

# Week 6

Electronic Properties 2

Ohmic and Space Charge Conduction

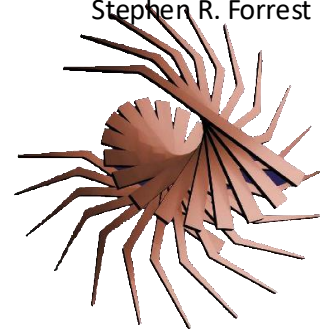
Doping

Recombination

Heterojunctions

Chapter 4.3-4.6

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# Current and Conductivity

## 1. Ohm's Law (gives DC mobility).

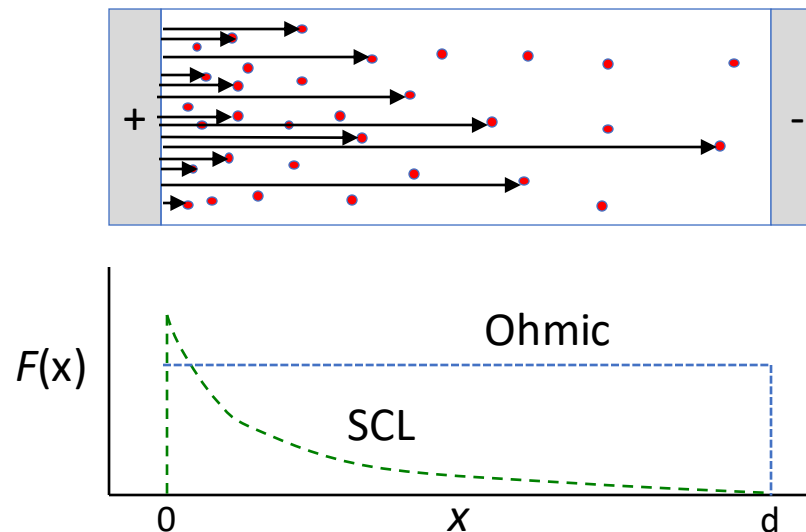
- For a single carrier (holes in this case) in a uniform electric field:

$$j = qp\mu F = qp\mu \frac{V}{d}$$

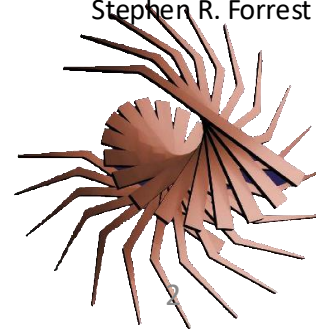
- Gives the product  $p\mu \Rightarrow$  requires independent determination of charge density.
- Ohmic regime* identified by *linear* relationship between  $j$  and  $V$ .

## 2. Space charge limited current (gives DC mobility).

- When the injected carrier density  $p_{inj} > p_0$  (the background charge density), charge accumulates at electrodes:



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# Space Charge Limited Current

- In the space charge regime, we make the following assumptions to solve  $j$  vs.  $V$ :
  - $p_{inj} > p_0$
  - Only one carrier type is present
  - $\mu \neq \mu(F)$  (Field-independent mobility)
  - Free carrier distribution follows Boltzmann statistics
  - Trapped charge occupation defined by Fermi statistics
  - $F$  is large enough for drift (and not diffusion) to dominate
  - Field not so large that field emission is important

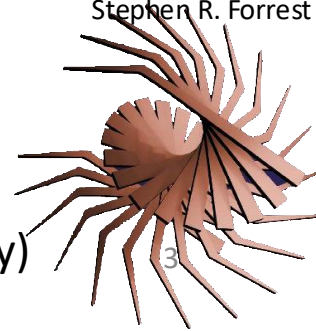
- In 1D, Gauss says: 
$$\frac{dF}{dx} = \frac{q(p_{inj}(x) + p_t(x) + p_0)}{\epsilon} \approx \frac{qp_{inj}(x)}{\epsilon} \text{ (trap free case)}$$

- $\epsilon = \epsilon_0 \epsilon_r$

- Current in the absence of trapped charge,  $p_t(x)$ :  $j(x) = q\mu_p p_{inj}(x) F(x)$

- Now: 
$$\frac{dF^2(x)}{dx} = 2F(x) \frac{dF(x)}{dx} = \frac{2qp_{inj}(x)F(x)}{\epsilon} = \frac{2j(x)}{\epsilon\mu_p}$$

- Since  $j$  is constant across layer  $\Rightarrow F^2(x) = \frac{2jx}{\epsilon\mu_p}$  (This is current continuity)



# $j$ - $V$ in the SCL regime

$$F^2(x) = \frac{2jx}{\epsilon\mu_p} \quad \square \quad F(x) = \sqrt{\frac{2jx}{\epsilon\mu_p}} \quad \left. \vphantom{\frac{2jx}{\epsilon\mu_p}} \right\} \text{ Note: } F(x) \sim x^{1/2} \text{ vs. } F(x) = \text{constant for Ohmic}$$

Now potential is:  $-\frac{dV}{dx} = F(x)$

Integrating between  $0 < V < V_a$  and  $0 < x < d$

We obtain:  $V_a = \frac{2}{3} \sqrt{\frac{2jd^3}{\epsilon\mu_p}}$

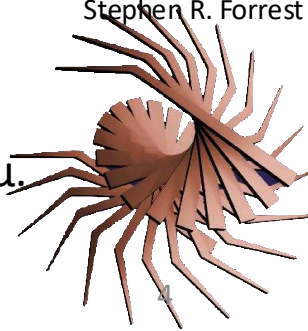
Giving the **Mott-Gurney relationship**:

$$j = \frac{9}{8} \mu_p \epsilon \frac{V_a^2}{d^3}$$

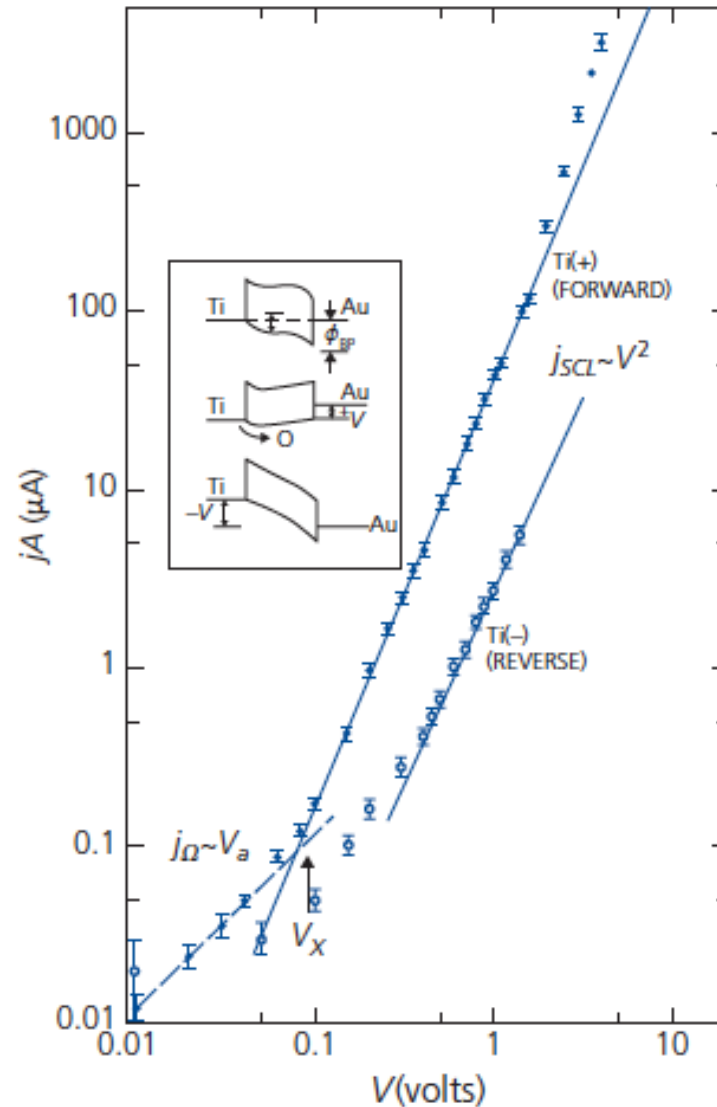
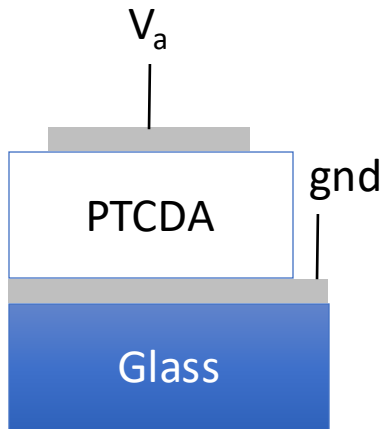
Note the absence of  $p$ !

$\Rightarrow$  Only need the dielectric constant and the film thickness to find  $\mu$ .

Use the Ohmic region of the  $j$ - $V$  curve to determine  $p_0$ .



# SCL Current in PTCDA



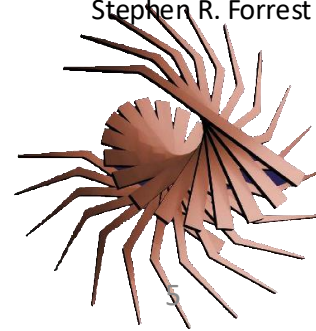
To find background carrier density:

At  $V_x$ :  $j(\text{ohmic}) = j(\text{SCL})$

$$\Rightarrow qn\mu \frac{V_x}{d} = \frac{9}{8} \mu \epsilon \frac{V_x^2}{d^3}$$

$$\Rightarrow n = \frac{9}{8} \frac{\epsilon}{q} \frac{V_x}{d^2}$$

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# But what happens if things aren't so simple?

- We have assumed no traps. In organics, this is not often the case due to **static disorder**.
- Simplest case: A single discrete, shallow trap where  $\frac{p_{inj}}{p_t} = \Theta \ll 1$
- Then you can show:  $j = \frac{9}{8} (\Theta \mu_p) \varepsilon \frac{V_a^2}{d^3}$

➤ That is, the mobility is now reduced by  $\Theta$

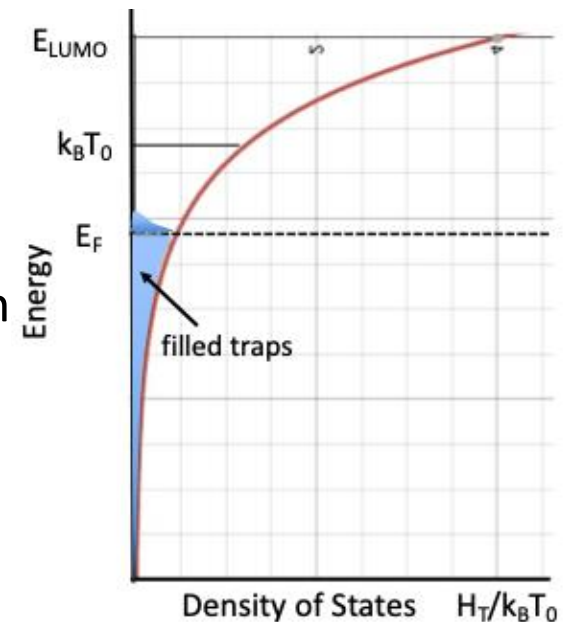
- More often there is an exponential distribution of traps, in which case we have trap-filled limited conduction:

$$j_{TFL} = q\mu N_{HOMO} \left[ \frac{\varepsilon m}{q(m+1)N_t} \right]^m \left[ \frac{2m+1}{m+1} \right]^{m+1} \frac{V_a^{m+1}}{d^{2m+1}}$$

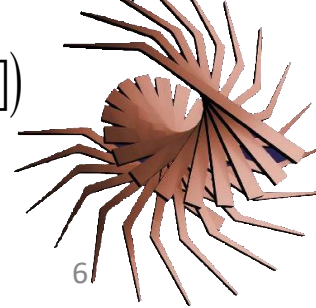
- $m = T_t/T$  where  $T_t$  is the characteristic trap temperature

- Define  $p_t = N_t \exp\left(-\left(E_{Fp} - E_{HOMO}\right)/k_B T_t\right)$
- Leading to:  $p = N_{HOMO} \exp\left(-\left(E_{Fp} - E_{HOMO}\right)/k_B T\right) = N_{HOMO} \exp\left(-\left(E_{Fp} - E_{HOMO}\right)/k_B T_t \left[T_t/T\right]\right)$

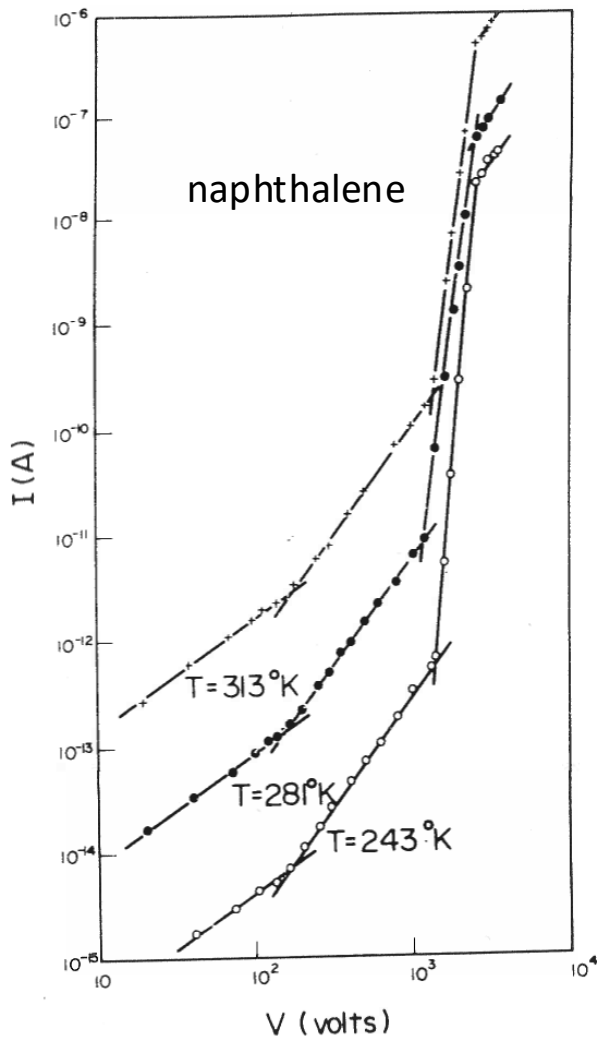
$$p = N_{HOMO} \left( \frac{p_t}{N_t} \right)^{T_t/T} \Rightarrow p_t = N_t \left( \frac{p}{N_{HOMO}} \right)^{1/m}$$



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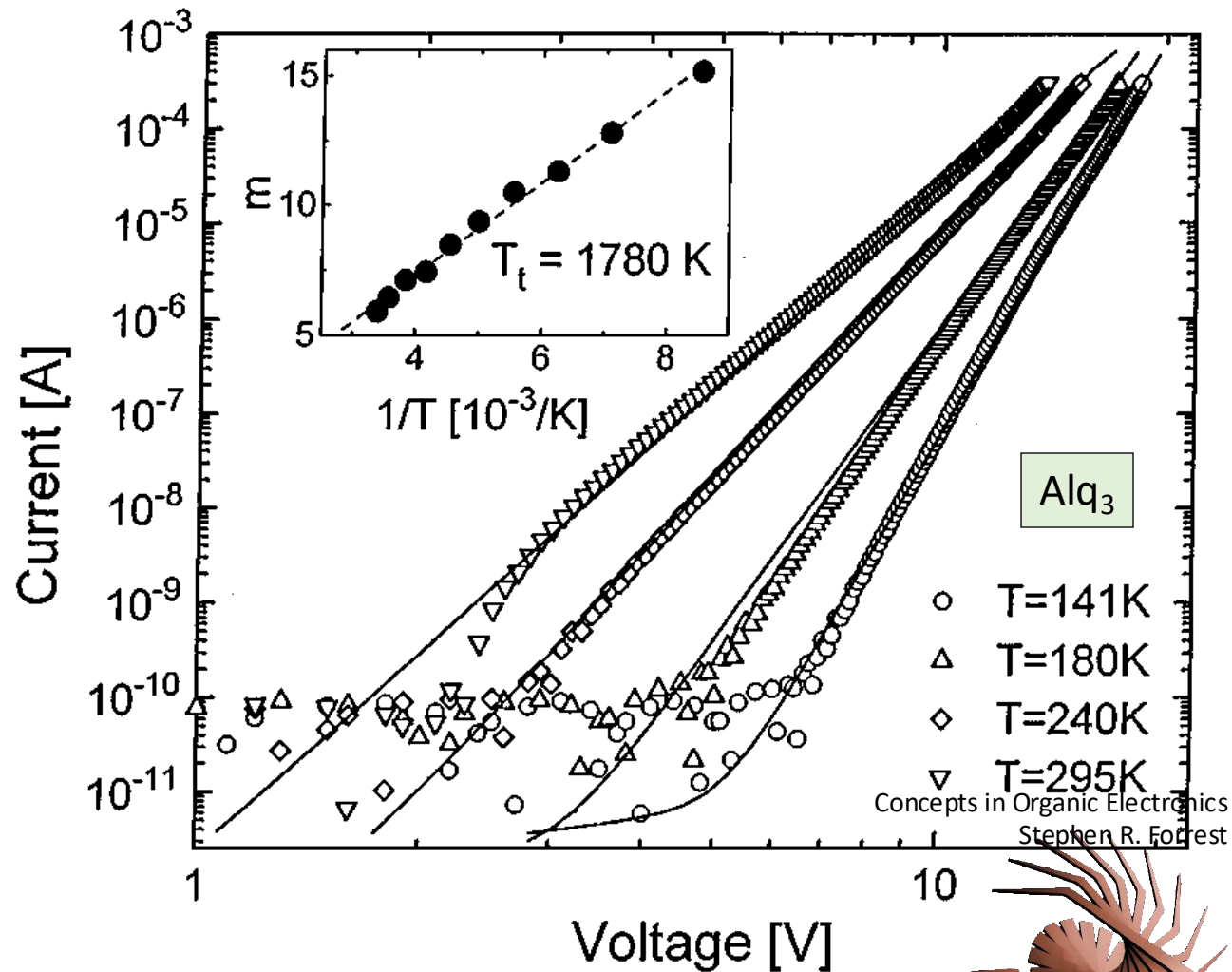


# Examples of TFL-SCL

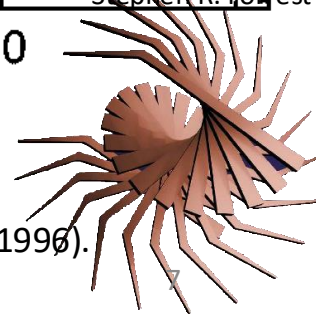


Multiple ohmic, SCL and TFL regions

M. Campos, Mol. Cryst. Liq. Cryst. **18**, 105 (1972)

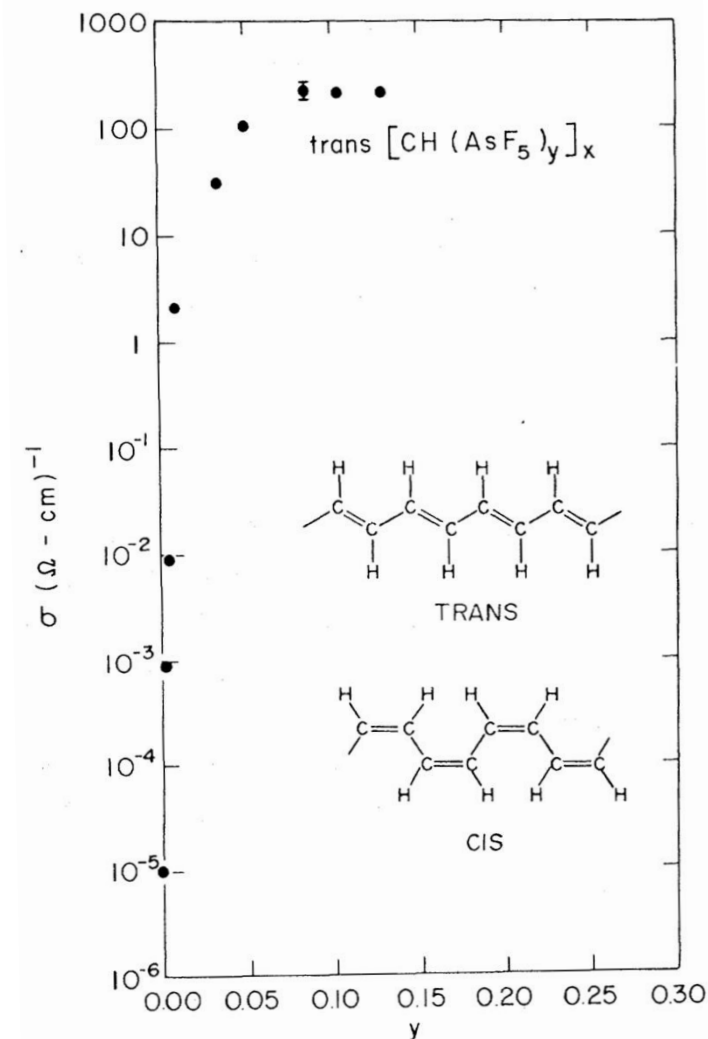
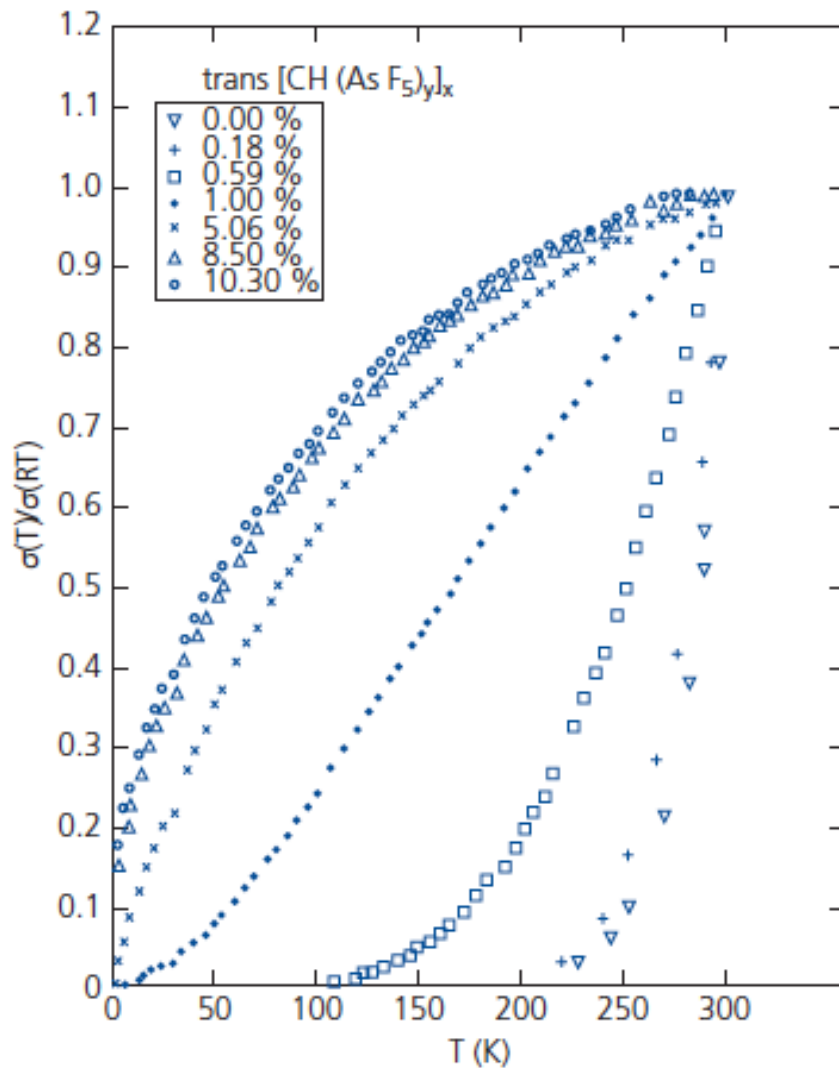


P. E. Burrows, et al., *J. Appl. Phys.*, **79**, 7991 (1996).



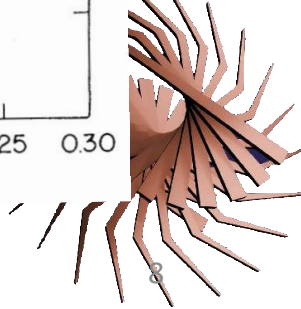
# Doping of Organics to Increase Conductivity

The first demonstration: polyacetylene



Heeger, Shirakawa, MacDiarmid, et al. Phys. Rev. Lett., **39** 1098 (1977)

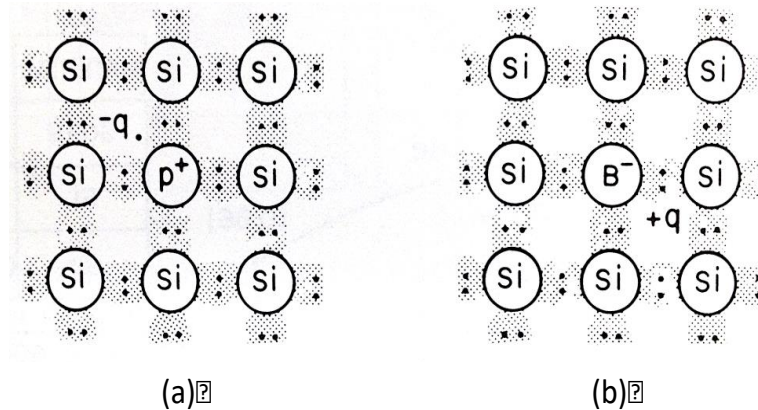
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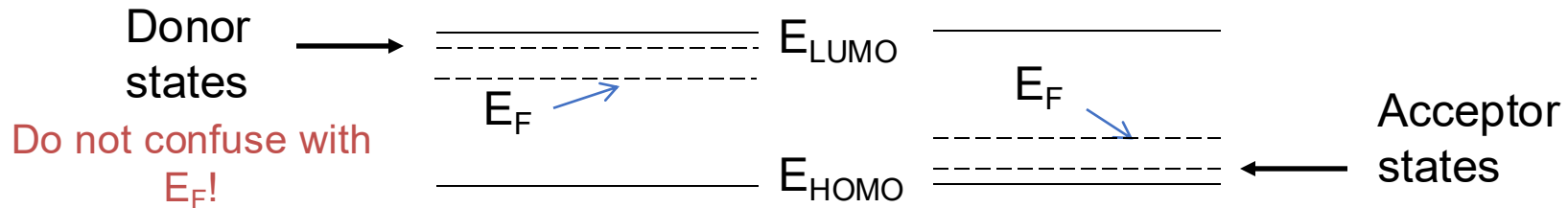


# Doping in Organics: Not entirely similar to inorganics

Substitutional doping in inorganics



But no shared bonds in organics!

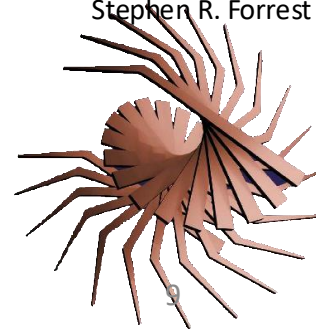


$$n = N_{LUMO} \exp\left(\frac{E_F - E_{LUMO}}{k_B T}\right)$$

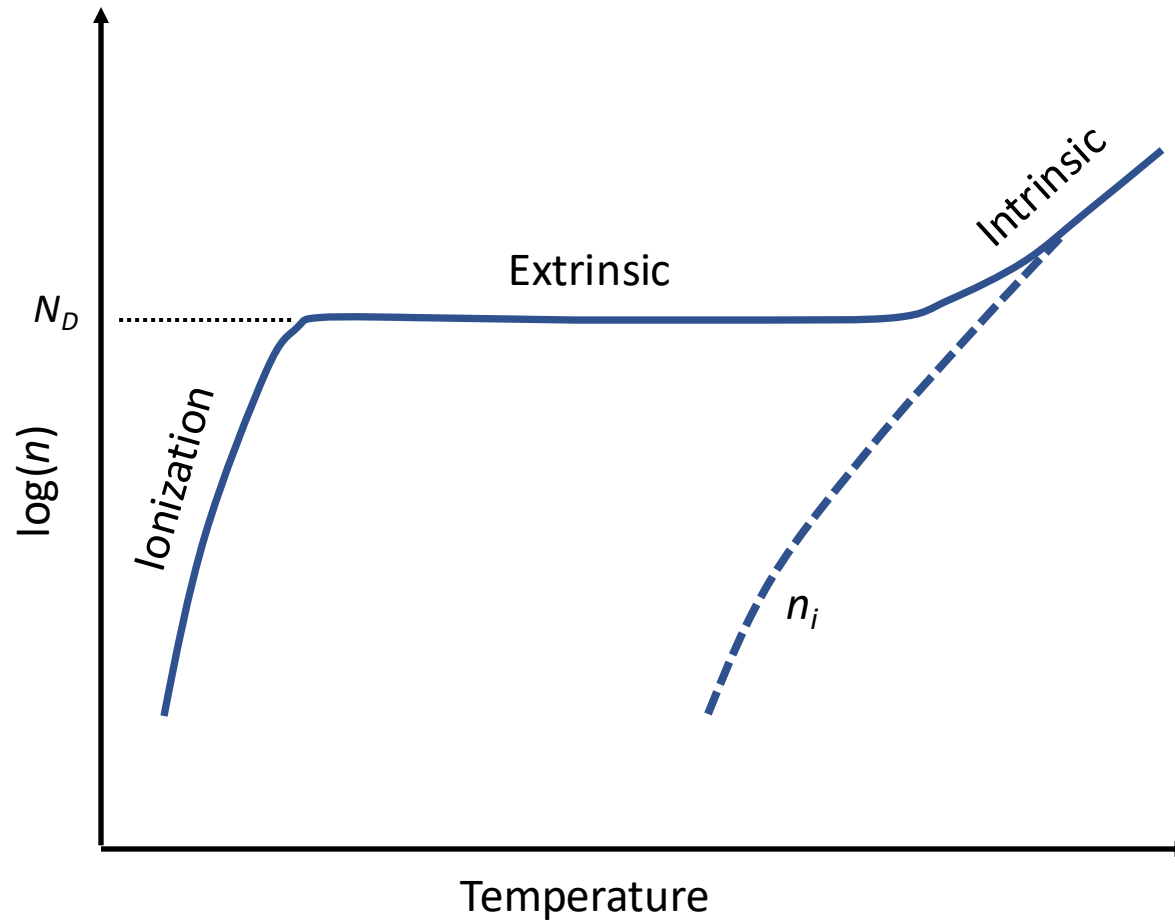
$$p = N_{HOMO} \exp\left(\frac{E_{HOMO} - E_F}{k_B T}\right)$$

$$\Rightarrow \text{Law of mass action: } n_i^2 = N_{HOMO} N_{LUMO} \exp\left[-\frac{E_G}{k_B T}\right]$$

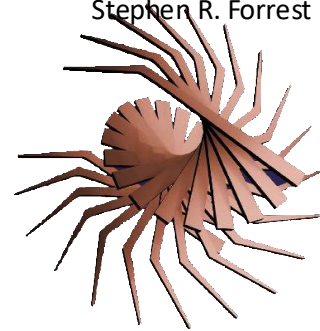
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# Doping regimes of an n-type semiconductor

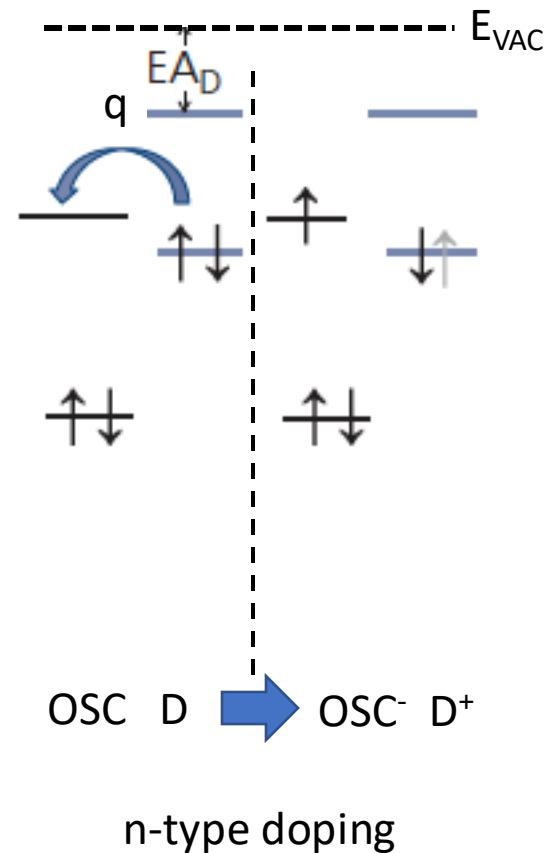
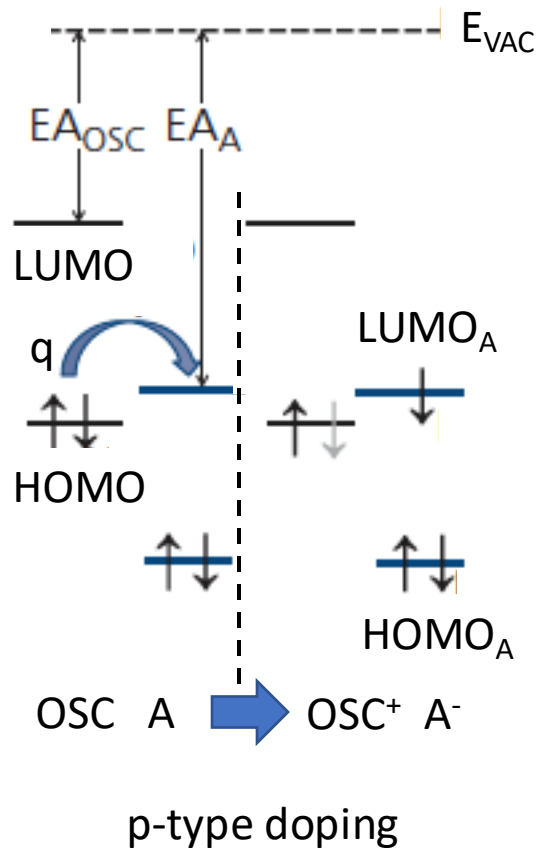


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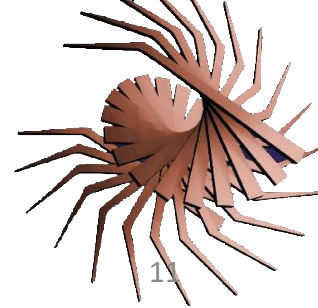


# Doping at the molecular level

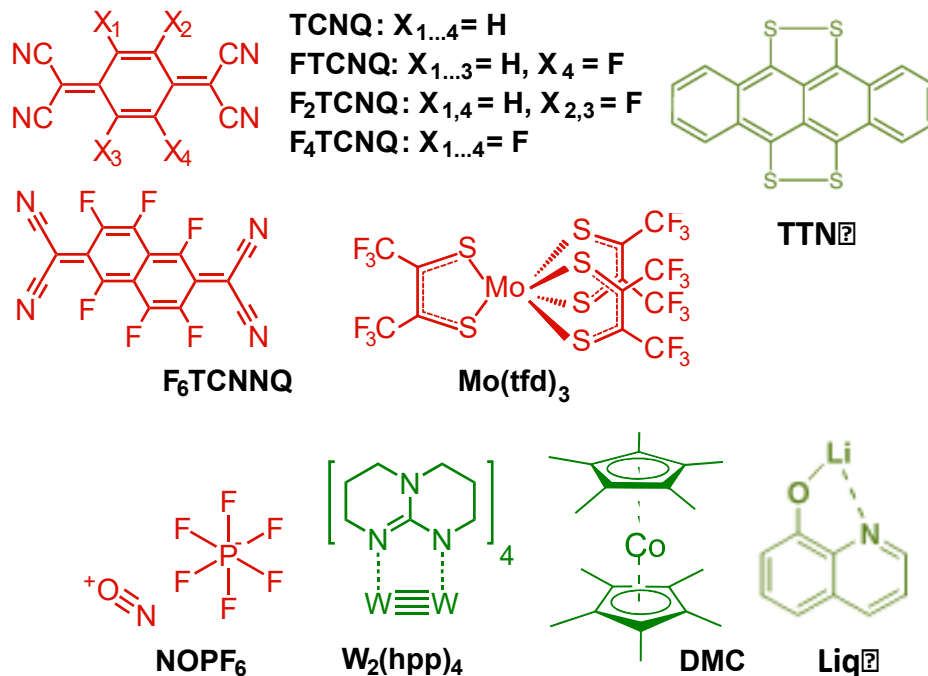
Involves charge transfer between dopant and host



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# Example *molecular* dopants



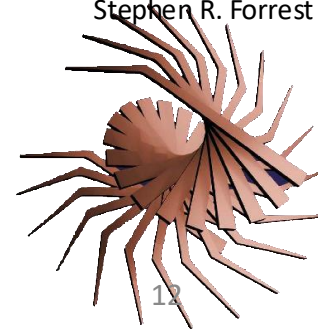
red=acceptors; green=donors

But there are metallic dopants too: Cs, Li, etc.

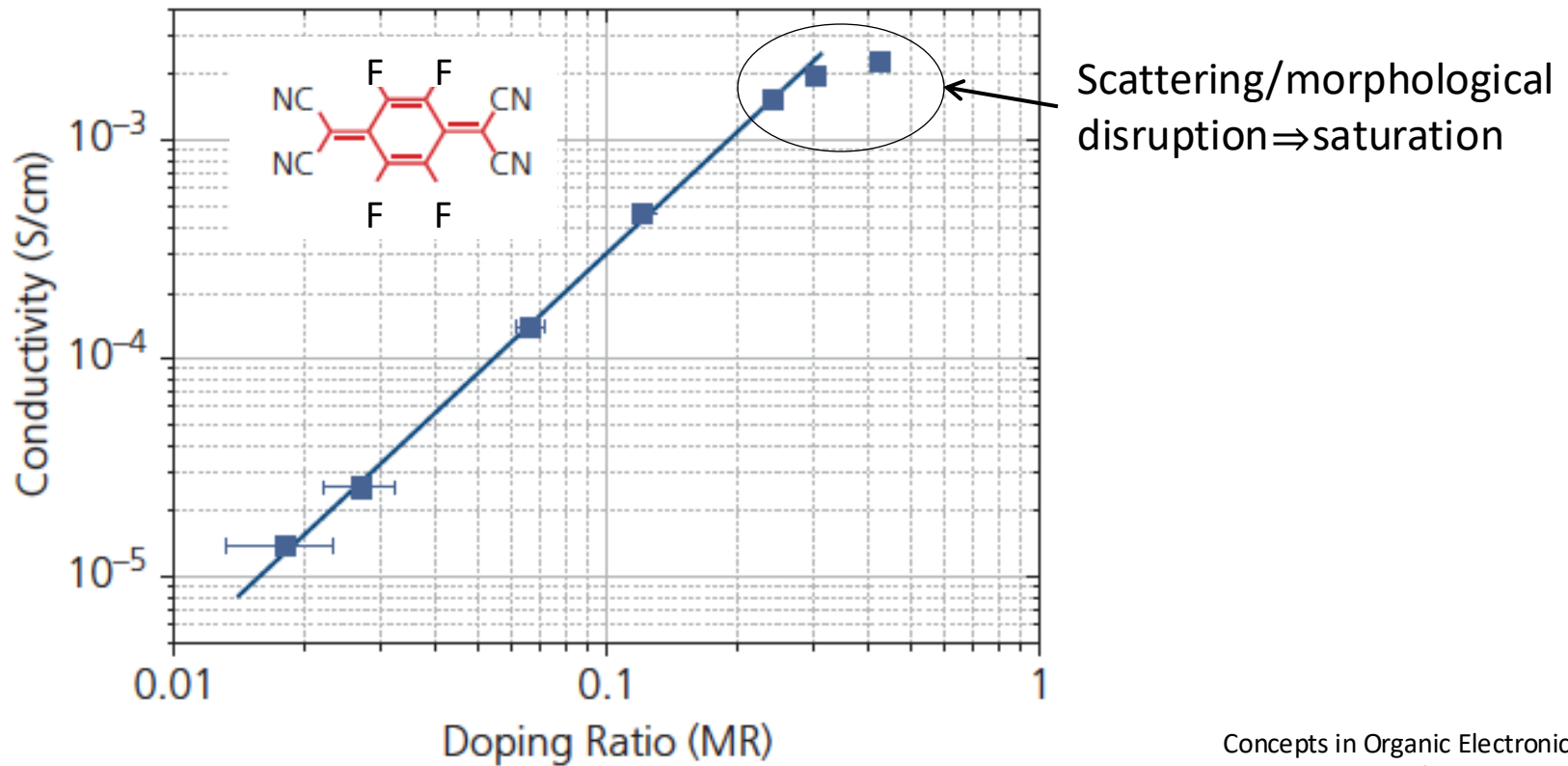
LiF + Al cathodes  
common in OLEDs:



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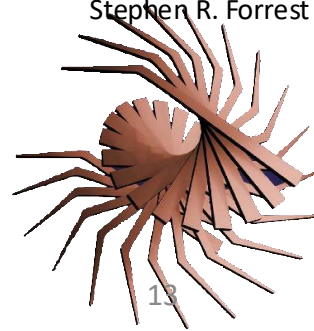
# Difficult to get a high conductivity (it takes *a lot* of dopant)



N,N,N',N'-tetrakis(4-methoxyphenyl)-benzidine with  $F_4$ -TCNQ.

Olthof et al., J. Appl. Phys., **106**, 103711 (2009)

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# Recombination

## Charge diffusion equations

$$\frac{\partial n}{\partial t} = \frac{1}{q} \nabla \cdot \mathbf{j}_e - R_e + G_e$$

$$\frac{\partial p}{\partial t} = -\frac{1}{q} \nabla \cdot \mathbf{j}_h - R_h + G_h$$

$$\mathbf{j}_e = qD_e \nabla n$$

Using Fick's Law

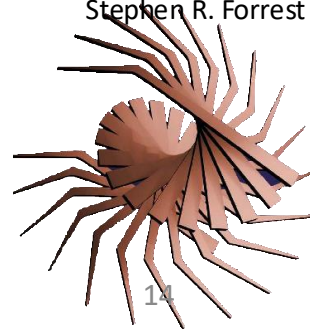
$$\mathbf{j}_h = -qD_h \nabla p$$

Gives:

$$\frac{\partial n}{\partial t} = D_e \nabla^2 n - R_e + G_e$$

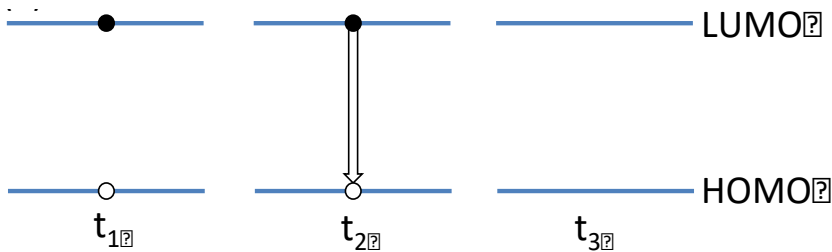
$$\frac{\partial p}{\partial t} = D_h \nabla^2 p - R_h + G_h$$

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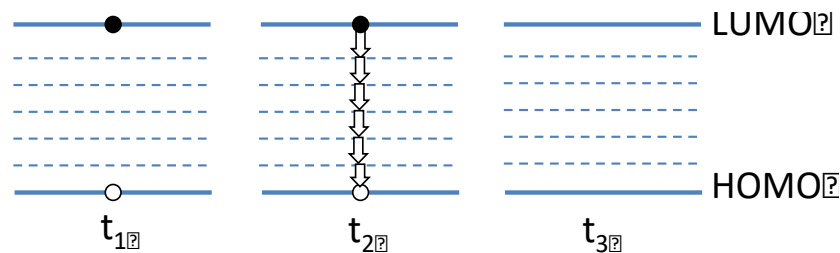


# Direct HOMO-LUMO Recombination and via Midgap States

## Direct (Band-to Band) Recombination

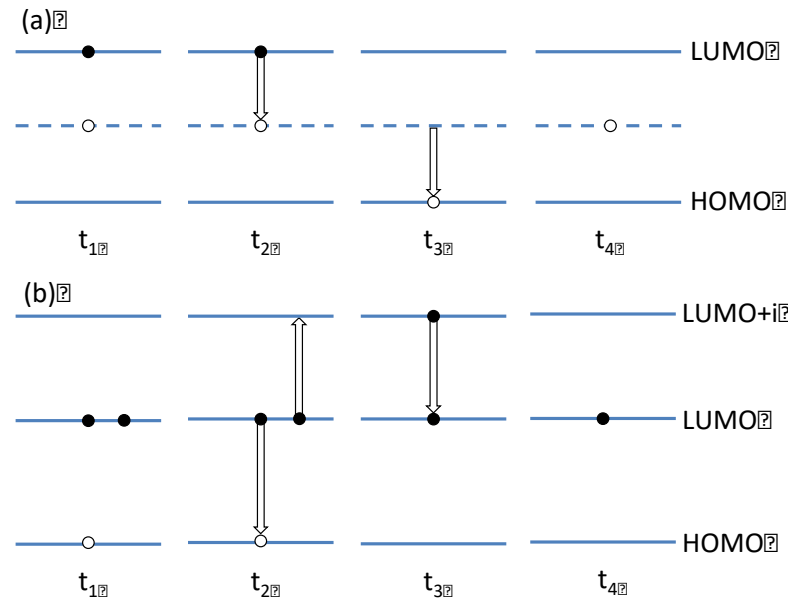


## Multiple Step Recombination



$$R_e^{dir} = \frac{n - n_0}{\tau_e} = \frac{\Delta n}{\tau_e}$$

## Shockley-Read-Hall Recombination



## Auger Recombination

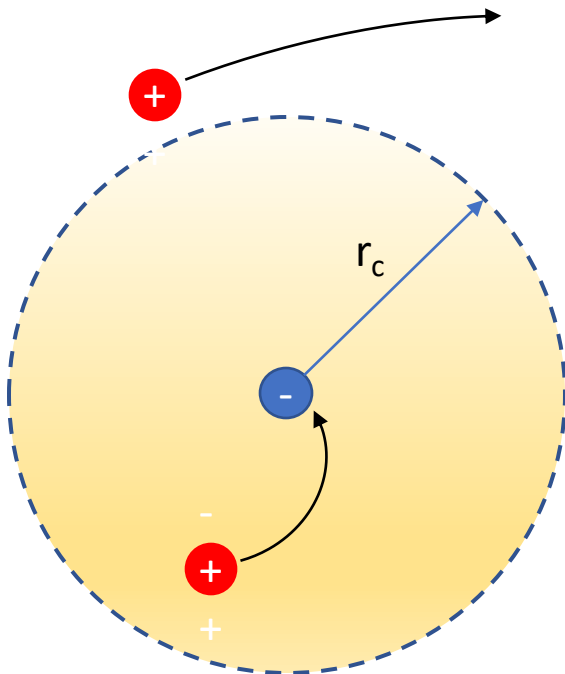
Concepts

equilibrium restoring force

$$R^{SRH} = \frac{np - n_i^2}{\tau_e(p + p_1) + \tau_h(n + n_1)}$$

# Langevin (Bimolecular) Recombination

- When two carriers meet....



Capture radius: When Coulomb = thermal energy

$$r_c = \frac{q^2}{4\pi\epsilon_r\epsilon_0 k_B T}.$$

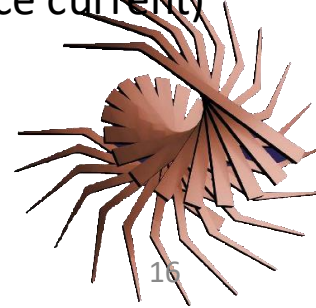
Langevin recombination rate constant:

$$\gamma_L = \frac{q}{\epsilon_r\epsilon_0}(\mu_e + \mu_h) = \frac{q}{\epsilon_r\epsilon_0}\mu_T.$$

Yielding the recombination rate (and hence current)

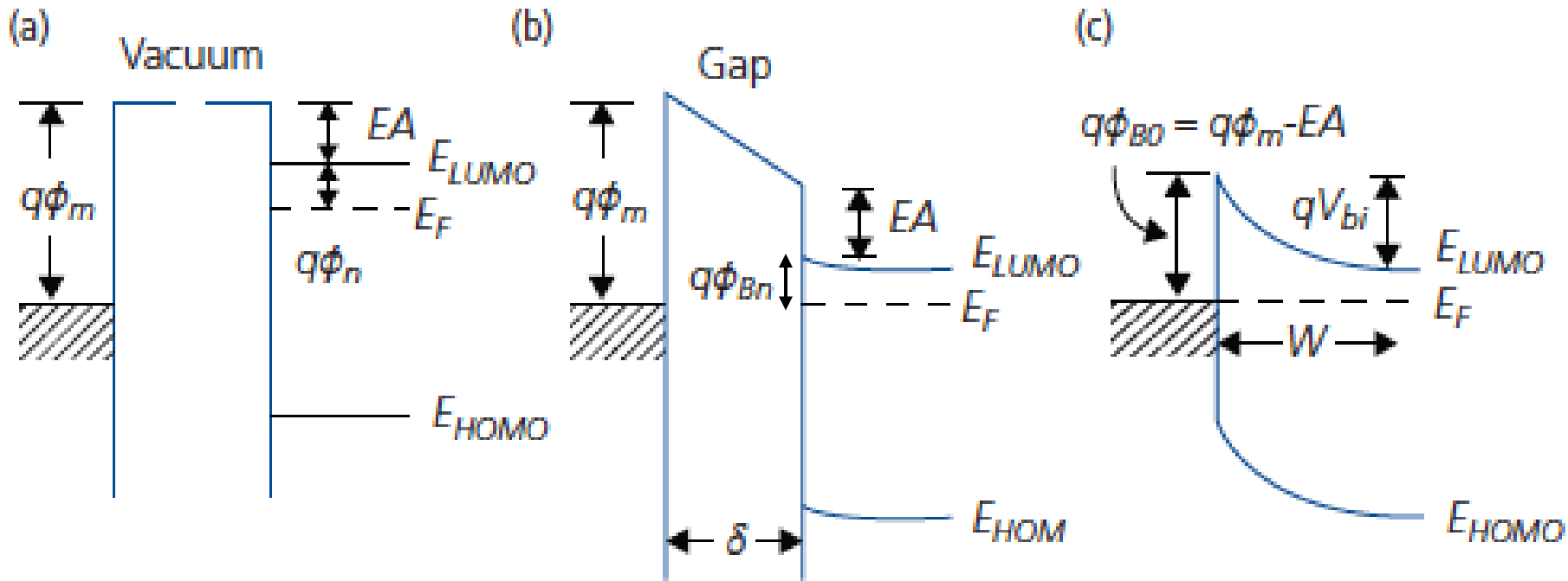
$$R^L = \gamma_L (pn - n_i^2)$$

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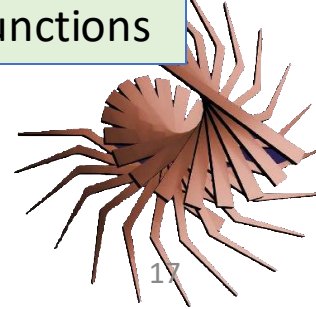


# Metal-semiconductor Junctions: Schottky barriers

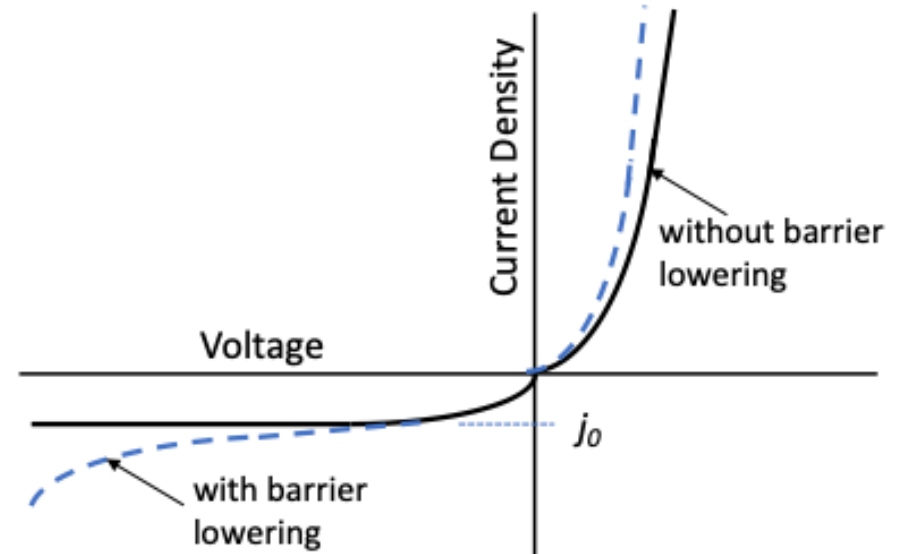
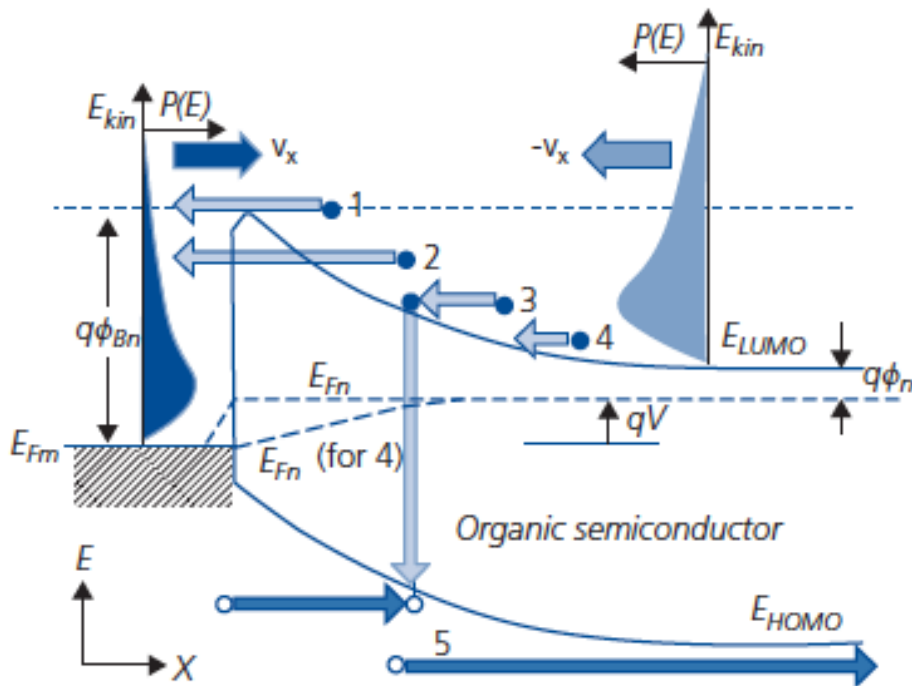


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Traps Play a Big Role in Determining Barrier Heights at Metal-Semiconductor Junctions



# Current sources across M-O Junctions

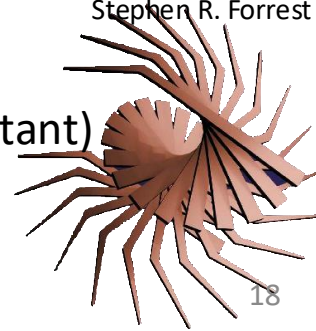


$$j = j_0 \left( \exp(qV / k_B T) - 1 \right)$$

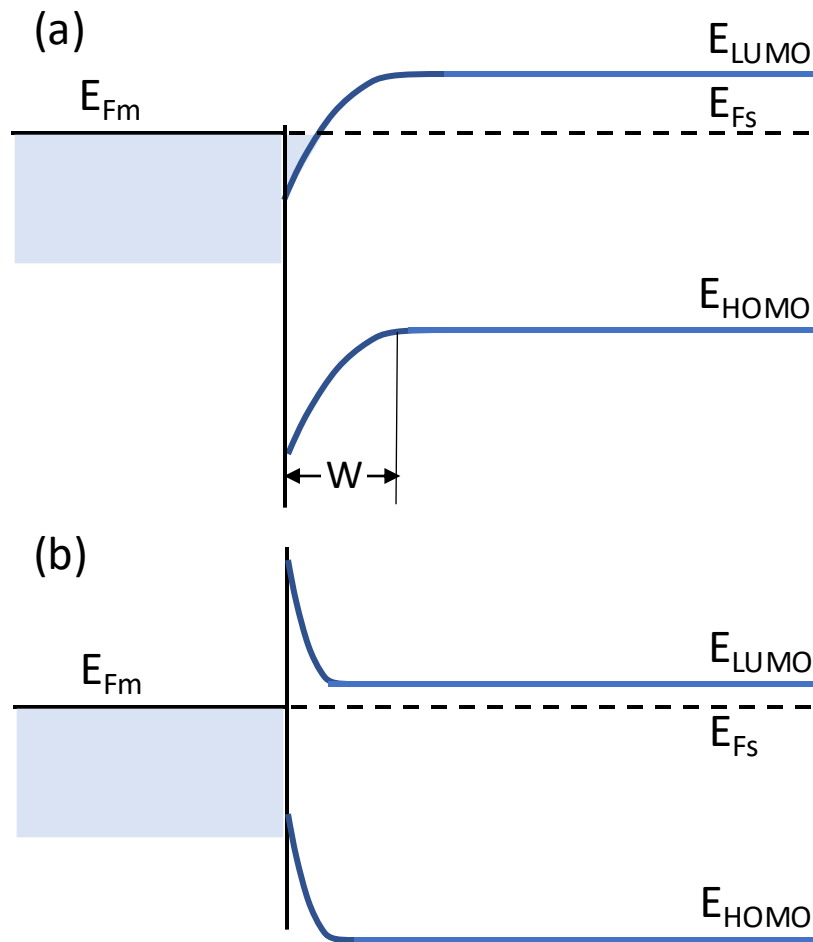
$$j_0 = j_{0TE} = A^* T^2 \exp(-q\phi_{B0} / k_B T) \quad A^* = \frac{4\pi q m^* k_B^2}{h^3}$$

(Richardson Constant)

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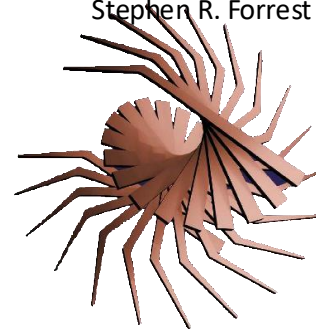
Metal-organic junctions can be low resistance (Ohmic) if the semiconductor is highly doped at the surface



Depletion width at the interface:

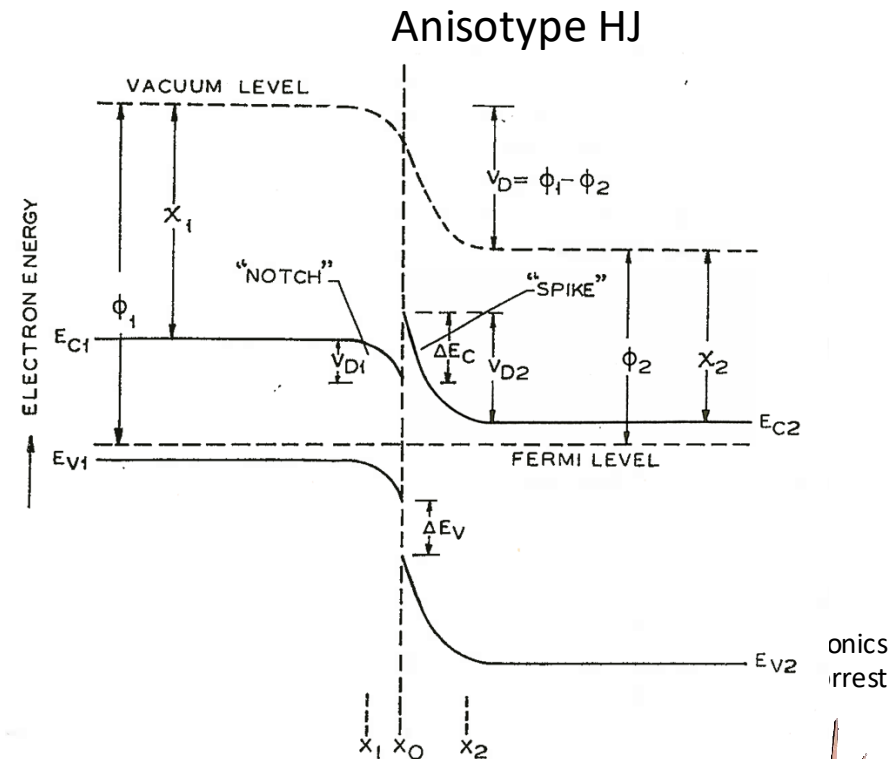
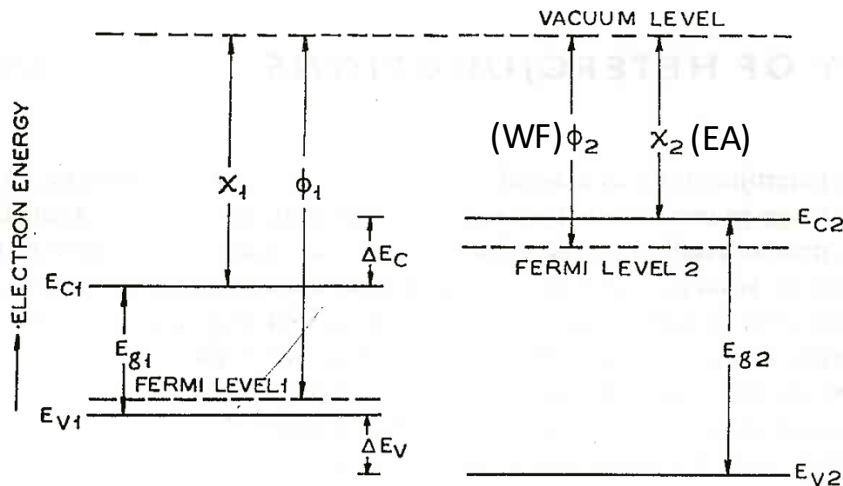
$$W = \sqrt{\frac{2\epsilon(V - V_{bi})}{qN_D}}$$

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# Heterojunctions: Organic-organic contacts

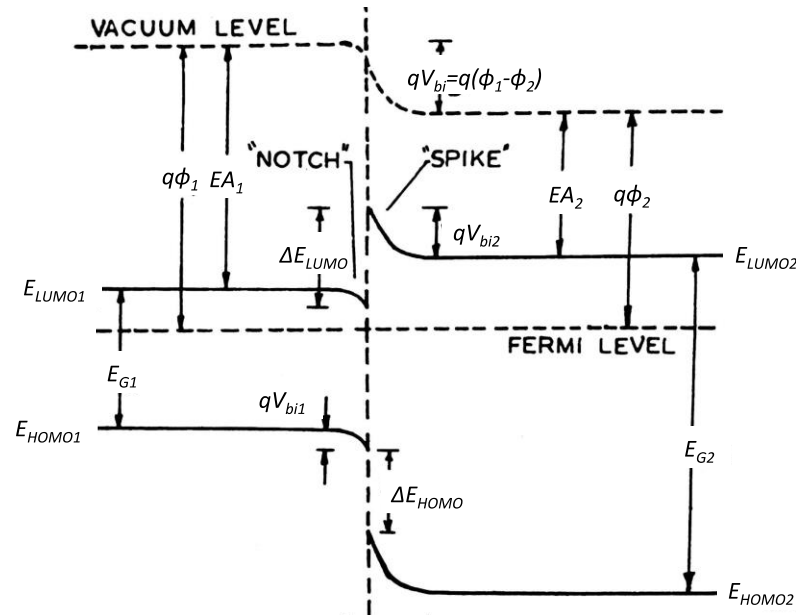
- A heterojunction is a contact between two dissimilar materials (typically semiconductors)
- HJs play a vital role in almost all photonic devices, and many electronic devices too.
- Some definitions:



- Anderson's rule:  $\Delta E_c = |\chi_1 - \chi_2|$  (doesn't work so well for inorganics due to charge transfer; better for organics)
- $\Delta E_v = \Delta E_g - \Delta E_c$
- Band bending due to free charge: organics tend toward flat bands

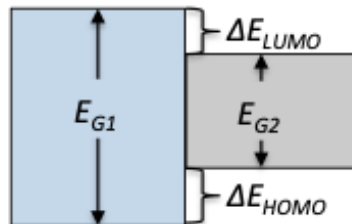


# Isotype vs. Anisotype HJ

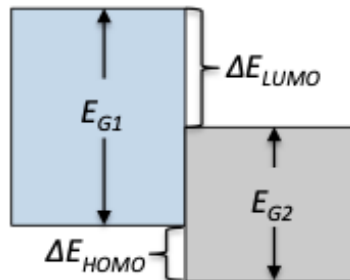


*n-N* isotype HJ

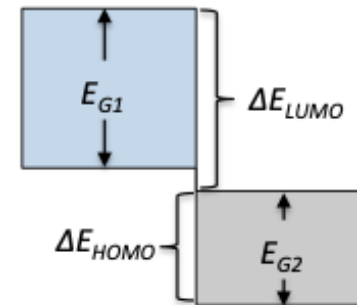
## Classification of HJ types



Type I  
Nested

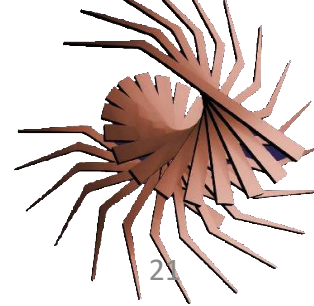


Type II  
Staggered



Type III  
Broken Gap

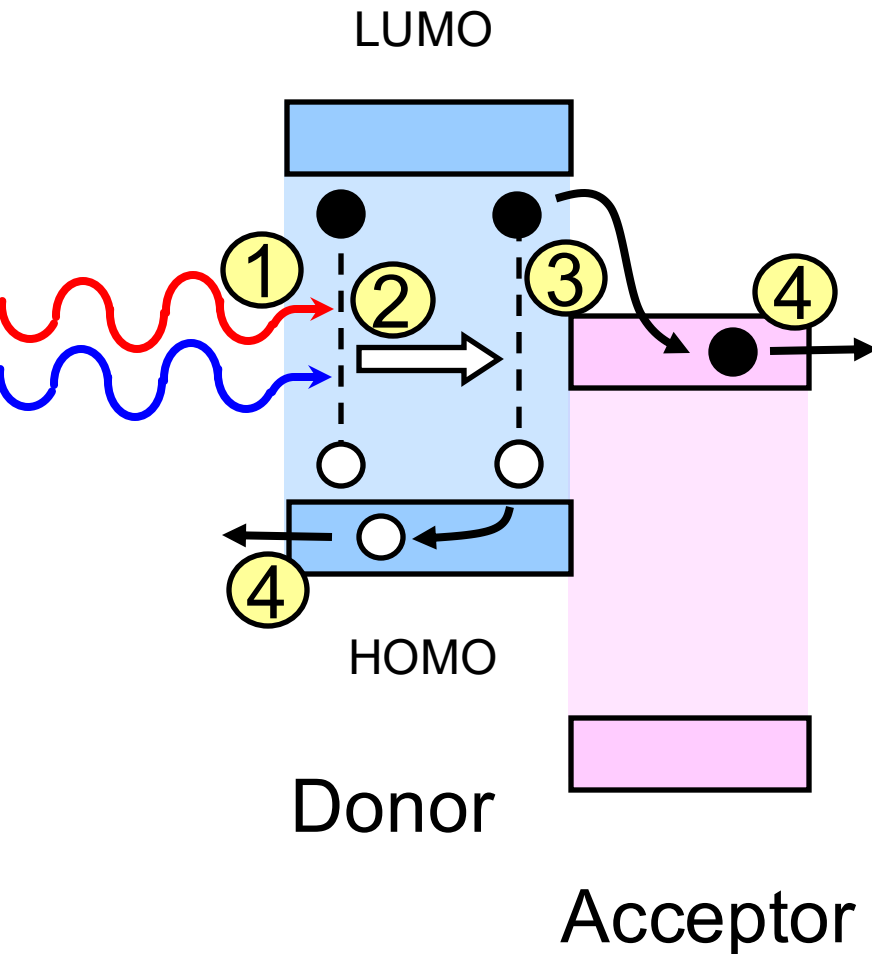
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# Photoinduced Charge-Transfer at a Type II HJ

## The Basis of OPV Operation

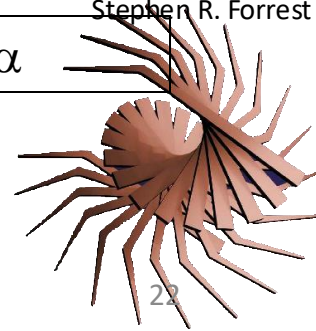
### Processes occurring at a Donor-Acceptor heterojunction



- ① Exciton generation by absorption of light ( $1/\alpha$ )
- ② Exciton diffusion over  $\sim L_D$
- ③ Exciton dissociation by rapid and efficient charge transfer
- ④ Charge extraction by the internal electric field

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Typically:  $L_D \ll 1/\alpha$



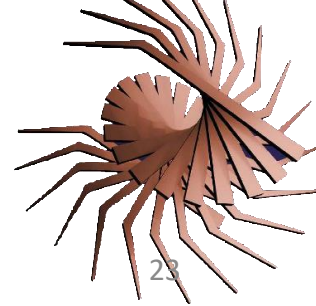
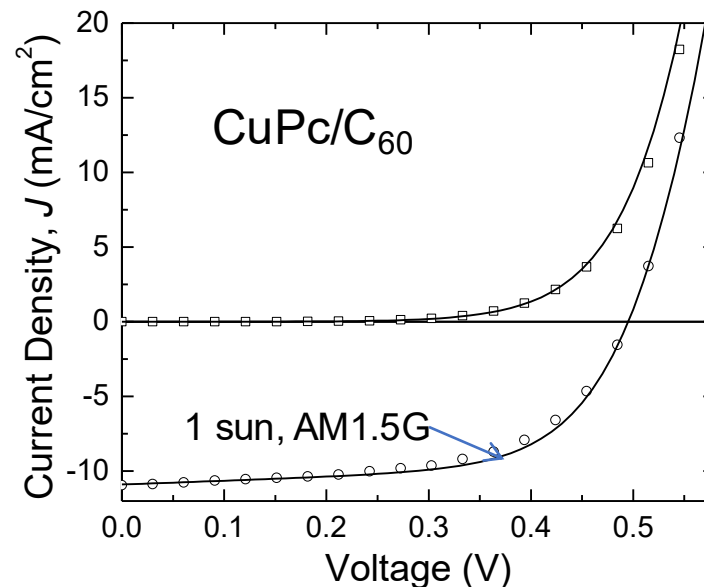
# Ideal Diode Equation: Problem Statement

- The Shockley Equation (1949):

$$J = J_o(\exp(qV_a / k_bT) - 1) - J_{ph}$$

has been successfully applied (e.g. Xue and Forrest, 2004) to organic heterojunction cells. But the physics is wrong!

- Why does it “work”?
- Is there a more appropriate relationship for organic (i.e. *excitonic*) HJs?



# Excitonic Heterojunctions:

Controlled by **energy transport**, *not* charge transport

1. Excitons diffuse with current  $J_x$  to HJ
2. Separate into polaron pairs across HJ
3. PP can either dissociate into carriers
4. Or recombine to ground state

$\zeta$ =PP density

$k_{ppr}$ =PP recombination rate

$k_{ppd}$ =PP dissociation rate

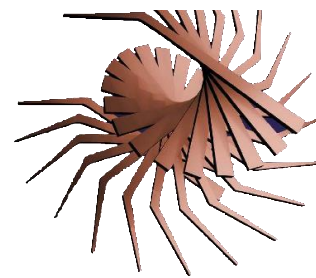
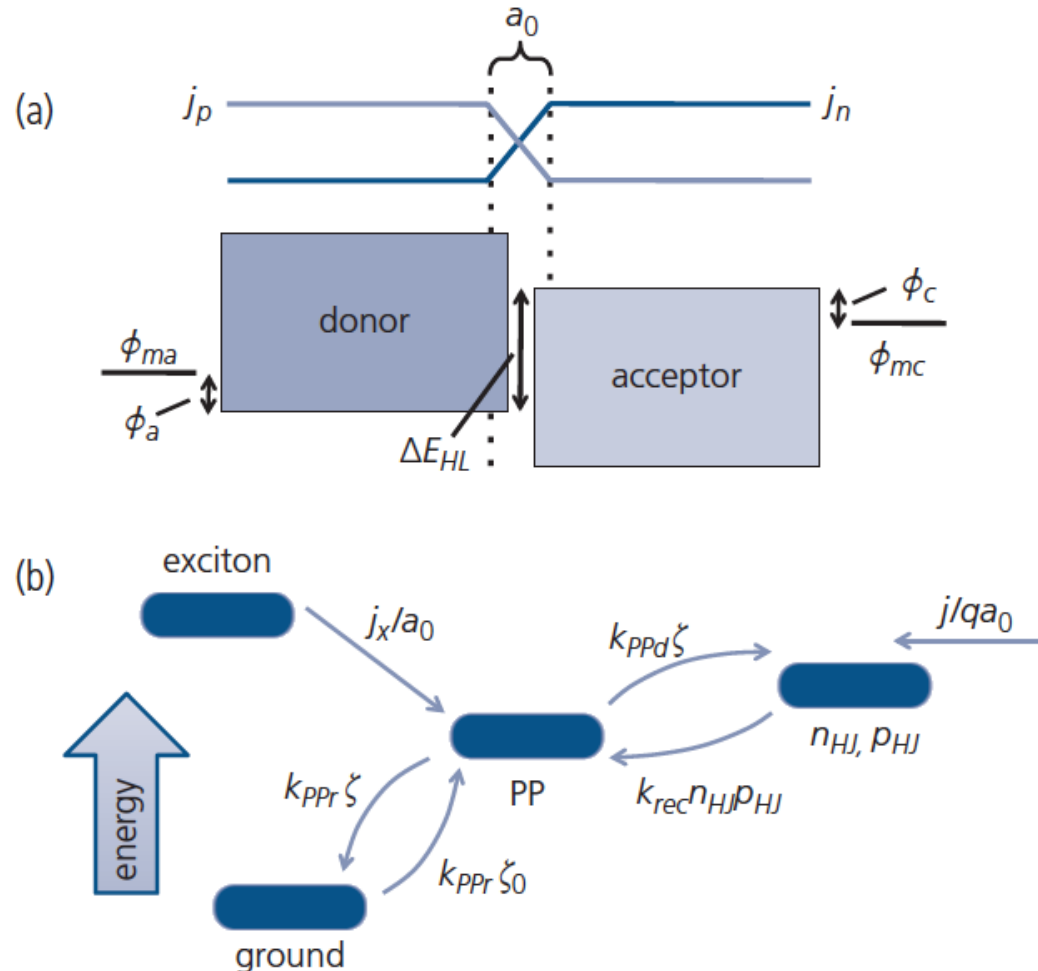
$k_{rec}$ =charge recombination rate

$J$ =electron current

$WF$ =work function

$n_i, p_i$ =charge at interface

A polaron pair at the interface is equivalent to a charge transfer (CT) state





# Derivation of the Ideal Diode Eq.

*"Just because you have an ideal diode equation does not mean you have an ideal diode"*

- The rate equations in steady state:

- Excitons:  $\frac{J_X}{a_0} - k_{PPr}(\zeta - \zeta_{eq}) - k_{PPd}\zeta + k_{rec}n_I p_I = 0,$

- Polarons:  $k_{PPd}\zeta - k_{rec}n_I p_I + \frac{J}{qa_0} = 0,$

## Rate Equations + Fermi Stats:

$$J_0 \left\{ \exp(qV_a / k_B T) - \frac{k_{PPd}}{k_{PPd,eq}} \right\} - J_{ph}$$

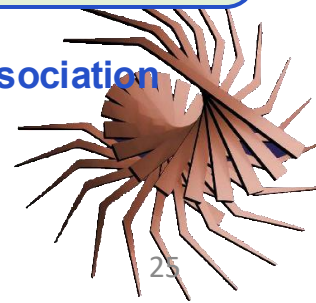
$$J = qa_0 k_{rec} N_{HOMO} N_{LUMO} (1 - \eta_{PPd}) \exp(-\Delta E_{HL} / k_b T) \left\{ \exp(qV_a / k_b T) - \frac{k_{PPd}}{k_{PPd,eq}} \right\} - q \eta_{PPd} J_X$$

electron & hole  
DOS

PP dissociation  
efficiency

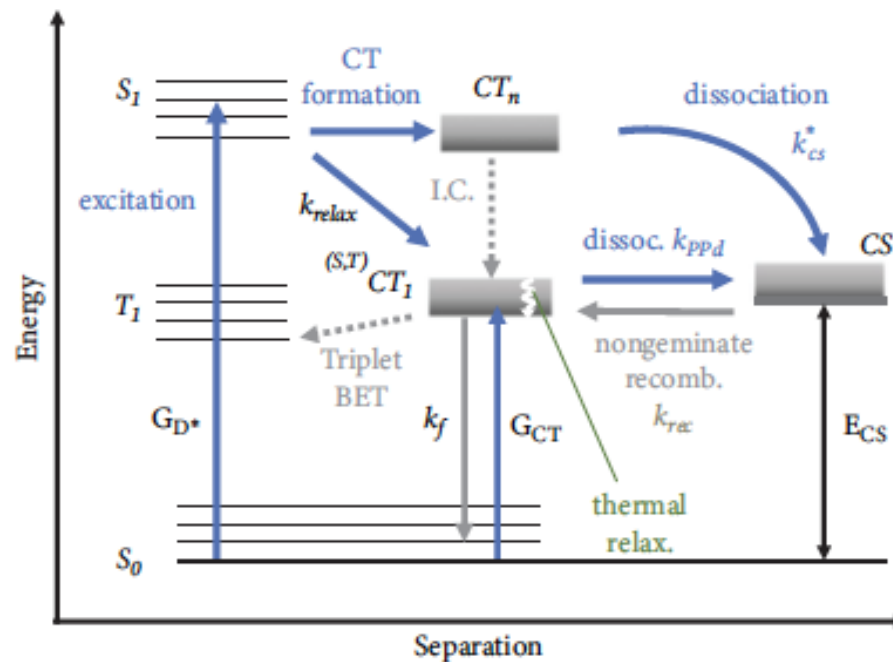
$$\left[ \eta_{PPd} = \frac{k_{PPd}}{k_{PPr} + k_{PPd}} \right]$$

equilibrium dissociation  
rate



# Ideal diode theory suggests the CT state is the precursor to free charge

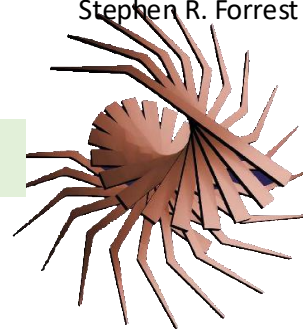
Energy landscape for free charge generation into the charge separated (CS or PP) state



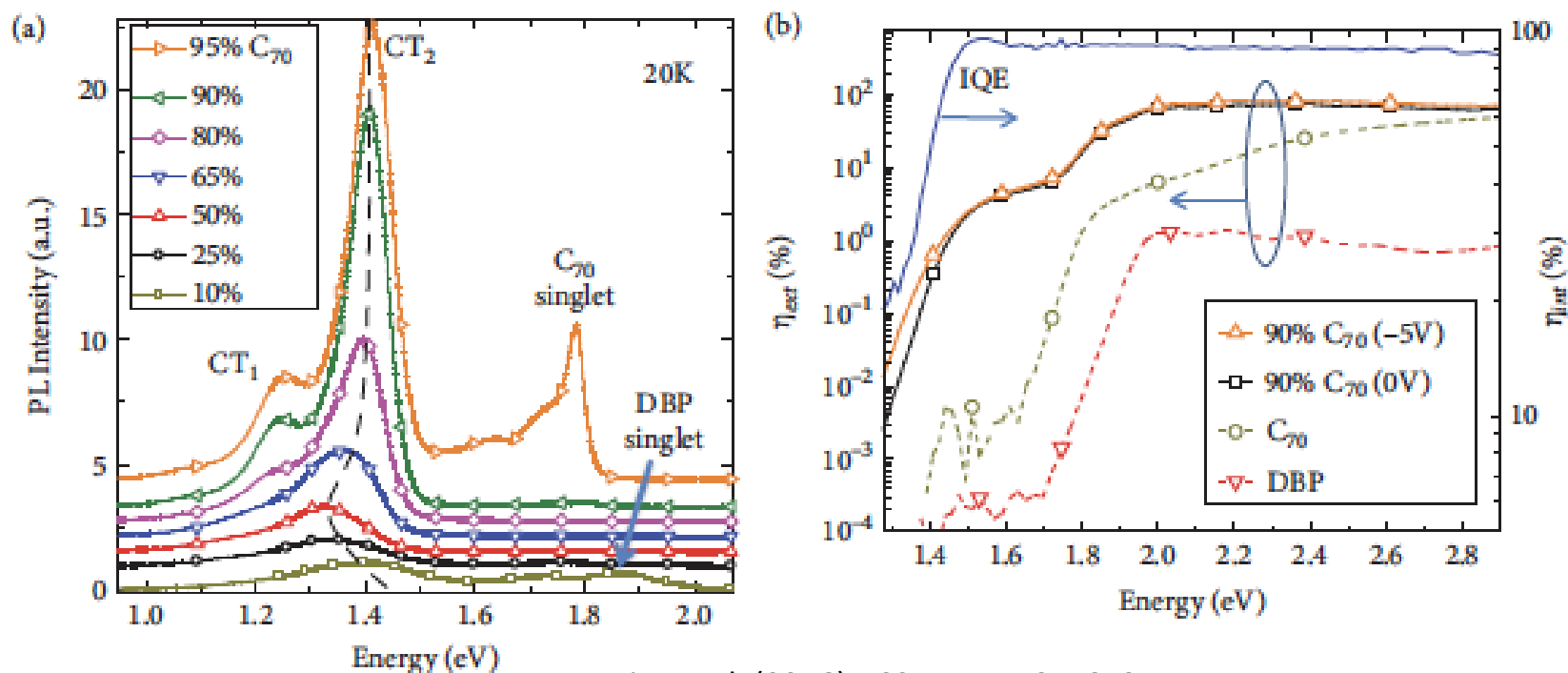
X. Liu, et al. (2019) Trends in Chemistry, **1**, 815.

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Back transfer into the triplet is a major source of non-radiative loss of excitons



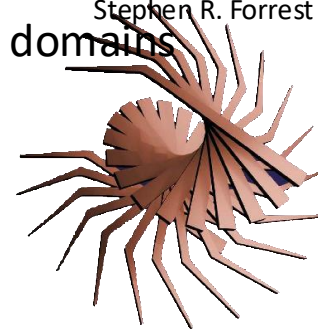
# CT state precursors in the DBP:C<sub>70</sub> Donor-Acceptor System



X. Liu, et al. (2016) ACS Nano, **10**, 7619

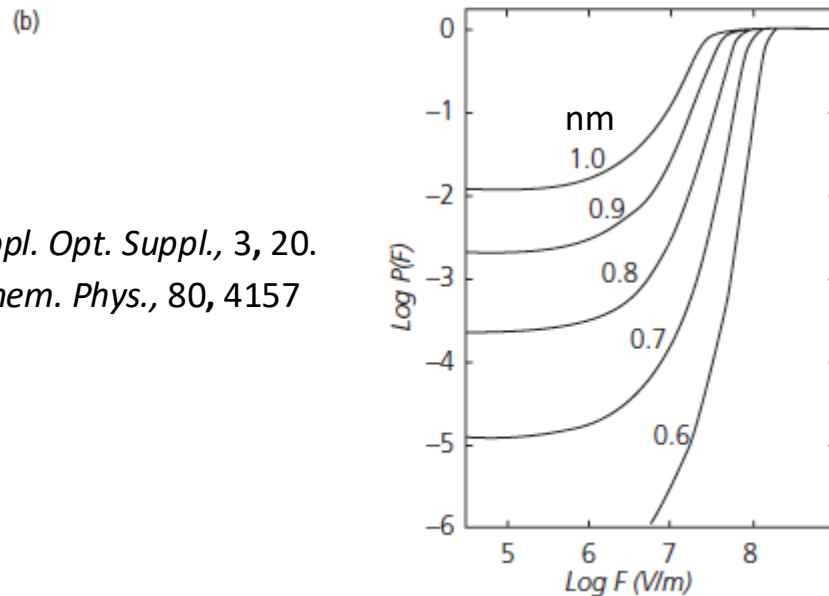
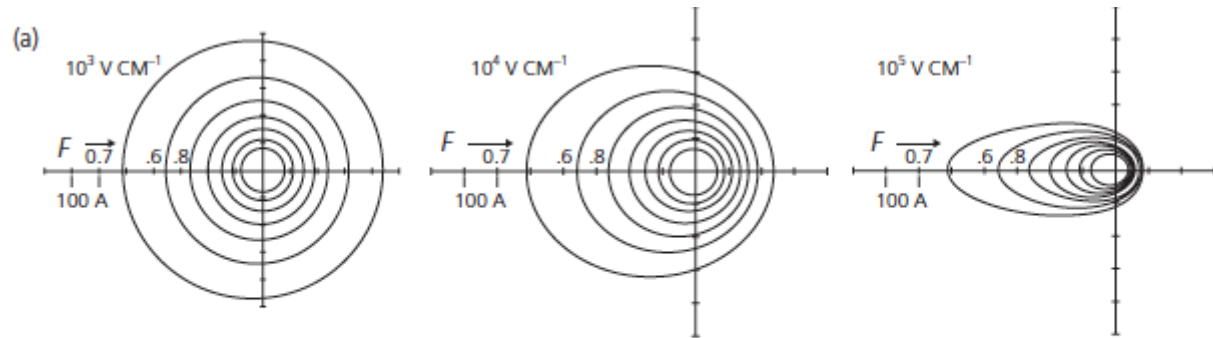
- PL shows two CT states: one for amorphous and the other for crystalline C<sub>70</sub> domains
- The shelf in the external efficiency is due to CT state dissociation

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# Onsager-Braun Exciton Polarization

- Why there is a voltage dependence to  $k_{ppd}$  that gives  $j$ - $V$  slope under reverse bias

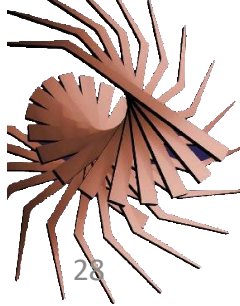


R. Batt, et al. 1969. *Appl. Opt. Suppl.*, 3, 20.

C. L. Braun. 1984. *J. Chem. Phys.*, 80, 4157

Probability for exciton ionization

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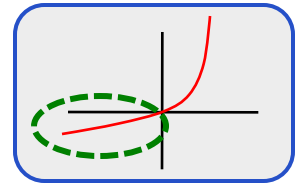


# Consequences of the diode equation

$$J_0 \left\{ \exp(qV_a / k_B T) - \frac{k_{PPd}}{k_{PPd,eq}} \right\} - J_{ph}$$

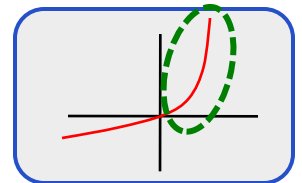
## Reverse Bias:

- strong dissociation:  $k_{PPd} > k_{PPd,eq}$  → saturation current increases →



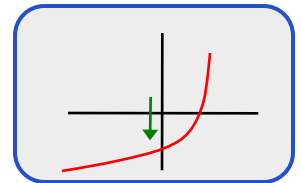
## Forward Bias:

- weak dissociation:  $k_{PPd} < k_{PPd,eq}$  → exponential diode current →



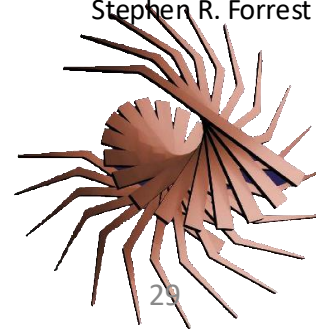
## Illumination:

- photogenerated PPs:  $J_X, \eta_{PPd} > 0$  → photocurrent addition →



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N. C. Giebink, et al. Phys. Rev. B, **82**, 155305 & 155306 (2010).



# Including traps

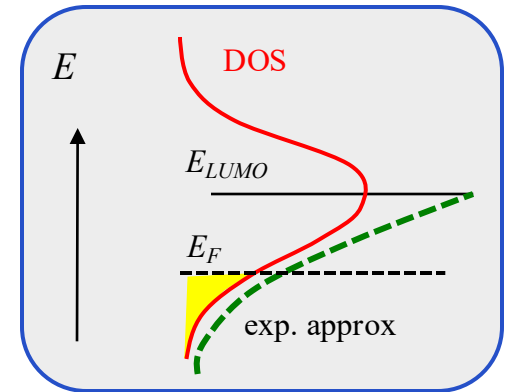
Disordered materials:

- broad density of states (DOS)  $\Rightarrow$  continuous trap distribution:

## Trap Distribution Function

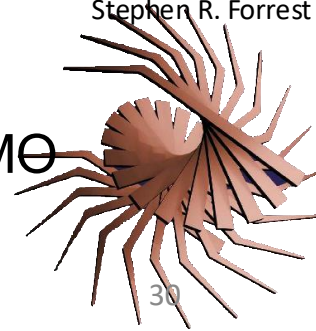
$$n_t = H_A \exp\left(\frac{E_{Fn} - E_{LUMO}}{k_B T}\right) = H_A \left(\frac{n}{N_{LUMO}}\right)^{1/m_A}$$

$$\text{where } m_A = T_{t,A}/T \quad \Rightarrow \quad n_A = \frac{m_A}{\delta_D(m_A - 1) + 1}$$



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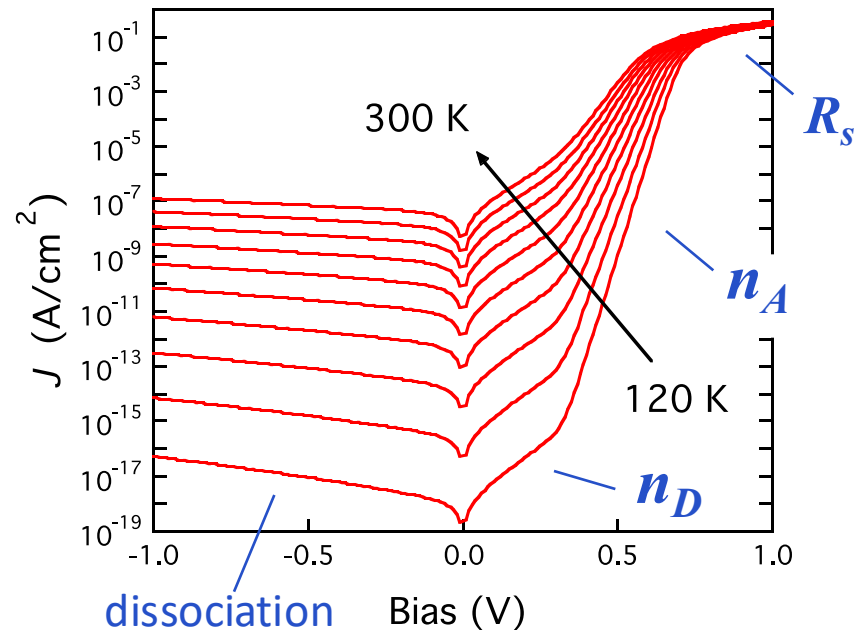
- Ideality factors:  $n_D$ ,  $n_A$  depend on *shape* of trap DOS
  - e.g.  $n=2$  for uniform distribution between HOMO and LUMO



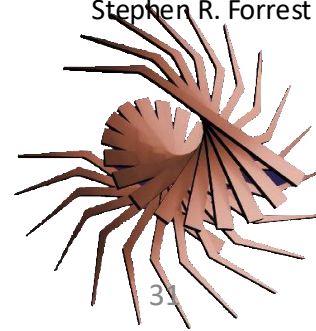
# Dark Current With Traps

- General form including series resistance:

$$J = J_{sD} \left[ \exp \left( \frac{q(V_a - JR_s)}{n_D k_b T} \right) - \frac{k_{PPd}}{k_{PPd,eq}} \right] + J_{sA} \left[ \exp \left( \frac{q(V_a - JR_s)}{n_A k_b T} \right) - \frac{k_{PPd}}{k_{PPd,eq}} \right] - q\eta_{PPd} J_X$$



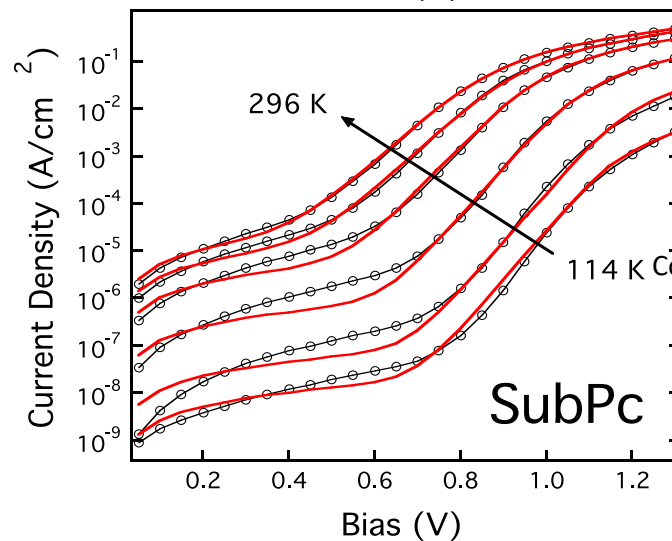
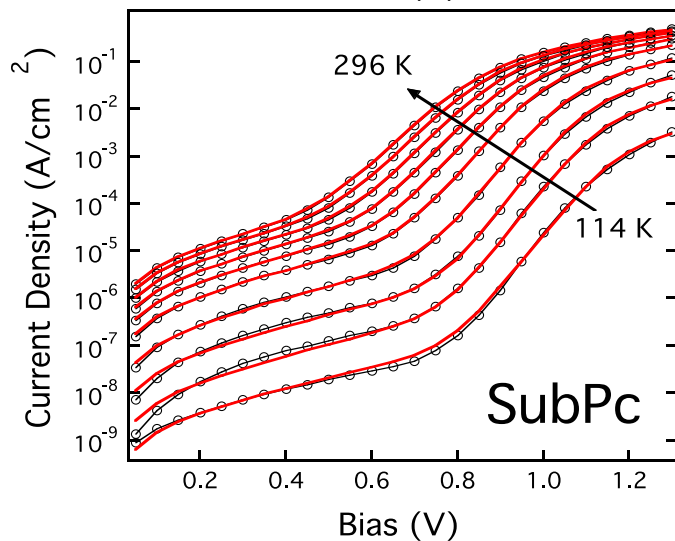
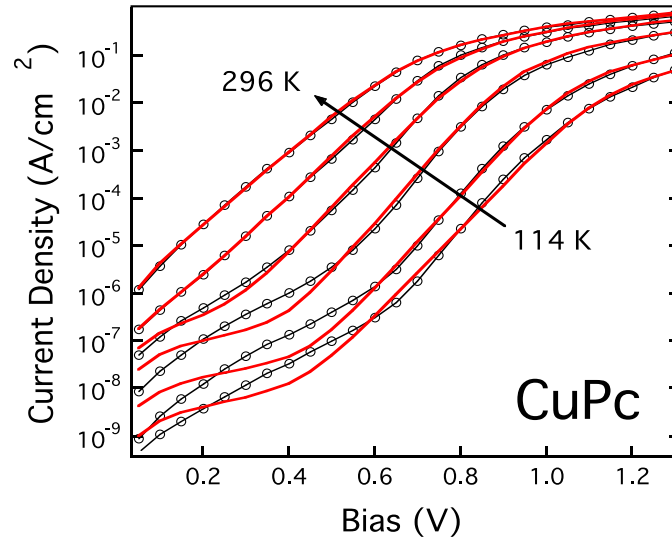
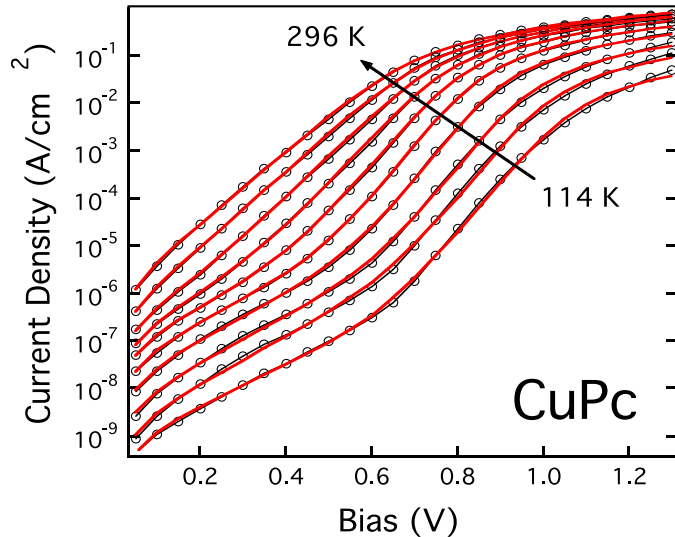
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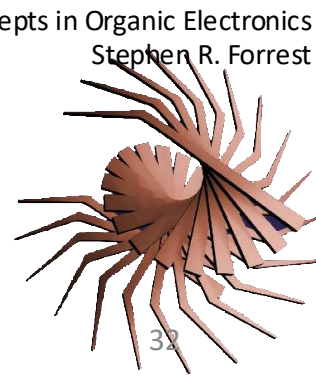
# $J$ - $V$ Fits to Diode Eq. with Traps

Org. HJ with Traps

Shockley Eq.

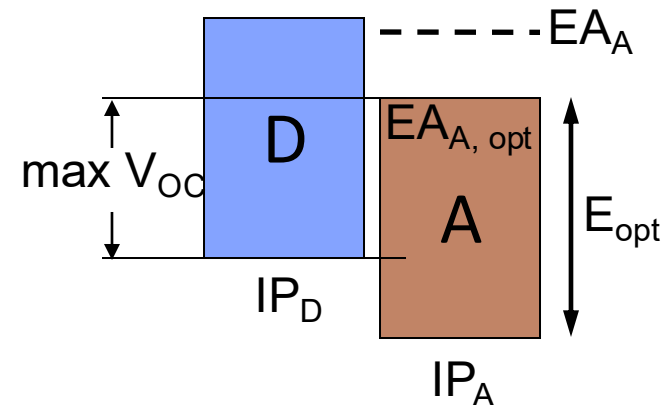
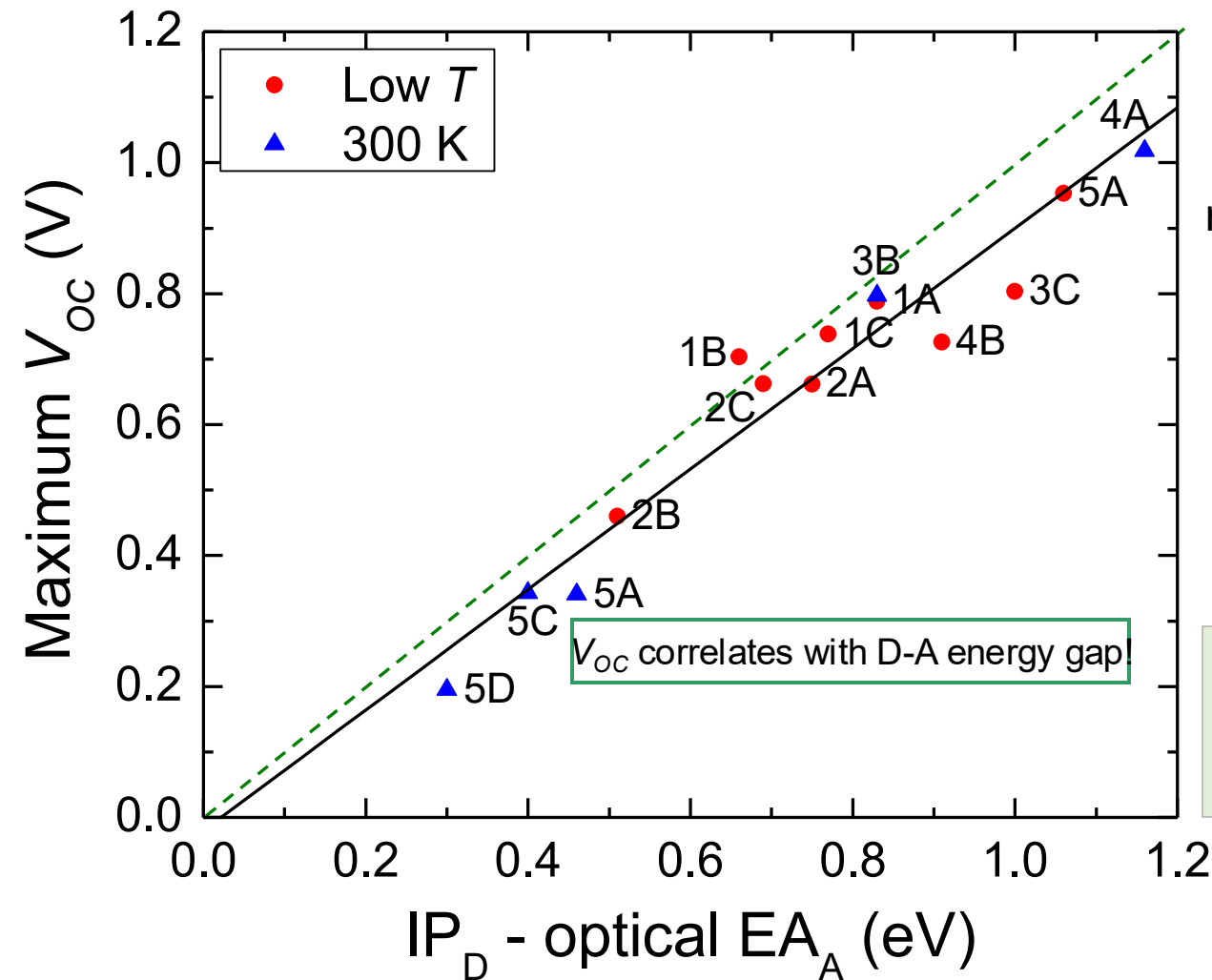


Acceptor  
 $\text{C}_{60}$





# Dependence of $V_{oc}$ on HJ Energies for Many Different D-A Combinations



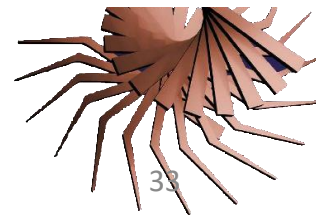
A single rule fits all materials

$$qV_{oc}^{max} = IP_D - EA_A - \frac{q^2}{4\pi\epsilon_0\epsilon_r r_{DA}}$$

$E_{HL}$        $-E_B$

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PP Binding Energy



# What the theory tells us

## Open Circuit Voltage

$$qV_{oc} = (\Delta E_{HL} - E_B) - k_b T \ln \left[ \frac{k_{PPr} N_{HOMO} N_{LUMO}}{\zeta_{\max} J_X / a_0} \right]$$

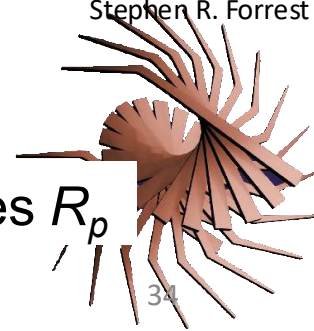
- At maximum sustainable power  $J_x \sim a_0 N_{HOMO} k_{PPr}$ 
  - More excitons cannot be supported.

Also:  $\zeta_{\max} \sim N_{HOMO} \sim N_{LUMO}$

Thus:  $qV_{oc} = \Delta E_{HL} - E_B \rightarrow$  *as observed!*  
( $E_B$ =polaron energy)

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- Slope under reverse bias due to PP recombination – eliminates  $R_p$



# Electronic Transport in Organics

## -What we learned

- Origins of electronic band structure
- Concept of polarons (large and small)
- Charge transfer
- Conductivity, effective mass and mobility
- Doping
- Effects of trapped charge
- Schottky Barrier Diodes
- Organic Heterojunctions

