```
T_1 = \operatorname{append}([a,b],[c,d],\operatorname{Ls}) T_2 = \operatorname{append}([X|Xs],Ys,[X|Zs]) \operatorname{failure} = \operatorname{false} \Theta = \{\}
```

```
Input: Two terms T_1 and T_2 to be unified
```

Output: Θ , the mgu of T_1 and T_2 , or failure

Algorithm: Initialize the substitution Θ to be empty, the stack to contain the equation $T_1 = T_2$, and failure to *false*.

And then...

```
append([a,b],[c,d],Ls) =
append([X|Xs],Ys,[X|Zs])
```

```
T_1 = append([a,b],[c,d],Ls)

T_2 = append([X|Xs],Ys,[X|Zs])

failure = false

\Theta = {}
```

append([a,b],[c,d],Ls) =
append([X|Xs],Ys,[X|Zs])

while stack not empty and no failure do

pop X = Y from the stack

case

X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ

Y is a variable that does not occur in X: substitute X for Y in the stack and in Θ add Y = X to Θ

X and Y are identical constants or variables: continue

X is $f(X_1,...,X_n)$ and Y is $f(Y_1,...,Y_n)$ for some functor f and n > 0: push $X_i = Y_i$, i = 1...n, on the stack

otherwise: failure is *true*

```
T_1 = \operatorname{append}([a,b],[c,d],Ls)
T_2 = \operatorname{append}([X|Xs],Ys,[X|Zs])
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X is f(X_1,...,X_n) and Y is f(Y_1,...,Y_n)
for some functor f and n > 0:
push X_i = Y_i, i = 1...n, on the stack
```

otherwise: failure is *true*

append([a,b],[c,d],Ls) =
append([X|Xs],Ys,[X|Zs])

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T_1 = append([a,b],[c,d],Ls)

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while stack not empty and no failure do
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```

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append([a,b],[c,d],Ls) = append([X|Xs],Ys,[X|Zs])
```

```
[a,b] = [X|Xs]

[c,d] = Ys

Ls = [X|Zs]
```

while stack not empty and no failure do

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T_1 = append([a,b],[c,d],Ls)

T_2 = append([X|Xs],Ys,[X|Zs])

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```

$$[a,b] = [X|Xs]$$

 $[c,d] = Ys$
 $Ls = [X|Zs]$

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T_1 = append([a,b],[c,d],Ls)

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[a,b] = [X|Xs] [c,d] = YsLs = [X|Zs] while stack not empty and no failure do

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\Theta = \{\}
```

[c,d] = YsLs = [X|Zs]

[a,b] = [X|Xs]

while stack not empty and no failure do

pop X = Y from the stack

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X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ

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T_2 = append([X|Xs],Ys,[X|Zs])

failure = false

\Theta = {}
```

```
[c,d] = Ys
Ls = [X|Zs]
```

while stack not empty and no failure do

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```

otherwise: failure is *true*

Excuse me?

```
We have this: [a,b] = [X|Xs]
and this: X is f(X_1,...,X_n) and Y is f(Y_1,...,Y_n)
for some functor f and n > 0:
push X_i = Y_i, i = 1...n, on the stack
```

where exactly is the functor in [a,b] = [X|Xs] ???

Excuse me?

```
We have this: [a,b] = [X|Xs]
and this: X is f(X_1,...,X_n) and Y is f(Y_1,...,Y_n)
for some functor f and n > 0:
push X_i = Y_i, i = 1...n, on the stack
```

where exactly is the functor in [a,b] = [X|Xs] ???

It's right there. You just can't see it. It's the dot functor or dot operator, or just the dot. It's how cons pairs are formally represented.

Equivalent forms of lists

```
Cons pair syntax Element syntax
                                       Functor or dot syntax
           [a | [ ]]
               [a]
                           .(a ,[])
[a | [b | [ ]]] [a, b]
                               .(a, .(b, []))
               [a, b, c]
[a | [b | [c | [ ]]]]
                                   .(a, .(b, .(c, [])))
[a | X]
                               .(a, X)
               [a | X]
[a | [b | X]]
           [a, b | X]
                              .(a, .(b, X))
```

```
T_1 = \operatorname{append}([a,b],[c,d],Ls)
T_2 = \operatorname{append}([X|Xs],Ys,[X|Zs])
failure = false
\Theta = \{\}
[a,b] = [X|Xs]
```

```
[c,d] = Ys
Ls = [X|Zs]
```

while stack not empty and no failure do

pop X = Y from the stack

case

X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ

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otherwise: failure is *true*

```
T_1 = append([a,b],[c,d],Ls)

T_2 = append([X|Xs],Ys,[X|Zs])

failure = false

\Theta = {}
```

```
a = X
[b] = Xs
[c,d] = Ys
Ls = [X|Zs]
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while stack not empty and no failure do

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failure = false
\Theta = \{\}
```

```
a = X
[b] = Xs
[c,d] = Ys
Ls = [X|Zs]
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\Theta = {}
```

$$a = X$$

```
[b] = Xs
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\Theta = {}
```

```
[b] = Xs
[c,d] = Ys
Ls = [X|Zs]
```

a = X

while stack not empty and no failure do

```
pop X = Y from the stack
```

case

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failure = false

\Theta = {}
```

```
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Ls = [a|Zs]
```

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```
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T_2 = \operatorname{append}([X|Xs],Ys,[X|Zs])
failure = false
\Theta = \{X = a\}
```

```
[b] = Xs
[c,d] = Ys
Ls = [a|Zs]
```

a = X

while stack not empty and no failure do

pop X = Y from the stack

case

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otherwise: failure is *true*

```
T_1 = append([a,b],[c,d],Ls)

T_2 = append([X|Xs],Ys,[X|Zs])

failure = false

\Theta = \{X = a\}
```

```
[b] = Xs
[c,d] = Ys
Ls = [a|Zs]
```

while stack not empty and no failure do

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case

X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ

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T_2 = append([X|Xs],Ys,[X|Zs])

failure = false

\Theta = {X = a}
```

```
[b] = Xs
[c,d] = Ys
Ls = [a|Zs]
```

while stack not empty and no failure do

pop X = Y from the stack

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X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ

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```
T_1 = append([a,b],[c,d],Ls)
```

$$T_2 = \text{append}([X|Xs], Ys, [X|Zs])$$

failure = false

$$\Theta = \{X = a\}$$

$$[b] = Xs$$

[c,d] = YsLs = [a|Zs] while stack not empty and no failure do

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$$[b] = Xs$$

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[c,d] = Ys
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```
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Ls = [a|Zs]
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$$[c,d] = Ys$$

Ls = $[a|Zs]$

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$$Ls = [a|Zs]$$

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```

Ys = [c,d]

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Ys = [c,d]

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```
while stack not empty and no failure do
```

pop X = Y from the stack

case

- X is a variable that does not occur in Y: substitute Y for X in the stack and in Θ add X = Y to Θ
- Y is a variable that does not occur in X: substitute X for Y in the stack and in Θ add Y = X to Θ
- X and Y are identical constants or variables: continue
- X is $f(X_1,...,X_n)$ and Y is $f(Y_1,...,Y_n)$ for some functor f and n > 0: push $X_i = Y_i$, i = 1...n, on the stack

otherwise: failure is *true*

```
T_1 = \text{append}([a,b], [c,d], Ls)
T_2 = \text{append}([X|Xs], Ys, [X|Zs])
failure = false
\Theta = \{X = a, Xs = [b], Ys = [c,d], Ls = [a|Zs]\}
Ls = [a|Zs]
```

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$$f(X_1,...,X_n)$$
 and Y is $f(Y_1,...,Y_n)$
for some functor f and $n > 0$:
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T_2 = \operatorname{append}([a|\operatorname{Xs}],\operatorname{Ys},[a|\operatorname{Zs}])
\operatorname{failure} = \operatorname{\it false}
\Theta = \left\{ \begin{array}{l} X = a, Xs = [b], \\ Ys = [c,d],\operatorname{Ls} = [a|\operatorname{Zs}] \end{array} \right\}
```

```
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\Theta = \{X = a, Xs = [b], Ys = [c,d], Ls = [a|Zs]\}
```

Questions?