

Discovery of Novel Superconducting Materials with Deep Learning

Colin Burdine

E. P. Blair

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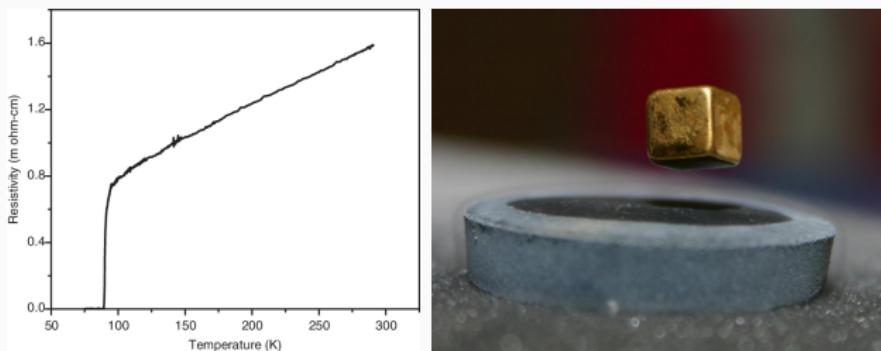


Background

Superconductors

- Superconductors are materials that exhibit two key properties at low temperatures:
 1. The resistivity ρ drops to 0Ω (Current flows without resistance).
 2. Magnetic fields are expelled in the bulk. (Meissner Effect)

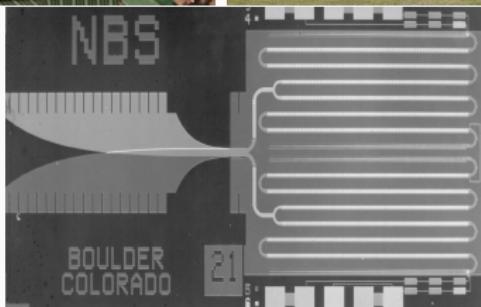
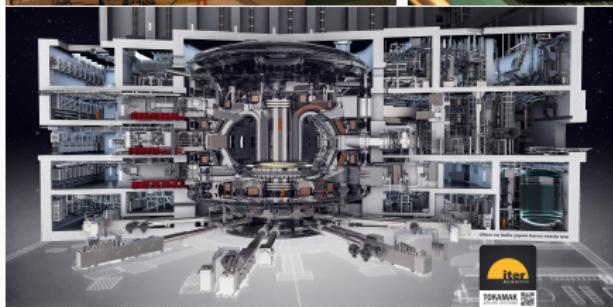
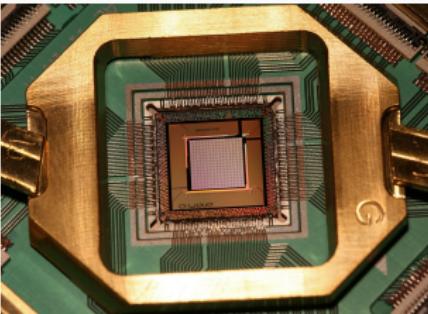
Example: $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ [VBR14]



- A superconductor's **critical temperature (T_c)** is the highest temperature at which it exhibits these two properties.

Superconductors

Industrial Applications of Superconductors



<https://www.flickr.com/photos/14646075@N03/2833410223>

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Superconductors

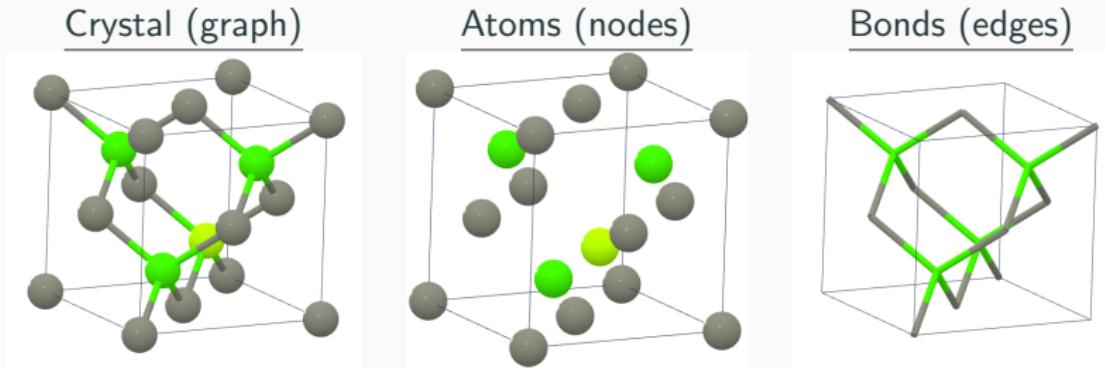
- Superconductivity occurs due to anomalous quantum mechanical pairing of electrons [Coo60].
- Pairing allows for condensation of conducting electrons into a single energy state at the Fermi level, E_F :

$$\begin{array}{ccc} \underbrace{|\uparrow\rangle, |\downarrow\rangle}_{\text{Spin-1/2 electrons}} & \longrightarrow & \underbrace{\frac{(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)}{\sqrt{2}}}_{\text{Spin-0 Singlet Cooper pair}} \\[10pt] \underbrace{|\uparrow\rangle, |\uparrow\rangle}_{\text{Spin-1/2 electrons}} & \longrightarrow & \underbrace{|\downarrow\downarrow\rangle, \frac{(|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle)}{\sqrt{2}}, |\uparrow\uparrow\rangle}_{\text{Spin-1 Triplet Cooper pairs}} \quad [m = -1, 0, +1] \end{array}$$

- Pairing in **conventional** (i.e. BCS) superconductors is mediated by phonons [BCS57].
- Pairing in **unconventional superconductors** has not yet been fully explained [ZLI⁺21].

Alternative Methods for Predicting T_c

- There has been great interest in applying machine learning to superconductor discovery (e.g. see: [SOK⁺18][KKN⁺21][XQH⁺22])
- Very few of these approaches directly incorporate atomic structure (e.g. [CG22]).
- Crystalline structures are naturally interpreted as periodic graphs:



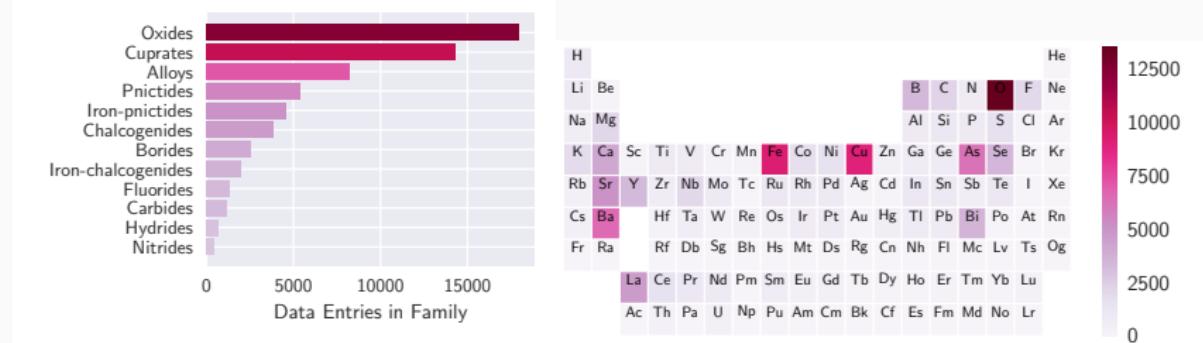
- In this work, we applied graph neural networks to identify superconductors and predict T_c from raw crystalline structure.

Methods

Data Sources

- We combined two large experimental measurement datasets (*Supercon v1* [SOK⁺18] and *Supercon v2* [FdCS⁺23]).

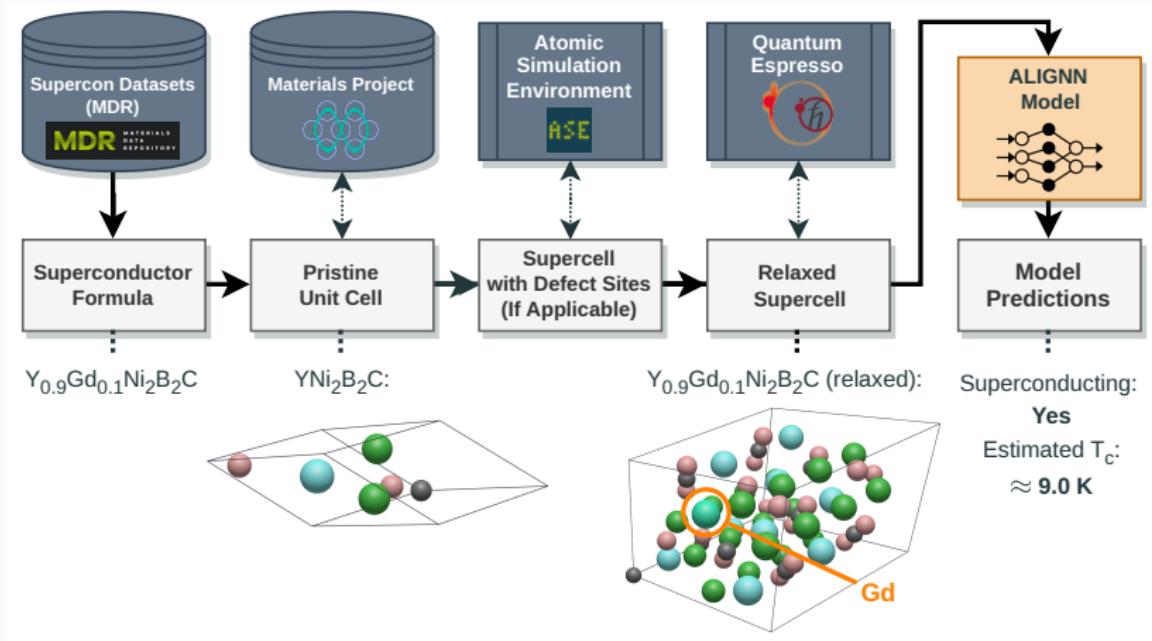
Dataset Distribution



- These datasets had T_c measurements, chemical formulas, and other important metadata, but no atomic structure.

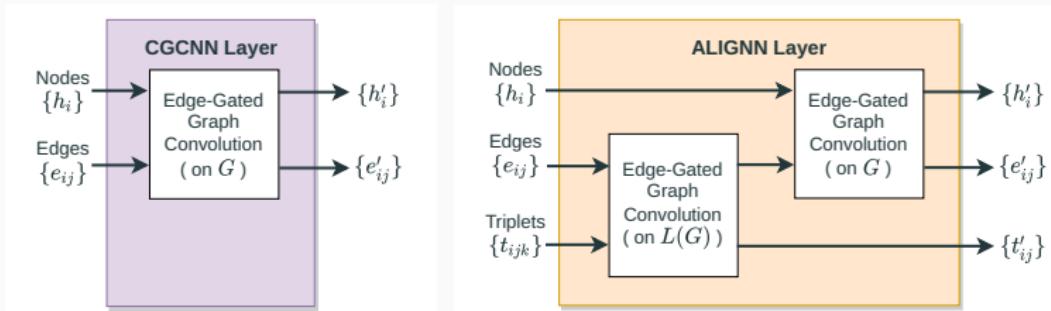
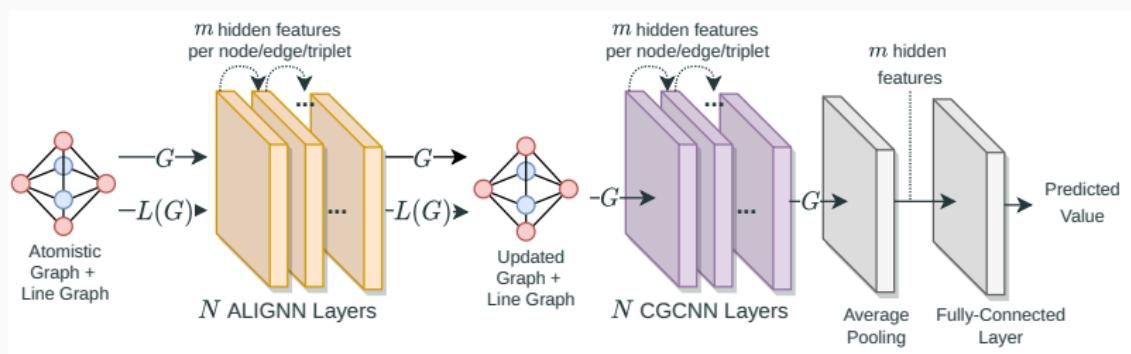
Generating Atomic Structures

Data Generation Pipeline



ALIGNN Model

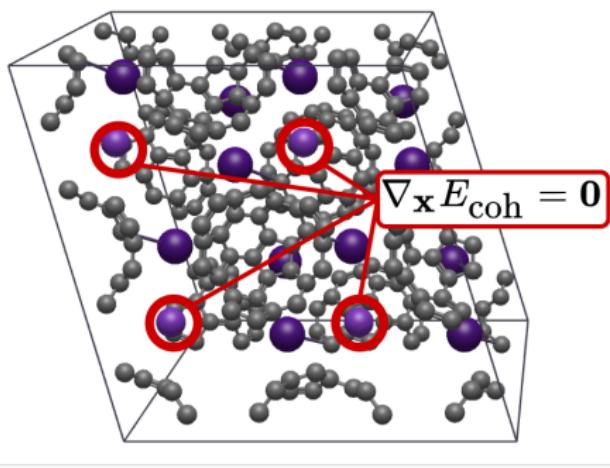
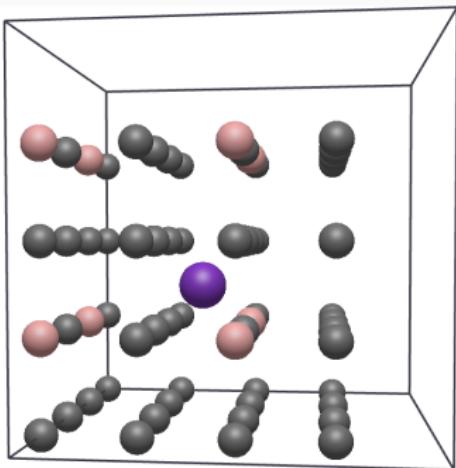
ALIGNN Model Architecture [XG18][CD21]



Data Sources

- A significant challenge was handling the placement of defects (vacancies, interstitials, etc. via the *Embedded Atom Method* [?])

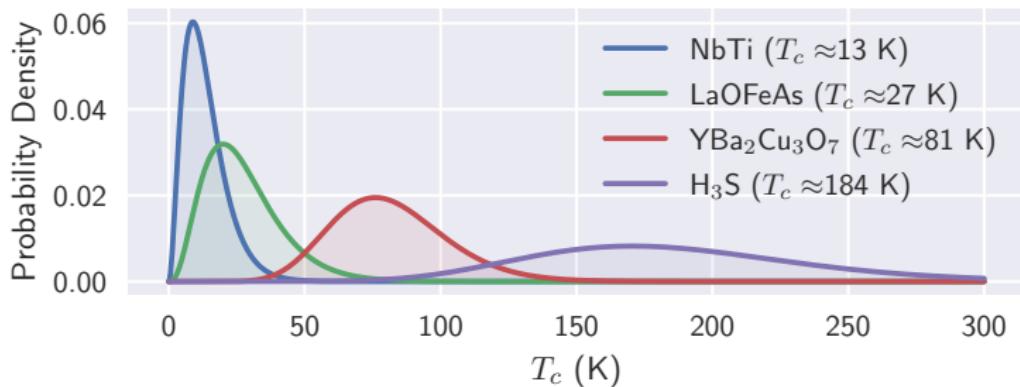
Defect Placement Examples: Fake Lattice (left), KCs₃C₆₀ (right).



Experimental T_c Data

- For each superconducting material, many differing measurements were reported due to various factors (applied pressure, choice of substrate, film thickness, etc.)
- We constructed “empirical” distributions of reported T_c values, and had the model predict these distributions:

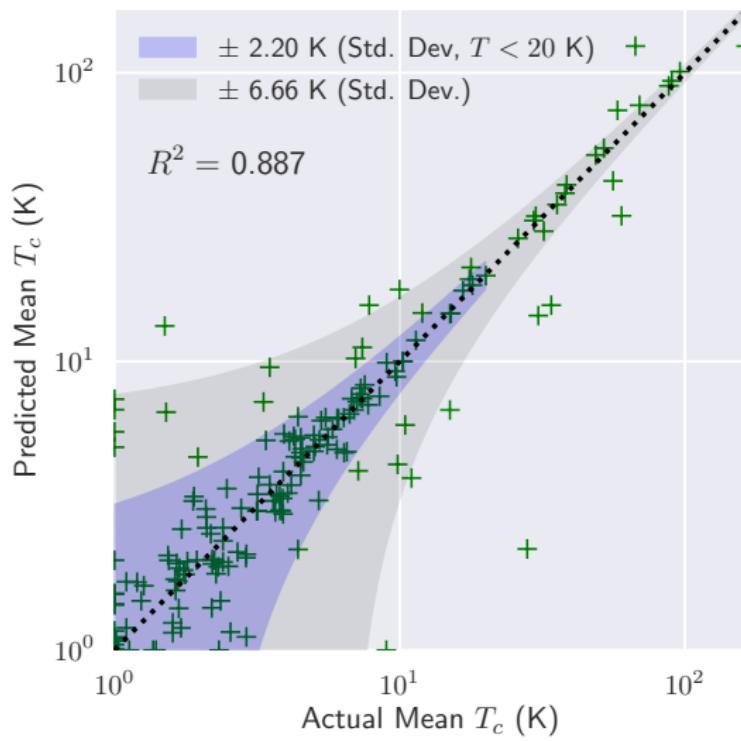
Examples of Empirical T_c Distributions:



Results

Model Evaluation

Predicting Empirical T_c Distributions

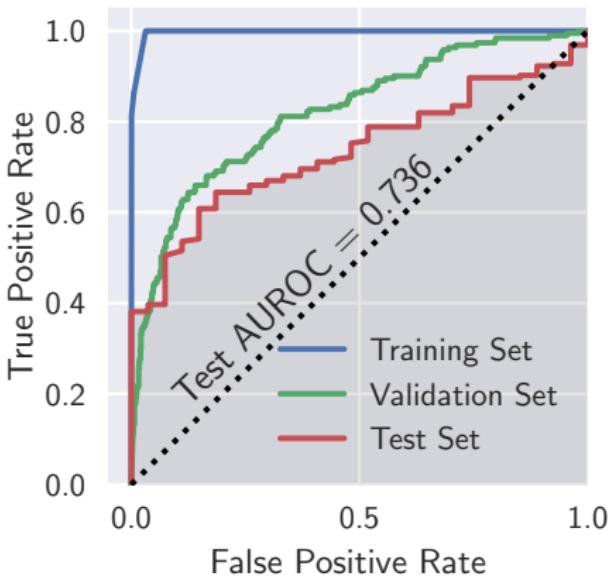


Model Evaluation

Classifying Superconductors (Confusion Matrix and ROC Curve)

		Predicted Superconductor	
		Yes	No
Contained in Dataset	Yes	Total: 102 TaSe ₃ , AlCu, W ₂ C, Nb ₃ , RhGe, Ce, TlNiSe ₂ , SrIr ₂	Total: 92 LaPd ₂ Al ₃ , Ru ₂ Zr, In ₃ Sn, La ₃ Sn, PdZr ₂
	No	Total: 95 YbLuB ₂₄ , Ti₃Ir* , CePb₃* , SrAu ₅ , SrGe₃*	Total: 917 Sc ₃ Nb, Yb ₅ Sn ₃ , Ba(SmSe ₂) ₂ , YAsO ₄ , Th ₂ Zn

* Materials that are actual superconductors, but were not contained in the dataset.



Identified Superconductors

- Using the model, we screened over 40,000 metals, oxides, metallic compounds, and hydrides from the Materials Project database [JOH⁺13].
- We identified **over 600 candidate superconductors** not contained in our dataset:

Materials Project ID	Formula	Stable	Experimentally Observed	Predicted Mean T_c	Closest Superconductor in Dataset
mp-672238	CeCuSb ₂	Yes	Yes	1.88 K	Cu ₂ Sb
mp-1025564	LuAl ₂ Pd ₅	Yes	No	8.12 K	Pd
mp-10898	ScAlNi ₂	Yes	Yes	1.25 K	Ni ₃ Al
mp-573601	Th ₇ Ru ₃	Yes	Yes	0.95 K	Th
mp-28280	K ₅ V ₃ O ₁₀	Yes	Yes	4.93 K	KO ₃
mp-1224184	HfZrB ₄	Yes	No	2.57 K	HfB ₂
mp-1228895	AlGaSb ₂	No	No	4.15 K	AlSb
mp-1222266	Lu ₃ S ₄	Yes	No	3.63 K	LuS
mp-1079796	Ti ₃ Pd	Yes	No	4.24 K	Ti
mp-1218331	Sr ₃ CaSig	No	No	1.88 K	Sr(Si) ₂
mp-1021328	H ₄ C	Yes	No	50.97 K	H ₂
mp-11494	LuPb ₃	No	Yes	3.80 K	Pb
mp-1226890	Ce ₄ H ₁₁	Yes	No	331.83 K	CeHg
mp-22266	GdB ₆	Yes	Yes	2.22 K	B
mp-1184695	Ho ₂ Er	No	No	6.22 K	Ho
...

Conclusion

Conclusion

- We trained a structure-based graph neural network model (ALIGNN) to predict the T_c with a standard deviation error of 6.66 K (2.20K for low- T_c).
- After screening the Materials Project database, we found more than 600 candidate superconductors.

Ongoing and Future Work

- We are currently collaborating with an inorganic chemistry lab at Baylor University to synthesize some of the more promising candidates.
- Additional work needs to be done incorporating electronic features (e.g. band structure) and incorporating structural features (e.g. substrates) into the model.

Questions

Superconductor Candidates List



<https://cburdine.github.io/files/qce23.html>

GitHub repository: <https://github.com/cburdine/sc-screening>

For more detailed questions, email: colin_burdine1@baylor.edu

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