Understanding the Growth in Data Science StackOverflow Questions

Alana Willis, Clare Cruz, Dan Nason, & Megan Christy
Department of Statistics and Data Science
Carnegie Mellon University

April 24, 2022

Executive Summary

StackOverflow is a public question-forum that is popular among data scientists and programmers. In this analysis, it is used to quantify the use of programming languages, such as Python and R, and data science topics, such as Regression and Time Series. Using time series modeling methods on monthly question counts of such languages and topics, we hope to see which data science topics significantly contribute to the number of StackOverflow questions for R and Python and which tool between R and Python has the greatest predicted growth from 2019 to 2021. The dataset used for analysis was obtained from Kaggle and includes the monthly question counts from December 2011 to December 2019 for 82 data science tags. We began our analysis by exploring the data through several time series visualizations, building univariate SARIMA models for the R and Python series to identify complex patterns of trend and seasonality, and finally building multivariate VAR models in an attempt to answer our research questions. Based on our analysis we found that Python is forecasted to have a 17.97% growth rate from December 2011 to December 2019 while R is forecasted to have a 26.24% growth rate. We also concluded that R has an overall better fit with the data science topics than Python with Classification and Cluster Analysis as significant predictors. We believe that the difference in results between Python and R could be attributed to the fact that R is primarily used for statistical modeling while Python has many other uses, such as software engineering tasks. One major limitation of our analysis is that we chose the variables for our models based on intuition and previous experiences. Thus, there may be better features to predict Python and R question counts. With more time, we would like to extend the time frame of our analysis by including data from 2020 and 2021 to verify the results of our model forecasts. Overall, we believe this analysis provides informative insights on the usage of data science methods in Python and R and how the use of these tools for data science is predicted to grow.

Introduction

Python and R are two data science tools used frequently in both industry and academia. It would be interesting to know whether these platforms are being used for similar data science topics,

such as regression or classification, or whether people tend to use one over the other for certain topics. It would also be interesting to know which of these tools is expected to dominate over the other in terms of usage for data science. We investigate the use of these programming languages through counts of questions on StackOverflow, a public question-forum that is popular for data scientists and programmers. The main research questions we aim to answer are:

- Which data science topics significantly contributed to the number of StackOverflow questions for Python and R?
- Which tool between R and Python has the greatest predicted growth between 2019 and 2021?

Data

The data for this analysis was provided by Aishwarya and Vaishnavi V. at TactLabs via the public data warehouse Kaggle (Aishwarya 2020). The data set consists of question counts for various Stack Overflow data science topics. The raw data file has 82 columns of different topics, and 133 rows of monthly question counts from December 2009 to December 2019. Below are the variables used in our analysis:

- python
- r
- regression
- machine learning
- classification
- cluster analysis
- time series

While we were performing the exploratory data analysis, we decided to exclude the first two years (January 2009 to December 2010) from the dataset for a few reasons. To start, some of the topics had no recorded questions in these first two years which negatively affects the modeling process. Similarly, 2009 is around the period when data science and StackOverflow became popular and utilized by people in the field. Consequently, the data in the first two years look drastically different than the remainder of the dataset. Therefore, we decided that it was best to focus on the data from 2011 to 2019. The dataset used in all exploratory data analysis and subsequent modeling contains the monthly counts from December 2011 to December 2019.

Methods

Exploratory Data Analysis

We began our analysis by exploring our data through several time series visualizations. First, each of the relevant time series was plotted on the same graph to understand how each series compared to another and to see if there were any overall patterns. Then, a correlation matrix was created to calculate the strength of the relationships between the series. Monthly plots and decompositions were also made to see if there was any seasonality and where the seasonal components were taking place. Finally, an ACF and PACF plot was made to measure the temporal correlations within each series.

SARIMA Modeling

As will be explained later in the results, our exploratory data analysis found that our time series had complex patterns. However, the visualizations from the exploratory data analysis were not sufficient to make modeling conclusions. Consequently, we decided to build an autoregressive integrated moving average model or SARIMA model for the R and Python series to better understand what transformations were needed before fitting a final model. We started the model-building process by selecting SARIMA orders based on the ACF and PACF plots in the exploratory data analysis. Then, we checked the model by examining the residuals, fitted versus observed plots, ACF and PACF plots, QQ plots, and running multiple simulations. After the initial diagnostics, we created an additional model by using the auto.arima() function in R. The parameters for this automatic modeling selection function were decided based on the information gained from the initial model we built. If the model that was created from the auto.arima() function matched the model that was constructed from the exploratory data analysis and the model diagnostics showed no glaring errors, the similar SARIMA model was used to calculate forecasted values. But if the auto.arima() function produced a different model, then the model diagnostics listed earlier were applied again to see if the new model is a better fit to the data. The models with similar diagnostics were compared using AIC, RMSE, and MAE. In the end, the orders from the final SARIMA models are further examined to determine what data transformations are needed before fitting a VAR model.

VAR Modeling

While the ARIMA models are helpful in our understanding of the data, they cannot suggest which data science topics are significant to the R and Python series. This is because ARIMA models are used specifically for univariate time series, but our inference question requires understanding the relationships between several time series. Therefore, we fit a vector autoregressive moving average model or VAR model using the VARselect() function in the vars package since it can evaluate the relationship between multiple time series. In the function, we

set the 'type' of fitting to none since we manually detrended and deseasonalized the series before fitting the model and set the maximum lag to 13 since any variables past this point would not be constructive to the analysis. This transformation was done by adding an indicator variable for each month to capture the seasonality and modeling the residuals of a simple linear regression for the time series to account for the trends. Again, we performed model checks to see if the selected model from the function was a good fit for the data. The diagnostics included a plot of the fitted versus actuals, ACF and PACFs of the residuals, the forecasts, and the plot of the residuals as well as generating the model summary statistics. If any transformations are required to fit a VAR model, we reversed all alterations in the final forecasts and conclusions. Now that we have a final model, we answered our research questions by analyzing the coefficients and forecasts. Specifically, we checked the model coefficients to determine which data science topics contributed to the R and Python models. Then, we calculated a simple percent growth rate from the final forecasts using the last actual and predicted value to see if R or Python had the highest predicted growth from 2019 to 2021.

Results

Exploratory Data Analysis

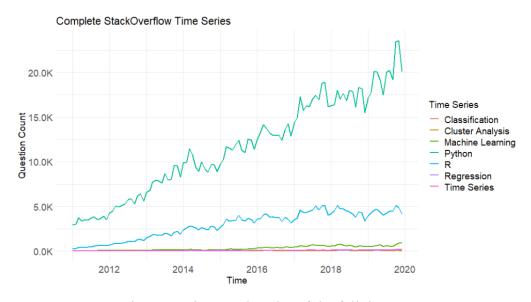


Figure 1: Times series plot of the full data set

Recall that our exploratory data analysis started with a complete view of our time series (Figure 1). Unsurprisingly, Python stands out among all the time series with the largest number of questions since it is arguably the most popular data science tool. R has the second most number of questions, which is expected since R is also favored for academic research but has fewer uses than Python. The remaining topics have significantly fewer monthly questions, with machine

learning having the most questions out of the data science topics. In the individual plots in Figure 2, we can see that every series has an increasing trend which aligns with our general observations in the growing data science job market and demand for these skills. The increasing trend was supported by our correlation plot (Figure 3), which shows that all the series have a strong positive correlation with each other. It is worth noting that R and Python have one of the strongest correlations, which may cause issues with multicollinearity in the modeling process.

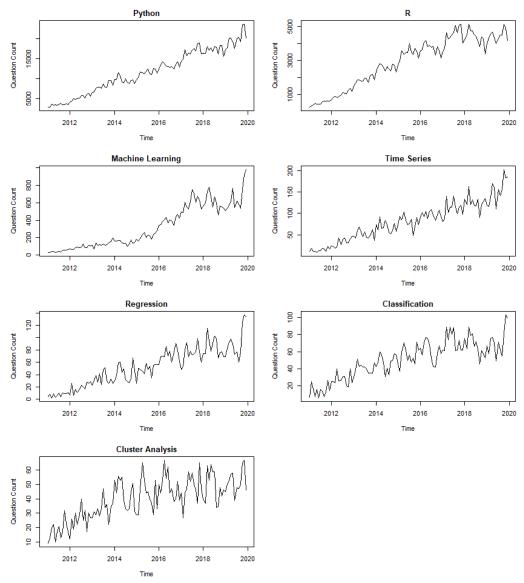


Figure 2: Individual plots for all time series

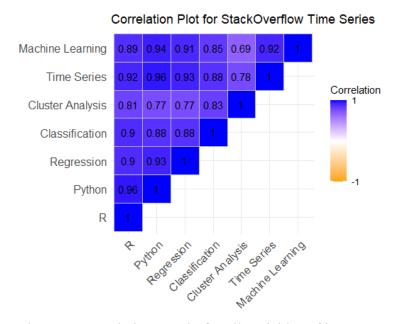


Figure 3: Correlation matrix for all variables of interest

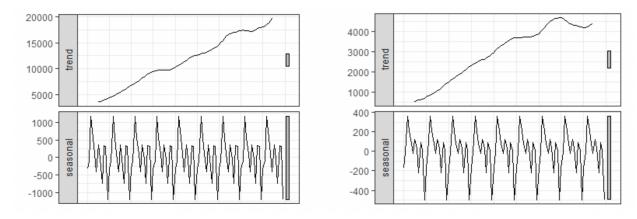


Figure 4: Decomposition of Python (left) and R (right) time series

Additionally, the decomposition of the time series for R and Python shows that there may be seasonality in the time series since there are higher question counts in March, April, and November (Figure 4). The plots also support the idea that a trend is present since the trend component of the decomposition has an increasing linear line. Next, the ACF plots for all the time series show a slow decay with increasing lags, which suggests that there may be an autoregressive behavior to the series (Tech. Apx. page 11). Additionally, the PACF plots occasionally show a small significant correlation around a year-long lag (Tech. Apx. page 12). This supports our observations for the decomposition plots which suggest a seasonality component to the time series.

SARIMA Modeling

The first step in our modeling process was to fit a SARIMA model to our Python and R series to learn more about the behaviors we observed in the exploratory data analysis. Recall that the Python process showed autoregressive behavior in the autocorrelation plots, increasing trend, and semi-annual seasonality. Therefore, the first SARIMA model was fitted with a non-seasonal autoregressive term, a seasonal autoregressive term, and a seasonal difference term. Now that we found the first model, we created several diagnostic plots to see if our initial observations translated into a model that fits well with the data. All the diagnostic plots for the R and Python SARIMA models can be viewed in the technical appendix starting on page 13. Firstly, the fitted versus observed plot for Python indicated that the model fits the data well since the predicted values were close to the original values, with a few possible exceptions in 2018 (Figure 5). In some parts of the series, it looks like the model is predicting slightly ahead of the observed values, but overall, it looks to be a good fit for the data.

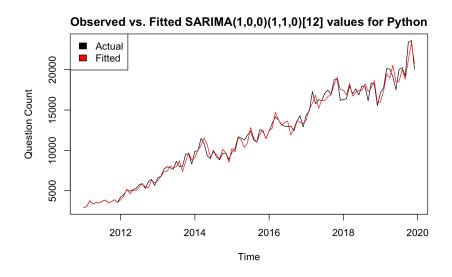


Figure 5: Observed versus fitted plot for Python SARIMA() model

The residuals also appear to be approximately stationary white noise with a constant mean and variance. However, the ACF and PACF plots display a small significant correlation around the 13th lag. These correlations are not significant enough to warrant any action, but it is worth noting that there may be an underlying behavior in the series that the model is not capturing. Also, the QQ plot shows that the residuals are approximately normal. Several of the simulations exhibited similar behaviors to the original StackOverflow time series since they had constant increasing trends with slight annual variations. Lastly, the forecasts from the SARIMA model for Python have an increasing trend with some variations within the year which is what we would expect based on the previous findings (Figure 6). All of these observations suggest that the SARIMA(1,0,0)(1,1,0) model is a good fit to the data and that the original Python time series needs to be detrended and deseasonalized.

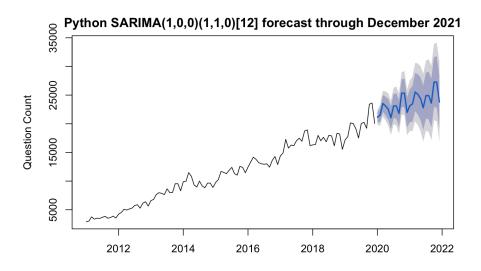


Figure 6: Forecasted Python SARIMA() series through December 2021

The same initial SARIMA(1,0,0)(1,1,0) model was fit to the R time series since the exploratory data analysis showed similar trends and seasonality for both the Python and R time series. Overall, the R time series had similar results for most of the model diagnostic checks except for the ACF and PACF plots. Specifically, the Python time series had some small significant correlations in the ACF and PACF plots while there appear to be no such significant correlations in the R time series.

However, the auto.arima() function in R produced a different model than the one suggested by the exploratory data analysis. Specifically, the auto.arima() function suggests adding a non-seasonal difference term, removing a seasonal autoregressive component, and adding a seasonal moving average term to make a SARIMA(1,1,0)(0,1,1) model. However, when these changes were made, the model diagnostics produced similar results to the initial model created from the exploratory data analysis. Since the diagnostic plots did not suggest a superior model, we looked at the model summary statistics to select a final model. Looking at the summary output on page 30 in the technical appendix, the model that the auto.arima() function picks has slightly lower AIC and RMSE/MAE. Therefore, we selected the SARIMA(1,1,0)(0,1,1) as the best model for the data. The presence of a seasonal and trend effect in the SARIMA model indicates that a transformation to the R series is needed before the VAR modeling process.

The diagnostic plots for the final R model led to similar conclusions about model validity that we discussed previously with the Python model. In the observed versus fitted plot (Figure 7), the model appears to fit the data well since the observed values line up well with the predicted values, despite the predictions being slightly ahead of the observed values in some parts of the series. The residuals appear to be white noise and there are no significant lags in the ACF and

PACF of the residuals. The QQ plot shows the residuals are approximately normal and the simulated plots look like they could reasonably come from the same underlying stochastic process as the observed data. Finally, the forecasts for the R process seem to follow the generally increasing trend with a bit of within-year variability that has been observed in the data so far (Figure 8).

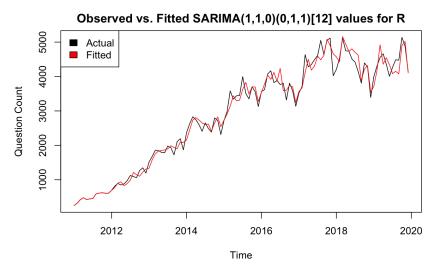


Figure 7: Observed versus fitted plot for R SARIMA() model

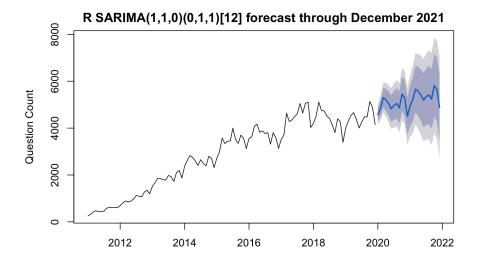


Figure 8: Forecasted R SARIMA() series through December 2021

VARMA Modeling

The final SARIMA models and the exploratory data analysis showed that both the R and Python series had a trend and seasonal effect. Therefore, both series were detrended and deseasonalized before fitting a VAR model to answer our research questions about the growth and contributors to the StackOverflow questions. The series were first detrended by linearly regressing the respective time series on their time index and extracting the residuals from these model fits. Another linear regression was then fitted with the detrended series using indicator variables for each month as predictors. Extracting the residuals from this model fit yielded the detrended and deseasonalized data. After transforming the data, we used the VARselect function to fit a VAR model using the data science topics for both the R and Python series. For our Python time series, the automatic model selection found that a VAR(1) model is the best fit for the data (Table 1).

Variable (Lag 1)	Coefficient Est	Std Error
Python	0.67***	0.07
Machine Learning	0.39	0.69
Classification	4.87	6.86
Regression	-5.43	5.81
Time Series	0.24	4.29
Cluster Analysis	-2.65	7.35

^{***} Indicates a p-value below 0.05

Table 1: Python VAR(1) model coefficients

Interestingly, the summary statistics of the VAR(1) in Table 1 showed that the model for the detrended and deseasonalized Python series can not be explained by any of the data science topics since all their p-values are above 0.05. The only variable that seems to predict the Python question count is the lagged variable of the Python series itself. The summary also revealed that the R-squared for the model is 0.43 which suggests that the model does not have strong predictive power. In the model diagnostics, the plot of the observed versus fitted values for the Python VAR(1) model showed that the model fit well to the data. However, the predicted values had a worse fit in the data's peaks and troughs (Figure 9).

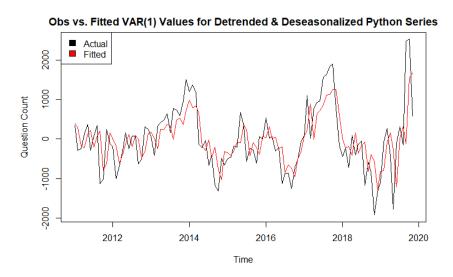


Figure 9: Observed versus expected values for the VAR(1) fitted to the detrended and deseasonalized Python

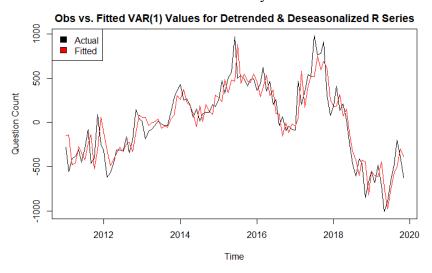


Figure 10: Observed versus expected values for the VAR(1) fitted to the detrended and deseasonalized R time series

Additionally, the ACF and CCF plots occasionally showed significant correlations around the year-long lag. All of these characteristics indicate that the variables selected for the VAR(1) were not constructive and the model may not be the best fit with the data. However, the cause for the poor fit was not obvious from the SARIMA modeling and exploratory data analysis. Therefore, the VAR(1) was kept as the final model. Using the final VAR(1) model, the forecasted values for the Python series were calculated for the next two years (Figure 11). Specifically, Python's predicted number of questions is forecasted to grow from 20,058 in December 2019 to 23,661 in December 2021, a 17.97% growth rate.

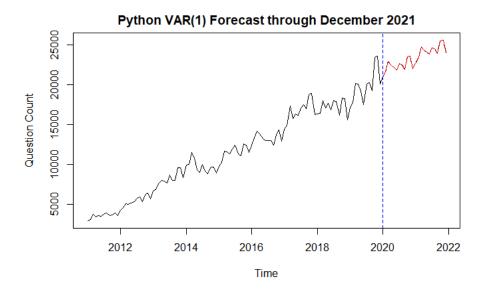


Figure 11: Forecasted Python VAR(1) series through December 2021

Variable (Lag 1)	Coefficient Est	Std Error
R	0.87***	0.05
Machine Learning	-0.24	0.21
Classification	7.79***	2.15
Regression	-2.57	1.78
Time Series	0.73	1.36
Cluster Analysis	-6.18***	2.25

^{***} Indicates a p-value below 0.05

Table 2: R VAR(1) model coefficients

Moving on to the R time series, the VARselect function determined that a VAR(1) model was also the best fit for the data. Unlike the Python model, the VAR(1) model for R has two variables that significantly contribute to the model: classification and cluster analysis. Both variables have p-values below 0.05 which suggest that they explain a significant amount of variance in the Python series. It is worth noting that the cluster analysis variable has a negative coefficient estimate, which indicates that an increase in the number of cluster analysis questions in the previous month is associated with a decrease in the number of Python questions this month. Additionally, the R-squared value is 0.81 which suggests that the model has strong predictive power. The superior fit is also present in the fitted versus observed plot since the lines are closer

together and have similar values in unusual spikes. The diagnostics for the VAR(1) also indicated a better fit to the data since the residuals for the detrended and deseasonalized R series follow a stationary behavior, with a constant mean and variance. Plus, the ACF and PACF plots also showed fewer instances of significant correlations around the annual lag point. The affirmative evidence from the model diagnostics suggested a good fit for the data, so we selected the VAR(1) model as the final model for the R series. From the model, we calculated that R's predicted number of questions is forecasted to grow from 4,150 in December 2019 to 5,238 in December 2021, a 26.24% growth rate (Figure 12).

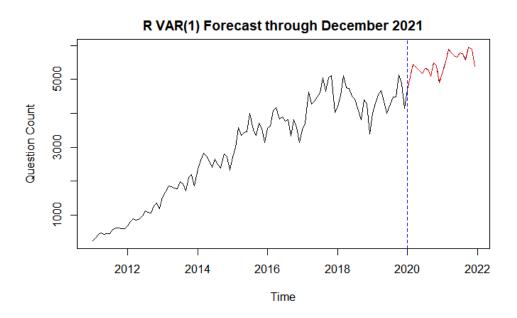


Figure 12: Forecasted R VAR(1) series through December 2021

Discussion

In this analysis, we built models to predict the number of StackOverflow questions for Python and R using SARIMA modeling. We found that for Python, a model with seasonal and non-seasonal autoregressive terms and a seasonal difference term fits the data well while for R, a model with a non-seasonal autoregressive term, a seasonal moving average term, and a seasonal and non-seasonal difference term fits the data well. We also saw that according to these models, the number of questions is forecasted to continue the generally increasing trend with some within-year variability that has been observed in the data thus far.

We also examined the relationship between different data science topics and the number of StackOverflow questions for Python and R using VAR models. We found that classification and clustering are associated with the number of R questions, and we discovered that none of the data

science topics included in modeling are significantly associated with the number of Python questions. We found that R has an overall better fit with data science topics than Python does. In addition, R is predicted to have a faster growth rate in the number of StackOverflow questions than Python (26.24% vs 17.97%) between the years 2019 and 2021.

We believe that the difference in results we see between Python and R could be attributable to the fact that R is primarily used for statistical modeling while Python has many other uses, such as software engineering tasks. This distinction could help explain the differences we found in significant predictors, adjusted R-squared, and growth rate. We are not sure why clustering and classification are the only significant predictors of R question counts and would be curious to investigate this further in a future analysis.

It is important to note that the series used in this analysis are highly correlated with each other. This correlation may be contributing to the lack of statistically significant predictors we find in the VAR models. Since R and Python are highly correlated with each other, we tried including Python as a predictor in the VAR model for R and vice versa, but these additions did not significantly improve the model fit.

One limitation of this analysis is that we used a limited selection of data science topics to keep the models manageable. We chose the topics based on our intuition and previous experiences, but there may be better features to predict Python and R question counts. Another limitation is feature redundancy in the data. Since posts on StackOverflow can be tagged with multiple topics, it is possible that some questions are being double counted in the data. For example, there is a Python column and a Python 3.0 column, and these tags may both be used on a single question. In addition, we may be losing important or interesting patterns in the data due to monthly aggregation. A future study may examine the counts of questions at a daily or weekly frequency and see if the results are consistent. Finally, it may not be reasonable to compare R and Python since, as previously mentioned, R is primarily used for statistical modeling while Python has several additional uses. This makes it unsurprising that we find that some data science topics are significant predictors of the number of R questions, but not of the number of Python questions.

Some next steps we would take include extending the time frame of our analysis by including data from 2020 and 2021 and verifying the results of our model forecasts with this new data. We would also try including more predictors in the model, such as decision trees and support vector machines, to see if they can predict question counts better than the current data science topics. In addition, we would like to add an indicator variable for whether the observation takes place during the academic semester to account for potential differences in question frequencies when students are in and not in school. Finally, we would consider performing a log transformation on all of the time series before modeling to see if the transformed data produces better model fits.

In summary, this analysis provides informative insights on the usage of data science methods in Python and R and how the use of these tools for data science is predicted to grow. It will be interesting to see whether the model predictions are accurate in determining that R will grow faster than Python in terms of StackOverflow data science topic question counts.

References

Aishwarya, and Vaishnavi V. (2020), "StackOverflow Questions Count Time Series", Kaggle, Available at

https://www.kaggle.com/datasets/aishu200023/stackindex?select=MLTollsStackOverflow.csv.

Code Appendix

Contents

Research Questions	2		
Prediction	2		
Inference			
Script Setup	2		
Packages Load	2		
Data Load	3		
Time Series Objects	3		
Exploratory Data Analysis	4		
Full Time Series Visualization	4		
Correlation Plot	5		
Individual Series Plots	6		
Month Plots	7		
Decompositions	9		
ACF and PACF	10		
ARIMA Modeling	13		
Python	13		
Manual ARIMA Modeling	13		
Manual ARIMA Diagnostics	13		
Model Validation	17		
Forecasts	18		
R	19		
Manual ARIMA Modeling	19		
Manual ARIMA Diagnostics	19		

Model Validation	23
Model Fit - Auto ARIMA	24
Model Diagnostics - Auto ARIMA	24
Forecasts	28
MA Modeling	30
rthon	31
Deseasonalize and Detrend	31
Variable Selection	32
Model Validation	35
Forecasts	40
	42
Deseasonalize and Detrend	43
Variable Selection	43
Model Validation	47
Forecasts	52
	Thon Deseasonalize and Detrend Variable Selection Model Validation Forecasts

Research Questions

Prediction

Which data science programs between R and Python had the highest predicted growth rate in from 2019 to 2022?

Inference

Which data science topics (classification, regression, cluster analysis, time series, and machine learning) significantly contributed to the growth rates in R and Python?

Script Setup

Packages Load

```
# Package Load
library(ggplot2)
library(tidyverse)
library(lubridate)
library(vars)
library(xts)
library(scales)
library(fGarch)
library(ggcorrplot)
library(forecast)
```

Data Load

```
# Read in the data
#stack.data <- read.csv("C:/Users/cbrig/OneDrive/CMU/Time Series/Course Project/time_series_project_dat
stack.data <- read.csv("C:/Users/Owner/CMU/Spring/36-618/Project/time_series_project_data.csv")

clean.stack.data <- stack.data %>%
    mutate(date = lubridate::mdy(date)) %>%
    dplyr::select(date, r, python, regression, classification, cluster_analysis, time_series, machine_lead
mutate(id = row_number()) %>%
    dplyr::filter(id > 24) %>%
    dplyr::select(-id)
#head(clean.stack.data)
```

Please note that the first two years were excluded from the data set for a few reasons. To start, some of the topics had no recorded questions in these first two years which negatively affects the modeling process. Similarly, 2009 is around the time period where data science and StackOverflow became popular and utilized by people in the field. Consequently, the data in the first two years looks drastically different than the remainder of the dataset. Therefore, we decided that it was best to focus on the data from 2011 to 2019.

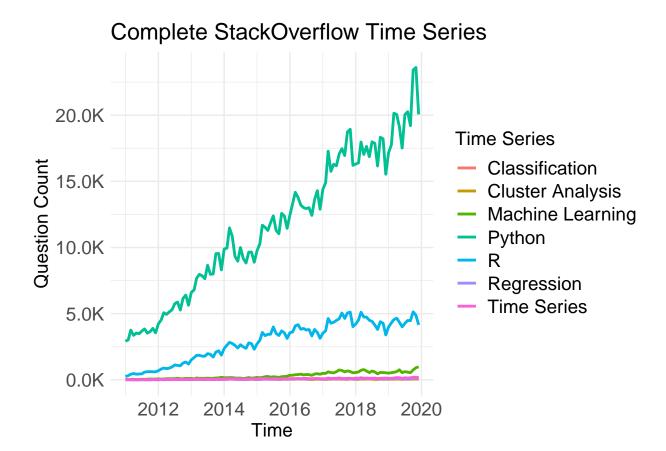
Time Series Objects

```
# Create a formal time series for every series
for(variable in predictor.list){
  name <- pasteO(variable, '.ts')
  assign(name, ts(clean.stack.data[variable], start = c(2011,1), frequency = 12))
}
# Store the time series in a list so that we can access them easily</pre>
```

Exploratory Data Analysis

Full Time Series Visualization

```
# Visualizes the entire data set
# Create the data needed for the visualization
full.ts.viz <- clean.stack.data %>%
  dplyr::select(all_of(full.var.list)) %>%
 rename(Python = python, R = r, 'Machine Learning' = machine_learning,
         Classification = classification, 'Cluster Analysis' = cluster_analysis,
         'Time Series' = time_series, Regression = regression) %>%
  gather(key = "variable", value = "value", -date)
# Create the visualization
ggplot(full.ts.viz, aes(x = date, y = value, color = variable, group = variable)) +
  geom_line(size = 1) +
  theme_minimal()+
    scale_y_continuous(labels = label_number(suffix = "K", scale = 1e-3))+
  labs(color='Time Series', y = 'Question Count', x = 'Time', title = "Complete StackOverflow Time Seri
  theme(text = element_text(size=14),
       axis.text.x = element text(size = 14),
       axis.text.y = element_text(size = 14),
       legend.text = element_text(size = 14))
```

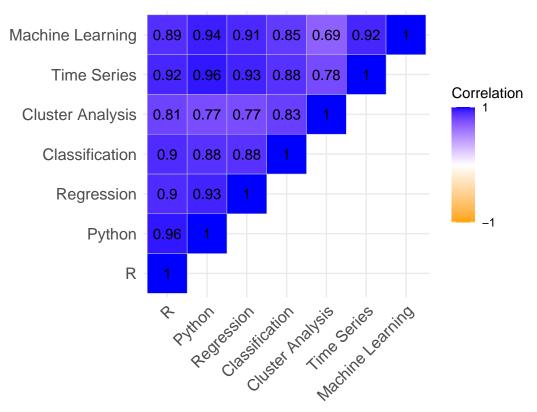


Unsurprisingly, Python stands out among all the time series with the largest number of questions since it is the most popular data science tool. The magnitude can also be explained by the other applications in different fields. R has the second most amount of questions which is also expected since R has other uses. The remaining topics have significantly less monthly questions, with machine learning having the most questions out of the data science topics. While it is hard to see the behavior in the models, every series has an increasing trend. This aligns with the growing data science job market and demand for these skills.

Correlation Plot

Scale for 'fill' is already present. Adding another scale for 'fill', which ## will replace the existing scale.

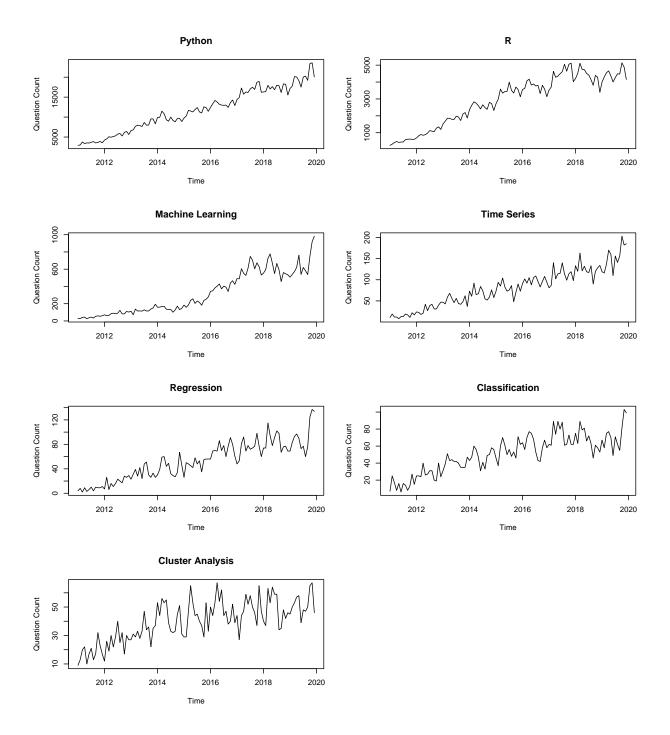
Correlation Plot for StackOverflow Time Series



The correlation plot shows that all the series have a strong positive correlation with each other. This matches the observations from the full time series since they all have an increasing trend. It is worth noting that R and Python have one of the strong correlations which may cause issues with multicollinearity in the modeling process.

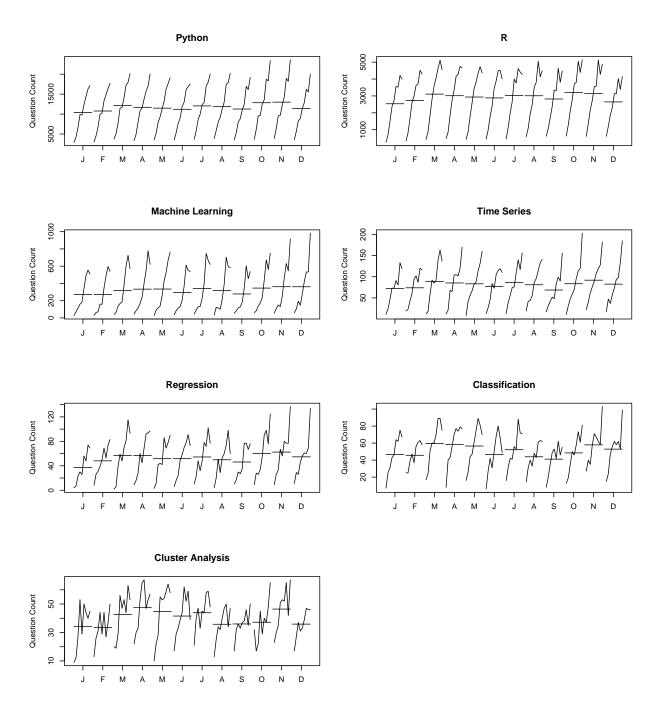
Individual Series Plots

```
par(mfrow = c(4,2))
for(i in 1:length(series.list)){
  plot(series.list[[i]], main = pretty.names[[i]], ylab = 'Question Count')}
```



Month Plots

```
par(mfrow = c(4,2))
for(i in 1:length(series.list)){
  monthplot(series.list[[i]], main = pretty.names[[i]], ylab = 'Question Count')}
```



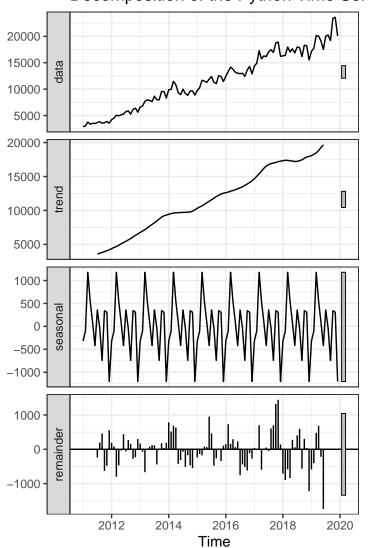
The decomposition of the time series for R and Python show that there may be seasonality in the time series since there are higher question counts in March, April, and November. While there may be several causes for this, one possible explanation could be the academic semester. In other words, students tend to start using these tools during these months.

Decompositions

```
# Commented out to save space
# for(i in 1:length(series.list)){
# plot(decompose(series.list[[i]]))}

# Nice decomposition plots for the presentation and paper
python.ts %>%
    decompose() %>%
    autoplot()+
    theme_bw() +
    labs(title = 'Decomposition of the Python Time Series')
```

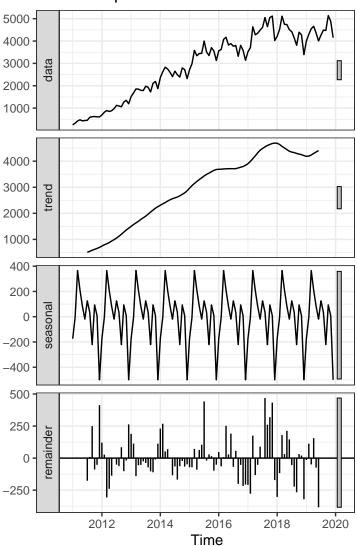
Decomposition of the Python Time Ser



```
r.ts %>%
decompose() %>%
```

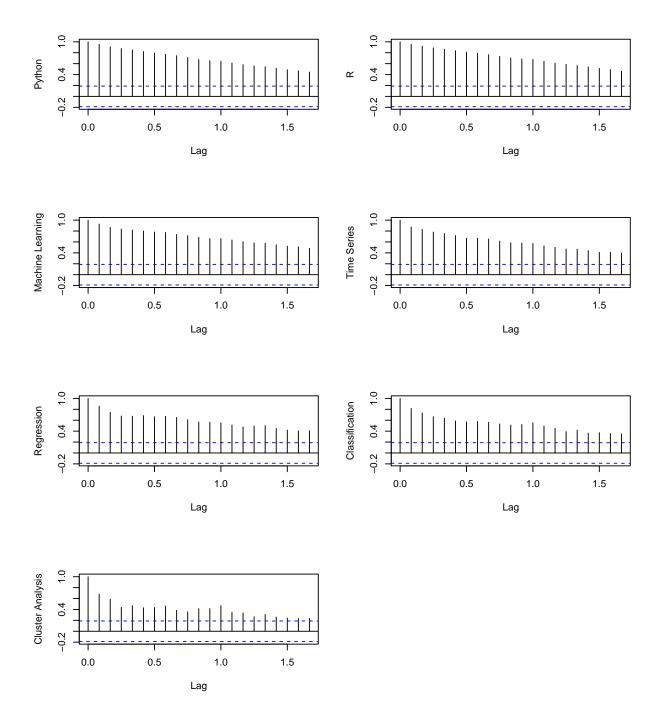
```
autoplot() +
theme_bw() +
labs(title = 'Decomposition of the R Time Series')
```

Decomposition of the R Time Series

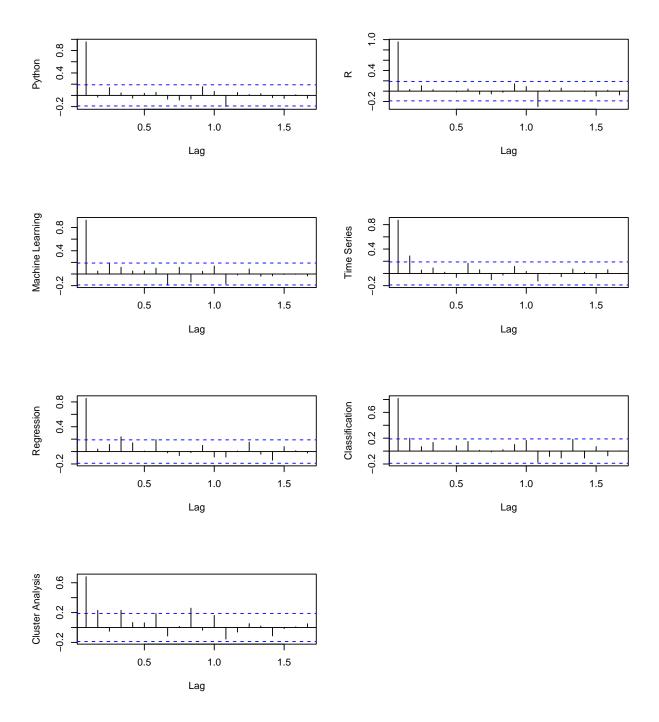


ACF and PACF

```
# ACF
par(mfrow = c(4,2))
for(i in 1:length(series.list)){
   acf(series.list[[i]], ylab = pretty.names[[i]], main = '')}
# PACF
par(mfrow = c(4,2))
```



```
for(i in 1:length(series.list)){
  pacf(series.list[[i]], ylab = pretty.names[[i]], main = '')}
```



The ACF plots for all the time series show a slow decay with increasing lags which suggests that there may be an autoregressive behavior to the series. Additionally, the PACF plots occasionally show a small significant correlation around a year long lag. This supports our observations for the decompositions which suggests a seasonality component to the time series.

ARIMA Modeling

Our exploratory data analysis showed that our time series has increasing trends with a possible annual seasonal component. To better understand our series, an ARIMA model will be built for the R and Python series. The model building process will start by fitting a model based on the findings from the exploratory data analysis. Then, the model will be checked through residual versus observed plots, ACF and PACF plots, QQ plots, and multiple simulations to see if the fitted model is a good fit to the data. After the initial diagnosis, an additional model will be created using the auto.arima() function in R. The parameters for this function will be decided based on the initial model built from the exploratory data analysis. If the model from the auto.arime() function matches the model that was built from the exploratory data analysis and the model diagnostics showed no glaring errors, the ARIMA model will be used to calculate forecasted values. If the auto.arima() function produces a different model, then the model diagnostics listed earlier will be applied again to see if the new model is a better fit to the data. The orders from the final ARIMA model will determine what actions need to be taken before fitting the VARMA model.

Python

Manual ARIMA Modeling

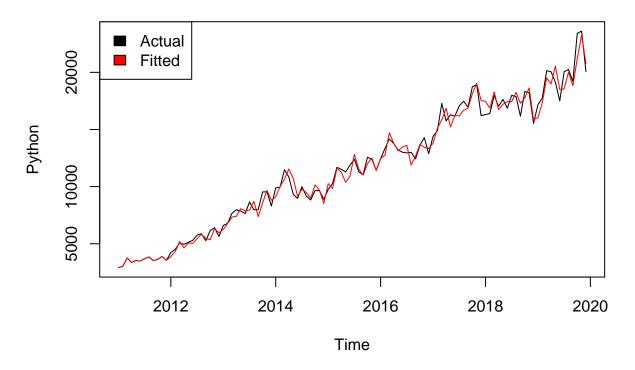
```
# Python Model 1 by Manual Fits
python.mod1 = arima(python.ts, order = c(1,0,0), seasonal = list(order = c(1,1,0), period = 12))
```

The exploratory data analysis showed autoregressive behavior, increasing trend, and annual seasonality. Therefore, the first ARIMA model was fitted with a non-seasonal autoregressive term, a seasonal autoregressive term, and a seasonal trend term.

Manual ARIMA Diagnostics

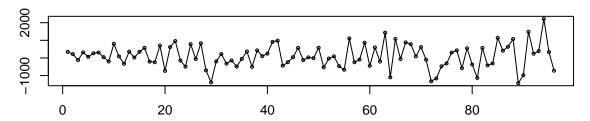
Residuals

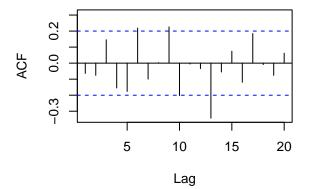
Observed vs. Fitted ARIMA values for Manual Python Model

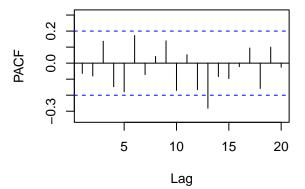


tsdisplay(resid(python.mod1)[13:length(python.mod1\$resid)], main= "Manual ARIMA Python Model Residuals"

Manual ARIMA Python Model Residuals

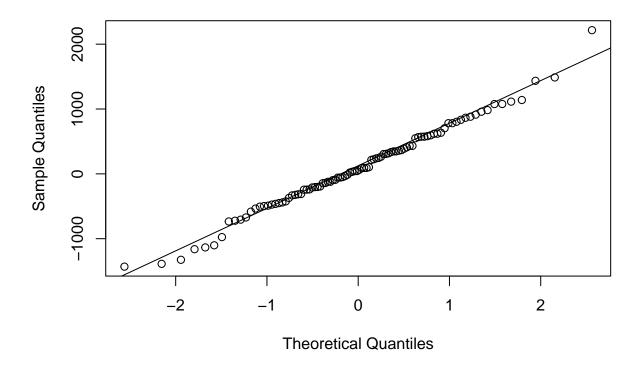






qqnorm(python.mod1\$resid[13:length(python.mod1\$resid)])
qqline(python.mod1\$resid[13:length(python.mod1\$resid)])

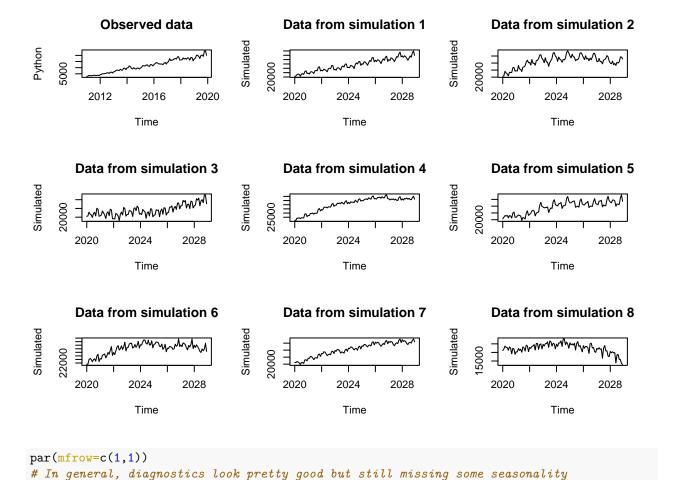
Normal Q-Q Plot



The fitted versus observed plot shows that the model fits the data well, with a few possible exceptions in 2018. The residuals also appear to be approximately stationary with a constant mean and variance. However, the ACF and PACF plots display a small significant correlation around the 13th lag. These correlations are not significant enough to warrant any action, but it is worth noting that there may be an underlying behavior in the series. Also, the QQ plot shows that the residuals are approximately normal.

Simulations

```
# Plot Multiple Simulations
par(mfrow=c(3,3))
plot(python.ts, ylab = 'Python', main = 'Observed data')
for (i in 1:8){
   set.seed(i)
   plot(simulate(python.mod1),
       ylab = 'Simulated',
       main = paste('Data from simulation', i, sep = ' '))
}
```



Finally, the simulations support the idea that the model is a good fit to the data since the simulations exhibit similar behaviors to the original StackOverflow time series.

Model Validation

```
# Python auto.arima with these arguments, auto.arima fits the same model we fit auto.arima(python.ts, trace = T, stepwise = T, approximation = F, allowdrift = F)
```

```
##
##
    ARIMA(2,0,2)(1,1,1)[12]
                                                 : 1537.191
                                                   1770.099
##
    ARIMA(0,0,0)(0,1,0)[12]
    ARIMA(1,0,0)(1,1,0)[12]
                                                   1529.993
##
##
    ARIMA(0,0,1)(0,1,1)[12]
                                                   1670.929
##
    ARIMA(1,0,0)(0,1,0)[12]
                                                   1534.045
##
    ARIMA(1,0,0)(2,1,0)[12]
                                                   1532.153
                                                   1532.154
##
    ARIMA(1,0,0)(1,1,1)[12]
##
    ARIMA(1,0,0)(0,1,1)[12]
                                                   1530.23
##
    ARIMA(1,0,0)(2,1,1)[12]
                                                   1534.302
    ARIMA(0,0,0)(1,1,0)[12]
                                                 : 1747.661
    ARIMA(2,0,0)(1,1,0)[12]
                                                   1531.854
##
```

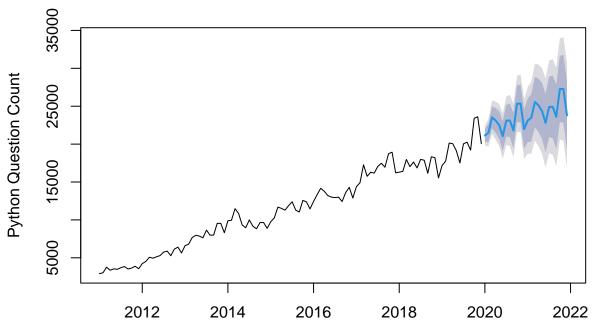
```
## ARIMA(1,0,1)(1,1,0)[12]
                                              : 1531.791
## ARIMA(0,0,1)(1,1,0)[12]
                                              : 1664.227
##
  ARIMA(2,0,1)(1,1,0)[12]
                                              : 1534.297
##
## Best model: ARIMA(1,0,0)(1,1,0)[12]
## Series: python.ts
## ARIMA(1,0,0)(1,1,0)[12]
##
## Coefficients:
##
            ar1
                    sar1
         0.9751 -0.2847
##
## s.e. 0.0206
                0.1107
## sigma^2 = 450183: log likelihood = -761.87
## AIC=1529.73 AICc=1529.99
                               BIC=1537.43
# stepwise = F very slow for seasonal models
# fits a different model when restrict to stationary model, but diagnostics are worse
# also played around with changing max.p and max.q, but don't get anything new/anything that performs b
```

The auto arima function produced the same model that was suggested by the exploratory data anlaysis. Therefore, the model diganostics were not performed again.

Forecasts

```
# Python forecast
plot(forecast(python.mod1, h = 24), ylab = "Python Question Count")
```

Forecasts from ARIMA(1,0,0)(1,1,0)[12]



The forecasts from the ARIMA model for Python have an increasing trend with some variations within the year which is what we would expect based on the previous observations. All of these observations suggest that the ARIMA(1,0,0)(1,1,0) model is a good fit to the data.

\mathbf{R}

Manual ARIMA Modeling

```
# Python Model 1 by Manual Fits
r.mod1 = arima(r.ts, order = c(1,0,0), seasonal = list(order = c(1,1,0), period = 12))
```

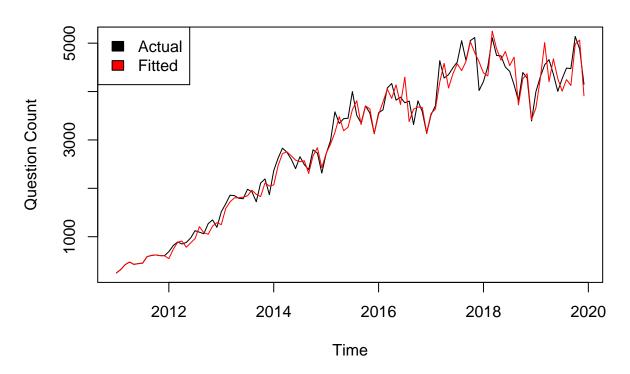
The same initial ARIMA model was fit to the R time series since the exploratory data analysis showed similar behavior for both series.

Manual ARIMA Diagnostics

Residuals

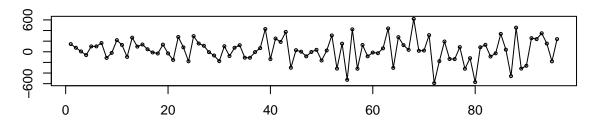
```
lines(r.ts - r.mod1$resid, col = "red")
legend("topleft", fill = c("black", "red"), c("Actual", "Fitted"))
```

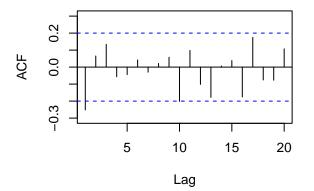
Observed vs. Fitted SARIMA values for Manual R Model

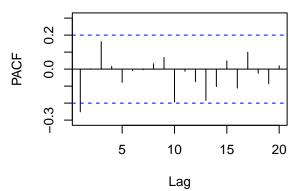


tsdisplay(resid(r.mod1)[13:length(r.mod1\$resid)], main= "Manual ARIMA R Model Residuals")

Manual ARIMA R Model Residuals

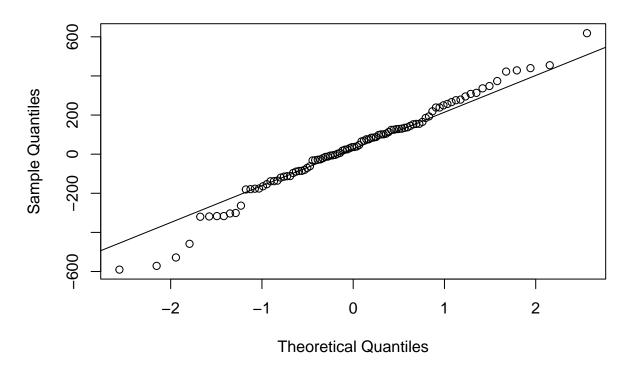






```
qqnorm(r.mod1$resid[13:length(r.mod1$resid)])
qqline(r.mod1$resid[13:length(r.mod1$resid)])
```

Normal Q-Q Plot

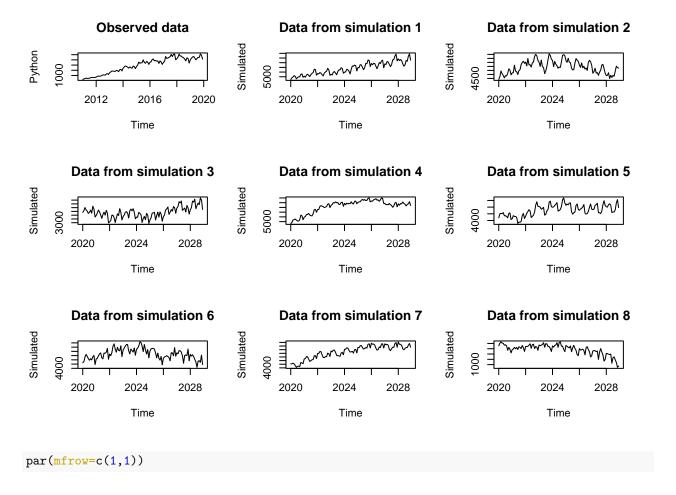


In general, diagnostics look pretty good

The fitted versus observed plot shows that the model fits the data well, again with a few possible exceptions in 2018. The residuals also appear to be approximately stationary with a constant mean and variance. But unlike the Python series, there appears to be no significant correlations in the ACF and PACF plots. Also, the QQ plot shows that the residuals are approximately normal.

Simulations

```
# Plot Multiple Simulations
par(mfrow=c(3,3))
plot(r.ts, ylab = 'Python', main = 'Observed data')
for (i in 1:8){
   set.seed(i)
   plot(simulate(r.mod1),
       ylab = 'Simulated',
       main = paste('Data from simulation', i, sep = ' '))
}
```



Several of the simulations exhibit similar behaviors to the original StackOverflow time series since they have constant increasing trends with slight annual variations.

Model Validation

ARIMA(0,1,1)(0,1,0)[12]

ARIMA(0,1,1)(1,1,1)[12]

ARIMA(0,1,1)(0,1,2)[12]

ARIMA(0,1,1)(1,1,0)[12]

ARIMA(0,1,1)(1,1,2)[12]

##

##

##

##

```
# R auto.arima
# tried similar differences in auto.arima arguments here
# fits a different model when restrict to stationary model, but diagnostics are worse
# also played around with changing max.p and max.q, but don't get anything new/anything that performs b
auto.arima(r.ts, trace = T, stepwise = T, approximation = F, allowdrift = F)
##
##
   ARIMA(2,1,2)(1,1,1)[12]
                                                : 1304.26
   ARIMA(0,1,0)(0,1,0)[12]
                                                  1316.466
                                                  1301.434
   ARIMA(1,1,0)(1,1,0)[12]
##
##
   ARIMA(0,1,1)(0,1,1)[12]
                                                  1299.439
```

1316.298

1301.386

: 1301.365

: 1302.021

: 1303.594

```
ARIMA(0,1,0)(0,1,1)[12]
                                                : 1301.922
##
  ARIMA(1,1,1)(0,1,1)[12]
                                                : 1301.336
## ARIMA(0,1,2)(0,1,1)[12]
                                                : 1300.934
## ARIMA(1,1,0)(0,1,1)[12]
                                                : 1299.171
##
   ARIMA(1,1,0)(0,1,0)[12]
                                                : 1315.693
## ARIMA(1,1,0)(1,1,1)[12]
                                                : 1301.108
## ARIMA(1,1,0)(0,1,2)[12]
                                                : 1301.075
## ARIMA(1,1,0)(1,1,2)[12]
                                                : 1303.293
##
   ARIMA(2,1,0)(0,1,1)[12]
                                                : 1301.318
                                                : Inf
##
   ARIMA(2,1,1)(0,1,1)[12]
##
   Best model: ARIMA(1,1,0)(0,1,1)[12]
##
## Series: r.ts
## ARIMA(1,1,0)(0,1,1)[12]
##
## Coefficients:
##
             ar1
                     sma1
##
         -0.2231
                  -0.5008
## s.e.
          0.0996
                   0.1006
##
## sigma^2 = 46908: log likelihood = -646.45
## AIC=1298.91
                 AICc=1299.17
                                BIC=1306.57
```

 $\textit{\# auto.arima actually fits a different model here than what we tried-fits \textit{d} \textit{ and } \textit{D} \textit{ difference and an MA} } \\$

The auto arima function produced a different model than the one suggested by the exploratory data analysis. Specifically, the auto function determined to add a non-seasonal trend, remove a seasonal autoregressive component, and add a seasonal moving average term.

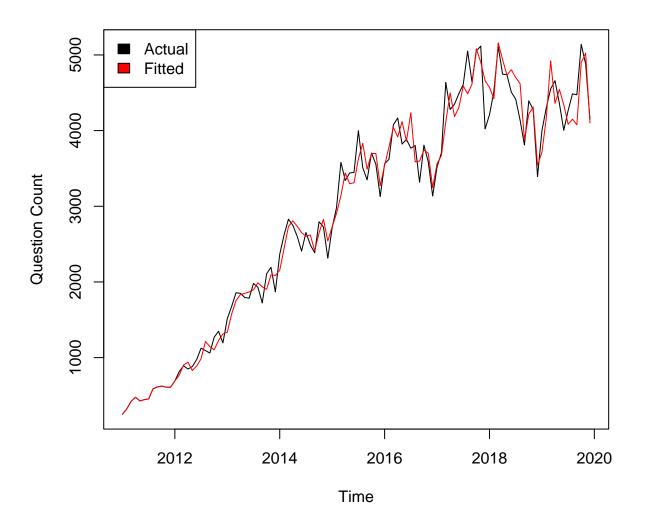
Model Fit - Auto ARIMA

```
# R Model 2 (with auto.arima results)
r.mod2 = arima(r.ts, order = c(1,1,0), seasonal = list(order = c(0,1,1), period = 12))
```

Model Diagnostics - Auto ARIMA

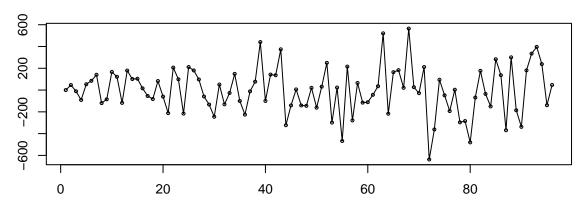
Since the auto arima function produced a different model, we will fit this model and perform the model diagnostics to see if it is a better fit to the data.

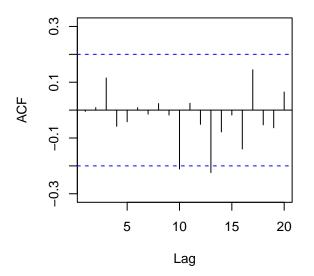
Observed vs. Fitted SARIMA values for Auto ARIMA R Model

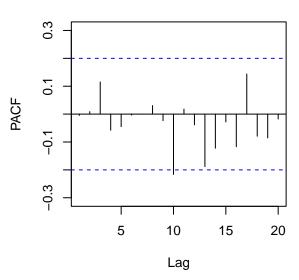


tsdisplay(resid(r.mod2)[13:length(r.mod2\$resid)], main = "Auto ARIMA R Residuals")

Auto ARIMA R Residuals

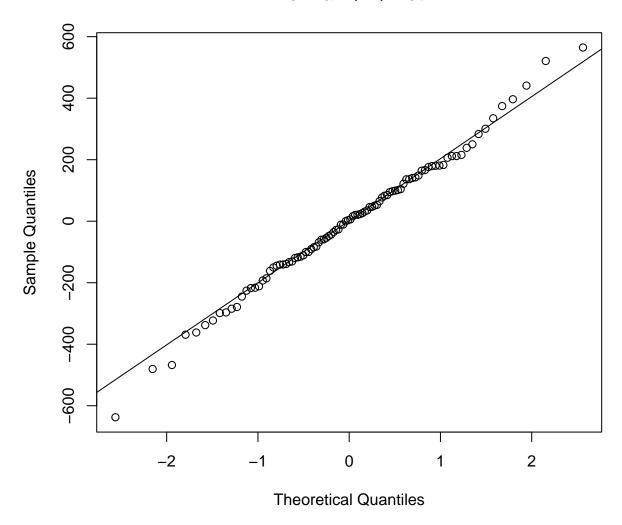






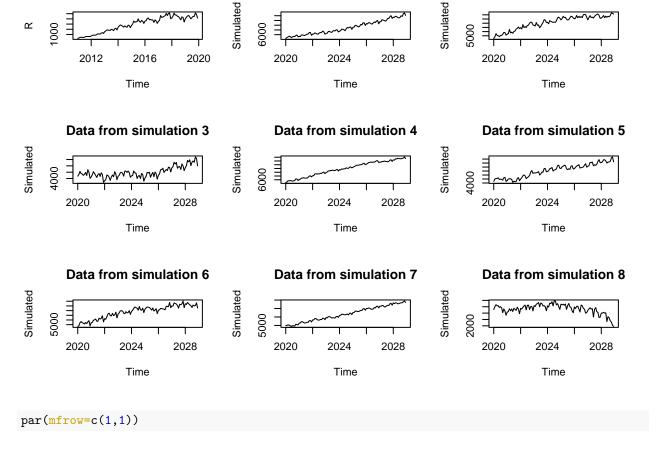
```
qqnorm(r.mod2$resid[13:length(r.mod2$resid)])
qqline(r.mod2$resid[13:length(r.mod2$resid)])
```

Normal Q-Q Plot



The fitted versus observed plot shows that the model fits the data well, again with a few possible exceptions in 2018. The residuals also appear to be approximately stationary with a constant mean and variance. However, there appear to be a few correlations on the border of being significant. Also, the QQ plot shows that the residuals are approximately normal.

```
# Second Round of Simulations
par(mfrow=c(3,3))
plot(r.ts, ylab = 'R', main = 'Observed data')
for (i in 1:8){
   set.seed(i)
   plot(simulate(r.mod2),
      ylab = 'Simulated',
      main = paste('Data from simulation', i, sep = ' '))
}
```



Data from simulation 1

Data from simulation 2

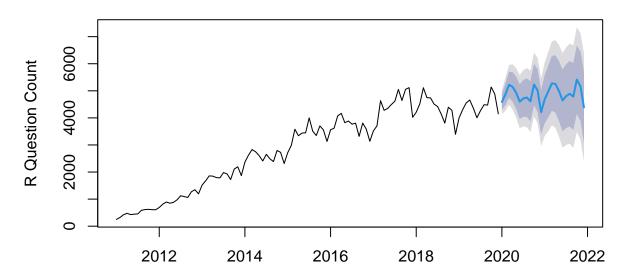
Several of the simulations exhibit similar behaviors to the original StackOverflow time series since they have constant increasing trends with slight annual variations.

Forecasts

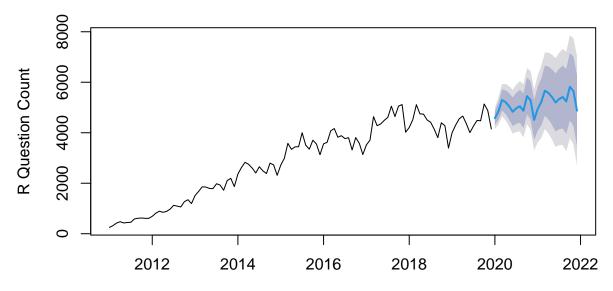
Observed data

```
# R forecasts
par(mfrow = c(2,1))
plot(forecast(r.mod1, h = 24), ylab = "R Question Count")
plot(forecast(r.mod2, h = 24), ylab = "R Question Count")
```

Forecasts from ARIMA(1,0,0)(1,1,0)[12]



Forecasts from ARIMA(1,1,0)(0,1,1)[12]



Based on the diagnostics, fit, and forecasts, the models suggested by the exploratory data analysis and by the auto arima functions are very similar. Looking at the summary output, the model that auto.arima picks has slightly lower AIC and RMSE/MAE, so overall this is the best model to the data.

```
# Summaries of R models
summary(r.mod1)
##
## Call:
## arima(x = r.ts, order = c(1, 0, 0), seasonal = list(order = c(1, 1, 0), period = 12))
## Coefficients:
##
            ar1
                    sar1
##
         0.9589
                 -0.3484
## s.e. 0.0262
                  0.1008
##
## sigma^2 estimated as 50893: log likelihood = -658.26, aic = 1322.52
##
## Training set error measures:
                      ΜE
                                                MPE
                                                        MAPE
                                                                   MASE
                                                                              ACF1
                            RMSE
                                       MAE
## Training set 26.03888 212.692 154.5326 1.259088 5.221512 0.6355945 -0.2503665
summary(r.mod2)
##
## Call:
## arima(x = r.ts, order = c(1, 1, 0), seasonal = list(order = c(0, 1, 1), period = 12))
##
## Coefficients:
##
                     sma1
             ar1
         -0.2231
                  -0.5008
##
## s.e.
          0.0996
                   0.1006
##
## sigma^2 estimated as 45920: log likelihood = -646.45, aic = 1298.91
##
## Training set error measures:
                               RMSE
                                                    MPE
##
                       ME
                                         MAE
                                                             MAPE
                                                                       MASE
## Training set -3.195138 200.9797 147.5508 -0.1045264 4.885689 0.6068783
                        ACF1
## Training set -0.004649645
```

VARMA Modeling

The final ARIMA model and the exploratory data analysis suggests that there is a trend and seasonal component to our time series. Therefore, we will detrend and deseasonalize the data before fitting the VARMA model.

Python

Deseasonalize and Detrend

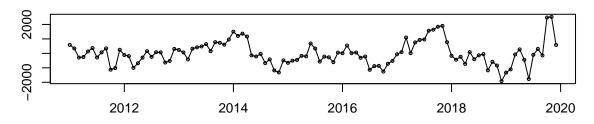
```
# Python
# Grab the months for the Python series
python.mon <- factor(cycle(python.ts), labels=month.abb)

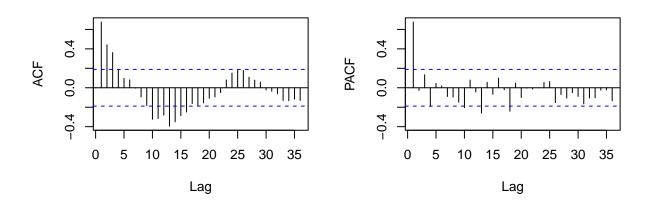
# Creating a detrended and deseasonalized
# Detrend
python.lm <- lm(python.ts ~ time(python.ts), na.action = NULL)
python.detrend <- resid(python.lm)

# Deseasonalize
python.detrend.lm <- lm(python.detrend ~ python.mon, na.action = NULL)
python.detrend.deseason <- resid(python.detrend.lm)

tsdisplay(python.detrend.deseason, main = 'Python Detrendend and Deseasonalized')</pre>
```

Python Detrendend and Deseasonalized





Variable Selection

```
VARselect(python.series, lag.max = 13, type = 'none')$selection
## AIC(n)
         HQ(n)
                 SC(n) FPE(n)
##
      13
              1
                     1
    The VARselect function concludes that a VAR(1) model is the best fit to the data.
python.fit <- VAR(python.series, p = 1, type = 'none')</pre>
summary(python.fit)
##
## VAR Estimation Results:
## ==========
## Endogenous variables: python.detrend.deseason, machine_learning.ts, classification.ts, regression.ts
## Deterministic variables: none
## Sample size: 107
## Log Likelihood: -2992.646
## Roots of the characteristic polynomial:
## 1.011 0.9199 0.6774 0.3206 0.3206 0.3118
## Call:
## VAR(y = python.series, p = 1, type = "none")
##
## Estimation results for equation python.detrend.deseason:
## python.detrend.deseason = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1
##
                             Estimate Std. Error t value Pr(>|t|)
                                                 9.111 8.11e-15 ***
## python.detrend.deseason.ll 0.67013
                                        0.07355
## machine_learning.ts.l1
                              0.39098
                                        0.68782
                                                 0.568
                                                           0.571
## classification.ts.l1
                             4.86766
                                        6.85791
                                                  0.710
                                                           0.479
## regression.ts.l1
                             -5.42537
                                        5.80533 -0.935
                                                           0.352
## time_series.ts.l1
                              0.24284
                                        4.29441
                                                  0.057
                                                           0.955
## cluster_analysis.ts.l1
                             -2.65232
                                        7.35109 -0.361
                                                           0.719
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## Residual standard error: 610.4 on 101 degrees of freedom
## Multiple R-Squared: 0.4685, Adjusted R-squared: 0.4369
## F-statistic: 14.84 on 6 and 101 DF, p-value: 4.253e-12
##
##
## Estimation results for equation machine_learning.ts:
## machine_learning.ts = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + r
##
##
                              Estimate Std. Error t value Pr(>|t|)
```

python.detrend.deseason.l1 0.002963 0.007171 0.413 0.6803

```
## machine_learning.ts.l1
                                      0.067067 12.129
                                                        <2e-16 ***
                            0.813471
                                                0.557
## classification.ts.l1
                            0.372261
                                      0.668696
                                                        0.5790
                                                1.257
## regression.ts.l1
                            0.711362
                                      0.566062
                                                        0.2118
                                                1.823
                                                        0.0712 .
## time_series.ts.l1
                            0.763473
                                      0.418737
## cluster_analysis.ts.l1
                           -1.263630
                                      0.716786 - 1.763
                                                        0.0809 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 59.52 on 101 degrees of freedom
## Multiple R-Squared: 0.9794, Adjusted R-squared: 0.9782
## F-statistic: 800.9 on 6 and 101 DF, p-value: < 2.2e-16
##
## Estimation results for equation classification.ts:
## classification.ts = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + reg
##
                             Estimate Std. Error t value Pr(>|t|)
##
## python.detrend.deseason.l1 -0.0007343 0.0013456 -0.546
## machine_learning.ts.l1
                          -0.0114503 0.0125841 -0.910
                                                         0.3650
## classification.ts.l1
                            ## regression.ts.l1
                            0.2163720 0.1062118
                                                 2.037
                                                         0.0442 *
## time series.ts.l1
                            0.0689901 0.0785688
                                                 0.878
                                                         0.3820
                                                         0.3320
## cluster_analysis.ts.l1
                            0.1310930 0.1344926
                                                 0.975
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 11.17 on 101 degrees of freedom
## Multiple R-Squared: 0.9617, Adjusted R-squared: 0.9594
## F-statistic: 422.8 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation regression.ts:
## regression.ts = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regress
##
                             Estimate Std. Error t value Pr(>|t|)
##
## python.detrend.deseason.l1 -5.754e-05 1.525e-03 -0.038 0.96998
## machine_learning.ts.l1
                            2.772e-02 1.426e-02 1.943 0.05478
## classification.ts.l1
                            4.627e-02 1.422e-01 0.325 0.74556
## regression.ts.l1
                            3.657e-01 1.204e-01
                                                 3.038 0.00303 **
## time_series.ts.l1
                            1.973e-01 8.905e-02
                                                 2.215 0.02899 *
## cluster_analysis.ts.l1
                            1.788e-01 1.524e-01
                                                1.173 0.24359
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 12.66 on 101 degrees of freedom
## Multiple R-Squared: 0.9598, Adjusted R-squared: 0.9574
## F-statistic: 401.4 on 6 and 101 DF, p-value: < 2.2e-16
##
##
```

```
## Estimation results for equation time_series.ts:
## time_series.ts = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regres
##
                            Estimate Std. Error t value Pr(>|t|)
## python.detrend.deseason.11 -0.003808 0.002226 -1.711 0.0901 .
## machine learning.ts.l1
                                      0.020815 1.813
                                                        0.0728 .
                            0.037734
                                               1.740
## classification.ts.l1
                            0.361173
                                      0.207535
                                                        0.0849 .
## regression.ts.l1
                            0.059839 0.175682
                                               0.341
                                                        0.7341
## time_series.ts.l1
                            0.600359
                                      0.129958
                                               4.620 1.14e-05 ***
## cluster_analysis.ts.l1
                           -0.010559
                                      0.222460 -0.047
                                                        0.9622
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 18.47 on 101 degrees of freedom
## Multiple R-Squared: 0.963, Adjusted R-squared: 0.9608
## F-statistic: 437.6 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation cluster_analysis.ts:
## cluster_analysis.ts = python.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + r
##
                            Estimate Std. Error t value Pr(>|t|)
## python.detrend.deseason.l1 -0.000679 0.001210 -0.561 0.575759
## machine_learning.ts.l1
                           ## classification.ts.l1
                                               3.441 0.000844 ***
                            0.388061
                                    0.112776
## regression.ts.l1
                            0.075714 0.095466
                                               0.793 0.429582
## time_series.ts.l1
                            0.091683 0.070620
                                               1.298 0.197157
                           0.387401
## cluster_analysis.ts.l1
                                      0.120886
                                               3.205 0.001810 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 10.04 on 101 degrees of freedom
## Multiple R-Squared: 0.9475, Adjusted R-squared: 0.9444
## F-statistic: 304 on 6 and 101 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
                        python.detrend.deseason machine_learning.ts
## python.detrend.deseason
                                        372634
                                                         12443.1
## machine_learning.ts
                                         12443
                                                          3542.0
## classification.ts
                                          2033
                                                           360.0
## regression.ts
                                          1629
                                                           391.7
## time_series.ts
                                          3646
                                                           619.2
## cluster_analysis.ts
                                          1262
                                                           127.8
                        classification.ts regression.ts time_series.ts
## python.detrend.deseason
                             2033.49
                                              1628.64
                                                             3645.7
                                               391.71
## machine_learning.ts
                                  360.04
                                                             619.2
## classification.ts
                                  123.35
                                                65.54
                                                             116.4
## regression.ts
                                   65.54
                                               160.24
                                                              138.4
```

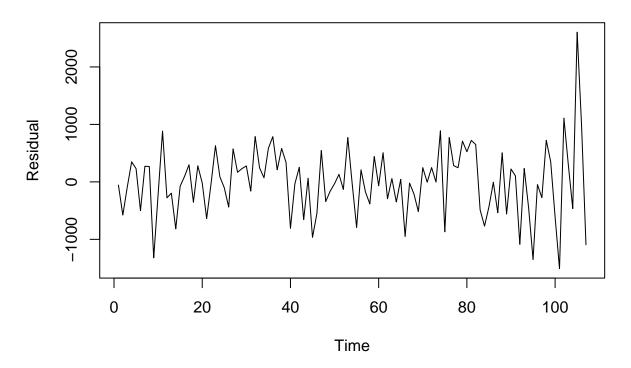
```
## time series.ts
                                       116.40
                                                      138.44
                                                                       340.2
## cluster_analysis.ts
                                        63.37
                                                       37.15
                                                                        85.6
##
                            cluster analysis.ts
## python.detrend.deseason
                                        1262.35
## machine_learning.ts
                                          127.82
## classification.ts
                                           63.37
## regression.ts
                                           37.15
                                           85.60
## time_series.ts
## cluster_analysis.ts
                                           98.90
##
## Correlation matrix of residuals:
##
                            python.detrend.deseason machine_learning.ts
## python.detrend.deseason
                                              1.0000
                                                                   0.3425
                                              0.3425
                                                                   1.0000
## machine_learning.ts
## classification.ts
                                              0.2999
                                                                   0.5447
## regression.ts
                                              0.2108
                                                                   0.5199
## time_series.ts
                                              0.3238
                                                                   0.5641
## cluster_analysis.ts
                                              0.2079
                                                                   0.2160
                            classification.ts regression.ts time_series.ts
## python.detrend.deseason
                                       0.2999
                                                      0.2108
## machine_learning.ts
                                       0.5447
                                                      0.5199
                                                                      0.5641
## classification.ts
                                       1.0000
                                                      0.4662
                                                                      0.5682
                                       0.4662
## regression.ts
                                                      1.0000
                                                                      0.5930
## time series.ts
                                                      0.5930
                                                                      1.0000
                                       0.5682
## cluster_analysis.ts
                                       0.5737
                                                      0.2951
                                                                      0.4667
                            cluster_analysis.ts
## python.detrend.deseason
                                          0.2079
## machine_learning.ts
                                          0.2160
## classification.ts
                                          0.5737
## regression.ts
                                         0.2951
## time_series.ts
                                          0.4667
## cluster_analysis.ts
                                          1.0000
```

The summary of the VAR(1) on page X shows that the model for the detrended and deseasonalized Python series can be explained by any of the data science topics since all their p-values are above 0.05. The only variable that seems to predict the Python question count is the lagged variable of the Python series. Additionally, the R-squared for the model is 0.43 which suggests that the model does not have strong predictive power.

Model Validation

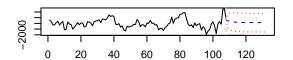
```
# Plot the residuals
plot(ts(resid(python.fit))[,1], main = 'Residuals for Python VAR(1) Model', ylab = 'Residual')
```

Residuals for Python VAR(1) Model

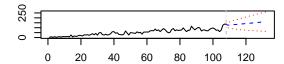


```
# Predictions
python.pred <- predict(python.fit, n.ahead = 24, ci = 0.95)
plot(python.pred)</pre>
```

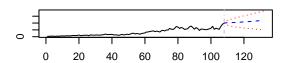
Forecast of series python.detrend.deseason



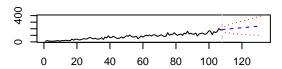
Forecast of series regression.ts



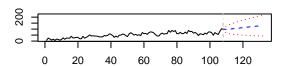
Forecast of series machine_learning.ts



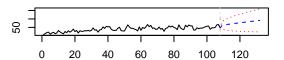
Forecast of series time_series.ts



Forecast of series classification.ts

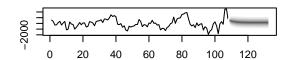


Forecast of series cluster_analysis.ts

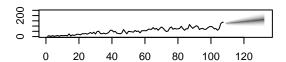


fanchart(python.pred)

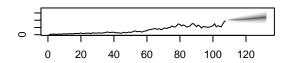
Fanchart for variable python.detrend.deseasor



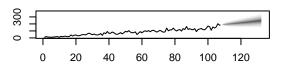
Fanchart for variable regression.ts



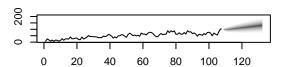
Fanchart for variable machine_learning.ts



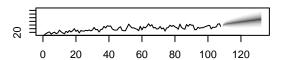
Fanchart for variable time_series.ts



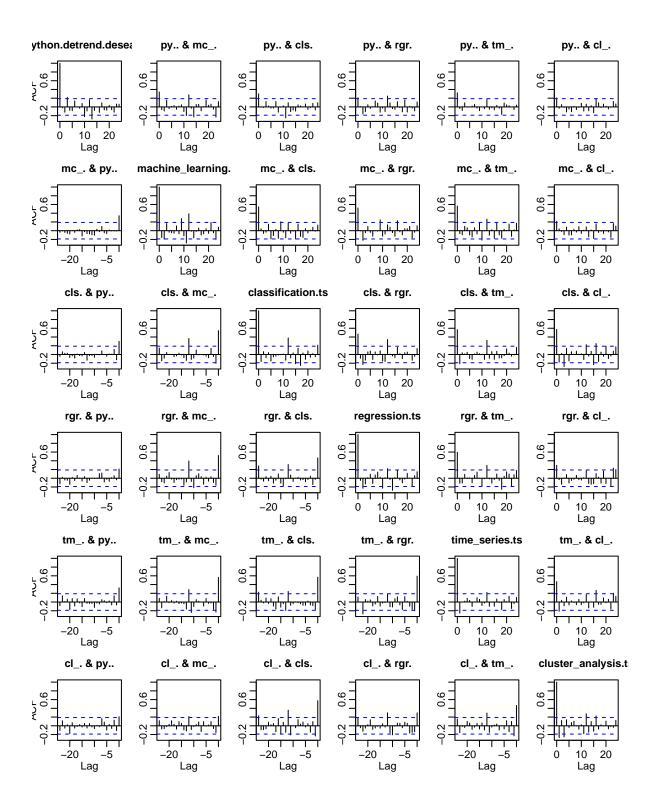
Fanchart for variable classification.ts



Fanchart for variable cluster_analysis.ts



ACF Plots
acf(resid(python.fit), 24)



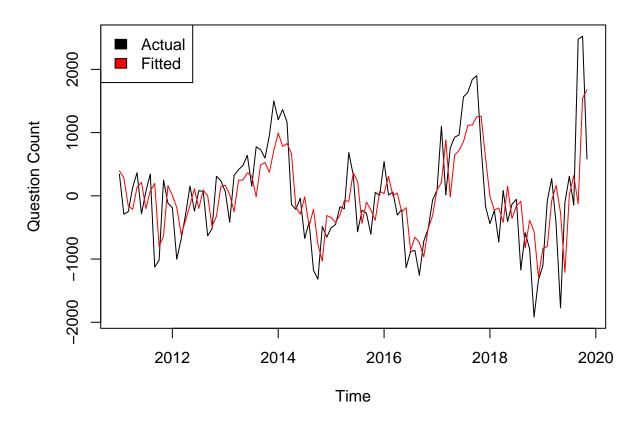
The plot of the residuals versus fitted values for the Python VAR(1) model shows higher variance in the last year of the data. The ACF and CCF plots occassionally show significant correlations around the year-long lag.

Forecasts

Recall that before fitting the VARMA model, the original time series was detrended and deseasonalized in order to get the best model fit. But, for the forecasted series, it is better to report the predictions in their original scale. Therefore, here we are transforming the forecasted values from the VAR(1) model back into their original scale.

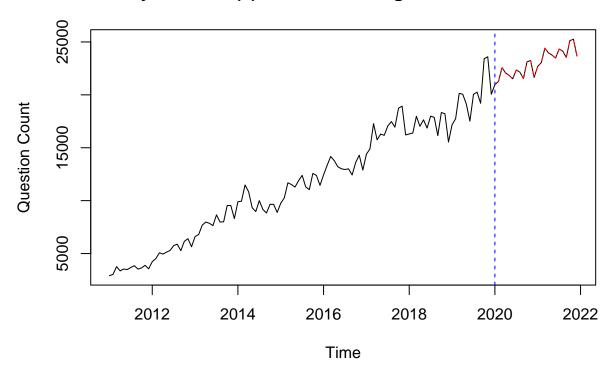
```
# Python
# Plot of actual vs fitted values
plot(ts(python.detrend.deseason[2:length(python.detrend.deseason)], start = c(2011,1), frequency = 12),
    main = paste("Obs vs. Fitted VAR(1) Values for Detrended & Deseasonalized Python Series"),
    ylab = paste("Question Count"))
lines(ts(python.detrend.deseason[2:length(python.detrend.deseason)] - python.fit$varresult$python.detrend.start = c(2011,1), frequency = 12), col="red")
legend("topleft",legend = c("Actual", "Fitted"), fill = c("black", "red"))
```

Dbs vs. Fitted VAR(1) Values for Detrended & Deseasonalized Python S



```
python.fcsts <- NULL</pre>
# Creates a matrix that stores the forecasts for the linear model with trend
python.fcsts <- rbind(rep(coef(python.lm)[[1]],length(python.forecast.time)),</pre>
               coef(python.lm)[[2]]*python.forecast.time)
# getting seasonality model coefficient estimates
tmp <- matrix(rep(0, length(coef(python.detrend.lm))^2), ncol = length(coef(python.detrend.lm)))</pre>
diag(tmp) <- coef(python.detrend.lm)</pre>
tmp[1,] <- tmp[1,1] # since deasonalized model has dummy variables measuring difference from intercept
python.fcsts <- rbind(python.fcsts, rep(colSums(tmp), length.out = python.months.past.current.projection
# Gets the forecasted values based on the VAR model and appends to matrix
python.fcst.detrend.deseason <- ts(python.pred$fcst$python.detrend.deseason[,1], start = c(2020,1), fre
python.fcsts <- rbind(python.fcsts, python.fcst.detrend.deseason)</pre>
# Now, each column is a forecast for a future month (24 cols = 2 years)
# each row (except the last one) is the forecasted value at that month associated with a coefficient
# from the original models fit when detrending/deasonalizing
# colSums will give us this forecast
python.fcsts <- ts(colSums(python.fcsts), start = c(2020,1), frequency = 12)
python.total <- ts(c(python.ts, python.fcsts), start = c(2011,1), frequency = 12)
# Plot the transformed predicted values
# Plotting over the whole time series initially so R sets the correct boundaries
plot(python.total,
     main = paste('Python VAR(1) Forecast through',
                  month.name[(max(time(python.total))
                              - floor(max(time(python.total))))*max(cycle(python.total)) + 1],
                  floor(max(time(python.total)))),
     ylab = 'Question Count')
# Plot the forecasted values
lines(python.fcsts, col = 'red', lty = 6)
# Cutoff for data and predicted values
abline(v = max(time(python.ts)) + 1/max(cycle(python.ts)), lty = 2, col = 'blue')
```

Python VAR(1) Forecast through December 2021



```
paste('Ending actual data count:', python.ts[length(python.ts)])

## [1] "Ending actual data count: 20058"

paste('Ending projection data count:', floor(python.fcsts[length(python.fcsts)]))

## [1] "Ending projection data count: 23661"
```

paste('Forecasted growth %:',round((floor(python.fcsts[length(python.fcsts)]) - python.ts[length(python

[1] "Forecasted growth %: 17.96"

The forecasted values indicated that the positive trend will continue to 2022. Python's predicted number of questions is forecasted to grow from 20,058 in December 2019 to 23,661 in December 2022, a 17.96% growth rate.

 \mathbf{R}

Again, the final ARIMA model and the exploratory data analysis suggests that there is a trend and seasonal component to our time series. Therefore, we will detrend and deseasonalize the data before fitting the VARMA model.

Deseasonalize and Detrend

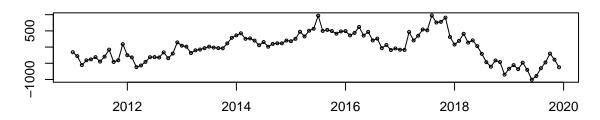
```
# Grab the months for the R series
r.mon <- factor(cycle(r.ts), labels=month.abb)

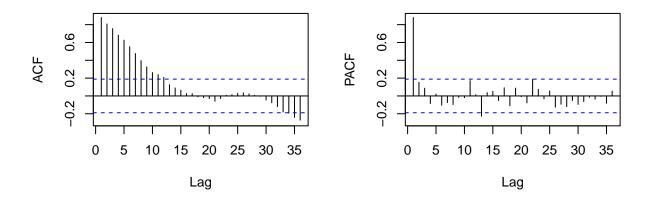
# Creating a detrended and deseasonalized
# Detrend
r.lm <- lm(r.ts ~ time(r.ts), na.action = NULL)
r.detrend <- resid(r.lm)

# Deseasonalize
r.detrend.lm <- lm(r.detrend ~ r.mon, na.action = NULL)
r.detrend.deseason <- resid(r.detrend.lm)

tsdisplay(r.detrend.deseason, main = 'R Detrendend and Deseasonalized')</pre>
```

R Detrendend and Deseasonalized





Variable Selection

```
VARselect(r.series, lag.max = 13, type = 'none')$selection
## AIC(n) HQ(n) SC(n) FPE(n)
##
      13
              1
                     1
    The VARselect model also suggests that a VAR(1) model is the best fit to the data.
r.fit <- VAR(r.series, p = 1, type = 'none')</pre>
summary(r.fit)
## VAR Estimation Results:
## ==========
## Endogenous variables: r.detrend.deseason, machine_learning.ts, classification.ts, regression.ts, tim
## Deterministic variables: none
## Sample size: 107
## Log Likelihood: -2868.287
## Roots of the characteristic polynomial:
## 1.015 0.9244 0.8683 0.328 0.3082 0.3082
## Call:
## VAR(y = r.series, p = 1, type = "none")
##
##
## Estimation results for equation r.detrend.deseason:
## r.detrend.deseason = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regress
##
##
                         Estimate Std. Error t value Pr(>|t|)
                                    0.04623 18.902 < 2e-16 ***
## r.detrend.deseason.l1
                         0.87379
## machine_learning.ts.l1 -0.23731
                                    0.20841 -1.139 0.257540
## classification.ts.l1
                         7.78787
                                    2.15498
                                             3.614 0.000472 ***
                         -2.57262
## regression.ts.l1
                                    1.78455 -1.442 0.152506
## time_series.ts.l1
                         0.73486
                                     1.36172
                                             0.540 0.590622
## cluster_analysis.ts.l1 -6.17744
                                    2.24920 -2.747 0.007133 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 186.8 on 101 degrees of freedom
## Multiple R-Squared: 0.8179, Adjusted R-squared: 0.8071
## F-statistic: 75.63 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation machine_learning.ts:
## machine_learning.ts = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regres
##
##
                          Estimate Std. Error t value Pr(>|t|)
## r.detrend.deseason.ll -0.009753
                                   0.014714 -0.663
                                                       0.5089
## machine_learning.ts.l1 0.816558 0.066338 12.309
                                                       <2e-16 ***
## classification.ts.l1
                          0.488736
                                   0.685923
                                              0.713
                                                       0.4778
```

1.304

0.1953

0.568015

0.740550

regression.ts.l1

```
## time series.ts.l1
                        0.670931
                                  0.433429
                                            1.548
                                                    0.1248
## cluster_analysis.ts.l1 -1.268998
                                 0.715911 -1.773 0.0793 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## Residual standard error: 59.44 on 101 degrees of freedom
## Multiple R-Squared: 0.9795, Adjusted R-squared: 0.9782
## F-statistic: 803.1 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation classification.ts:
## classification.ts = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regressi
##
##
                          Estimate Std. Error t value Pr(>|t|)
## r.detrend.deseason.11 -0.0001731 0.0027685 -0.063
                                                     0.9503
## machine_learning.ts.l1 -0.0124192 0.0124817 -0.995
                                                     0.3221
## classification.ts.l1
                        0.6282735 0.1290598
                                             4.868 4.17e-06 ***
## regression.ts.l1
                        0.2203418 0.1068749
                                             2.062
                                                     0.0418 *
## time_series.ts.l1
                        0.0710195 0.0815517
                                              0.871
                                                     0.3859
## cluster_analysis.ts.l1 0.1301398 0.1347022
                                             0.966
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.18 on 101 degrees of freedom
## Multiple R-Squared: 0.9616, Adjusted R-squared: 0.9593
## F-statistic: 421.6 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation regression.ts:
## ===============
## regression.ts = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regression.t
##
##
                       Estimate Std. Error t value Pr(>|t|)
## r.detrend.deseason.ll 0.002147 0.003126
                                           0.687 0.49370
## machine_learning.ts.l1 0.027810
                                            1.973 0.05121 .
                                0.014094
## classification.ts.l1
                       0.022868
                                 0.145732
                                            0.157 0.87562
## regression.ts.l1
                                0.120681
                                            2.955 0.00389 **
                       0.356656
## time series.ts.l1
                       0.214878
                                 0.092087
                                            2.333 0.02161 *
## cluster_analysis.ts.l1 0.180630
                                 0.152103 1.188 0.23780
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## Residual standard error: 12.63 on 101 degrees of freedom
## Multiple R-Squared: 0.9599, Adjusted R-squared: 0.9576
## F-statistic: 403.4 on 6 and 101 DF, p-value: < 2.2e-16
##
## Estimation results for equation time_series.ts:
## time_series.ts = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regression.
```

```
##
##
                          Estimate Std. Error t value Pr(>|t|)
## r.detrend.deseason.ll -0.009391
                                    0.004543 -2.067
## machine_learning.ts.l1 0.032040
                                     0.020484
                                                1.564
                                                        0.1209
## classification.ts.l1
                          0.448254
                                     0.211798
                                                2.116
                                                        0.0368 *
## regression.ts.l1
                                                0.668
                          0.117166
                                     0.175391
                                                        0.5056
                                                4.052 9.97e-05 ***
## time series.ts.l1
                          0.542339
                                     0.133833
## cluster_analysis.ts.l1 -0.022992
                                     0.221058 -0.104
                                                        0.9174
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 18.35 on 101 degrees of freedom
## Multiple R-Squared: 0.9634, Adjusted R-squared: 0.9613
## F-statistic: 443.5 on 6 and 101 DF, p-value: < 2.2e-16
##
##
## Estimation results for equation cluster analysis.ts:
## cluster_analysis.ts = r.detrend.deseason.l1 + machine_learning.ts.l1 + classification.ts.l1 + regres
##
##
                          Estimate Std. Error t value Pr(>|t|)
## r.detrend.deseason.ll -0.001159
                                     0.002486 -0.466 0.642056
## machine learning.ts.l1 -0.024484
                                     0.011208 -2.185 0.031236 *
## classification.ts.l1
                          0.398022
                                    0.115890
                                                3.434 0.000863 ***
## regression.ts.l1
                          0.083706
                                     0.095969
                                                0.872 0.385160
## time_series.ts.l1
                          0.085497
                                     0.073230
                                                1.168 0.245751
## cluster_analysis.ts.l1 0.385638
                                     0.120957
                                                3.188 0.001906 **
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## Residual standard error: 10.04 on 101 degrees of freedom
## Multiple R-Squared: 0.9475, Adjusted R-squared: 0.9444
## F-statistic: 303.7 on 6 and 101 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
##
                      r.detrend.deseason machine_learning.ts classification.ts
## r.detrend.deseason
                                 34877.2
                                                      2071.9
## machine learning.ts
                                  2071.9
                                                      3533.5
                                                                        359.07
## classification.ts
                                   441.0
                                                       359.1
                                                                        123.66
## regression.ts
                                   242.4
                                                       395.0
                                                                         65.49
                                                       597.6
## time_series.ts
                                   677.6
                                                                        118.44
## cluster_analysis.ts
                                   395.9
                                                       125.6
                                                                         63.68
                      regression.ts time_series.ts cluster_analysis.ts
## r.detrend.deseason
                             242.41
                                            677.57
                                                                395.95
## machine_learning.ts
                             394.99
                                            597.55
                                                                125.56
## classification.ts
                              65.49
                                            118.44
                                                                 63.68
                                                                 37.42
## regression.ts
                             159.46
                                            141.79
## time_series.ts
                             141.79
                                            336.43
                                                                 86.11
                              37.42
## cluster_analysis.ts
                                             86.11
                                                                 99.08
```

##

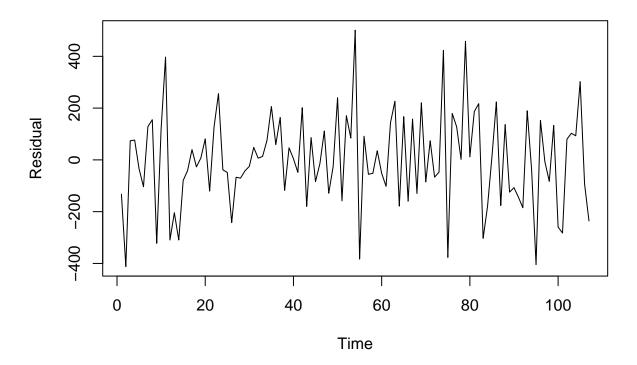
```
## Correlation matrix of residuals:
##
                       r.detrend.deseason machine_learning.ts classification.ts
## r.detrend.deseason
                                    1.0000
                                                         0.1866
## machine_learning.ts
                                    0.1866
                                                         1.0000
                                                                            0.5432
## classification.ts
                                    0.2123
                                                         0.5432
                                                                            1.0000
## regression.ts
                                    0.1028
                                                         0.5262
                                                                            0.4663
## time series.ts
                                    0.1978
                                                         0.5481
                                                                            0.5807
## cluster_analysis.ts
                                                         0.2122
                                                                            0.5753
                                    0.2130
                       regression.ts time_series.ts cluster_analysis.ts
##
## r.detrend.deseason
                               0.1028
                                                                   0.2130
                                              0.1978
## machine_learning.ts
                               0.5262
                                              0.5481
                                                                   0.2122
## classification.ts
                               0.4663
                                                                    0.5753
                                              0.5807
## regression.ts
                               1.0000
                                                                    0.2977
                                              0.6122
## time_series.ts
                               0.6122
                                               1.0000
                                                                    0.4716
## cluster_analysis.ts
                               0.2977
                                              0.4716
                                                                    1.0000
```

Unlike the Python model, the VAR(1) model for R has two variables that significant contribute to the model: classification and cluster analysis. Both of these variables have p-values below 0.05 which suggests that they explain a significant amount of variance in the Python series. Additionally, the R-squared value is 0.81 which suggests that the model has strong predictive power.

Model Validation

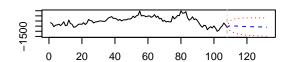
```
plot(ts(resid(r.fit))[,1], main = 'Residuals for R VAR(1) Model', ylab = 'Residual')
```

Residuals for R VAR(1) Model

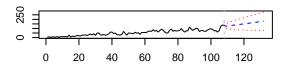


```
r.pred <- predict(r.fit, n.ahead = 24, ci = 0.95)
plot(r.pred)</pre>
```

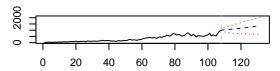
Forecast of series r.detrend.deseason



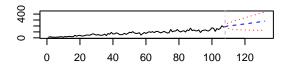
Forecast of series regression.ts



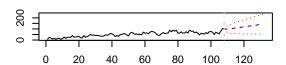
Forecast of series machine_learning.ts



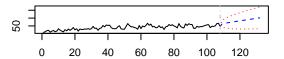
Forecast of series time_series.ts



Forecast of series classification.ts

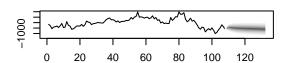


Forecast of series cluster_analysis.ts

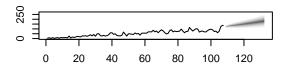


fanchart(r.pred)

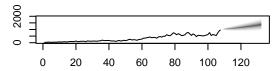
Fanchart for variable r.detrend.deseason



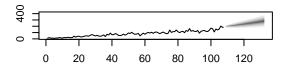
Fanchart for variable regression.ts



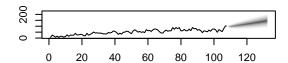
Fanchart for variable machine_learning.ts



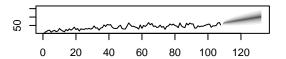
Fanchart for variable time_series.ts



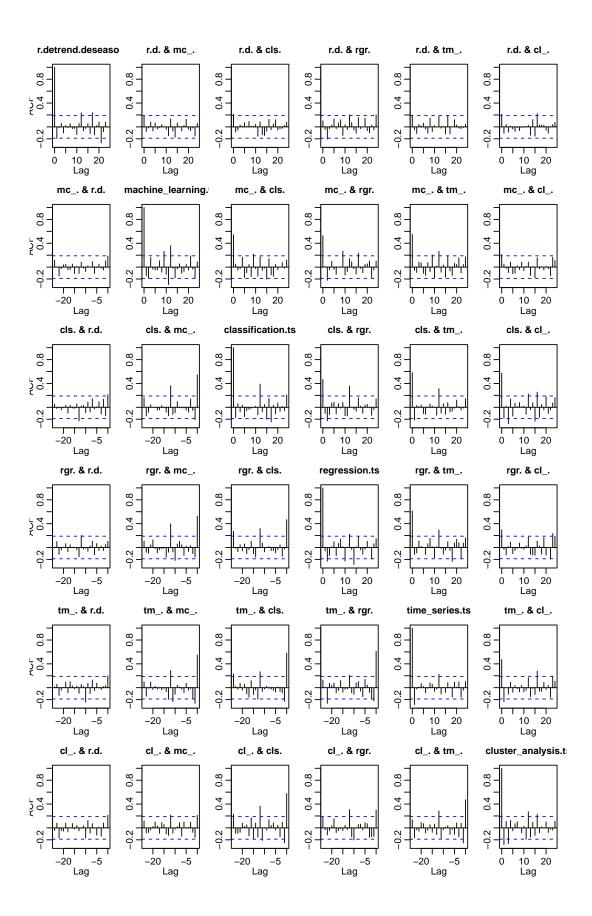
Fanchart for variable classification.ts



Fanchart for variable cluster_analysis.ts



acf(resid(r.fit), 24)

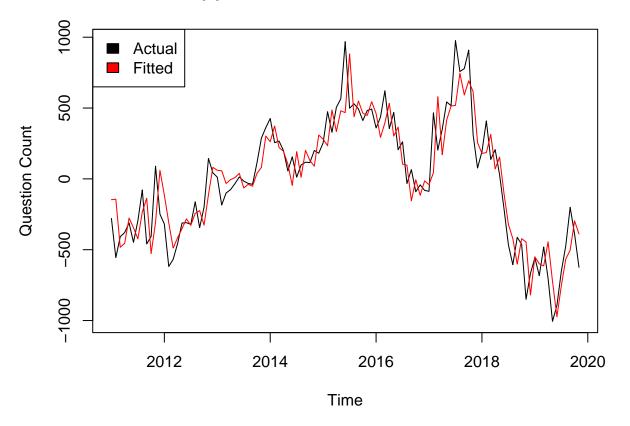


The residuals for the detrended and deasonalized R series follow a stationary behavior, with a constant mean and variance. The ACF and PACF plots also show less instances of significant correlations around the annual lag point.

Forecasts

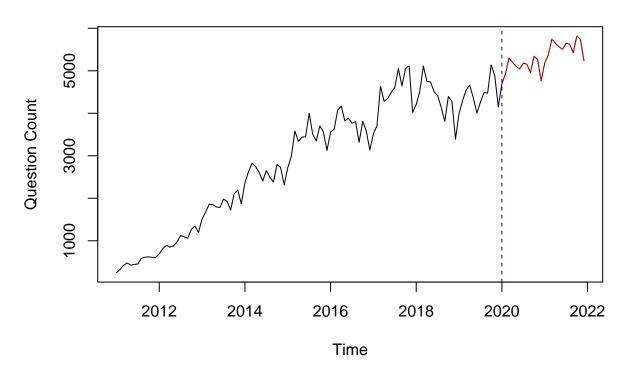
```
# R
# Plot of actuals vs fitted values
plot(ts(r.detrend.deseason[2:length(r.detrend.deseason)], start = c(2011,1), frequency = 12),
    main = paste("Obs vs. Fitted VAR(1) Values for Detrended & Deseasonalized R Series"),
    ylab = paste("Question Count"))
lines(ts(r.detrend.deseason[2:length(r.detrend.deseason)] - r.fit$varresult$r.detrend.deseason$residual
        start = c(2011,1), frequency = 12), col="red")
legend("topleft",legend = c("Actual", "Fitted"), fill = c("black", "red"))
```

Obs vs. Fitted VAR(1) Values for Detrended & Deseasonalized R Serie



```
r.fcsts <- NULL
# creates a matrix that stores the forecasts for the linear model with trend
r.fcsts <- rbind(rep(coef(r.lm)[[1]],length(r.forecast.time)),</pre>
               coef(r.lm)[[2]]*r.forecast.time)
# getting seasonality model coefficient estimates
tmp <- matrix(rep(0, length(coef(r.detrend.lm))^2), ncol = length(coef(r.detrend.lm)))</pre>
diag(tmp) <- coef(r.detrend.lm)</pre>
tmp[1,] <- tmp[1,1] # since deasonalized model has dummy variables measuring difference from intercept
r.fcsts <- rbind(r.fcsts, rep(colSums(tmp), length.out = r.months.past.current.projection))</pre>
# R translated forecasts
# Get the forecasted values based on the VAR model and appends to matrix
r.fcst.detrend.deseason <- ts(r.pred$fcst$r.detrend.deseason[,1], start = c(2020,1), frequency = 12)
r.fcsts <- rbind(r.fcsts, r.fcst.detrend.deseason)</pre>
# Now, each column is a forecast for a future month (24 cols = 2 years)
# each row (except the last one) is the forecasted value at that month associated with a coefficient
# from the original models fit when detrending/deasonalizing
# colSums will give us this forecast
r.fcsts <- ts(colSums(r.fcsts), start = c(2020,1), frequency = 12)
r.total \leftarrow ts(c(r.ts, r.fcsts), start = c(2011,1), frequency = 12)
# Plot the transformed forecasted values
# Plotting over the whole time series initially so R sets the correct boundaries
plot(r.total, main = paste('R VAR(1) Forecast through',
              month.name[(max(time(r.total)) - floor(max(time(r.total))))*max(cycle(r.total)) + 1],
              floor(max(time(r.total)))),
     ylab = 'Question Count')
# Plot the forecasted values
lines(r.fcsts, col = 'red', lty = 6)
# Line to show the divide between actual and predicted values
abline(v = max(time(r.ts)) + 1/max(cycle(r.ts)), lty = 2, col = 'blue')
```

R VAR(1) Forecast through December 2021



```
paste('Ending projection data count:', floor(r.fcsts[length(r.fcsts)]))

## [1] "Ending projection data count: 5238"

paste('Ending actual data count:', r.ts[length(r.ts)])

## [1] "Ending actual data count: 4150"

paste('Forecasted growth %:',round((floor(r.fcsts[length(r.fcsts)]) - r.ts[length(r.ts)])/r.ts[length(r.fcsts)])
```

[1] "Forecasted growth %: 26.22"

The forecasted values indicated that the positive trend will continue to 2022. R's predicted number of questions is forecasted to grow from $4{,}150$ in December 2020 to $5{,}238$ in December 2021, a 26.2% growth rate.