

1. B
2. E (in terms of general complexity class) or G (empirically)
3. A
4. A
5. A
- 6a. reals
- b. reals
- c. positive, non-zero reals
- d. cannot map to negatives, therefore not onto;  $x = 2$  and  $x = -2$  map to the same value, therefore not one-to-one (thus neither)

9.

```
void merge( int a[], int n1, int b[], int n2, int c[], int n3) {
```

```
    int j,k = 0;
    for( int i=0; i<n3; i++ ) {
        if( j<n1 && k<n2 ) {
            if( a[j] < b[k] ) {
                c[i] = a[j];
                j++;
            } else {
                c[i] = b[k];
                k++;
            }
        }
        else if( j>n1 && k<n2 ) { c[i] = b[k]; k++; }
        else if( j<n1 && k>n2 ) { c[i] = a[j]; k++; }
    }
}
```

10.

$I(n) : s = i(i+1)/2, n=i$

BC:  $i = 0$

$s = 0$  by code

$s = 0$  by LI

IH: assume for some iteration  $k$

IS:  $s_{\text{new}} = s_{\text{old}} + (k+1)$

$s_{\text{new}} = k(k+1)/2 + (k+1)$  (by IH)

$s_{\text{new}} = (k^2 + k)/2 + (k+1)$

$s_{\text{new}} = (k^2 + k)/2 + 2(k+1)/2$

$s_{\text{new}} = (k^2 + 3k + 2)/2$

$$s_{\text{new}} = (k+1)(k+2)/2$$

$s_{\text{new}} = (k+1)(k+1+1)/2$  as predicted by the LI

11.

		7	8	2	-3	<b>10</b>		12	21	15	11
		2	-3	<b>7</b>	8			11	<b>12</b>	21	15
-3	<b>2</b>				<b>8</b>			<b>11</b>		15	<b>21</b>
<b>-3</b>										<b>15</b>	

2.

```

      8
     / \
    10  2
   / \ / \
  4  9 6 12
 / \
1  10

```

```

      8
     / \
    10  2
   / \ / \
  1  9 6 12
 / \
4  10

```

```

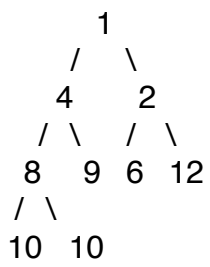
      8
     / \
    10  2
   / \ / \
  4  9 6 12
 / \
1  10

```

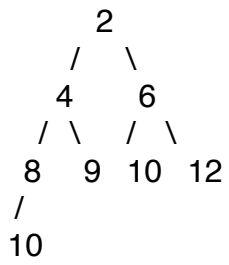
```

      8
     / \
    1  2
   / \ / \
  4  9 6 12
 / \
10 10

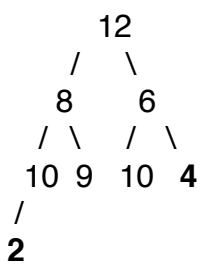
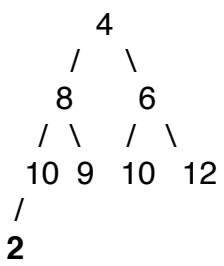
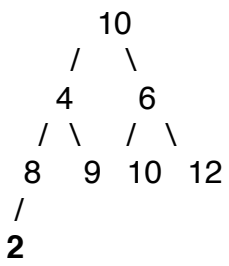
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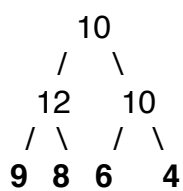
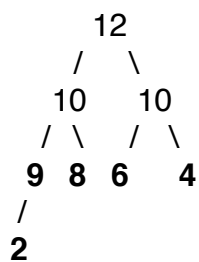
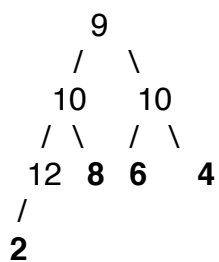
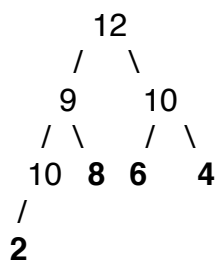
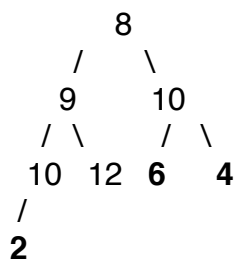
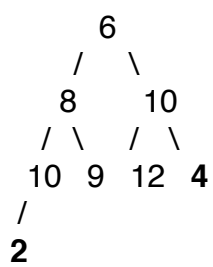


b.

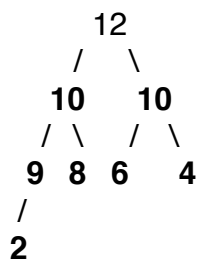
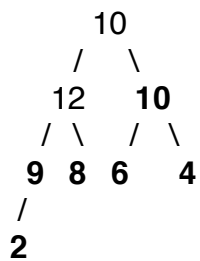


c.

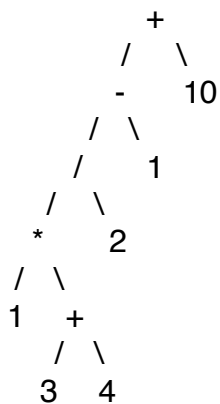




/  
2



4.



b. 1 3 4 + \* 2 / 1 - 10 +

5.

- 3/4 Building a heap (heapify)
- 2 Searching a BST in the worst case.
- 1 Searching a binary tree in the best case.
- 3/4 Searching a heap in the worst case.
- 5 Heapsort

6. Not relevant for this class.

7.

```
if( !root ) return false  
if( root->item == item ) return true;  
if( root->item > item ) return false;  
if( !heapSearch( root->left, item ) return heapSearch( root->right, item );
```