

1. (tayloreerror:expatapoint)
Find a bound on the error of the approximation of $e^{\frac{1}{3}}$ by $1 + \frac{1}{3} + \frac{1}{3^2 2!} + \frac{1}{3^3 (3!)}$.
2. (tayloreerror:sinconvergence)
Find a bound for $R_n^0 \sin(x)$ and use this to show that $T_n^0 \sin(x) \rightarrow \sin(x)$ for all x as $n \rightarrow \infty$.
3. (tayloreerror:sin3convergence)
Find a bound for $R_n^0 \sin(3x)$ and use this to show that $T_n^0 \sin(3x) \rightarrow \sin(3x)$ for all x as $n \rightarrow \infty$.
4. (tayloreerror:exp2convergence)
Find a bound on $R_n^0 e^{2x}$ and use this to show that for every x , $T_n^0 e^{2x} \rightarrow e^{2x}$ as $n \rightarrow \infty$.
5. (tayloreerror:sincosconvergence)
Find a bound on $R_n^0 (\sin(x) + \cos(x))$ and use this to show that $T_n^0 (\sin(x) + \cos(x))$ converges to $\sin(x) + \cos(x)$ as $n \rightarrow \infty$.
6. (tayloreerror:cosgoodenough)
Find a bound on $|R_n \cos(x)|_{x=1}$ and use this information to find a decimal approximation of $\cos(1)$ with an error of at most .1.