 \qquad n = 4/3$$

Scherk-Schwarz models

Scherk, Schwarz 1979

No-scale models with F-term and D-term

Dall'Agata, Zwirner 2013

# $\mathcal{N} = 1$ D = 4 Examples

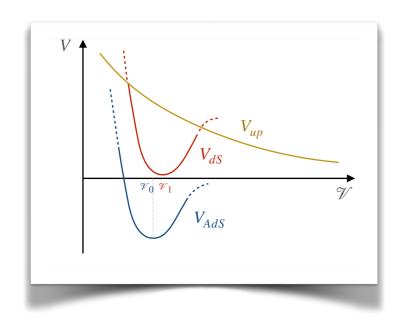
#### de Sitter

GMC in de Sitter can also be supported by its validity in anti-de Sitter spaces

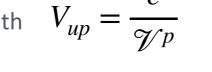


Some of the best and most studied dS constructions have

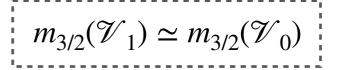
$$V_{dS} = V_{AdS} + V_{up}$$



$$V_{dS} = V_{AdS} + V_{up} \qquad \text{with} \quad V_{up} = \frac{c}{\mathcal{V}^p}$$





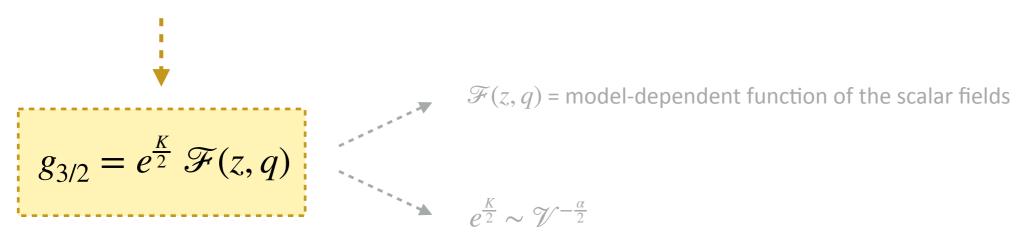


consequences of the GMC in de Sitter directly follow from the discussion of the GMC in anti-de Sitter

Content: spin-2 graviton  $g_{\mu\nu}$ , two spin-3/2 gravitini  $\psi_{\mu}^A$ , spin-1 graviphoton  $A_{\mu}^0$ , vector- and hyper-multiplets

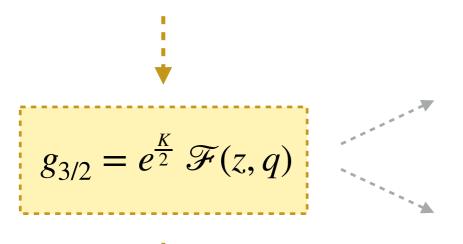
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#### We find a relation between the gravitino mass and the gravitino gauge coupling



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#### We find a relation between the gravitino mass and the gravitino gauge coupling



 $\mathcal{F}(z,q)$  = model-dependent function of the scalar fields

$$e^{\frac{K}{2}} \sim \mathcal{V}^{-\frac{\alpha}{2}}$$



$$g_{3/2} \to 0$$

implies

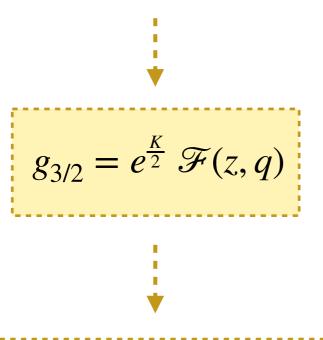
$$m_{3/2} \rightarrow 0$$
 and

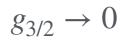
restoration of global symmetries



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Example: **STU model** 

$$K = -\log(stu)$$

$$S_{AB} = \frac{i}{2\sqrt{2}}q_{3/2} g_{3/2} \operatorname{diag}(1, -1)$$

$$m_{3/2} \rightarrow 0 \quad \Leftrightarrow \quad g_{3/2} \rightarrow 0$$

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## **Gravitino and Quantum Gravity Cut-off**

$$\Lambda_{QG} = \frac{M_P}{\sqrt{N}}$$

quantum gravity cut-off = "species scale"

Dvali 2007 Dvali, Redi 2007

$$N = \frac{\Lambda_{QG}}{m}$$

number of states below the cut-off

in the case of states equally spaced (as for KK or winding modes)

$$m \sim M_P \left(\frac{m_{3/2}}{M_P}\right)^n$$

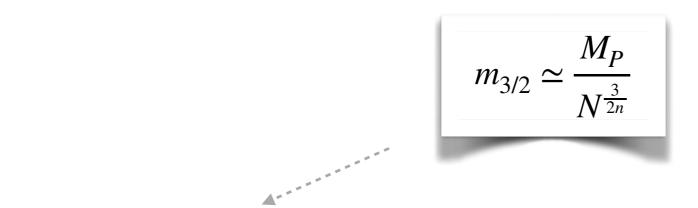
mass of the tower

## **Gravitino and Quantum Gravity Cut-off**

The mass of the gravitino sets the quantum gravity cut-off

$$\Lambda_{QG} \simeq M_P \left(\frac{m_{3/2}}{M_P}\right)^{\frac{n}{3}}$$

 $\blacktriangleright$  The mass of the gravitino depends on the number of states with mass under  $\Lambda_{OG}$ 



$$m_{3/2} < \Lambda_{QG}$$
 if  $n < 3$ 

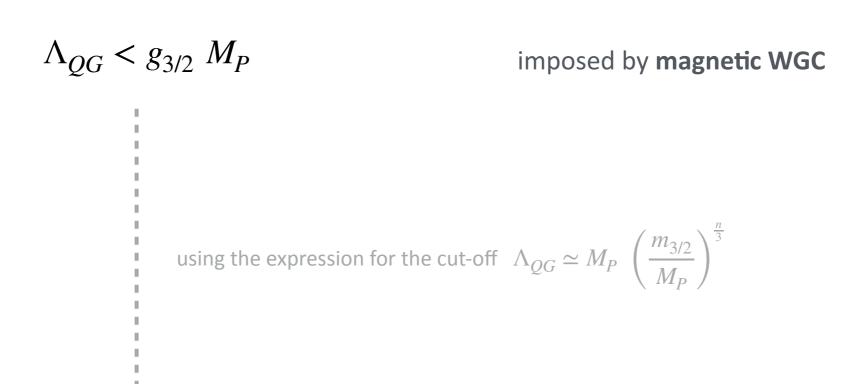
for  $n \ge 3$ , no EFT of SUSY breaking!

For the strong GMC (n = 1)

$$m_{3/2} \simeq \frac{M_P}{N^{\frac{3}{2}}} = \frac{\Lambda_{QG}^3}{M_P^2} < \Lambda_{QG}$$

## **Gravitino and Quantum Gravity Cut-off**

In the case of a charged gravitino



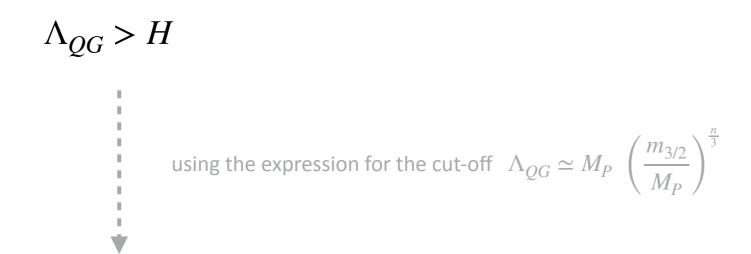
$$m_{3/2} < (g_{3/2})^{3/n} M_P < g_{3/2} M_P$$

of the form suggested by the **electric WGC** 

(if n < 3 and assuming  $g_{3/2} < 1$ )

## **Gravitino and (Quasi-)de Sitter Space**

#### Perturbative control of our EFT of de Sitter requires

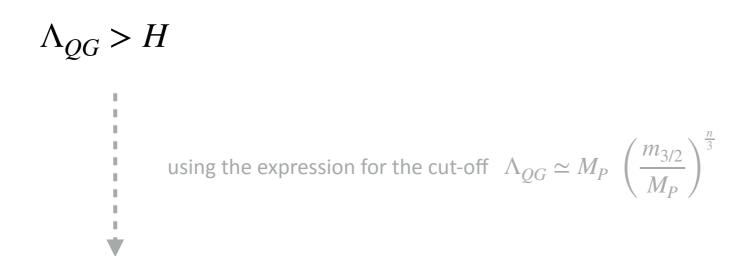


$$m_{3/2} > M_P^{\frac{n-3}{n}} H^{\frac{3}{n}}$$

model-independent lower bound on the gravitino mass in terms of the Hubble parameter

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model-independent lower bound on the gravitino mass in terms of the Hubble parameter

for 
$$n = 3$$

- explicit dependence from  $M_P$  drops
- we recover  $m_{3/2} > H$
- but, no EFT of SUSY breaking!



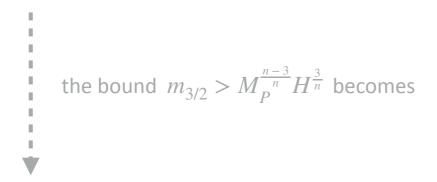
"catastrophic" gravitino production Kolb, Long, McDonough 2021

volume destabilization in KKLT *Kallosh, Linde 2004* 

# A lower bound on $m_{3/2}$ from CMB

#### In the slow-roll approximation

$$H = \sqrt{\frac{\pi^2 A_s r}{2}} M_P \simeq 10^{-4} \sqrt{r} M_P$$



$$m_{3/2} > \left(10^{-12} \ r^{\frac{3}{2}}\right)^{\frac{1}{n}} \ M_P$$

**lower bound** on the gravitino mass in terms of the **tensor-to-scalar ratio** r

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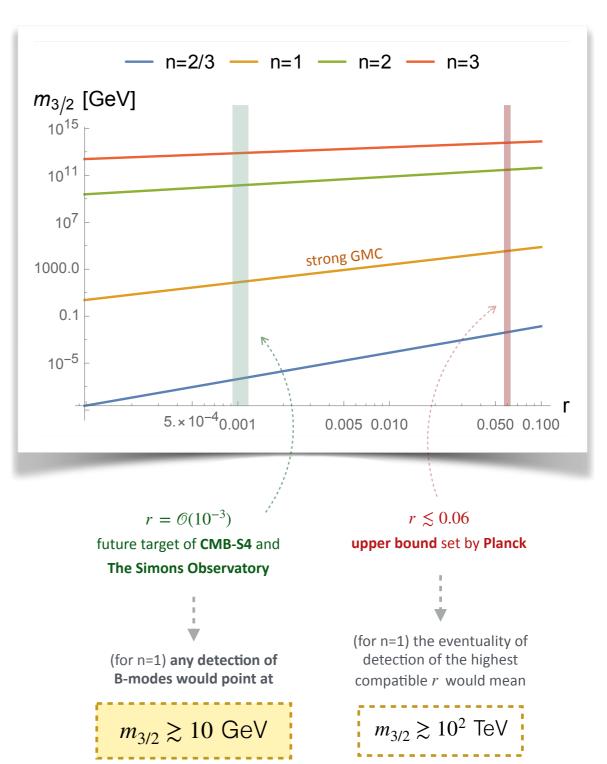
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the bound  $m_{3/2} > M_P^{\frac{n-3}{n}} H^{\frac{3}{n}}$  becomes

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**lower bound** on the gravitino mass in terms of the **tensor-to-scalar ratio** r

#### (log-log Plot)



# An upper bound on the scalar field range in terms of $m_{\rm 3/2}$

If the quasi-de Sitter phase is **sustained by a scalar field displacement,** the **Swampland Distance Conjecture** (SDC) predicts

with  $\Lambda_0 \leq M_P$  original naive cut-off of the EFT

Ooguri, Vafa 2006

$$\Lambda_{QG} = \Lambda_0 \ e^{-\lambda \Delta \phi}$$

$$\Delta \phi < \frac{1}{\lambda} \log \frac{M_P}{\Lambda_{QG}}$$

see for example MS, Valenzuela 2018

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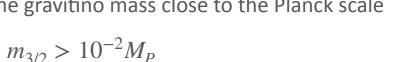
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$$\Delta \phi < \frac{n}{3\lambda} \log \frac{M_P}{m_{3/2}}$$

for  $n \simeq \lambda \simeq 1$  , it constrains large scalar field variations (i.e.  $\Delta \phi > 1$ )

just for very high values of the gravitino mass close to the Planck scale

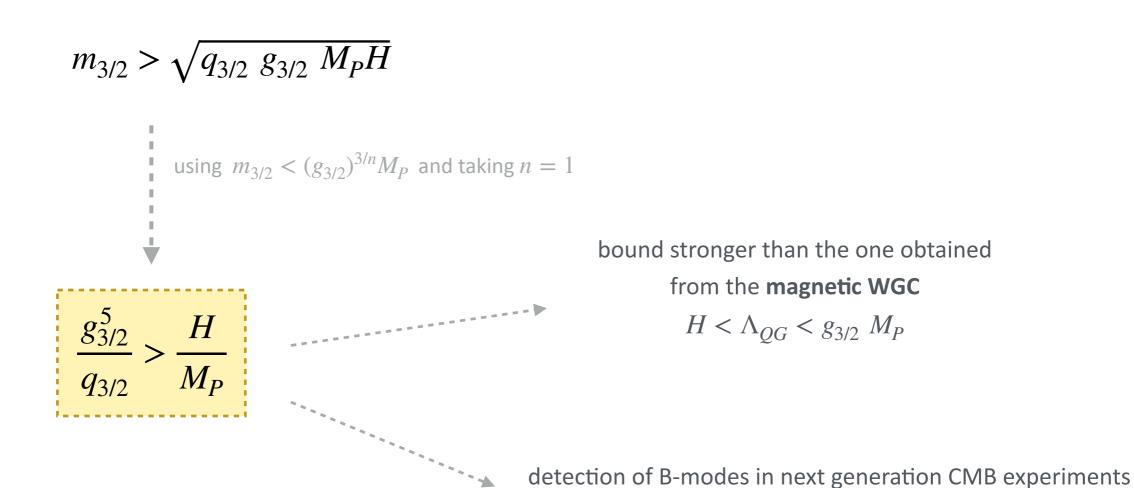




### **Gravitino coupling constant and Hubble parameter**

Montero, Van Riet and Venken have shown the existence of a lower bound on the mass of a charged particle in de Sitter space. In the case of the gravitino, it reads

Montero, Van Riet, Venken 2019



would point at a bound  $g_{3/2} \gtrsim 0.08$ 

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 $m_{3/2} \gtrsim 10 \text{ GeV}$ 



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