Intro to Labor Macro

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What is Labor Macro?

- Kydland, Prescott, Hansen, ect.
 - real business cycle models
 - understanding total hours and employment
 - no labor market frictions
 - loosely speaking: models of participation

What is Labor Macro?

- Diamond, Mortensen, Pissarides, ect.
 - labor market frictions
 - models of unemployment
 - understanding how people search for jobs
 - understanding how people flow between E and U

Where is Labor Macro going?

- understanding participation and search decisions
 - is participation wanting a job? or searching for a job?
- understanding structural change in terms of
 - how people look for work
 - when people work
 - how firms recruit workers
 - what is a firm/worker (gig economy)

What are Frictions?

• **Search Frictions:** it takes time or money (or both) for buyers and seller to find each other

 Matching Frictions: when buyers and sellers meet they may not be a good, or the best match

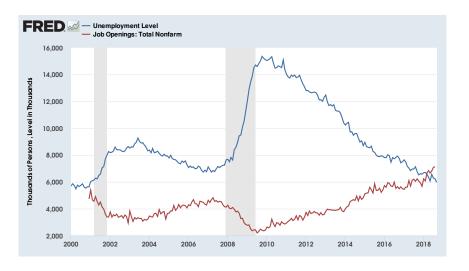
What are some markets with frictions?

- Labor Market: workers are looking for jobs, it takes time to apply to jobs. Firms are looking for workers, it costs money to interview people.
- Housing Market: buyers are looking for homes
- Marriage Market: everyone's looking for someone
- Asset Market: Over-the-counter markets for non-routine financial asses

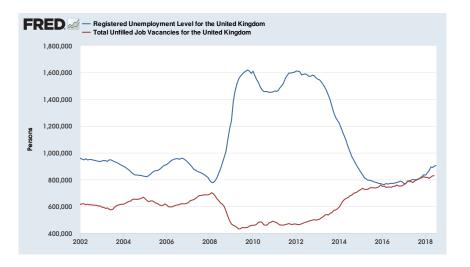
Walrasian Model does not work with frictions

- From a Walrasian perspective
 - Excess demand: vacant jobs
 - Excess supply: unemployed workers
 - Unemployment explained by wages being too high to clear the market
 - Vacancies explained by wages being too low to clear the market
- How can excess demand and excess supply coexist?

Labor Market in the US



Labor Market in the UK



How do we model markets with frictions

- the individual's decision problem:
 - how to search for a job, search effort
 - which jobs to accept
- the firm's decision problem:
 - how many workers they need
 - how much to pay
- an equilibrium
 - number of unemployed and vacancies
 - a wage distribution

A Short Chronological Outline

- One-sided Search: individual decision problem, optimal stoping problem.
 - McCall (1970)
- 1-st Generation Equilibrium Search: random search models with wage posting. Consider workers decisions of accepting jobs and firms decisions on wages.
- Matching and Bargaining: Diamond, Mortensen, Pissarides (DMP). Also take into consideration the firms decision to post vacancies.
- Directed (Competitive): Workers decide which jobs to apply to.

Outline for the next weeks

- Today: Stigler (1961) & McCall (1970)
- The wage distribution
- Diamond, Mortensen, Pissarides
- Student Presentations
- My current work / Some Data
- Assignment: Due 6th Dec.

Stigler (1961): The Economics of Information

- Observation: Prices of homogenous goods vary across seller
 - Chevrolets
 - Coal
- **Theory:** People must visit multiple sellers to get the best price, people search
- Question: How do you decide how many seller to visit before you know enough of the price distribution to buy the good?
 - How many wage offers should you get before you take the best job?

- Suppose there are two prices: \$2 and \$3
- Seller are split equally between the prices

Number of	Probability of Minimum	Expected
Prices	Price of	Minimum
Sampled	\$2 \$3	Price

- How many prices should you sample if it's costless to search?
- How many prices should you sample if it's costly to search?

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Number of	Proba	bility of Minimum	Expected
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1	0.5	0.5	2.5

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Number of	Probal	bility of Minimum	Expected
Prices	Price of		Minimum
Sampled	\$2	\$3	Price
1	0.5	0.5	2.5
2	0.75	0.25	2.25

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Number of	Probability of Minimum		Expected
Prices	Price of		Minimum
Sampled	\$2	\$3	Price
1	0.5	0.5	2.5
2	0.75	0.25	2.25
3	0.875	0.125	2.125

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1	0.5	0.5	2.5
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3	0.875	0.125	2.125
∞	1	0	2

- How many prices should you sample if it's costless to search?
- How many prices should you sample if it's costly to search?

Stigler (1961): The Economics of Information

- There exists some price distribution F(p)
- cost of making one draw: c
- Let M_n be the expected value of the min value of n samples

$$M_n = n \int_0^\infty p[1 - F(p)]^n f(p) dp$$

The gain from drawing one more sample

$$G_n = M_{n-1} - M_n$$

= $\int_0^\infty p[1 - F(p)]^{n-1} f(p)[nF(p) - 1] dp$

- G_n is decreasing in $n \Rightarrow \lim_{n \to \infty} G_n = 0$
- Optimal number of draws: n s.t. $G_{n+1} > c > G_n$

• Environment:

- ullet workers search for a jobs, infinitely lived, discount at eta
- ullet cost of search each period: κ
- while unemployed worker gets c
- if searching, each period she draws an offer from F(w)
- if she accepts the job, it lasts forever

- Objective:
 - maximize expected discounted earnings

$$\mathbb{E}\sum_{0}^{\infty}\beta^{t}Y_{t}$$

income each period depends on employment state

$$Y_t = \begin{cases} c - \kappa & \text{if unemployed} \\ w & \text{if employed} \end{cases}$$

- Trade off:
 - Waiting too long for a good offer is costly
 - Accepting too early is costly, since better offers might arrive in the future

- Solution:
 - optimal stoping problem
 - the reservation wage: *w_R*

$$w \ge w_R \Rightarrow \text{ accept the job}$$

 $w < w_R \Rightarrow \text{ keep searching}$

 How does this relate to Stigler's optimal number of draws problem?

- Solution:
 - optimal stoping problem
 - the reservation wage: w_R

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- How does this relate to Stigler's optimal number of draws problem?
 - **Stigler:** *n* determines the expected maximum price we are going to pay, non-sequential search

- Solution:
 - optimal stoping problem
 - the reservation wage: w_R

$$w \ge w_R \Rightarrow \text{ accept the job}$$

 $w < w_R \Rightarrow \text{ keep searching}$

- How does this relate to Stigler's optimal number of draws problem?
 - **Stigler:** *n* determines the expected maximum price we are going to pay, non-sequential search
 - Here: w_R determines the expected time of unemployment, how many periods on average we have to wait before we get an acceptable wage, sequential search

McCall Model - Solving Numerically

- With an offer of w in hand worker can
 - accept the job and get

$$\frac{w}{1-\beta}$$

• reject the job and get

$$c + \beta$$
[get new offer tomorrow]

• Recursive formulation of the objective:

$$V(w) = -\kappa + \max\left\{rac{w}{1-eta}\;,\; c+eta\int V(w)dF(w)
ight\}$$

McCall Model - Solving Numerically

- Policy Function
 - Let $\sigma(w)$ be the policy function, $\sigma(w)=1$ if we accept the job

$$\frac{w}{1-\beta} > c + \beta \int V(w) dF(w)$$

$$w > (1-\beta) \left[c + \beta \int V(w) dF(w) \right]$$

- This conditions depends on the value function!
- Solve value function numerically: QuantEcon

• Now that we have V(w) we can solve for

$$\bar{V} = c + \beta \int V(w) \ dF(w)$$

where $ar{V}$ is a constant

The reservation wage makes us indifferent

$$\frac{w_R}{1-\beta} = \bar{V}$$

• $w/(1-\beta)$ is an increasing function of β and \bar{V} is constant so we have a solution to w_R .

- But for this simple model we can do better than this
- Rewrite the problem with two value function: E(w), U
 - suppose $\kappa = 0$
- The value of employment at wage w

$$E(w) = w + \beta E(w)$$

$$E(w) = \frac{w}{1 - \beta}$$
(1)

• Value of unemployment

$$U = c + \beta \int \max\{U, E(w)\} dF(w)$$
 (2)

Reservation wage

$$E(w_R) = U$$
$$\frac{w_R}{1-\beta} = U$$

$$\frac{w_R}{1-\beta} = c + \beta \int_0^{w_R} \frac{w_R}{1-\beta} \ dF(w) + \beta \int_{w_R}^{\infty} \frac{w}{1-\beta} \ dF(w)$$

$$\int_0^{w_R} \frac{w_R}{1-\beta} + \int_{w_R}^{\infty} \frac{w_R}{1-\beta}$$

$$= c + \beta \int_0^{w_R} \frac{w_R}{1-\beta} \ dF(w) + \beta \int_{w_R}^{\infty} \frac{w}{1-\beta} \ dF(w)$$

$$w_R \int_0^{w_R} dF(w) - c = \beta \int_{w_R}^{\infty} \frac{\beta w - w_R}{1 - \beta} dF(w)$$

• Adding $w_R \int_{w_R}^{\infty} dF(w)$ to both sides

$$w_R - c = \frac{\beta}{1 - \beta} \int_{w_R}^{\infty} (w - w_R) dF(w)$$

Integration by parts:

$$\int_{w_R}^{\infty} (w - w_R) \ dF(w) = \int_{w_R}^{\infty} [1 - F(w)] \ dw$$

• So finally we have

$$w_R - c = \frac{\beta}{1-\beta} \int_{w}^{\infty} [1 - F(w)] dw$$

McCall Model - Unemployment Duration

• The probability of getting a job in a given period

$$H = 1 - F(w_R)$$

- H is called the hazard function
- What is the probability of being unemployed for *n* periods

$$P(dur = n) = (1 - H)^{n-1}H$$

• The expected unemployment duration

$$\mathbb{E}[\mathsf{dur}] = \sum_{n=0}^{\infty} n(1-H)^{n-1}H = \frac{1}{H}$$

Moving to Continuous Time

- McCall model is written in discrete time
 - each period you get one offer
 - each period you decide to accept or reject
- A lot of labor search models are written in continuous time
 - since we don't have periods we need an arrival rate of job offers ${\color{black}\alpha}$
- α is a Poisson arrival rate

Poisson Arrival Process

- In an infinitesimal unit of time dt only one arrival will occur with probability αdt
- The number of arrivals N(t) in a finite time period t has a poisson distribution

$$P(N(t) = n) = \frac{(\alpha t)^n}{n!} e^{-\alpha t}$$

 Arrival times are independent and the time until arrival has an exponential distribution

$$P(T > t) = e^{-\alpha t}$$

Poisson Arrival Process - Two Properties

• **Memoryless**: for $t_1 \ge 0$ and $t_2 \ge 0$

$$P(T > t_1 + t_2) = P(T > t_1)P(T > t_2)$$

 $P(T > t_1 + t_2|t_1) = P(T > t_2)$

- Is unemployment a memoryless process?
- Random Selection: if each arrival is selected with probability p, independent of other arrivals, then the resulting process is a poisson process with intensity αp
 - The reservation wage is independent of the number of offers you have received

Moving to Continuous Time

- Environment
 - w, b are an instantaneous flows
 - ullet α is a poisson arrival rate of jobs
 - r is the discount rate
- Value of Employment a period of length dt

$$E(w) = \frac{wdt + E(w)}{1 + rdt}$$

• Take the limit as $dt \rightarrow 0$

$$rE(w) = w$$

For next time

Homework:

- 1. Write down the value function for employment (1) and unemployment (2) if you have a probability δ of losing your job every period.
- 2. Derive the continuous time value functions if δ is the poisson rate of losing your job
- Think About: Where does the wage distribution come from?