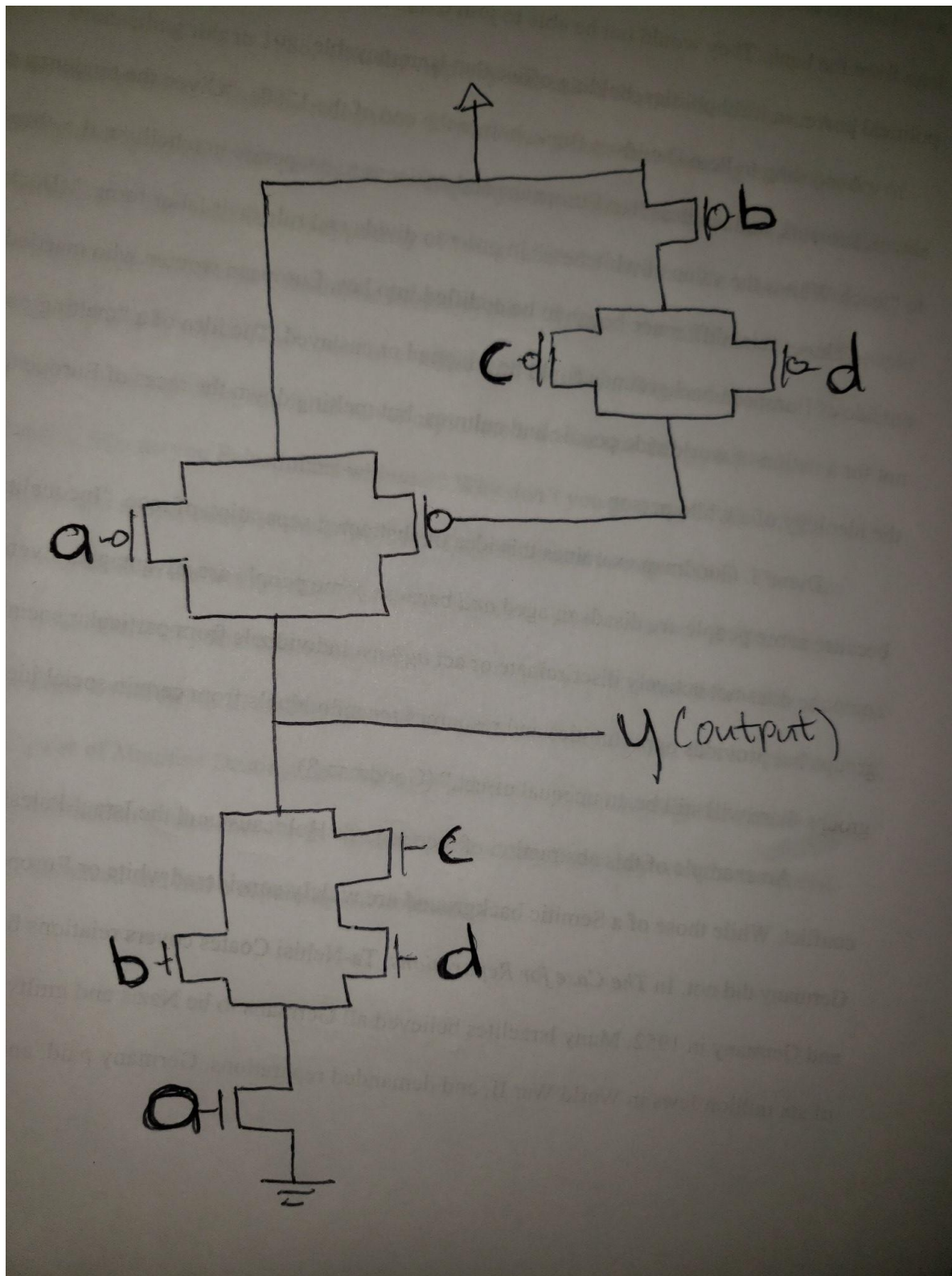


1) $y(a, b, c, d) = [a(b + cd)]'$



2)

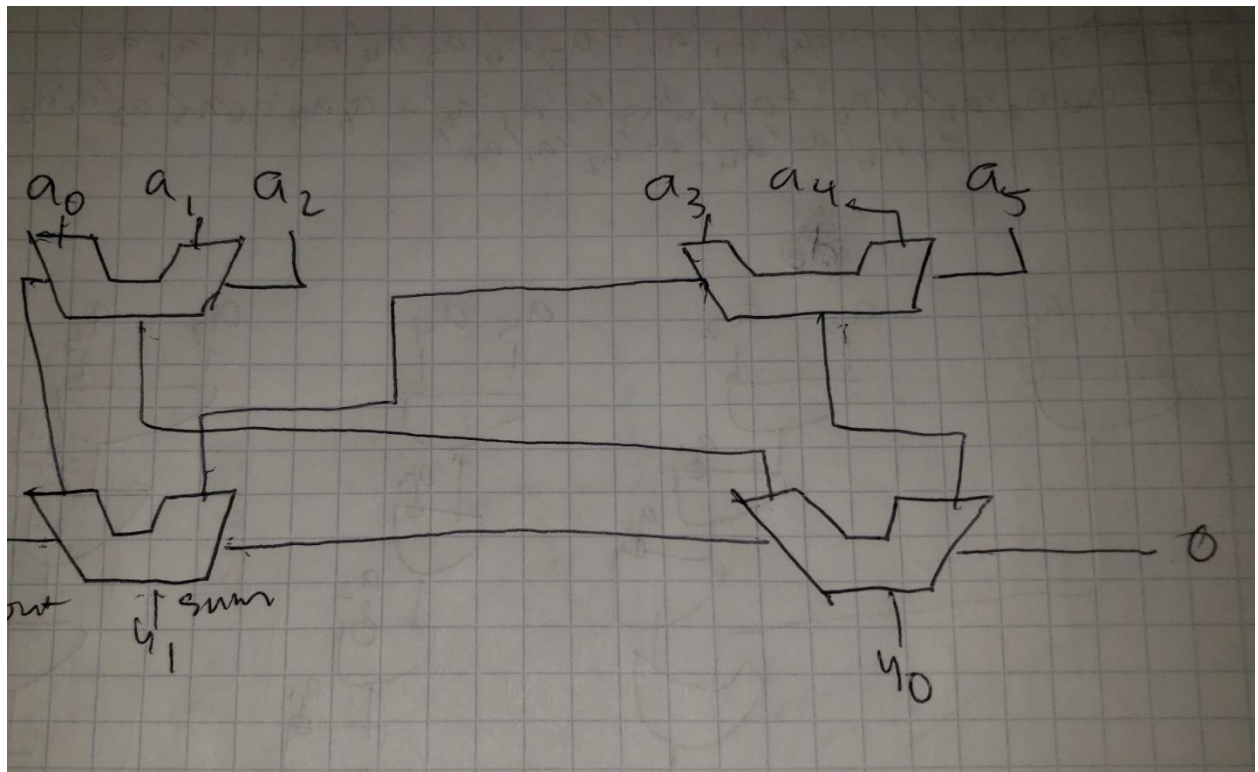
| a5 | a4 | a3 | a2 | a1 | a0 | | y2 | y1 | y0 |
|----|----|----|----|----|----|--|----|----|----|
| 0 | 0 | 0 | 0 | 0 | 0 | | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 1 | | 0 | 0 | 1 |
| 0 | 0 | 0 | 0 | 1 | 0 | | 0 | 0 | 1 |
| 0 | 0 | 0 | 0 | 1 | 1 | | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 | 0 | 0 | | 0 | 0 | 1 |
| 0 | 0 | 0 | 1 | 0 | 1 | | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | | 0 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 1 | | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 | 0 | | 0 | 0 | 1 |
| 0 | 0 | 1 | 0 | 0 | 1 | | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 1 | 0 | | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 1 | 1 | | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 0 | 0 | | 0 | 1 | 0 |
| 0 | 0 | 1 | 1 | 0 | 1 | | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | 0 | | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | 1 | | 1 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | 1 | | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 1 | 0 | | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 1 | 1 | | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 0 | 0 | | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 | 1 | | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 1 | | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 | 1 | | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 0 | | 0 | 1 | 1 |
| 0 | 1 | 1 | 0 | 1 | 1 | | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 0 | 1 | | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 | | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | | 1 | 0 | 1 |
| 1 | 0 | 0 | 0 | 0 | 0 | | 0 | 0 | 1 |
| 1 | 0 | 0 | 0 | 0 | 1 | | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 0 | | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 | 1 | | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 0 | 0 | | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 | | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 | | 0 | 1 | 1 |
| 1 | 0 | 0 | 1 | 1 | 1 | | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 | 0 | | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 | 1 | | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 | | 0 | 1 | 1 |

| | | | | | | | | | |
|---|---|---|---|---|---|--|---|---|---|
| 1 | 0 | 1 | 0 | 1 | 1 | | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 0 | | 0 | 1 | 1 |
| 1 | 0 | 1 | 1 | 0 | 1 | | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 0 | 1 | | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 0 | | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 1 | | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 0 | 0 | | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 | | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 0 | | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 | 1 | | 1 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 0 | | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 | 0 | 1 | | 1 | 0 | 0 |
| 1 | 1 | 0 | 1 | 1 | 0 | | 1 | 0 | 0 |
| 1 | 1 | 0 | 1 | 1 | 1 | | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 | 0 | 0 | | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 0 | 1 | | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 0 | | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 | 1 | 1 | | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 | | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 | 0 | 1 | | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 | 0 | | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | | 1 | 1 | 0 |

$Y_0 = a_5'a_4'a_3a_2'a_1'a_0' + a_5'a_4'a_3'a_2'a_1a_0' + a_5'a_4'a_3'a_2a_1'a_0' + a_5'a_4'a_3'a_2a_1a_0 + a_5'a_4'a_3a_2'a_1'a_0' +$
 $a_5'a_4'a_3a_2'a_1a_0 + a_5a_4'a_3'a_2'a_1'a_0' + a_5a_4'a_3'a_2'a_1a_0 + a_5a_4'a_3'a_2a_1'a_0 + a_5a_4'a_3'a_2a_1a_0' +$
 $a_5a_4'a_3a_2'a_1'a_0 + a_5a_4'a_3a_2'a_1a_0' + a_5a_4'a_3a_2a_1'a_0' + a_5a_4'a_3a_2a_1a_0 + a_5'a_4a_3'a_2'a_1'a_0' +$
 $a_5'a_4a_3'a_2'a_1a_0 + a_5'a_4a_3'a_2a_1'a_0 + a_5'a_4a_3'a_2a_1a_0' + a_5'a_4a_3a_2'a_1'a_0 + a_5'a_4a_3a_2'a_1a_0' +$
 $a_5'a_4a_3a_2a_1'a_0' + a_5'a_4a_3a_2a_1a_0 + a_5a_4a_3'a_2'a_1'a_0 + a_5a_4a_3'a_2'a_1a_0' + a_5a_4a_3'a_2a_1'a_0' +$
 $a_5a_4a_3'a_2a_1a_0 + a_5a_4a_3a_2'a_1'a_0' + a_5a_4a_3a_2'a_1a_0 + a_5a_4a_3a_2a_1'a_0 + a_5a_4a_3a_2a_1a_0'$

$Y_1 = a_5'a_4'a_3'a_1a_0 + a_5'a_4'a_3'a_2a_1 + a_5'a_4'a_3a_2'a_0 + a_5'a_4'a_3a_2'a_1 + a_5'a_4'a_3a_2a_0' + a_5'a_4'a_2a_1'a_0 +$
 $a_5a_4'a_3'a_2a_0' + a_5a_4'a_3a_2'a_1' + a_5a_4'a_2'a_1a_0' + a_5a_4'a_2'a_1'a_0 + a_5a_4'a_3'a_1'a_0 + a_5a_4'a_3'a_2'a_1 +$
 $a_5'a_4a_3'a_2a_0' + a_5'a_4a_3a_1'a_0' + a_5'a_4a_2'a_1a_0' + a_5'a_4a_2'a_1'a_0 + a_5'a_4a_3'a_2'a_0 + a_5'a_4a_3'a_1'a_0 +$
 $a_5a_4a_3'a_2'a_1' + a_5a_4a_3'a_2'a_0' + a_5a_4a_3'a_1'a_0' + a_5a_4a_2'a_1'a_0' + a_5a_4a_3a_2a_1a_0$

$Y_2 = a_5'a_4'a_3a_2a_1a_0 + a_5a_4'a_2a_1a_0 + a_5a_4'a_3a_1a_0 + a_5a_4'a_3a_2a_0 + a_5a_4'a_3a_2a_1 + a_5'a_4a_2a_1a_0 +$
 $a_5'a_4a_3a_1a_0 + a_5'a_4a_3a_2a_0 + a_5a_4a_3a_2 + a_5a_4a_1a_0 + a_5a_4a_2a_0 + a_5a_4a_3a_0 + a_5a_4a_2a_1 + a_5a_4a_3a_1$



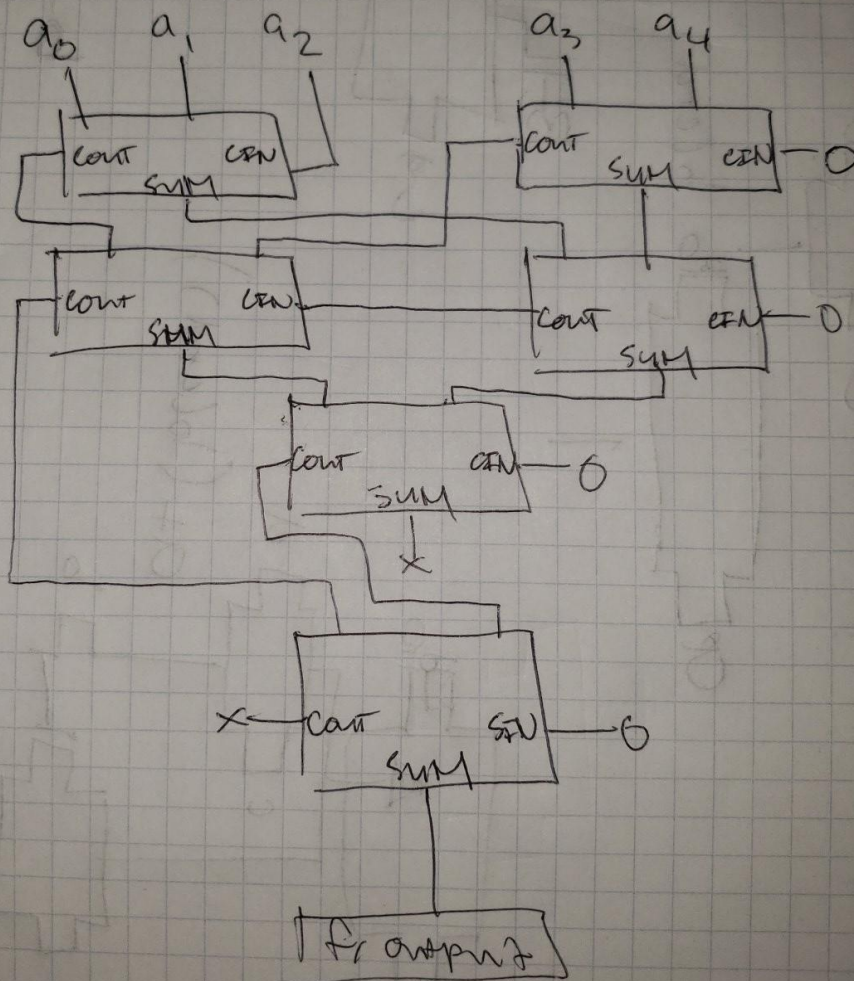
3)

3)

(a)

$$a_2a_3a_4 + a_1a_3a_4 + a_0a_2a_3 + a_0a_1a_4 + a_0a_1a_3 + a_0a_1a_2 + a_1a_2a_4 + a_1a_2a_3 + a_0a_3a_4 + a_0a_2a_4$$

(b)

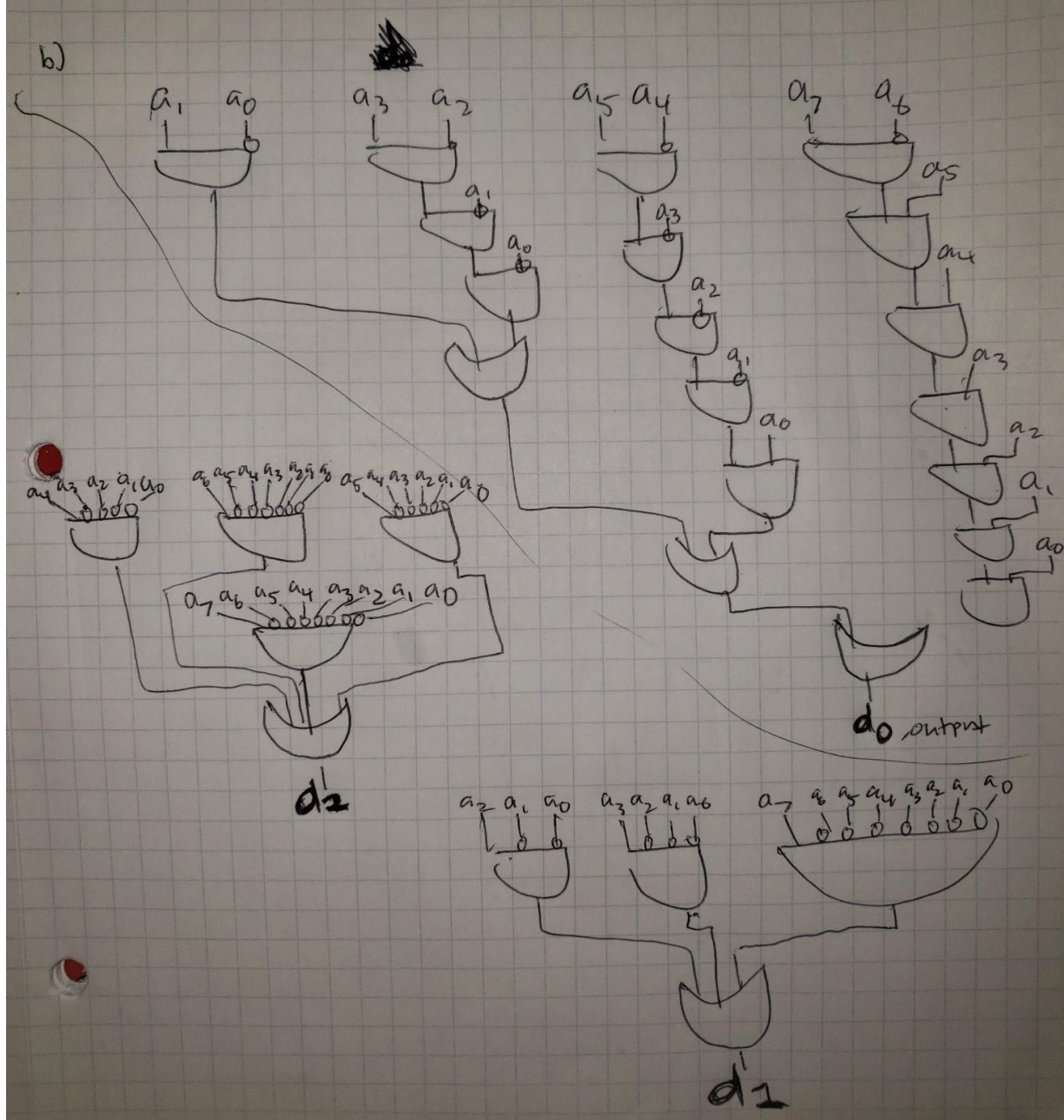


4)

a)
$$d_0 = a_1 a_0' + a_3 a_2' a_1' a_0' + a_5 a_4' a_3' a_2' a_1' a_0' + a_7 a_6' a_5' a_4' a_3' a_2' a_1' a_0'$$

$$d_1 = a_2 a_1' a_0' + a_3 a_2' a_1' a_0' + a_7 a_6' a_5' a_4' a_3' a_2' a_1' a_0'$$

$$d_2 = a_4 a_3' a_2' a_1' a_0' + a_5 a_4' a_3' a_2' a_1' a_0' + a_6 a_5' a_4' a_3' a_2' a_1' a_0' + a_7 a_6' a_5' a_4' a_3' a_2' a_1' a_0'$$



5)

1)

| C \ ab | 00 | 01 | 11 | 10 |
|--------|----|----|----|----|
| | 0 | 1 | 0 | 1 |
| 0 | 1 | X | 0 | 1 |
| 1 | X | 0 | 1 | 1 |

0 2 6 4

1 3 7 5

$$f(a,b,c) = b' + ac$$

2)

| cd \ ab | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
| | 0 | 1 | 0 | 1 |
| 00 | X | 0 | X | 1 |
| 01 | 0 | 1 | 0 | X |
| 11 | 1 | 0 | 1 | 1 |
| 10 | 1 | 1 | 0 | 0 |

0 4 12 8

1 5 13 9

3 7 15 11

2 6 14 10

$$\begin{aligned}
 f &= a'bcd + acd' + a'cd' + b'cd' + a'b'c \\
 &= a'bcd + acd + a'cd' + abc' + a'b'c \\
 &= a'bcd + acd + a'cd' + ac'd' + a'b'c \\
 &= a'bcd + acd + a'cd' + b'c'd' + b'cd \\
 &= a'bcd + acd + a'cd' + ab'c' + b'cd \\
 &= a'bcd + acd + a'cd' + ac'd' + b'cd
 \end{aligned}$$

3)

| de \ abc | 000 | 001 | 010 | 011 | 100 | 101 | 110 | 111 |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|
| | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |
| 00 | X | 0 | 1 | 1 | 1 | 0 | X | 1 |
| 01 | 0 | 0 | 1 | X | 0 | 1 | X | 0 |
| 11 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 |
| 10 | X | 1 | 0 | 1 | X | 1 | 0 | 1 |

$$\begin{aligned}
 f &= acd'e + c'e' + a'b'd' + b'e'd + bce + a'cde \\
 &= acd'e + c'e' + a'b'd' + b'e'd + bce + a'b'cd
 \end{aligned}$$

6)

6)

0 2 6 4
1 3 7 5

①

| | | | | | |
|---|---|----|----|----|----|
| | | ab | | | |
| | | 00 | 01 | 11 | 10 |
| c | 0 | 1 | x | 0 | 0 |
| | 1 | x | 0 | 1 | x |

$$f(a,b,c) = \prod M(3,4,6) + \sum d(1,2,5)$$

$$= (a' + c')(a + b')$$

$$= (a' + c')(a + c')$$

②

| | | | | | |
|----|---|----|----|----|----|
| | | ab | | | |
| | | 00 | 01 | 11 | 10 |
| cd | 0 | 0 | 1 | 1 | 0 |
| | 1 | 0 | 0 | 0 | 1 |
| | x | 0 | 1 | 1 | x |
| | 1 | 0 | x | 0 | 0 |

$$y = (b + d + c)(b' + d' + c')(a + c' + b')(a' + c' + b)$$

$$= (b + d + c)(b' + d' + c')(a + c' + b')(d' + b + d)$$

$$= (b + d + c)(b' + d' + c')(a + c' + b)(c' + c + d)$$

③

③

| | | | | | | | | | |
|----|---|-----|-----|-----|-----|-----|-----|-----|-----|
| | | abc | | | | | | | |
| | | 000 | 001 | 010 | 011 | 100 | 101 | 110 | 111 |
| de | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 | x |
| | 1 | 0 | 0 | 1 | x | 0 | 0 | 0 | 0 |
| | 1 | x | 0 | 1 | 1 | 1 | x | 0 | 1 |
| | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | x |

$$y = (c + e)(a' + d + e)(a' + c' + e)(b' + c' + e)(c' + d' + e)(a + b + d' + e)$$

$$= (c + e)(a' + d + e)(a' + c' + e)(b' + c' + e)(c' + d' + e)(a + b + c' + d)$$