

1.

a.

$\leq (2n^2 + 4n^2)/4n = 1.5n, n_0 = 1, c=1.5, O(n)$

$\geq 2n^2/4n = 1/2n, n_0 = 1, c=1/2, O(n)$

b.

$\leq n^2 + 5n^2, n_0=1, c=6, O(n^2)$

$\geq 5n^2, n_0=1, c=5, O(n^2)$

c.

$\leq n \lg n, n_0=1, c=1, O(n \lg n)$

$\geq$  \*\*\*This was only meant to be a Big-O question\*\*\*.

2.

The outer loop will run in  $O(\lg n)$ , the inner loop will never run.

3.

Quicksort, merge sort, heapify, binary search

4.

```
if( !root ) return false;
if( root->empID == key ) { name = root->name; salary = root->salary; return true; }
if( root->empID > key ) return findEmployee( root->left, key, name, salary );
else return findEmployee( root->right, key, name, salary );
```

5.

```
if(!root) return NULL;
```

```
// Just the root and no children:
```

```
if(!last_parent)
```

```
{
```

```
    delete root;
```

```
    return NULL;
```

```
}
```

```
if( last_parent->right )
```

```
{
```

```
    root->key = last_parent->right->key;
```

```
    delete (last_parent->right);
```

```
    last_parent->right = NULL;
```

```
} else {
```

```
    root->key = last_parent->left->key;
```

```
    delete (last_parent->left);
```

```
    last_parent->left = NULL;
```

```

}
reheapDown(root);
return root;
}

```

There could be some variation here depending on reheapDown... if I were to give a question like this I would provide the implementation in the appendix, or at least a function signature so you'd know the specifics of the implementation works.

6.

$$15 \% 13 = 2$$

$$17 \% 13 = 4$$

$$30 \% 13 = 4 \implies 4 + (9 - (30 \% 7)) = 4 + (9 - 2) = 11$$

$$4 \% 13 = 4 \implies 4 + (9 - (4 \% 7)) = 4 + 5 = 9$$

$$54 \% 13 = 2 \implies 2 + (9 - (54 \% 7)) = 2 + 4 = 6$$

$$6 \% 13 = 6 \implies 6 + (9 - (6 \% 7)) = 6 + 3 = 9 \implies 6 + 2(9 - (6 \% 7)) = 12$$

7.

**\*\*Note that i is set to 1 to start, so BC is when i=1!**

I(m):  $\text{exp} = x^i$

I(1):  $\text{exp} = x^1 = x$  by LI, and  $\text{exp} = x$  by program code

I(k): Assume true for  $0 \leq k \leq m$

I(k+1):

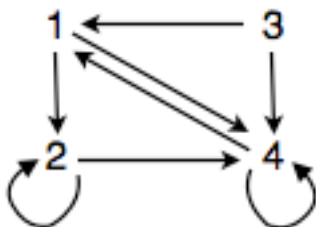
$$\begin{aligned}
 \text{exp\_new} &= \text{exp\_old} * x \\
 &= x^k * x \\
 &= x^{(k+1)} \text{ (which matches what is predicted by LI)}
 \end{aligned}$$

8.

a. A, B, F, D, C, E

b. F, D, A, E, C, B

9.



10.

$$C(13,1) * C(4,3) * C(12,1) * C(4,2)$$

11.

a.  $n/2+1$

b.  $n$

c.  $26^2+1$

12. -8, -5, 0, 2, 6, 1, 3, 4, 17 (but drawn as nearly-complete tree)

-5, 2, 0, 4, 6, 1, 3, 17, -8

0, 2, 1, 4, 6, 17, 3, -5, -8

1, 2, 3, 4, 6, 17, 0, -5, -8

2, 4, 3, 17, 6, 1, 0, -5, -8

3, 4, 6, 17, 2, 1, 0, -5, -8

4, 17, 6, 3, 2, 1, 0, -5, -8

6, 17, 4, 3, 2, 1, 0, -5, -8

17, 6, 4, 3, 2, 1, 0, -5, -8

13.

Express as nearly complete tree:

+, -, +, 2, \*, 4, /, empty, empty, 3, 4, empty, empty, 8, 2

14.

m

15.

$$m(m-1)$$

16.

| 13 | \_ |

| 7 | \_ |    | 16 | 21 |

| 1 | 2 |    | 8 | \_ |    | 14 | \_ |    | 17 | \_ |    | 22 | \_ |

17.

bar(0)

foo(1)

bar(2)

```
foo(3)  
main
```

```
foo== isEven  
bar== isOdd
```