

1. (seqseries:quiz1)

(a) Find

$$\lim_{n \rightarrow \infty} \frac{n^2 + n + 1}{3n^2 - n - 2}$$

(b) Find an example of a sequence a_n which is bounded but not convergent.

2. (seqseries:quiz2)

(a) Find

$$\lim_{n \rightarrow \infty} \frac{3n^2 + n + 1}{n^2 - n - 2}$$

(b) Find an example of a sequence a_n which is bounded but not convergent.

3. (seqseries:geom2/x)

If $x > 2$, use the geometric series formula to find $\sum_{n=0}^{\infty} \frac{2^{n+1}}{x^n}$.

4. (seqseries:pftelecope)

Let $a_n = \frac{1}{n^2 - n}$ and $S_N = \sum_{k=2}^N a_n$.

(a) Use partial fractions to rewrite a_n .

(b) Use part (a) to write out S_2 , S_3 and S_4 explicitly and notice how terms cancel. Generalize this to find a formula for S_N .

(c) Compute $\sum_{k=2}^{\infty} a_n (= \lim_{N \rightarrow \infty} S_N)$.

5. (seqseries:serieslist)

Determine whether the following series converge:

(a) $\sum_{n=1}^{\infty} \frac{1}{n^3}$

(b) $\sum_{n=1}^{\infty} \frac{e^n}{n^3}$

(c) $\sum_{n=3}^{\infty} \frac{1}{n^3 + n - 1}$

(d) $\sum_{n=1}^{\infty} \left(\frac{n^3}{n!} \right)^n$

(e) $\sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!}$

$$(f) \sum_{n=2}^{\infty} \frac{1}{n \ln(n)}$$

$$(g) \sum_{n=1}^{\infty} e^{-(\ln(n))^2} \text{ (Hints: } a^{bc} = (a^b)^c \text{ and } e^{-\ln(n)} = \frac{1}{n} \text{)}$$

6. (seqseries:serieslist2)

Determine whether the following series converge. If the series depends on x , determine for which values of x it converges.

$$(a) \sum_{n=0}^{\infty} e^{-nx}$$

$$(b) \sum_{n=1}^{\infty} \frac{1}{n^6 + 5n}$$

$$(c) \sum_{n=1}^{\infty} \frac{n!}{e^n}$$

$$(d) \sum_{n=1}^{\infty} \frac{\ln(n)}{n}$$

$$(e) \sum_{n=1}^{\infty} \left(1 - \frac{1}{n}\right)^n$$

7. (seqseries:quiz3)

Determine whether or not the series $\sum_{n=1}^{\infty} n e^{-n}$ converges.

8. (seqseries:quiz4)

Determine whether or not the series $\sum_{n=1}^{\infty} n e^{-2n}$ converges.