

Worksheet 6

Trig & UV Substitution

USEFUL FORMULAS FOR TRIG SUB

$\sin^2 \theta = 1 - \cos^2 \theta$	for	$\sqrt{a^2 - x^2}$
$1 + \tan^2 \theta = \sec^2 \theta$	for	$\sqrt{x^2 + a^2}$
$\sec^2 \theta - 1 = \tan^2 \theta$	for	$\sqrt{x^2 - a^2}$
SOH CAH TOA	for	$\sin(\arccos x)$ $\cos(\arcsin x)$ etc...
$\sin(2\theta) = 2 \sin \theta \cos \theta$	for	$\sin(2 \arccos x)$ $\sin(2 \arctan x)$ etc...
Completing the Square	for	anything math related

USEFUL FORMULAS FOR UV SUB

$$\begin{aligned}
 U(t) &= \frac{1}{2} \left(t + \frac{1}{t} \right) & V(t) &= \frac{1}{2} \left(t - \frac{1}{t} \right) \\
 t &= U(t) + V(t) & \frac{1}{t} &= U(t) - V(t)
 \end{aligned}$$

$1 + V^2(t) = U^2(t)$	for	$\sqrt{x^2 + a^2}$
$U^2(t) - 1 = V^2(t)$	for	$\sqrt{x^2 - a^2}$

USING TRIG-SUB

1. $\int \sqrt{16-x^2} \, dx.$

2. $\int \frac{x^3}{\sqrt{4-x^2}} \, dx$

3. $\int \frac{e^t}{\sqrt{4-e^{2t}}} \, dx$

4. $\int \frac{1}{x^2+2x+5} \, dx$

USING UV-SUB

Concerning UV-Sub, I usually recommend trying an appropriate trig substitution first and if you get a trig integral that you aren't sure how to solve then trying UV-sub.

5. $\int \sqrt{x^2 - 4} \, dx$

6. $\int \sqrt{4 + x^2} \, dx$