

What if P has rules?

The program (P):

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father(fred,pebbles).
father(bamm-bamm,roxy).
father(barney,bamm-bamm).
father(bamm-bamm,chip).
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mother(wilma,pebbles).
mother(betty,bamm-bamm).
grandmother(X,Y) :-
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```

?-

resolvent =

Initialize resolvent to goal G (the query)
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OOPS! Time to modify things a bit.

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resolvent = **grandmother(betty,roxy)**

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