

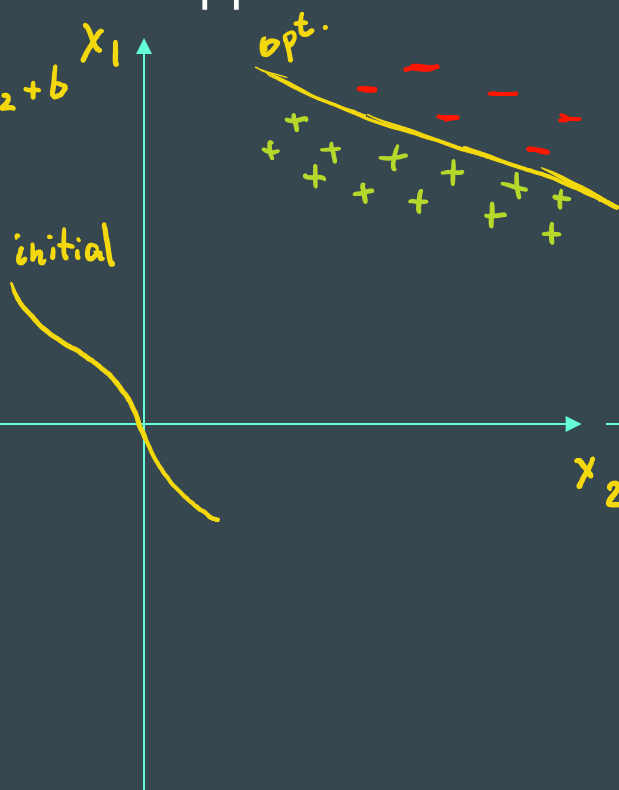
# Часть 9: Нормализация



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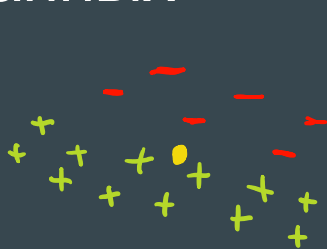
# Центрирование данных

$$\sigma(\vec{x}) = w_1 x_1 + w_2 x_2 + b$$



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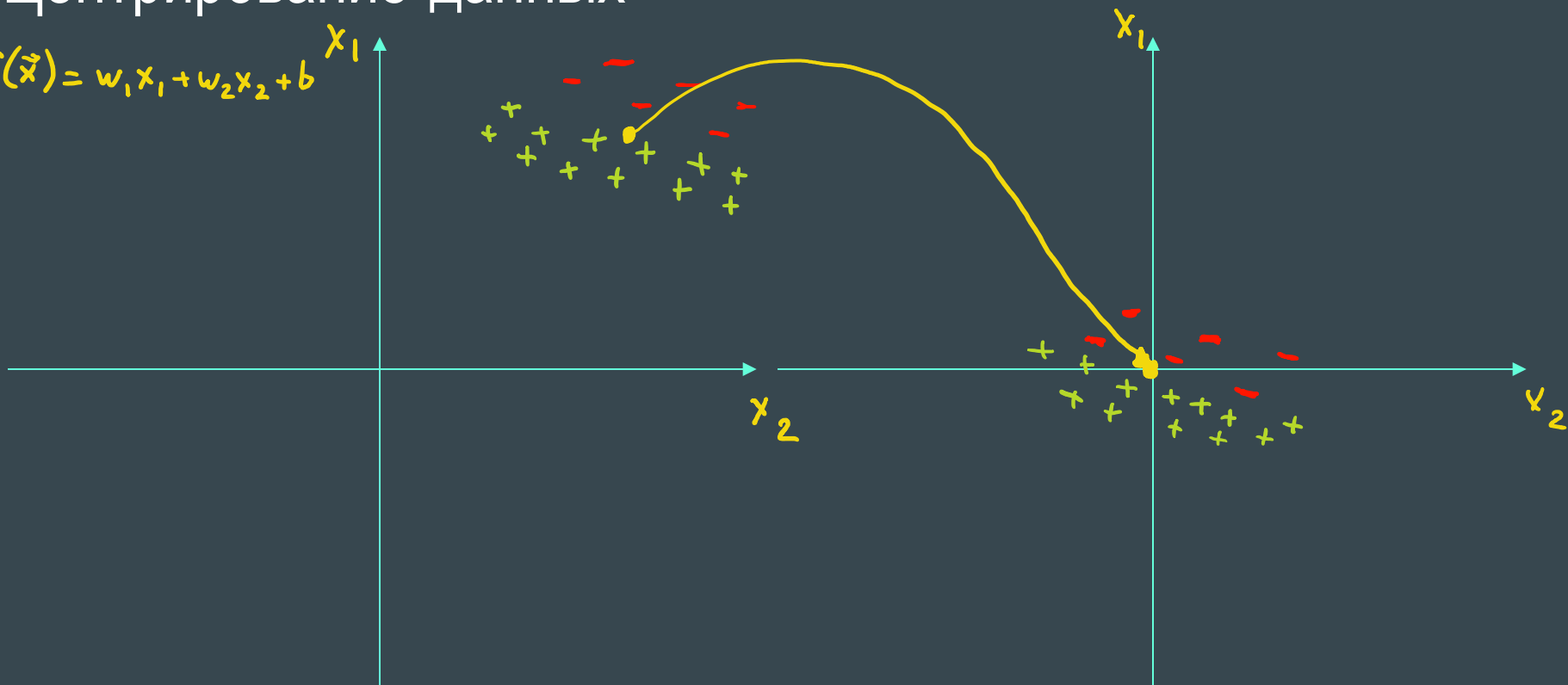
$x_1$

$x_2$

$x_2$

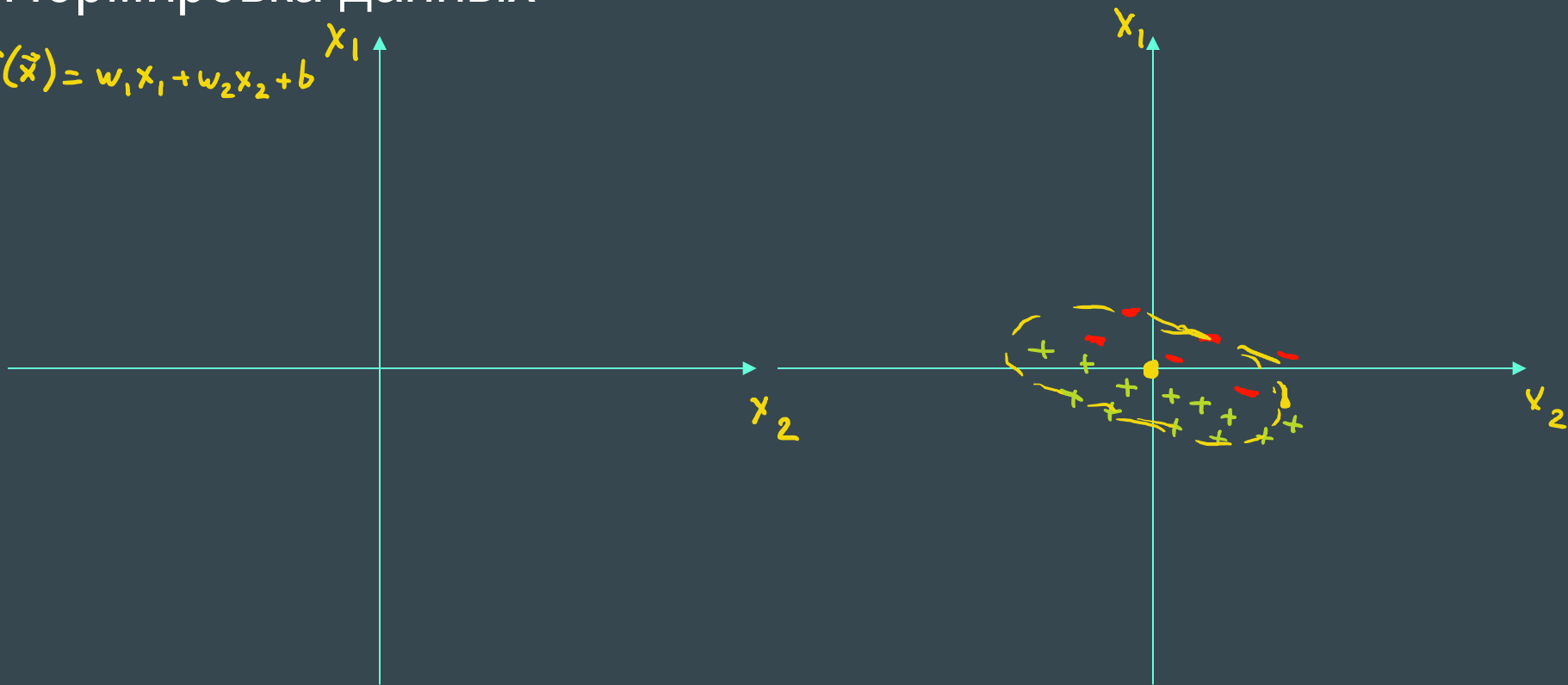
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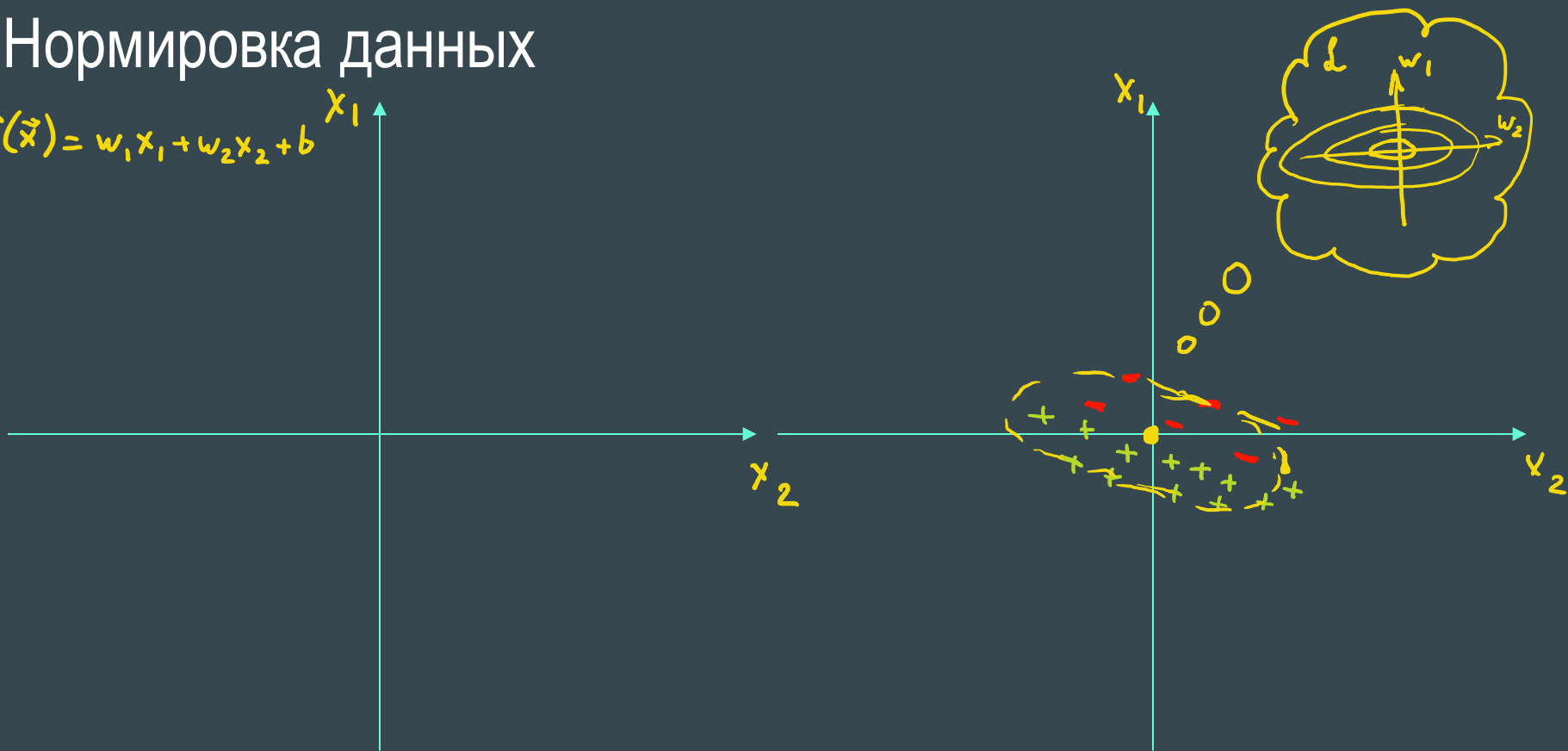
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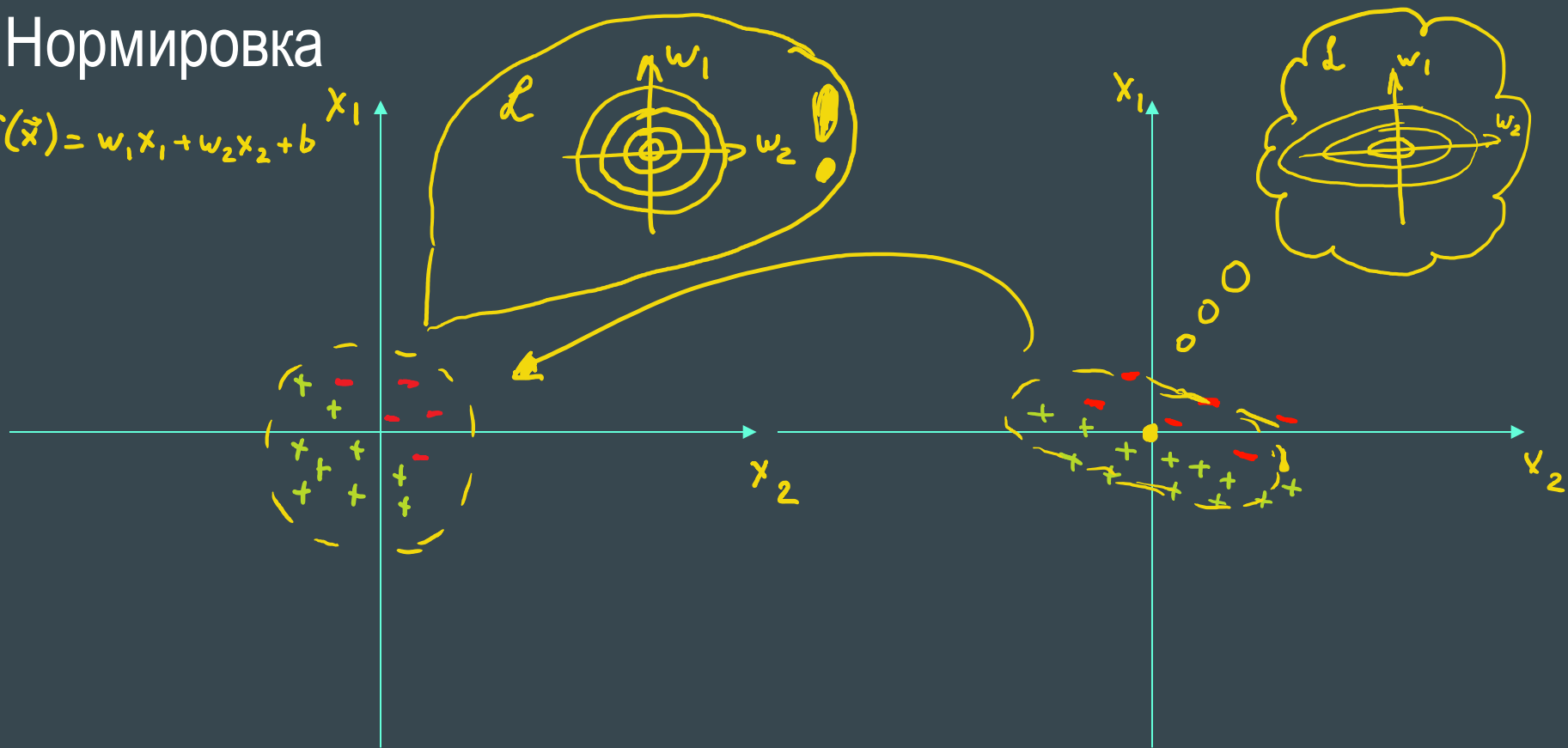
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# Нормировка

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# Нормировка данных

$$\vec{z} = \frac{\vec{x} - \vec{\mu}}{\sigma}, \text{ где } \vec{\mu} = \frac{\sum_i \vec{x}_i}{N}, \quad \sigma = \sqrt{\frac{\sum_i (\vec{x}_i - \vec{\mu}_i)^2}{N-1}}$$



# BatchNorm

$$\vec{\tilde{x}} = \frac{\vec{x} - \vec{\mu}_B}{\vec{\sigma}_B} \cdot \gamma + \beta$$

$$\vec{\mu}_B = \frac{\sum_{i=1}^{N_B} \vec{x}_i}{N_B}$$

$$\vec{\sigma}_B = \sqrt{\frac{\sum_{i=1}^{N_B} (\vec{x}_i - \vec{\mu}_B)^2}{N_B - 1}}$$

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Inference:

$$\begin{aligned}\hat{\vec{\mu}} &= \text{EMA } \vec{\mu}_B \\ \hat{\vec{\sigma}} &= \text{EMA } \vec{\sigma}_B\end{aligned}$$