

1. (bg222:deriv1)  
Define  $f(x) = x \ln(x) + \sin(x^2 + 1)$ . Compute  $f'(x)$ .
2. (bg222:deriv2)  
Define  $f(x) = \ln(x) \sin(x) + \sqrt{x^4 + x^2}$ . Compute  $f'(x)$ .
3. (bg222:deriv3)  
Compute each of the following derivatives.
  - (a) Compute  $y'$  if  $y = x^3 \left(x^2 - \frac{1}{x}\right)$
  - (b)  $\frac{d}{dx} \sin(x^2 + 5)$
  - (c)  $\frac{d}{dx} (x^2 \cdot \cos x)$
  - (d)  $\frac{d}{dx} (x^2 \cdot \ln x \cdot \cos x)$
4. (bg222:ftoc1)  
Define  $f(x) = \int_x^{x^2} e^{t^3} dt$ . Compute  $f'(x)$ . Hint: split the integral into  $\int_x^1$  and  $\int_1^{x^2}$  and use the Fundamental Theorem of Calculus.
5. (bg222:ftoc2)  
Compute  $\frac{d}{dx} \int_x^1 \ln z \, dz$ . (Hint: remember the “Fundamental Theorem of Calculus”.)
6. (bg222:int1)  
Compute
 
$$\int \frac{\ln(\pi x)}{x} dx$$
7. (bg222:int2)  
Compute  $\int_e^{e^3} \frac{1}{x \ln(x)} dx$ .
8. (bg222:int3)  
Compute  $\int_0^{\frac{\pi}{2}} \cos(t) e^{\sin(t)} dt$ .

9. (bg222:int4)  
Compute  $\int e^x \sin(2\pi e^x) dx$
10. (bg222:int5)  
Compute  $\int_0^x \left( \int_0^t \cos(s) ds \right) dt$ .
11. (bg222:int6)  
Compute each of the following integrals.
- (a)  $\int x^2 \sin(x^3) dx$
  - (b)  $\int \frac{x^3 + \sqrt{x} + \sqrt{\pi}}{\sqrt{x}} dx$
  - (c)  $\int_{-2}^3 (x^2 + x + 1) dx$
12. (bg222:tf1)  
 $\frac{d}{dx} \left( \frac{1}{x} \right) = \ln x$ .
13. (background:TF)  
True or False:
- (a)  $\frac{d}{dx} \left( \frac{1}{x} \right) = \ln x$
  - (b)  $\frac{d}{dt} \int_0^t \frac{dx}{1+x^2} = \frac{1}{1+t^2}$
  - (c)  $\sqrt{x^2 + 9} = x + 3$
  - (d) The function  $f(x) = \frac{1}{x+4}$  is defined for all values of  $x$  except for  $x = -4$
  - (e)  $\int e^{(x^3)} = e^{(x^3)} + C$
  - (f) If  $f(x) = x^2 \cdot g(x)$  then  $f'(x) = 2x \cdot g'(x)$
14. (bg222:optimization)  
Which rectangle has the largest area, among all those rectangles for which the total length of the sides is 1?