CPSC 340: Machine Learning and Data Mining

Ensemble Methods Fall 2016

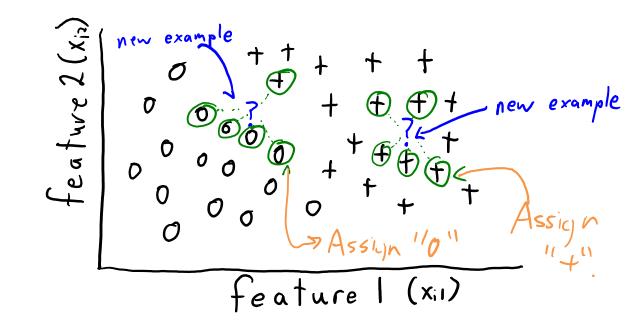
Admin

- Welcome to the course!
 - You should know if you are officially in/out.
- Assignment 1 is due Friday.
 - Setup your CS undergrad account ASAP to use Handin:
 - https://www.cs.ubc.ca/getacct
 - Instructions for handin posted to Piazza.
 - 1 late day to hand it in before Monday's class.
 - 2 late days to hand it in before Wednesday's class.
 - 3 late days to hand it in before Friday of next week's class.
 - 0 after that.

K-Nearest Neighbours (KNN)

- K-nearest neighbours algorithm for classifying 'x':
 - Find 'k' values of x_i that are most similar to x.
 - Use mode of corresponding y_i.

- Non-parametric:
 - Size of model grows with 'n'.



- Consistency:
 - Nearly-optimal test error with infinite data.
- But how many examples are needed?

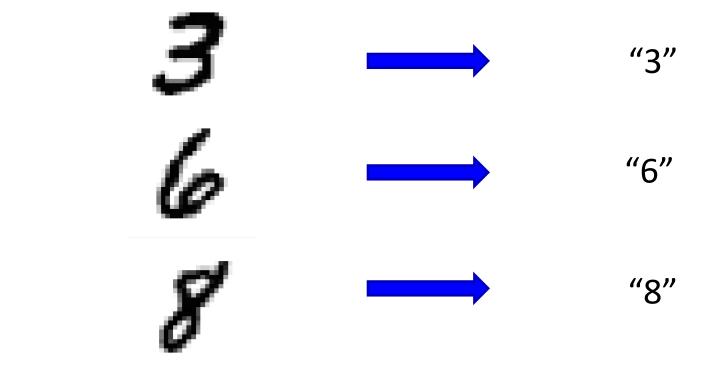
Curse of Dimensionality

- "Curse of dimensionality": problems with high-dimensional spaces.
 - Volume of space grows exponentially with dimension.
 - Need exponentially more points to 'fill' a high-dimensional volume.
 - Distances become less meaningful:
 - All vectors may have similar distances.
 - Emergence of "hubs":
 - some datapoints are neighbours to many more points than average.
- KNN is also problematic if features have different scales.

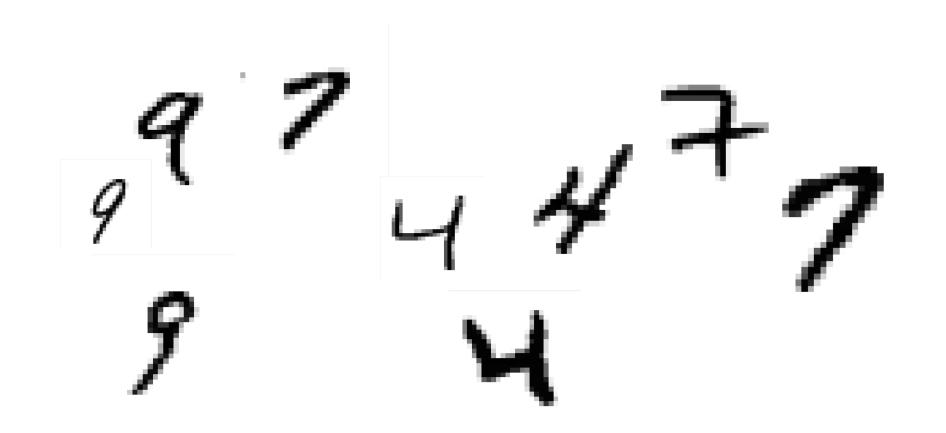
Nevertheless, KNN is really easy to use and often hard to beat!

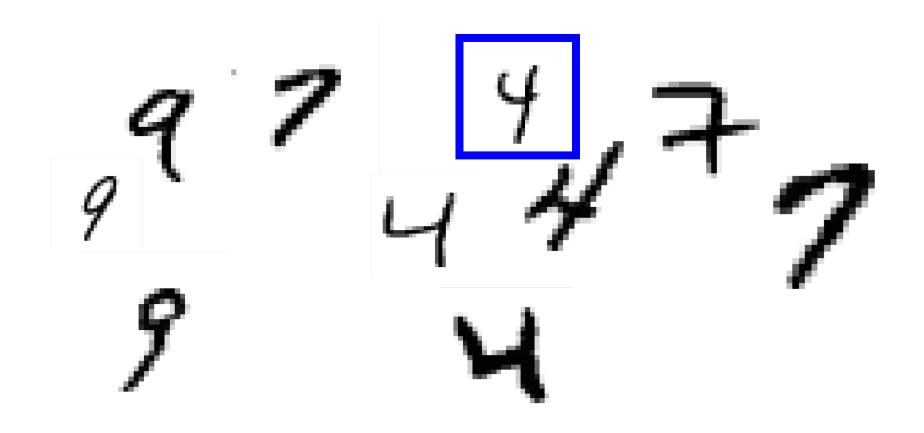
Application: Optical Character Recognition

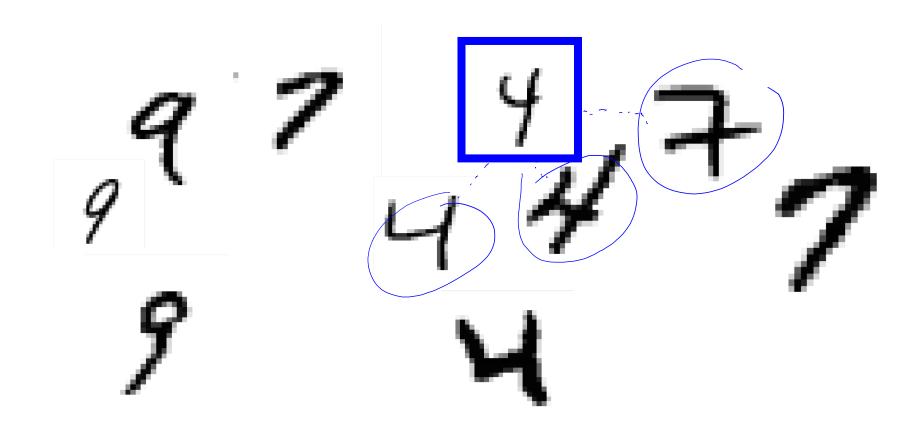
We have collection of letter/digit images, and corresponding labels:

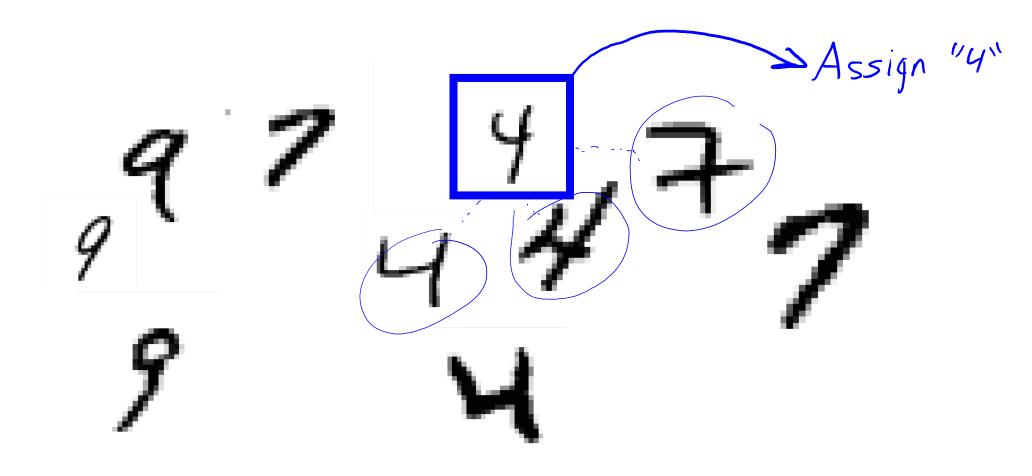


- Use supervised learning to automatically recognize letters/digits:
 - $-y_i$ could be the letter/digit, x_i could be the values of the pixels.









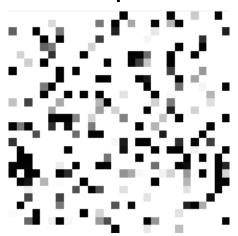
Human vs. Machine Perception

There is huge difference between what we see and what KNN sees:

What we see:



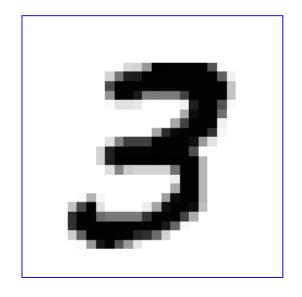
What the computer "sees":

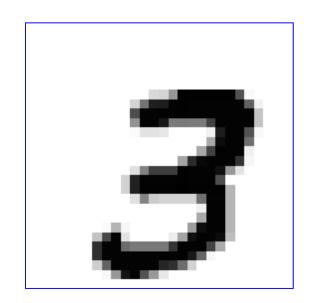


Actually, it's worse:

What the Computer Sees

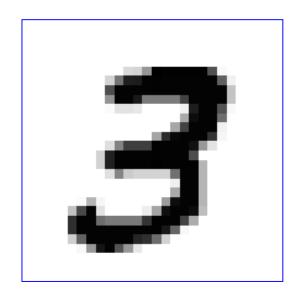
Are these two images 'similar'?

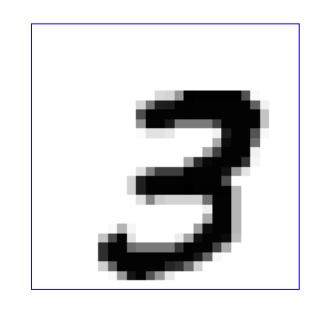




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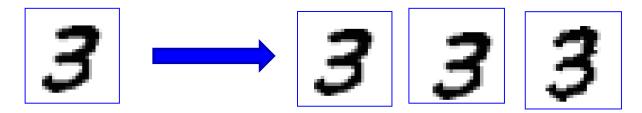




KNN does not know that labels should be translation invariant.

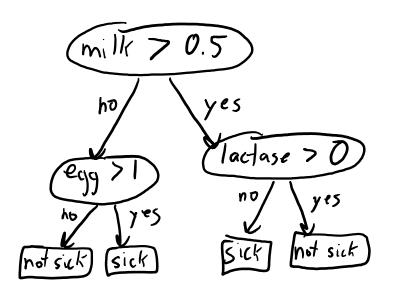
Encouraging Invariance

- May want classifier to be invariant to certain feature transforms.
 - Digits: translations, small rotations, changes in size, mild warping,...
- The hard/slow way is to modify your distance function:
 - Find neighbours that require the 'smallest' transformation of image.
- The easy/fast way is to just add transformed data during training:
 - Add translated/rotate/resized/warped versions of training images.



Crucial part of many successful vision systems.

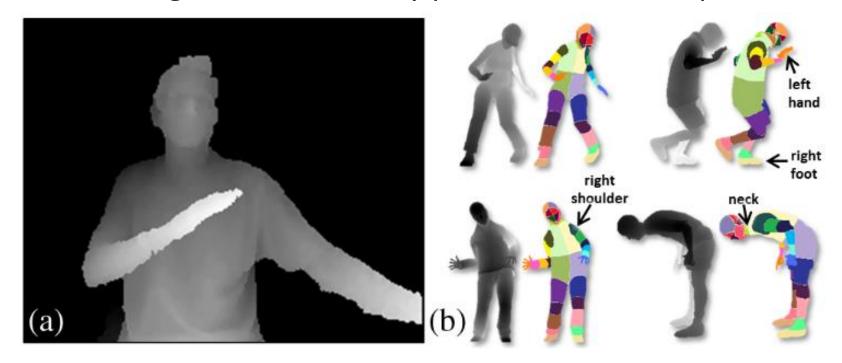
Decision Trees vs. Naïve Bayes vs. KNN



$$(milk = 0.6, egg = 2, lactase = 0, ?)$$
 is close to $(milk = 0.7, egg = 2, lactase = 0, sick)$ so predict sick.

Application: Body-Part Recognition

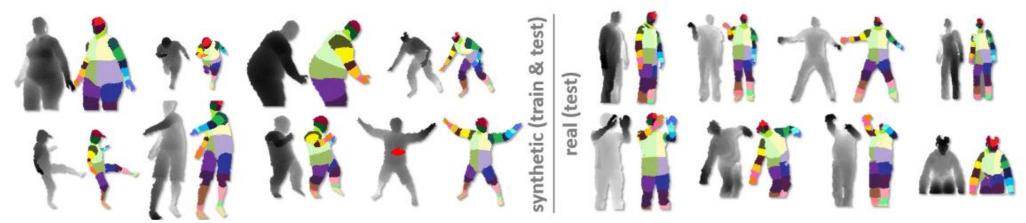
- Microsoft Kinect:
 - Real-time recognition of 31 body parts from laser depth data.



How could we write a program to do this?

Some Ingredients of Kinect

- 1. Collect hundreds of thousands of labeled images (motion capture).
 - Variety of pose, age, shape, clothing, and crop.
- 2. Build a simulator that fills space of images by making even more images.



- 3. Extract features of each location, that are cheap enough for real-time calculation (depth differences between pixel and pixels nearby.)
- 4. Treat classifying body part of a pixel as a supervised learning problem.
- 5. Run classifier in parallel on all pixels using graphical processing unit (GPU).

Supervised Learning Step

ALL steps are important, but we'll focus on the learning step.

- Do we have any classifiers that are accurate and run in real time?
 - Decision trees and naïve Bayes are fast, but often not very accurate.
 - KNN is often accurate, but not very fast.

Deployed system uses an ensemble method called random forests.

Ensemble Methods

- Ensemble methods are classifiers that have classifiers as input.
 - Also called "meta-learning".
- They have the best names:
 - Averaging.
 - Boosting.
 - Bootstrapping.
 - Bagging.
 - Cascading.
 - Random Forests.
 - Stacking.
- Meta-classifier often have higher accuracy than input classifiers.

Ensemble Methods

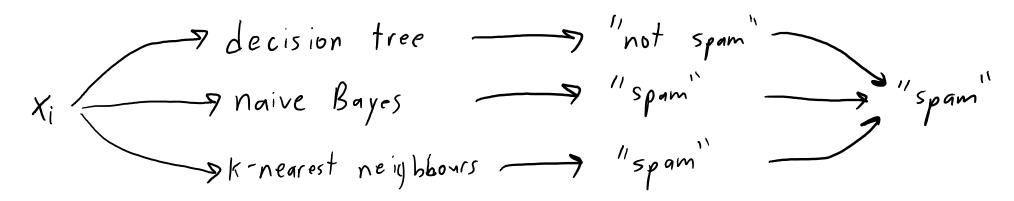
- Remember the fundamental trade-off:
 - 1. How small you can make the training error. vs.
 - 2. How well training error approximates the test error.
- Goal of ensemble methods is that meta-classifier:
 - Does much better on one of these than individual classifiers.
 - Doesn't do too much worse on the other.
- This (roughly) gives two types:
 - 1. Boosting: take simple classifier that underfits, improve its training error.
 - 2. Averaging: take complex classifier that overfits, improve its test error.

Boosting

- Input to boosting is classifier that:
 - Is simple enough that it doesn't overfit much.
 - Can obtain >50% weighted training accuracy.
- Example: decision stumps or low-depth decision trees.
- Basic steps:
 - 1. Fit a classifier on the training data.
 - 2. Give a higher weight to examples that the classifier got wrong.
 - 3. Fit a classifier on the weighted training data.
 - 4. Go back to 2.
- Final prediction: weighted vote of individual classifier predictions.
- Boosted decision trees are very fast/accurate classifiers.

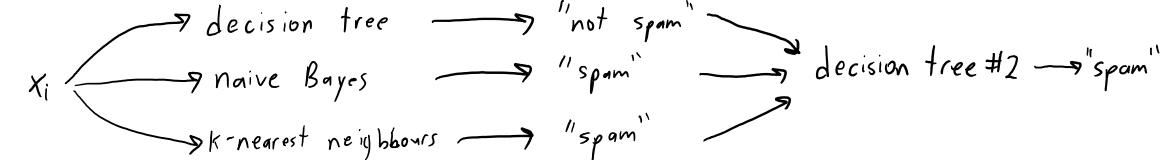
Averaging

- Input to averaging is the predictions of a set of models:
 - Decision trees make one prediction.
 - Naïve Bayes makes another prediction.
 - KNN makes another prediction.
- Simple model averaging:
 - Take the mode of the predictions (or average if probabilistic).



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- Stacking:
 - Fit another classifier that uses the predictions as features.



Averaging

- Averaging often performs better than individual models:
 - Averaging typically used by Kaggle winners.
 - E.g., Netflix \$1M user-rating competition winner was stacked classifier.
- Why does this work?
- Consider a set of classifiers that tend to overfit:
 - For example, deep decision trees.
- If they all overfit in exactly the same way, averaging does nothing.
- But if they make independent errors:
 - Probability of error of average can be lower than individual classifiers.
- Less attention on specific overfitting of each classifier.

Random Forests

- Random forests average a set of deep decision trees.
 - Tend to be one of the best 'out of the box' classifiers.
 - Often close to the best performance of any method on the first run.
 - And predictions are very fast.
- Do deep decision trees make independent errors?
 - If just fit a decision tree repeatedly to same data, all trees will be the same.
- Two key ingredients in random forests:
 - Bootstrap aggregation.
 - Random trees.

Random Forest Ingredient 1: Bagging

- Bootstrap sample of a list of 'n' objects:
 - A set of 'n' objects, chosen independently with replacement.

for
$$i=1:n$$
 $j=ceil(rand*n)$ % Pick a rondom number from $i:n$.

 $X_{boolstrop}(i,:)=X(j,:)$

- Gives new dataset of 'n' objects, with some duplicated and some missing.
 - ~63% of original objects will be included.
- Usually, it is used to estimate how sensitive a statistic is to the data.
- Bootstrap aggregation (bagging):
 - Generate several bootstrap samples of the objects (x_i, y_i) .
 - Fit a classifier to each bootstrap sample.
 - At test time, average the predictions.

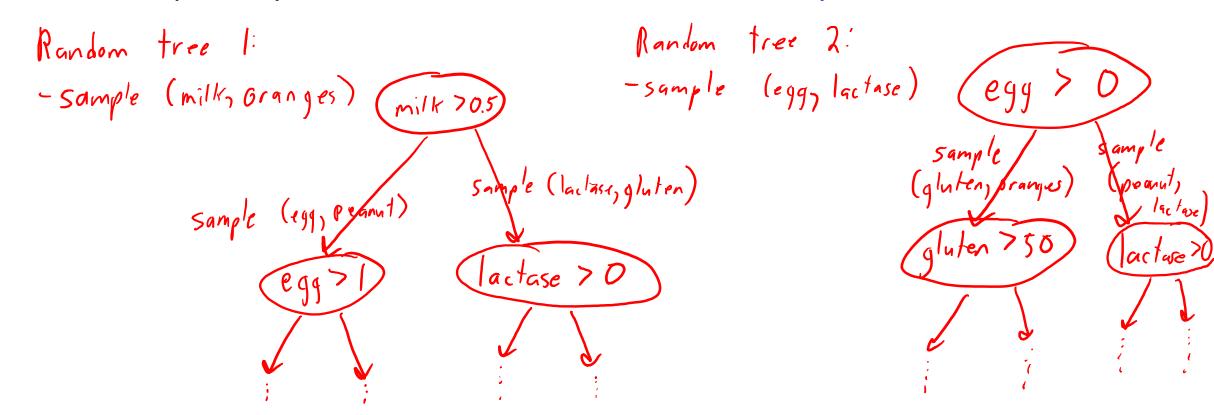
Decision trees will make S different splits.

Random Forest Ingredient 2: Random Trees

- When fitting each decision stump to construct deep decision tree:
 - Do not consider all features when searching for the optimal rule.
 - Each split only considers a small number of randomly-chosen features.

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 - Each split only considers a small number of randomly-chosen features.
- These random trees will tend to be very different from each other.
 - They will still overfit, but in *different* ways.
- The average tends to have a much lower test error.
- Empirically, random forests are one of the "best" classifiers.
- Fernandez-Delgado et al. [2014]:
 - Compared 179 classifiers on 121 datasets.
 - Random forests are most likely to be the best classifier.

Summary

1. Encouraging invariance:

- Add transformed data to be insensitive to the transformation.
- 2. Ensemble methods take classifiers as inputs.
- 3. Boosting turns 'weak' classifiers into 'strong' classifiers.
- 4. Averaging predictions often improves performance.
- 5. Random forests:
 - Averaging of deep randomized decision trees.
 - One of the best "out of the box" classifiers.

Next time:

We start unsupervised learning.

Bonus Slide: Why does Bootstrapping give 63%?

• Probability of an arbitrary x_i being selected in a bootstrap sample:

p(selected at least once in 'n' trials)

$$= |-p(not \ selected \ in \ any \ of \ 'n' \ trials)$$

$$= |-(p(not \ selected \ in \ one \ trial))^n \qquad (trials \ are \ independent)$$

$$= |-(1 - 1/n)^n \qquad (prob = \frac{n-1}{n} \ for \ choosing \ any \ of \ the \ n-1 \ other \ sumples$$

$$\approx |-1/e| \qquad (1-1/n)^n \rightarrow e^{-1} \ as \ n\rightarrow \infty)$$

Bonus Slide: Why Random Forests Work

- Consider 'k' independent classifiers, whose errors have a variance of σ^2 .
- If the errors are IID, the variance of the average is σ^2/k .
 - So the more classifiers you average, the more you decrease error variance.
 (And the more the training error approximates the test error.)
- Generalization to case where classifiers are not independent is:

$$co^2 + \underbrace{(1-c)o^2}_{k}$$

- Where 'c' is the correlation.
- So the decreasing correlation gets you closer to independent case.
- Randomization in random forests decreases correlation between trees.