porject-5 Chitra Karki 11/9/2021 Reading data df.crime = read.csv("crime.csv") 1. Data Preparation: Start with the data set crime.csv from the class website. We will first dosome minor data preparation and exploration. a. Remove the first five columns from the data since these are not predictive. df.crime = df.crime[,-c(1:5)] b. Take a look at the missing percentage of each remaining variable. Remove those heavy missing, say, over 60%. nrows = dim(df.crime)[1] col2drop = which(apply(df.crime, 2, function(x) sum(is.na(x))/nrows \* 100) > 60) # columns containing more then 60 % NA values col2drop ## LemasSwornFT LemasSwFTPerPop LemasSwFTFieldOps ## 98 ## LemasSwFTFieldPerPop LemasTotalReq LemasTotReqPerPop ## 101 ## PolicReqPerOffic PolicPerPop RacialMatchCommPol ## 103 104 PctPolicBlack ## PctPolicWhite PctPolicHisp ## 107 PctPolicMinor OfficAssgnDrugUnits PctPolicAsian ## ## 110 111 ##  ${\tt NumKindsDrugsSeiz}$ PolicAveOTWorked PolicCars ## 117 ## PolicOperBudg LemasPctPolicOnPatr LemasGangUnitDeploy ## 118 120 119 ##  ${\tt PolicBudgPerPop}$ ## 122 df.crime = df.crime[,-col2drop] # checking dimension after droping cols with heavy NAs dim(df.crime) ## [1] 1994 101 c. Impute or replace the remaining missing values appropriately. which(apply(df.crime, 2, function(x) sum(is.na(x))/nrows \* 100) > 0) ## OtherPerCap ## 26 # this shows now we are left with single NA value at the 26 i.e "otherpercap" column. # lets replace the missing with the median value. hist(df.crime\$OtherPerCap) # looking at the distribution of data points. Histogram of df.crime\$OtherPerCap 900 500 400 Frequency 300 200 100 0.0 0.2 0.4 0.6 8.0 1.0 df.crime\$OtherPerCap df.crime[which(is.na(df.crime\$0therPerCap)), "OtherPerCap"] = median(df.crime\$0therPerCap, na.rm = T) # checking for nas sum(is.na(df.crime)) # now the data is clean. ## [1] O d. Conduct some EDA (which could be involved). In particular, check the distribution of the target variable ViolentCrimesPerPop. hist(df.crime\$ViolentCrimesPerPop) Histogram of df.crime\$ViolentCrimesPerPop 900 Frequency 400 200 0 0.0 0.2 0.4 0.6 8.0 1.0 df.crime\$ViolentCrimesPerPop # the distribution is something like exp(-x)boxplot(df.crime\$ViolentCrimesPerPop) 1.0 9.0 0.0 # there are ceratin outliers. More amount of data are greater then median summary(df.crime\$ViolentCrimesPerPop) Min. 1st Qu. Median Mean 3rd Qu. Max. 0.000 0.070 0.238 0.330 1.000 0.150 library(corrplot) ## corrplot 0.90 loaded corrplot(cor(df.crime), type = "full", tl.pos = "n", method = "square") 8.0 0.6 0.4 0.2 -0.2 -0.4 -0.6 -0.8 # there are several variables correlated with each other. Also some other variables are positively and negatively correlated with the response variable. 2. Partitioning Data: Randomly partition your data into two sets: the training set D1 and the test set D2 with a ratio of 2:1. In order for your results to be reproducible, report the random seed that you use in the partitioning. set.seed(1) # seed 123 for reproducibility train.index = sample(1:nrows, 2/3\*nrows, replace = F) test.index = -train.index d1 = df.crime[train.index,] d2 = df.crime[test.index,] 3. Predictive Modeling: Referring to the sample R code R09.R from the class website, fit at least five models of your own choice from the following models using the training set D1: i. Linear regression with stepwise selection; ii. LASSO iii. Ridge Regression (RR) iv. Principal Components Regression (PCR) v. Partial least squares regression (PLSR) vi. Weighted orthogonal components regression (WOCR) vii. Total least squares regression (TLSR) viii. Stagewise regression ix. Least angle regression (LAR) You might want to describe how you select the tuning parameter if such decision needs to be made in each approach. Then apply the tted model to the test set D2. Report the mean square error of prediction (MSEP) and compare. i> linear regression with stepwise selections library(MASS) fit.full = lm(d1\$ViolentCrimesPerPop~.,data = d1) fit.step <- stepAIC(fit.full, direction="both", k=log(nrow(d1)))</pre> #fit.step\$anova best.model = summary(fit.step) best.formula = as.formula(best.model\$call) best.fit = lm(best.formula, data = d1) old.dat =as.data.frame(model.matrix(best.fit)) new.dat = d2[,names(old.dat)[-1]]y.pre = predict(best.fit,newdata = new.dat) y.obs = d2[, dim(d2)[2]]plot(y.obs,y.pre,pch=19,col="red",main = "stepwise Regression") abline(a=0, b=1, col="black") stepwise Regression 0.8 9.0 y.pre 4 o. 0.2 0.0 0.0 0.2 0.4 0.6 8.0 1.0 y.obs  $MSE.step = mean((y.obs-y.pre)^2); MSE.step$ ## [1] 0.02101974 ii> LASSO library(glmnet) ## Loading required package: Matrix ## Loaded glmnet 4.1-2 lambda= seq(0, 80.0, 0.01) # AGAIN, APPROPRIATE ADJUSTMENT MIGHT BE NEEDED # SETTING alpha=0 IN glmnet GIVES RIDGE REGRESSION X.train = as.matrix(d1[,-dim(d1)[2]])y.train = d1[,dim(d1)[2]]cv.LR <- cv.glmnet(x=X.train, y=y.train, alpha = 1, lambda = lambda, nfolds=10) # 10-FOLD CV BY DEFAULT plot(cv.LR) 7 5 4 3 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 Mean-Squared Error 0.04 0.03 0.02 2 -2  $Log(\lambda)$ names(cv.LR) "cvsd" "cvup" "cvlo" ## [1] "lambda" "glmnet.fit" "lambda.min" ## [6] "nzero" "call" "name" ## [11] "lambda.1se" "index" lmbd0 <- cv.LR\$lambda.min; lmbd0 # MINIMUM CV ERROR</pre> ## [1] 0 # lmbd0 <- cv.RR\$lambda.1se # 1SE RULE</pre> fit.LR <- cv.LR\$glmnet.fit</pre> y.pred <- predict(fit.LR, s=lmbd0, newx = as.matrix(d2[,-dim(d2)[2]])) yobs <- d2[, dim(d2)[2]]plot(yobs, y.pred, xlab="observed", ylab="predicted", col="blue", pch=19, cex=0.8, main="Lasso Regression") abline(a=0, b=1, col="green", lwd=2) **Lasso Regression** 0.8 9.0 predicted 0.4 0.2 8.0 0.0 0.2 0.4 0.6 1.0 observed MSEP.LR <- mean((yobs -y.pred)^2)</pre> MSEP.LR ## [1] 0.02041003 iii> Ridge Regression library(glmnet) lambda= seq(0, 80.0, 0.01) # AGAIN, APPROPRIATE ADJUSTMENT MIGHT BE NEEDED # SETTING alpha=0 IN glmnet GIVES RIDGE REGRESSION X.train = as.matrix(d1[,-dim(d1)[2]])y.train = d1[,dim(d1)[2]]cv.RR <- cv.glmnet(x=X.train, y=y.train, alpha = 0, lambda = lambda, nfolds=10) # 10-FOLD CV BY DEFAULT plot(cv.RR) 0.05 Mean-Squared Error 0.04 0.03 0.02 -2 0 2  $Log(\lambda)$ names(cv.RR) ## [1] "lambda" "cvm" "cvsd" "cvup" "cvlo" "glmnet.fit" "lambda.min" ## [6] "nzero" "call" "name" ## [11] "lambda.1se" "index" lmbd0 <- cv.RR\$lambda.min; lmbd0 # MINIMUM CV ERROR</pre> **##** [1] 0.01 # lmbd0 <- cv.RR\$lambda.1se # 1SE RULE</pre> fit.RR <- cv.RR\$glmnet.fit</pre> y.pred <- predict(fit.RR, s=lmbd0, newx = as.matrix(d2[,-dim(d2)[2]]))yobs <- d2[, dim(d2)[2]]plot(yobs, y.pred, xlab="observed", ylab="predicted", col="blue", pch=19, cex=0.8, main="Ridge Regression") abline(a=0, b=1, col="green", lwd=2) **Ridge Regression** 1.0 9.0 predicted 0.4 0.2 0 0.2 0.4 0.0 0.6 8.0 1.0 observed  $MSEP.RR \leftarrow mean((yobs -y.pred)^2); MSEP.RR$ ## [1] 0.01976178 iv> Principal Components Regression (PCR) #install.packages("pls") library(pls) ## Attaching package: 'pls' ## The following object is masked from 'package:corrplot': ## corrplot ## The following object is masked from 'package:stats': ## loadings ncol(d1)## [1] 101 fit.PCR <- pcr(d1\$ViolentCrimesPerPop ~ ., ncomp=100, data=d1, method = pls.options()\$pcralg,</pre> validation = "CV", segments = 10, segment.type ="random", scale=TRUE) #summary(fit.PCR) #names(fit.PCR); CV <- fit.PCR\$validation; names(CV)</pre> ## [1] "method" "pred" "coefficients" "gammas" "PRESS0" ## [6] "PRESS" "adj" "segments" "ncomp" par(mfrow=c(2,1), mar=rep(4,4))plot(1:CV\$ncomp, CV\$PRESS, xlab="number of PCs", ylab="PRESS", type="b", col="blue", lwd=2) # plot(fit.PCR) ncomp.best <- which.min(CV\$PRESS); ncomp.best</pre> ## [1] 73 # FIT THE BEST PCR MODEL WITHOUT V-FOLD CV (SETTING V=1 WOULD DO) fit.PCR.best <- pcr(d1\$ViolentCrimesPerPop ~ ., ncomp=ncomp.best, data=d1, method = pls.options()\$pcralg, segments = 1, scale=TRUE) #summary(fit.PCR.best) # PREDICTION ?predict.mvr ## starting httpd help server ... ## done yhat.PCR <- predict(fit.PCR.best, newdata=d2[,-dim(d2)[2]], comps=1:ncomp.best) # THE ARGUMENT comps= IS IMPORT</pre> yobs <- d2[, dim(d2)[2]]# PREDICTED VS. OBSERVED par(mfrow=c(1,1), mar=rep(4,4))**PRESS** 35 25 20 40 60 80 100 number of PCs plot(yobs, yhat.PCR, type="p", pch=18, col="blue", xlab="observed", ylab="predicted", main="PCR") abline(a=0, b=1, col="orange", lwd=2) **PCR** 1.0 0.8 9.0 predicted 0.4 0.2 0.0 1.0 observed # MEAN SQUARE ERROR FOR PREDICTION MSEP.PCR <- mean((yobs-yhat.PCR)^2); MSEP.PCR</pre> ## [1] 0.02004789 v> Partial least squares regression (PLSR) library(pls) fit.PLS <- plsr(d1\$ViolentCrimesPerPop ~ ., ncomp=100, data=d1, method = "simpls",</pre> validation = "CV", segments = 10, segment.type ="random", scale=TRUE) #summary(fit.PLS) CV <- fit.PLS\$validation par(mfrow=c(2,1), mar=rep(4,4))plot(1:CV\$ncomp, CV\$PRESS, xlab="number of PCs", ylab="PRESS", type="b", col="blue", lwd=2) # plot(fit.PLS) # ?validationplot validationplot(fit.PLS, val.type = "MSEP", main="mean squared error of prediction") 20 80 0 40 60 100 number of PCs mean squared error of prediction 0.05 0.02 0 20 40 60 80 100 number of components ncomp.best <- which.min(CV\$PRESS); ncomp.best</pre> ## [1] 23 fit.PLSR.best <- plsr(d1\$ViolentCrimesPerPop ~ ., ncomp=ncomp.best, data=d1, method = "simpls",</pre> validation = "none", scale=F) #summary(fit.PLSR.best) # MAKE PREDICTION  $yhat.PLSR <- predict(fit.PLSR.best, newdata=d2[,-dim(d2)[2]], comps=1:ncomp.best) \\ \# THE ARGUMENT comps=IS IMPO(d2)[2]], co$ yobs <- d2[,dim(d2)[2]]# PREDICTED VS. OBSERVED

par(mfrow=c(1,1), mar=rep(4,4))

0.8

9.0

0.4

0.2

0.0

## [1] 0.02031212

cbind(errors, values)

errors

## [2,] "MSEP.LR"

## [1,] "MSE.step" "0.02102"

## [3,] "MSEP.RR" "0.01976" ## [4,] "MSEP.PCR" "0.02005" ## [5,] "MSEP.PLSR" "0.02031"

0.2

MSEP.PLSR <- mean((yobs-yhat.PLSR)^2); MSEP.PLSR</pre>

values

"0.02041"

# MEAN SQUARE ERROR FOR PREDICTION

0.4

errors = c("MSE.step","MSEP.LR", "MSEP.RR","MSEP.PCR","MSEP.PLSR")
values = round(c(MSE.step, MSEP.LR, MSEP.RR, MSEP.PCR, MSEP.PLSR),5)

observed

0.6

comparing mse of all the models implemented above

The tuning parameters, if involved, were computed with cross validation method. The minimum error is for Ridge Regression.

predicted

abline(a=0, b=1, col="orange", lwd=2)

plot(yobs, yhat.PLSR, type="p", pch=18, col="blue",

xlab="observed", ylab="predicted", main="Partial LS")

**Partial LS** 

8.0

1.0