

Gender, culture, and mathematics performance

Janet S. Hyde^{a,1} and Janet E. Mertz^b

^aDepartment of Psychology, University of Wisconsin, Madison, WI 53706; and ^bMcArdle Laboratory for Cancer Research, University of Wisconsin School of Medicine and Public Health, Madison, WI 53706-1599

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Using contemporary data from the U.S. and other nations, we address 3 questions: Do gender differences in mathematics performance exist in the general population? Do gender differences exist among the mathematically talented? Do females exist who possess profound mathematical talent? In regard to the first question, contemporary data indicate that girls in the U.S. have reached parity with boys in mathematics performance, a pattern that is found in some other nations as well. Focusing on the second question, studies find more males than females scoring above the 95th or 99th percentile, but this gender gap has significantly narrowed over time in the U.S. and is not found among some ethnic groups and in some nations. Furthermore, data from several studies indicate that greater male variability with respect to mathematics is not ubiquitous. Rather, its presence correlates with several measures of gender inequality. Thus, it is largely an artifact of changeable sociocultural factors, not immutable, innate biological differences between the sexes. Responding to the third question, we document the existence of females who possess profound mathematical talent. Finally, we review mounting evidence that both the magnitude of mean math gender differences and the frequency of identification of gifted and profoundly gifted females significantly correlate with sociocultural factors, including measures of gender equality across nations.

exceptional talent | gender gap index | greater male variability hypothesis | International Mathematical Olympiad | Programme for International Student Assessment

Researchers first began investigating gender differences in abilities and behaviors in the 1880s (1). The scientists of the time concluded that women's smaller brains were sadly deficient. For example, George Romanes declared in 1887 that mental abilities were secondary sex characteristics attributable to brain size (2). Twenty-first century scientists have vastly better research methods available to them. Moreover, the behaviors and performance of women and men in 2009 are substantially different from what they were in the Victorian era. This article reviews and synthesizes the current evidence on gender differences in abilities, focusing on mathematical skills because of the crucial role they play in success in careers in science, technology, engineering, and mathematics, i.e., STEM fields. The review is organized around 3 questions: Do gender differences in mathematics performance exist in the general population? Do gender differences exist among the highly mathematically talented? Do females exist who possess profound mathematical talent? Last, we consider the evidence concerning the contribution of sociocultural factors to the gender differences observed in measured mathematical performance.

Do Gender Differences in Mathematics Performance Exist in the General Population?

In influential reviews published in 1966 and 1974, the noted developmental psychologist Eleanor Maccoby concluded that gender differences in mathematics performance were scientifically well es-

tablished, with males scoring higher (3, 4). She documented that boys and girls acquire early number concepts similarly in the preschool years, a conclusion fully supported by contemporary data (5), and that their performance throughout elementary school was similar; however, boys' skills in mathematics increased faster than girls' beginning around 12 or 13 years of age, creating a significant gender gap in performance by high school.

The technique of meta-analysis became available by the 1980s. It provides a powerful statistical method for synthesizing the results of numerous studies on a given question. In research on gender differences, the meta-analyst computes the effect size, d , for each study and then computes a weighted average effect size across all studies (6). The effect size is computed as $d = (M_M - M_F)/S_w$, where M_M is the mean score for males (M), M_F is the mean score for females (F), and S_w is the within-groups standard deviation. Thus, it is a measure of the distance between the male and female means in standard deviation units. Positive values represent better performance by males, whereas negative values represent better performance by females. According to standard guidelines, an effect size of 0.20 is small, 0.50 is moderate, and 0.80 is large (7).

Hyde and colleagues reported a 1990 meta-analysis on gender differences in mathematics performance involving 100 studies representing the testing of >3 million individuals, most from the U.S. but some from other nations such as Australia and Canada (8). Overall, they found $d = -0.05$ for samples of the general population, an effect so small as

to be considered no gender difference. Further analyses explored effects of age and cognitive level of test items on the magnitude of gender difference. Test items were coded as assessing simple computation (i.e., memorized math facts), deeper understanding of concepts, or, at the highest level, complex problem solving. The results indicated a slight female advantage in computation in elementary and middle school, and no difference in high school. There were no gender differences in understanding of concepts at any age. Complex problem solving displayed no gender difference in elementary school and middle school, but a gender difference favoring males emerged in high school, with $d = 0.29$. This latter finding is of concern because complex problem solving is an essential skill for success in life and in STEM careers.

These findings were largely replicated in a 1995 meta-analysis using large datasets based on the testing of excellent probability samples of U.S. adolescents (9). For high school students, d values ranged between 0.03 and 0.26 for mathematics performance, that is, boys performed better than girls by a small amount.

One prominent explanation for this measured gender difference in math performance in high school has been differential patterns of course taking

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¹To whom correspondence should be addressed. E-mail: jshyde@wisc.edu.

Table 5. Correlations among nations' percent girls on IMO team, GGI, team rank, and population (for nations with median team rank among top 30)

	% girls on IMO team 1989–2008	Median team rank 2000–2008	% of world population
Median team rank	−0.075	—	—
% of world population	−0.181	−0.333 [†]	—
Gender gap index 2007	0.441*	0.167	−0.323 [†]

[†], $P < 0.10$; *, $P < 0.05$.

centage of girls on a country's IMO teams during the past 2 decades (Table 4) and its 2007 GGI (Table 5 and Fig. 3). These findings stand in distinct contrast to Machin and Pekkarinen's (19) claim that no correlation exists between GGI and VR for mathematics.

Noteworthy in this context is the fact that the U.S. ranked only 31st best, between Estonia and Kazakhstan, among the 128 countries included in the 2007 *Global Gender Gap Report* (30). Countries such as the U.K. and Iceland, where the ratio of girls-to-boys scoring above the 99th percentile in the 2003 PISA was close to 1.0 or favored girls, had a GGI rank of 11 and 4, respectively. Likewise, Denmark and the Netherlands, where the VR was essentially 1.00, had GGI ranks of 8 and 12, respectively.

Similarly, Penner's cross-nation analysis of the 1995 TIMSS data (20) showed that the proportion of girls scoring above the 95th percentile positively and significantly correlated with several measures of female equality and status, including equity in educational opportunities and representation in the labor force and political offices. Numerous findings in Penner's recent study contradict the Greater Male Variability Hypothesis for mathematics. Our finding that the percentage of girls on a country's IMO team significantly correlates with its GGI, but not with its median

IMO team rank or percentage of world population (Table 5), is also inconsistent with the Greater Male Variability Hypothesis. If this hypothesis were valid, these latter factors should inversely and significantly correlate with percentage of girls because (i) the best 6-member IMO teams consist of multiple students gifted at the 1-in-a-million level where females would be rare, and (ii) countries with larger populations would be more likely to have several such 5-SD-above-the-mean students; the GGI would be largely irrelevant.

Thus, we conclude that gender inequality, not greater male variability, is the primary reason fewer females than males are identified as excelling in mathematics at the high and highest levels in most countries. Of course, gender inequity is complex and multifaceted. It can encompass dynamics in school classrooms leading teachers to provide more attention to boys; guidance counselors, biased by stereotypes, advising females against taking engineering courses; mathematically gifted girls not being identified and nurtured; scarcity of women role models in math-intensive careers leading girls to believe they do not belong in them; unconscious bias against females in hiring decisions; and hostile work environments leading qualified women to drop out in favor of friendlier climes. The data reviewed here did not determine which of these and other gender-related factors are

most influential; all likely contribute to some degree.

Conclusions and Future Directions

This review was organized around 3 questions: Do gender differences in mathematics performance exist in the general population? Do gender differences exist among the highly mathematically talented? Do females exist who possess profound mathematical talent? The answer to the first question is that U.S. girls now perform as well as boys on standardized mathematics tests at all grade levels. Among the mathematically gifted, there may be as many as 2- to 4-fold more boys than girls depending on precisely where the cutoff is set. However, this gender gap, too, has been closing over time at all levels, including even in the IMO. Thus, there is every reason to believe that it will continue to narrow in the future. Moreover, the gender ratio favoring boys above the 99th percentile is not ubiquitous and correlates well with measures of a country's gender equity, strongly indicating that the gap is due, in large part, to sociocultural and other environmental factors, not biology or gender per se.

One serious policy concern that arose from the Hyde et al. study (13) is that the tests developed by states in the U.S. to comply with the mandates of NCLB include almost no questions requiring complex problem solving. NCLB puts pressure on teachers to try to get all their students to pass, thus leading them increasingly to teach to the test (32). With complex problem solving not covered, mathematics teachers will be tempted to neglect teaching it in favor of teaching computation and other lower-level mathematics skills. Yet problem solving and high-level mathematical reasoning are essential skills for success in life and STEM careers. This neglect of problem-solving skills could place U.S. students at a disadvantage compared with their peers in countries where teaching and tests emphasize more challenging content (33). Therefore, it is crucial to address this issue.

Importantly, the U.S. also needs to do a better job of identifying and nurturing its mathematically talented youth, regardless of their gender, race, or national origin. Doing so is vital to the future of the U.S. economy as documented in Thomas Friedman's *The World Is Flat: A Brief History of the Twenty-First Century* (34), *Beyond Bias and Barriers: Fulfilling the Potential of Women in Academic Science and Engineering* (35), *Rising Above the Gathering Storm: Energizing and Employing America for a Brighter Economic Future* (36), *Foundations For Success: The Final Re-*

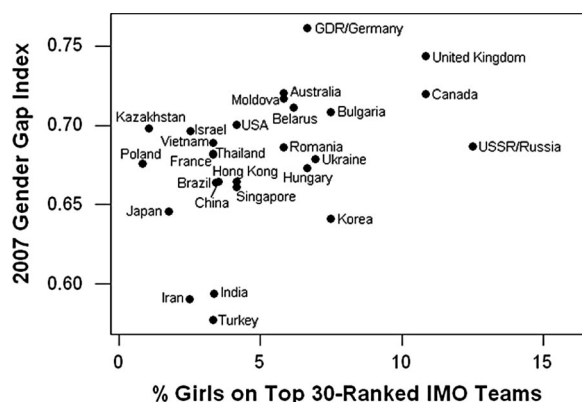


Fig. 3. Presence of females on top 30-ranked IMO teams strongly correlates ($r = 0.44$, $P < 0.05$) with measures of gender equity within countries. The IMO data for percentage of girls on countries' teams from 1989 to 2008 were taken from Table 4. The GGIs were taken from ref. 30.

port of the National Mathematics Advisory Panel (37), and *Identifying and Cultivating Extraordinary Mathematical Talent* (38) outline numerous steps the U.S. can and should take to ensure we

have the well-educated labor force needed to fill the STEM jobs of the future.

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