

Resource Guided Concurrent Deduction



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Focused Search

"... when he [the mathematician] does not succeed in quessing the whole answer, [he] tries to quess some part of the answer, some feature of the solution, some approach to the solution, or some feature of an approach to the solution. Then he seeks to expand his guess, and so he seeks to adapt his guess to the best information he can get at the moment."

Heuristic Search



Breadth First Search

Search

Heuristic

Focused

Breadth First

Focused Search



expensive

inexpensive

Resource Guided Concurrent Deduction

An attempt to combine the benefits of both approaches Preference to the integrated reasoning components is given due to the available re sources (knowledge, time, ...)

Traditional Automated Theorem Proving

Proof Planning

on a more abstract and

informed layer.

A human oriented approach employing heuristic search at proof method level, i.e.

A machine oriented approach typically aiming at exhaustive (complete) search through the search space at inference

promising search directions

Mathematical

Mind

Architecture

"Those who have an excessive faith in their ideas are not well fitted to make discoveries.

"In order to invent, one must think aside."

[Claude Bernard]

"Therefore, we see that the unconscious has the important property of being manifold; several and probably many things can and do occur in it simultaneously. This contrasts with conscious ego which is unique. We also see that this multiplicity of the unconscious enables it to carry out a work of synthesis."

Run integrated reasoning components concurrrently but give preference to the most promising ones with the help of an appropriate resource distribution. Periodically assesses the state of the proof search process, evaluate the progress, and choose a new promising direction for the further search, and redistribute the resources accordingly.

Resource Guided Reasoning Cycle

- 1. Assessment & evaluation of the proof progress

 - are the resulting partial proof plans new? do they contain more simplified expressions? do they contain simpler open goals? do they contain open goals similar to lemmata in the database?

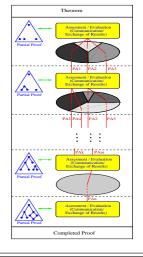
2. Selection of promising results

- choose the most promising partial proof plan according to the above criteria and make it the new actual proof plan - save the best of the remaining resuts for backtracking

3. Redistribution of available resources

what is the logic language the focused problem belongs to?
what is the mathematical theory the focused problem belongs to?
does the database provide information which a reasoner already
successfully used to solve similar problems in the past?

thinking aside



Planning Agents

Reliability

less brittle

robust

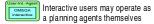
brittle

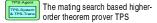
Approach

Adapt the Multi-Agent Planning (MPA) approach [Wilkins&Myers 1998] to the proof planning domain

Employ the mathematical database MBASE as domain server, OMEGA as plan server and an extension of OMEGA/LOUI as planning cell manager As planning cells use the algorithms and external reasoners already provided by the OMEGA/MATHWEB environment.

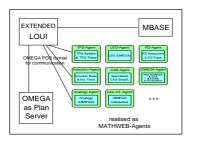
Some specialised **Planning Agents**



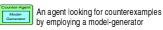


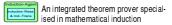
The extensional higher-order resolution based theorem prover LEO

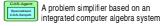
Various state of the art first-order theorem provers

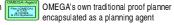


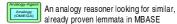
proof techniques











The O-ANTS system was originally developed to support the user in interactive theorem proving. Recent experiments have shown that this agentbased, hierarchically organised system can also fruitfully support the resource guided integration of

deliberative & reactive

external reasoning components. Hence O-ANTS provides the architectural and implementational basis for the Multi-Agent Proof Planning approach.



Reactive

Basis

Agent-based System Integration

Verv robust mechanism: faultv

agent specifications do not harm the functioning of the overall mechanism



~defagent Call-TPS c-predicate (tackle-by-TPS 'P1 & P2 & ... & Pn --> C')) (complexity-level 100))

Declarative Agent Specification in O-ANTS

Advantages of the O-ANTS Architecture

- Supports interaction & automation
- Agents can be defined at run-time Agents can be modified at run-time
- Agents can be dynamically activated & deactivated at run-time
- Supports resource-adaptive guidance

Implementation

The implementation employs the multiprocessing facilities of Allegro Common Lisp.

Currently we test the mechanism with up to 400 little software agents performing trivial computations

