

PRIMER PARCIAL - CIRCUITOS ELECTRICOS III

APELLIDOS:..... NOMBRES:.....
CARRERA:..... CARNET DE IDENTIDAD:.....

1.- Se aplica la corriente: $i_g(t) = 22u(-t) + 10e^{-500t}u(t)$ A al circuito de la figura.

a) Determinar la corriente del capacitor: $i_{0(0^+)}$ aplicando el teorema del valor inicial

b) Hallar para $t > 0$ la corriente $i_{0(t)}$

2.- En el circuito trifásico equilibrado de la figura, se conoce: $\bar{I}_{AN} = 4.25 \angle -85^\circ$ A r.m.s;

$\bar{I}_{AC} = 4.378 \angle -100.68^\circ$ A r.m.s; $Z_Y = 65 + j70\Omega$; $Z_L = 5.4 + j6.25\Omega$

a) Determinar el valor de la impedancia Z_A si la secuencia es positiva

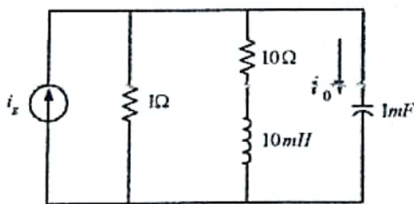
b) Determine la potencia trifásica total que entrega el generador por el método de los dos vatímetros

3.- En el circuito desequilibrado de la figura: $Z_L = 14 + j10\Omega$; $Z_1 = 55 + j65\Omega$; $Z_2 = 60 + j75\Omega$;

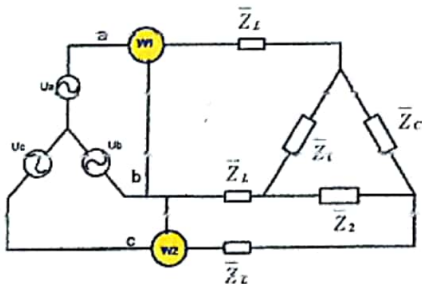
$Z_3 = 35 - j45\Omega$. Determinar la potencia trifásica por el método de los dos vatímetros y por la forma tradicional. Verifique que sale aproximadamente el mismo resultado sabiendo que el voltaje de línea en el generador trifásico es: $\bar{U}_{ab} = 345 \angle -155^\circ$ V r.m.s y la secuencia es negativa.

4.- Hallar el voltaje v_0 para $t > 0$ y para $t = 5$ s en el circuito mostrado en la figura

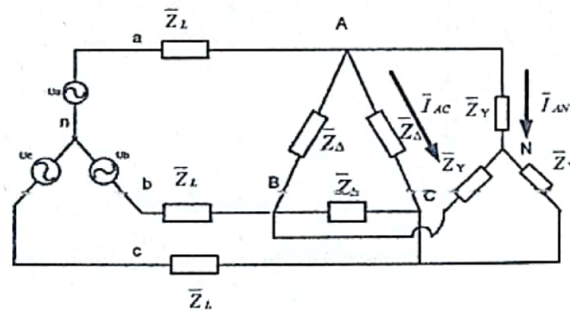
PROBLEMA 1



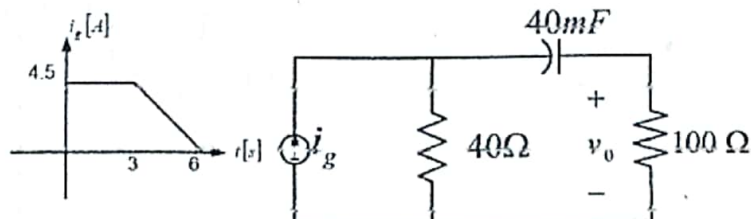
PROBLEMA 3



PROBLEMA 2



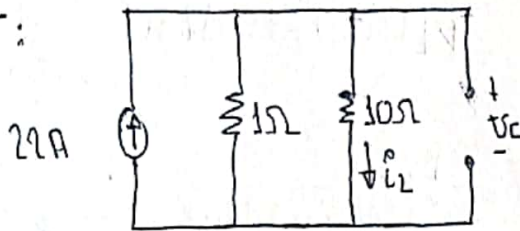
PROBLEMA 4



1^{er} Parcial - Cir 3

$$1.- i_g(t) = 22u(t) + 10e^{-500t}u(t)$$

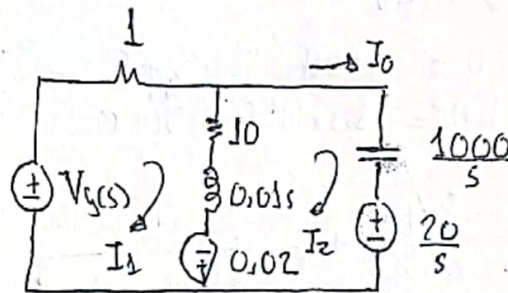
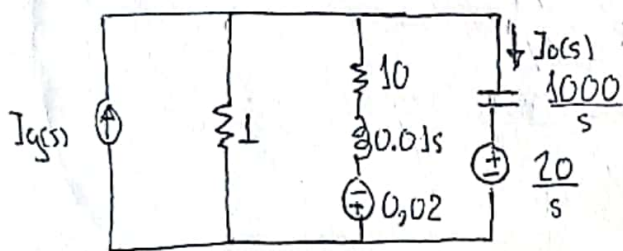
a) $t=0^-$:



$$i_L = \frac{1}{11} \cdot 22 \Rightarrow i_L = 2A$$

$$v_C = 20V$$

$$t > 0: I_g(s) = \frac{10}{s+500}$$



$$V_g(s) = \frac{10}{s+500}$$

$$\begin{cases} (11+0.01s)I_1 - (10+0.01s)I_2 = 0.02 + \frac{10}{s+500} \\ - (10+0.01s)I_1 + (10+0.01s + \frac{1000}{s})I_2 = -\frac{20}{s} - 0.02 \end{cases}$$

$$I_2 = \frac{\begin{vmatrix} 11+0.01s & 0.02 + \frac{10}{s+500} \\ -(10+0.01s) & -\frac{20}{s} - 0.02 \end{vmatrix}}{\begin{vmatrix} 11+0.01s & -(10+0.01s) \\ -(10+0.01s) & 10+0.01s + \frac{1000}{s} \end{vmatrix}} = \frac{(11+0.01s)(-\frac{20}{s} - 0.02) + (10+0.01s)(0.02 + \frac{10}{s+500})}{(11+0.01s)(10+0.01s + \frac{1000}{s}) - (10+0.01s)^2}$$

$$I_0(s) = \frac{-\frac{220}{s} - 0.22 - \cancel{0.2} - \cancel{2 \times 10^{-4}}s + \cancel{0.2} + \frac{100}{s+500} + \cancel{2 \times 10^{-4}}s + \frac{0.1s}{s+500}}{110 + 0.11s + \frac{11000}{s} + 0.1s + \cancel{1 \times 10^{-4}}s^2 + 10 - 100 - 0.2s - \cancel{1 \times 10^{-4}}s^2}$$

$$I_0(s) = \frac{-\frac{220}{s} - 0.22 + \frac{0.1s+100}{s+500}}{20 + 0.01s + \frac{11000}{s}} = \frac{-220s - 110000 - 0.22s(s+500) + 0.1s^2 + 100s}{s(20s + 0.01s^2 + 11000)}$$

$$I_0(s) = \frac{-0.12s^2 - 230s - 110000}{(s+500)(0.01s^2 + 20s + 11000)} \quad \times 0.01$$

$$I_0(s) = \frac{-12s^2 - 23000s - 11 \times 10^6}{(s+500)(s^2 + 2000s + 1.1 \times 10^6)}$$

$$a) \quad i_0(t) = \lim_{s \rightarrow \infty} \frac{-12s^3 - 23000s^2 - 11 \times 10^6 s}{(s+500)(s^2 + 2000s + 1.1 \times 10^6)} \Rightarrow \boxed{i_0(t) = -12 \text{ A}}$$

$$b) \quad \frac{-12s^2 - 23000s - 11 \times 10^6}{(s+500)(s^2 + 2000s + 1.1 \times 10^6)} = \frac{A}{s+500} + \frac{Bs+C}{s^2 + 2000s + 1.1 \times 10^6}$$

$$-12s^2 - 23000s - 11 \times 10^6 = A(s^2 + 2000s + 1.1 \times 10^6) + (Bs+C)(s+500) \quad \pm 1000^2$$

$$s^2: -12 = A+B$$

$$A = -50/7$$

$$s: -23000 = 2000A + 500B + C$$

$$B = -34/7$$

$$\text{cte: } -11 \times 10^6 = 1.1 \times 10^6 A + 500C$$

$$C = -\frac{44000}{7}$$

$$i_0(t) = \mathcal{L}^{-1} \left\{ \frac{-50/7}{s+500} + \frac{-\frac{34}{7}(s+1000-1000) - \frac{44000}{7}}{(s+1000)^2 + 1 \times 10^5} \right\}$$

$$\boxed{i_0(t) = \left[-\frac{50}{7} e^{-500t} + e^{-1000t} \left(-\frac{34}{7} \cos(316.2t) - 9.518 \cos(316.2t) \right) \right] \text{ u(t) A}}$$

$$2.- \quad \bar{I}_{AN} = 4.25 \angle -45^\circ \text{ A} \quad \bar{I}_{AC} = 4.378 \angle -100.68^\circ \text{ A}; \quad Z_Y = 65 + j70 \Omega; \quad Z_L = 5.4 + j6.25 \Omega$$

$$a) \quad \bar{U}_{AN} = Z_Y \cdot \bar{I}_{AN} = 405.98 \angle -37.88^\circ \text{ V} \Rightarrow \bar{U}_{AB} = 703.18 \angle -7.88^\circ \text{ V} \quad \text{Sec. (+)}$$

$$\pm 120^\circ \Rightarrow \bar{U}_{CA} = 703.18 \angle 112.12^\circ \text{ V}$$

$$\bar{U}_{AC} = -\bar{U}_{CA} = 703.18 \angle -67.88^\circ \text{ V}$$

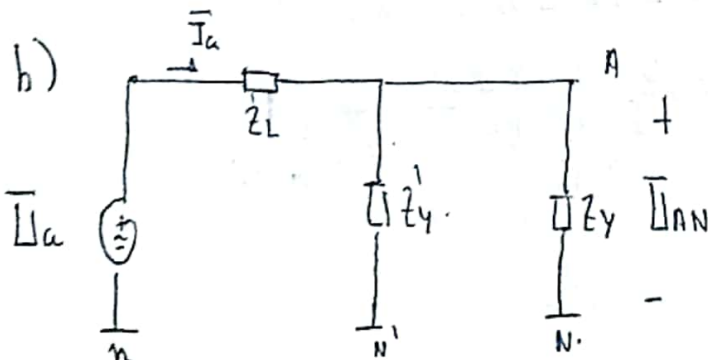
$$Z_\Delta = \frac{\bar{U}_{AC}}{\bar{I}_{AC}} \Rightarrow \boxed{Z_\Delta = 135 + j87 \Omega}$$

$$Z_Y = \frac{Z_\Delta}{3} = 45 + j29 \Omega$$

$$Z_1 = Z_Y \parallel Z_Y = 27.26 + j21.24 \Omega$$

$$Z_{eq} = Z_L + Z_1 = 32.66 + j27.5 \Omega$$

$$Z_{eq} = 42.67 \angle 40.1^\circ \Omega$$

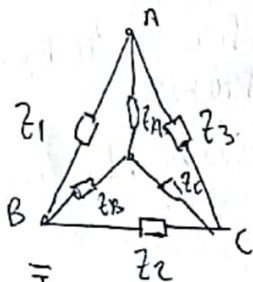


$$\bar{I}_a = \frac{\bar{U}_{AN}}{Z_1} = 11,75 \angle -75,8^\circ \text{ A} \quad I_L = 11,75 \text{ A} \quad \phi = 40,1^\circ$$

$$\bar{U}_a = \bar{I}_a \cdot Z_{eq} = 501,67 \angle -35,7^\circ \text{ V} \rightarrow U_L = 868,92 \text{ V}$$

$$\begin{aligned} W_1 &= 868,92 \times 11,75 \cos(40,1^\circ - 30^\circ) = 10051,6 \text{ W} \\ W_2 &= 868,92 \times 11,75 \cos(40,1^\circ + 30^\circ) = 3475,2 \text{ W} \end{aligned} \quad \boxed{P_T = 13527 \text{ W}}$$

$$\begin{aligned} 3.- \bar{U}_{an} &= 345 \angle -155^\circ \text{ V} \rightarrow \bar{U}_{ba} = 345 \angle 25^\circ \text{ V} \rightarrow \bar{U}_{ac} = 345 \angle -95^\circ \text{ V} \\ \bar{U}_a &= 199,2 \angle -125^\circ \text{ V} \rightarrow \bar{U}_b = 199,2 \angle -5^\circ \text{ V}; \bar{U}_c = 199,2 \angle 115^\circ \text{ V} \end{aligned}$$



$$Z_1 = 55 + j65 \Omega$$

$$Z_2 = 60 + j75 \Omega$$

$$Z_3 = 35 - j45 \Omega$$

$$Z_L = 14 + j10 \Omega$$

$$Z_A = \frac{Z_1 Z_3}{Z_1} = 22,47 - j15,57 \Omega$$

$$Z_B = \frac{Z_1 Z_2}{Z_1} = 16,69 + j42,93 \Omega$$

$$Z_C = \frac{Z_2 Z_3}{Z_1} = 25,82 - j16,86 \Omega$$

$$Z'_A = Z_L + Z_A = 36,47 - j5,57 \Omega$$

$$Z'_B = Z_L + Z_B = 30,69 + j52,93 \Omega$$

$$Z'_C = Z_L + Z_C = 39,82 - j6,86 \Omega$$

$$\bar{U}_0 = \frac{\frac{\bar{U}_a}{Z'_A} + \frac{\bar{U}_b}{Z'_B} + \frac{\bar{U}_c}{Z'_C}}{\frac{1}{Z'_A} + \frac{1}{Z'_B} + \frac{1}{Z'_C}} \Rightarrow$$

$$\bar{U}_0 = 89,63 \angle -130^\circ \text{ V} \Rightarrow$$

$$\bar{I}_a = \frac{\bar{U}_a - \bar{U}_0}{Z'_A} = 2,99 \angle -112,13^\circ \text{ A}$$

$$\bar{I}_b = \frac{\bar{U}_b - \bar{U}_0}{Z'_B} = 4,27 \angle -48,57^\circ \text{ A}$$

$$\bar{I}_c = \frac{\bar{U}_c - \bar{U}_0}{Z'_C} = 6,2 \angle 105,86^\circ \text{ A}$$

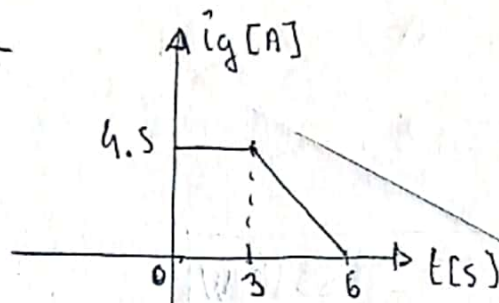
$$\bar{U}_{ab} = 345 \angle -155^\circ \text{ V}$$

$$\bar{U}_{cb} = 345 \angle 145^\circ \text{ V}$$

$$\begin{aligned} W_1 &= 345 \times 2,99 \cos(-155^\circ + 112,13^\circ) = 757,25 \text{ W} \\ W_2 &= 345 \times 6,2 \cos(145^\circ - 105,86^\circ) = 1659,02 \text{ W} \end{aligned} \quad \boxed{P_T = 2416,27 \text{ W}}$$

$$P_T = 2,99^2 \times 36,47 + 4,27^2 \times 30,69 + 6,2^2 \times 39,82 \Rightarrow \boxed{P_T = 2416,3 \text{ W}}$$

4.



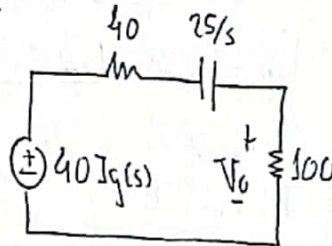
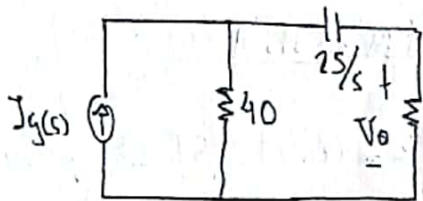
$$i_g(t) = \begin{cases} 4.5 \text{ A} & 0 \leq t < 3 \text{ s} \\ -1.5t + 9 \text{ A} & 3 \leq t < 6 \text{ s} \end{cases}$$

$$i_g(t) = 4.5(u(t) - u(t-3)) + (-1.5t + 9)(u(t-3) - u(t-6))$$

$$i_g(t) = 4.5u(t) + (-1.5t + 4.5)u(t-3) + (1.5t - 9)u(t-6)$$

$$I_g(s) = \frac{4.5}{s} + e^{-3s} \int \{-1.5(t+3) + 4.5\} + e^{-6s} \int \{1.5(t+6) - 9\}$$

$$I_g(s) = \frac{4.5}{s} - \frac{1.5}{s^2} e^{-3s} + \frac{1.5}{s^2} e^{-6s}$$



$$V_0(s) = \frac{100}{140 + 25} \cdot 40 I_g(s)$$

$$V_0(s) = \frac{4000s}{140s + 25} \cdot I_g(s)$$

$$V_0(s) = \frac{18000}{140s + 25} - \frac{6000 e^{-3s}}{s(140s + 25)} + \frac{6000 e^{-6s}}{s(140s + 25)}$$

7. 140

$$V_0(s) = \frac{900/7}{s + 5/28} - \frac{300/7 e^{-3s}}{s(s + 5/28)} + \frac{300/7 e^{-6s}}{s(s + 5/28)}$$

$$\mathcal{L}^{-1} \left\{ \frac{1}{s(s + 5/28)} \right\} = \int_0^t e^{-5/28 t} dt = -\frac{28}{5} e^{-5/28 t} + \frac{28}{5}$$

$$V_0(t) = \mathcal{L}^{-1} \{ V_0(s) \} = \frac{900}{7} e^{-5/28 t} u(t) - \frac{300}{7} \cdot \left(-\frac{28}{5} e^{-5/28(t-3)} + \frac{28}{5} \right) u(t-3) \\ + \frac{300}{7} \cdot \left(-\frac{28}{5} e^{-5/28(t-6)} + \frac{28}{5} \right) u(t-6)$$

$$V_0(t) = \frac{900}{7} e^{-5/28 t} u(t) + (240 e^{-5/28(t-3)} - 240) u(t-3) + (-240 e^{-5/28(t-6)} + 240) u(t-6) \text{ V}$$

$$t = 5 \text{ s} : V_0 = \frac{900}{7} e^{-25/28} + 240 e^{-5/28 \cdot 2} - 240$$

$$V_0 = -19.43 \text{ V}$$