Incentivizing Resource Pooling

Chen Chen



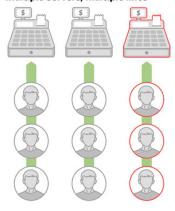
November 2023

Joint work with: Yilun Chen (CUHK-SZ) and Pengyu Qian (Purdue)

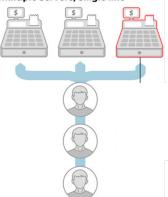
The Line Dance

Queuing theory, the mathematical study of lines, helps businesses, call centers, computer networks and others figure out how to keep things moving.

Multiple servers, multiple lines



Multiple servers, single line

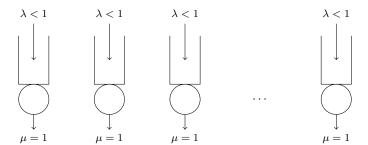


THE WALL STREET JOURNAL.



Resource pooling: known fact

N servers: job arrival rate $\lambda < 1$, server processing rate $\mu = 1$

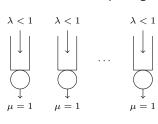


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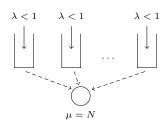
vs.

N servers: job arrival rate $\lambda < 1$, server processing rate $\mu = 1$

Without resource pooling:



With resource pooling:



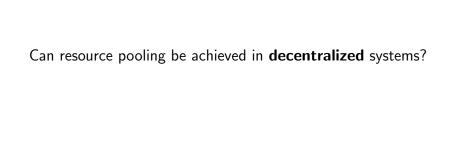
jobs in system: $N \cdot \frac{\lambda}{1-\lambda}$

$$N \cdot \frac{\lambda}{1 - \lambda}$$

linear

$$\frac{\lambda}{1-\lambda}$$

constant



Can resource pooling be achieved in decentralized systems?

Decentralization boosts security, privacy, and scalability

Motivation

- **Goal:** design mechanism to incentivize resource pooling in a decentralized setting.
- **Applications:** Decentralized computing marketplaces on blockchains

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iExec Market cap: \$75M

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Golem Network
Market cap: \$170M

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- Essential aspects of the problem:
 - lacktriangle Large-scale system: number of servers N is large
 - ► Servers have limited information about one another

Incentivize resource pooling, in private information setting

Incentivize resource pooling, in private information setting for queueing, matching, and general stochastic systems

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A talk on a different day...

lacktriangle Develop a simple token-based mechanism that incentives complete resource pooling in private information setting when N is large

⇒ System dynamics and performance match those under centralized control in the asymptotics

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- Propose an approximation-based analytical framework

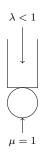
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 - ► Simplifies the design and analysis of token-based mechanisms
 - ► Provides tight theoretical guarantees
 - Can be applied to more general settings

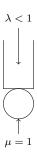
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 $\lambda < 1$

- Limited information:
 - (a) A server's arrivals and actions are private information
 - (b) Precise knowledge of number of servers N <u>not required</u> (except knowing that it is relative large)

Related Literature

Resource pooling:

- Power of resource pooling: [Tsitsiklis and Xu, 2013]
- Decentralized setup with two servers: [Hu and Caldentey, 2023]

Mean-field equilibrium:

- Analysis of complex operational problems: [lyer et al., 2014], [Balseiro et al., 2015], [Kanoria and Saban, 2021], [Arnosti et al., 2021]
- Fluid mean-field equilibrium similar in spirit to [Balseiro et al., 2015]

Scrip system:

Analysis of scrip system: [Kash et al., 2007], [Kash et al., 2015], [Johnson et al., 2014], [Bo et al., 2018]

Other related work:

- Cooperative game model: [Anily and Haviv, 2010], [Anily and Haviv, 2014], [Karsten et al., 2015]
- Supermarket game: [Xu and Hajek, 2013], [Yang et al., 2019]

Outline

- Motivation, research question, and literature review
- Token-based mechanism
 - ► Solution concept: Fluid mean-field equilibrium (FMFE)
 - ► Characterization of FMFE
 - Designing key element of mechanism
- FMFE strategy as near-optimal best response
 - Asymptotic analysis for large markets
 - ► Numerical analysis for small markets
- Extension to heterogeneous servers
- Takeaway

In the mechanism, a server can:

■ Request help from others <u>without recall</u> at any time.

When a capacity unit arrives, either: (i) serve its job, (ii) help others, or (iii) be idle and waste the unit without recall.

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 - Requested jobs relocate to shared pool

- When a capacity unit arrives, either: (i) serve its job, (ii) help others, or (iii) be idle and waste the unit without recall. If a server offers help:
 - ► The *oldest* job in shared pool is served (if pool is non-empty)

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- lacktriangle The value of ϕ is critical to system performance

Approximation methodology similar to (Balseiro et al. 2015)

- Mean-field approximation: each server optimizes by assuming state of shared pool is fixed at long-run average ⇒
 - Expected waiting time in shared pool is constant $w \ge 0$: value determined endogenously by equilibrium
 - \triangleright Probability that shared pool is non-empty is constant: equal to ϕ !

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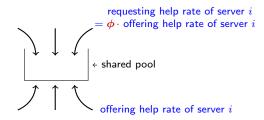
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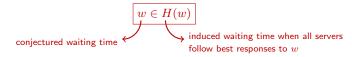
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 - ⇒ Closed-form characterization (next slide)

Equilibrium concept: Fluid mean-field equilibrium

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- Fluid mean-field equilibrium (FMFE):



Server's best response

Closed-form solution: threshold policy w.r.t. queue length:

- Request help only when queue length exceeds a threshold k (which depends on ϕ and w)
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Proposition. Suppose $\exists \, \bar{w} < \infty$ such that all servers believe that $w \leq \bar{w}$; then $w = O\left(\frac{1}{N}\right)$.

Proof: Using a drift analysis.

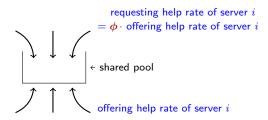
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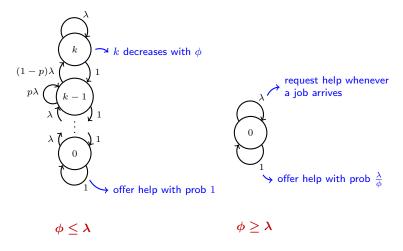
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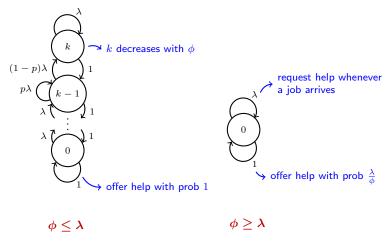
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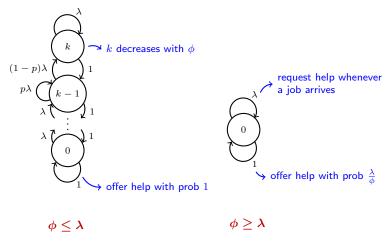
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Proposition. For any $\phi \in (0,1)$, if all servers play the above strategy, it forms a FMFE when number of servers N is large.

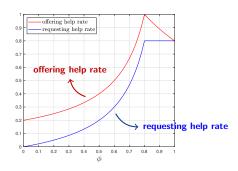
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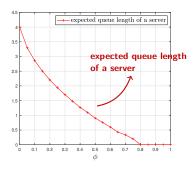
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Optimal value of ϕ

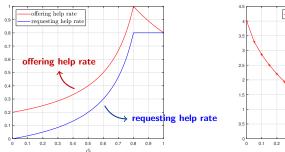


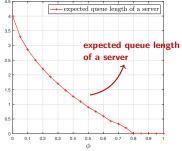


Proposition. The expected total number of jobs in system, denoted by $Q_{\Sigma}(\phi)$, satisfies:

- 1. When $\phi < \lambda$: $\lim_{N \to \infty} Q_{\Sigma}(\phi)/N = q(\phi) > 0$
- 2. When $\phi \geq \lambda$: $Q_{\Sigma}(\phi) = \frac{\phi}{1-\phi}$

Optimal value of ϕ





Main result. The optimal value is $\phi = \lambda$. Moreover, this induces complete resource pooling: it is each server's best strategy to (i) request help whenever a job arrives, (ii) offer help when queue is empty.

 \Longrightarrow System's dynamics and performance match those under centralized control



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Lemma. If server one also follows FMFE strategy, its time-average total cost is upper-bounded by $c\lambda + \mathbb{E}\big[Q^{\scriptscriptstyle \mathrm{F}}\big] + \frac{C_1(\lambda,\phi)}{N}$.

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Proof sketch:

- 1. A relaxation to server one's problem: empower the server to empty the shared pool at the end of every interaction with shared pool
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Proof sketch:

- A relaxation to server one's problem: empower the server to empty the shared pool at the end of every interaction with shared pool
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- 2. A coupling argument and a drift analysis to show:
 - (a) shared pool's queue length transitions to stationary distribution quickly as $N \to \infty$
 - (b) in stationary distribution, shared pool is non-empty with probability $\phi \frac{c(\lambda,\phi,\delta)}{N^{1-\delta}}$

Analysis for small market

- Mechanism uses $\phi = \lambda$.
- Consider the fluid setup: tokens can go negative but expected rates of earning and spending tokens are equal.
- Servers $i \ge 2$ adopt complete resource pooling; server one is strategic and minimizes own cost.

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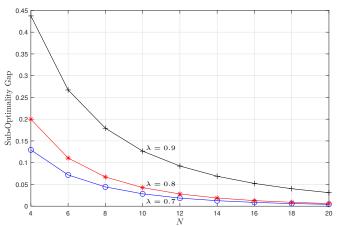
- \blacksquare Complete information about the shared pool's queue length (denoted by q_0)
- \Rightarrow Optimal strategy depends only on two states: q_1 (own queue length) and q_0

⇒ Tractable optimization problem!

Numerical results

(a) job processing cost c=1; (b) job arrival rate $\lambda \in \{0.7, 0.8, 0.9\}$

 ${\small {\sf Sub-optimality~gap} = \frac{{\small {\sf Cost~of~complete~resource~pooling-Cost~of~optimal~strategy}}{{\small {\sf Cost~of~optimal~strategy}}}}$



 The value of playing strategically is small even with few servers (and when server one can perfectly monitor the shared pool)

- For each server i: job arrival rate λ_i and processing rate μ_i ; let $\rho_i = \frac{\lambda_i}{\mu_i}$
- Assume $0<\rho\leq \rho_i\leq \bar{\rho}<1$ and $0<\underline{\lambda}\leq \lambda_i\leq \bar{\lambda}$ for all servers

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- Job processing costs are allocated $\propto \mu_i$ versus $\propto \lambda_i$
 - ⇒ Costs allocated fairly in our mechanism!

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- We study incentivizing resource pooling in a decentralized setting, where servers have limited information about others
- Operational takeaway: A simple **token-based mechanism** incentivizes complete resource pooling when number of servers is large
 - Analysis based on fluid mean-field equilibrium
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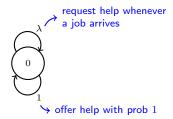
Reference: C. Chen, Y. Chen, and P. Qian. 2023. Incentivizing Resource Pooling. Under review.

Working paper available at https://papers.ssrn.com/abstract=4586771

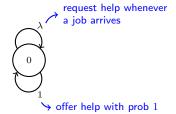


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