UNIVERSIDAD MAYOR DE SAN SIMÓN FACULTAD DE CIENCIAS Y TECNOLOGÍA

PRACTICA No. 3

Estudiante:

Caballero Burgoa, Carlos Eduardo.

Carrera:

Ingeniería Electromecánica.

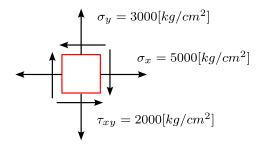
Docente:

Ing. Guido Gómez Ugarte.

Fecha de entrega: 11 de Octubre del 2022.

PROBLEMA 1:

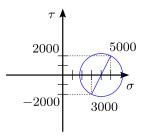
- a) Trazar el circulo de Mohr.
- b) Hallar: σ_{max} , σ_{min} , α y β .
- c) Las secciones principales.



Solución:

a) Circulo de Mohr:

$$\begin{split} \sigma_x &= 5000 [\text{kg/cm}^2] \\ \sigma_y &= 3000 [\text{kg/cm}^2] \\ \tau_{xy} &= 2000 [\text{kg/cm}^2] \end{split}$$



$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{8000}{2} = 4000 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{2000}{2} = 1000 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 2000 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{1000^2 + 2000^2} = 2236.07 \\ \sigma_{\text{max}} &= \sigma_0 + R = 6236.08 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = 1763.93 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 2236.07 [\text{kg/cm}^2] \end{split}$$

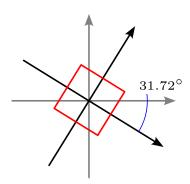
$$\tan 2\alpha = \frac{b}{a} = \frac{2000}{1000} = 1000$$

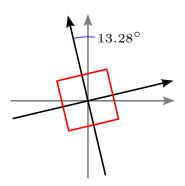
$$\alpha = \frac{\tan^{-1}(1000)}{2} = 31.72^{\circ}$$

$$2\alpha + 2\beta = 90^{\circ}$$

$$\beta = \frac{90 - 2\alpha}{2} = 13.28^{\circ}$$

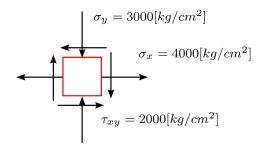
$$\begin{split} \sigma_{\rm max} &= 6236.08 [\rm kg/cm^2] \\ \sigma_{\rm min} &= 1763.93 [\rm kg/cm^2] \\ \alpha &= 31.72^{\circ} \\ \beta &= 13.28^{\circ} \end{split}$$





PROBLEMA 2:

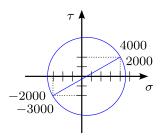
- a) Trazar el circulo de Mohr.
- b) Hallar: σ_{max} , σ_{min} , α y β .
- c) Las secciones principales.



Solución:

a) Circulo de Mohr:

$$\begin{split} \sigma_x &= 4000 [\mathrm{kg/cm^2}] \\ \sigma_y &= -3000 [\mathrm{kg/cm^2}] \\ \tau_{xy} &= 2000 [\mathrm{kg/cm^2}] \end{split}$$



$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{4000 - 3000}{2} = 500 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{4000 - (-3000)}{2} = 3500 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 2000 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{3500^2 + 2000^2} = 4031.13 \\ \sigma_{\text{max}} &= \sigma_0 + R = 4531.13 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = -3531.13 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 4031.13 [\text{kg/cm}^2] \end{split}$$

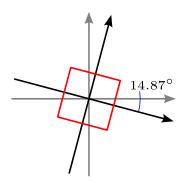
$$\tan 2\alpha = \frac{b}{a} = \frac{2000}{3500} = \frac{4}{7}$$

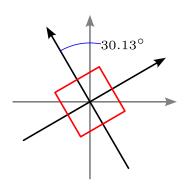
$$\alpha = \frac{\tan^{-1}(0.5714)}{2} = 14.87^{\circ}$$

$$2\alpha + 2\beta = 90^{\circ}$$

$$\beta = \frac{90 - 2\alpha}{2} = 30.13^{\circ}$$

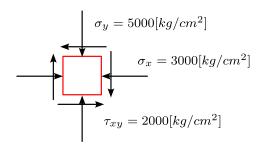
$$\begin{split} \sigma_{\rm max} &= 4531.13 [\rm kg/cm^2] \\ \sigma_{\rm min} &= -3531.13 [\rm kg/cm^2] \\ \alpha &= 14.87^{\circ} \\ \beta &= 30.13^{\circ} \end{split}$$





PROBLEMA 3:

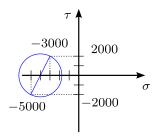
- a) Trazar el circulo de Mohr.
- b) Hallar: σ_{max} , σ_{min} , α y β .
- c) Las secciones principales.



Solución:

a) Circulo de Mohr:

$$\begin{split} \sigma_x &= -3000 [\mathrm{kg/cm^2}] \\ \sigma_y &= -5000 [\mathrm{kg/cm^2}] \\ \tau_{xy} &= 2000 [\mathrm{kg/cm^2}] \end{split}$$



$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{-3000 - 5000}{2} = -4000 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{-3000 - (-5000)}{2} = 1000 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 2000 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{1000^2 + 2000^2} = 2236.07 \\ \sigma_{\text{max}} &= \sigma_0 + R = -1763.93 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = -6236.07 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 2236.07 [\text{kg/cm}^2] \end{split}$$

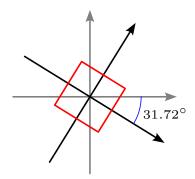
$$\tan 2\alpha = \frac{b}{a} = \frac{2000}{1000} = 2$$

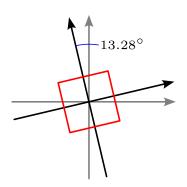
$$\alpha = \frac{\tan^{-1}(2)}{2} = 31.72^{\circ}$$

$$2\alpha + 2\beta = 90^{\circ}$$

$$\beta = \frac{90 - 2\alpha}{2} = 13.28^{\circ}$$

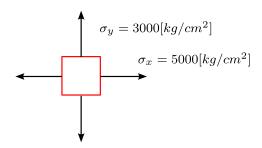
$$\begin{split} \sigma_{\rm max} &= -1763.93 [{\rm kg/cm^2}] \\ \sigma_{\rm min} &= -6236.07 [{\rm kg/cm^2}] \\ \alpha &= 31.72^{\circ} \\ \beta &= 13.28^{\circ} \end{split}$$





PROBLEMA 4:

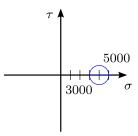
- a) Trazar el circulo de Mohr.
- b) Hallar: σ_{max} , σ_{min} , α y β .
- c) Las secciones principales.



Solución:

a) Circulo de Mohr:

$$\begin{split} \sigma_x &= 5000 [\mathrm{kg/cm^2}] \\ \sigma_y &= 3000 [\mathrm{kg/cm^2}] \\ \tau_{xy} &= 0 [\mathrm{kg/cm^2}] \end{split}$$



$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{5000 + 3000}{2} = 4000 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{5000 - 3000}{2} = 1000 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 0 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{1000^2 + 0^2} = 1000 \\ \sigma_{\text{max}} &= \sigma_0 + R = 5000 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = 3000 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 1000 [\text{kg/cm}^2] \end{split}$$

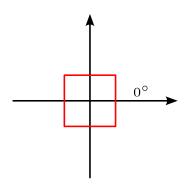
$$\tan 2\alpha = \frac{b}{a} = \frac{0}{1000} = 0$$

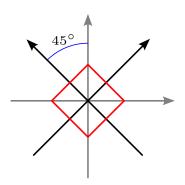
$$\alpha = \frac{\tan^{-1}(0)}{2} = 0^{\circ}$$

$$2\alpha + 2\beta = 90^{\circ}$$

$$\beta = \frac{90 - 2\alpha}{2} = 45^{\circ}$$

$$\begin{split} \sigma_{\rm max} &= 5000 [\rm kg/cm^2] \\ \sigma_{\rm min} &= 3000 [\rm kg/cm^2] \\ \alpha &= 0^{\circ} \\ \beta &= 45^{\circ} \end{split}$$



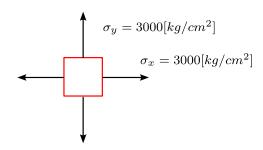


PROBLEMA 5:

a) Trazar el circulo de Mohr.

b) Hallar: σ_{max} , σ_{min} , α y β .

c) Las secciones principales.

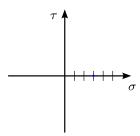


Solución:

a) Circulo de Mohr:

$$\sigma_x = 3000 [\text{kg/cm}^2]$$

$$\sigma_y = 3000 [\text{kg/cm}^2]$$



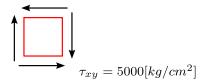
$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{3000 + 3000}{2} = 3000 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{3000 - 3000}{2} = 0 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 0 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{0^2 + 0^2} = 0 \\ \sigma_{\text{max}} &= \sigma_0 + R = 3000 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = 3000 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 0 [\text{kg/cm}^2] \\ \alpha &= \text{indeterminado} \end{split}$$

$\beta = \mathsf{indeterminado}$

$$\begin{split} \sigma_{\rm max} &= 3000 [\rm kg/cm^2] \\ \sigma_{\rm min} &= 3000 [\rm kg/cm^2] \\ \alpha &= {\rm indeterminado} \\ \beta &= {\rm indeterminado} \end{split}$$

PROBLEMA 6:

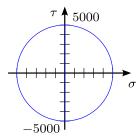
- a) Trazar el circulo de Mohr.
- b) Hallar: σ_{max} , σ_{min} , α y β .
- c) Las secciones principales.



Solución:

a) Circulo de Mohr:

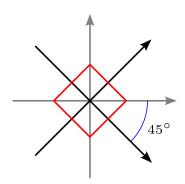
$$\begin{split} \sigma_x &= 0 [\mathrm{kg/cm^2}] \\ \sigma_y &= 0 [\mathrm{kg/cm^2}] \\ \tau_{xy} &= 5000 [\mathrm{kg/cm^2}] \end{split}$$

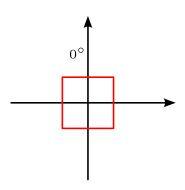


$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{0+0}{2} = 0 [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{0-0}{2} = 0 [\text{kg/cm}^2] \\ b &= \tau_{xy} = 5000 [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{0^2 + 5000^2} = 5000 \\ \sigma_{\text{max}} &= \sigma_0 + R = 5000 [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = -5000 [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = 5000 [\text{kg/cm}^2] \end{split}$$

$$\begin{split} \sin 2\alpha &= \frac{b}{R} = \frac{5000}{5000} = 1 \\ \alpha &= \frac{\sin^{-1}(1)}{2} = 45^{\circ} \\ 2\alpha + 2\beta &= 90^{\circ} \\ \beta &= \frac{90 - 2\alpha}{2} = 0^{\circ} \end{split}$$

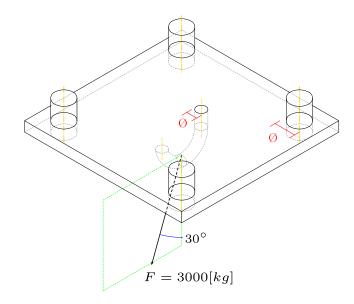
$$\begin{split} \sigma_{\rm max} &= 5000 [\rm kg/cm^2] \\ \sigma_{\rm min} &= -5000 [\rm kg/cm^2] \\ \alpha &= 45^{\circ} \\ \beta &= 0^{\circ} \end{split}$$



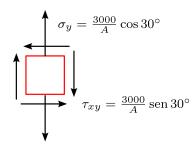


PROBLEMA 7:

- a) Hallar el diámetro del gancho para una SAE1020 con n=2.
- b) Hallar el diámetro de los pernos para una SAE1010 con n=2.



Solución:



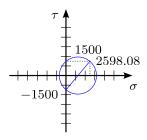
Circulo de Mohr:

$$\sigma_x=0[\mathrm{kg/cm^2}]$$

$$\sigma_y=\frac{3000}{A}\mathrm{cos}\,30^\circ=\frac{1500\sqrt{3}}{A}[\mathrm{kg/cm^2}]$$

$$\tau_{xy}=\frac{3000}{A}\mathrm{sen}\,30^\circ=\frac{1500}{A}[\mathrm{kg/cm^2}]$$

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$$\sigma_0 = \frac{\sigma_x + \sigma_y}{2} = \frac{0 + \frac{1500\sqrt{3}}{A}}{2} = \frac{750\sqrt{3}}{A} [\text{kg/cm}^2]$$

$$a = \frac{\sigma_x - \sigma_y}{2} = \frac{0 - \frac{1500\sqrt{3}}{A}}{2} = -\frac{750\sqrt{3}}{A} [\text{kg/cm}^2]$$

$$b = \tau_{xy} = \frac{1500}{A} [\text{kg/cm}^2]$$

$$R = \sqrt{a^2 + b^2} = \sqrt{\left(-\frac{750\sqrt{3}}{A}\right)^2 + \left(\frac{1500}{A}\right)^2} = \frac{\sqrt{3937500}}{A}$$

$$\sigma_{\text{max}} = \sigma_0 + R = \frac{3283.35}{A} [\text{kg/cm}^2]$$

$$\sigma_{\text{min}} = \sigma_0 - R = -\frac{685.28}{A} [\text{kg/cm}^2]$$

$$\tan 2\alpha = \frac{b}{a} = \frac{1500}{-750\sqrt{3}} = -\frac{2}{\sqrt{3}}$$

$$\alpha = \frac{\tan^{-1}(-1.1547)}{2} = -24.55^\circ$$

$$2\alpha + 2\beta = 90^\circ$$

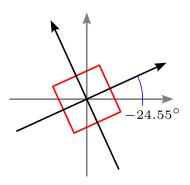
$$\beta = \frac{90 - 2\alpha}{2} = 69.55^\circ$$

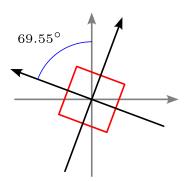
$$\sigma_{\text{max}} = \frac{3283.35}{A} [\text{kg/cm}^2]$$

$$\sigma_{\text{min}} = -\frac{685.28}{A} [\text{kg/cm}^2]$$

$$\alpha = -24.55^\circ$$

$$\beta = 69.55^\circ$$





a) Diámetro del gancho ($\sigma_f=2500[kg/cm^2]$):

$$\begin{split} \sigma_{\mathsf{max}} &\leq \bar{\sigma} \\ \frac{3283.35}{A} &\leq \frac{\sigma_f}{n} \\ \frac{3283.35}{\frac{\pi}{4} \varnothing^2} &\leq \frac{\sigma_f}{2} \\ \sqrt{\frac{(4)(2)(3283.35)}{\pi(2500)}} &\leq \varnothing \\ 1.8288[cm] &\leq \varnothing \end{split}$$

$$\emptyset \ge 18.29[mm]$$

$$\emptyset = \frac{3}{4}''$$

$$\begin{split} &\tau_{\mathsf{max}} \leq \bar{\tau} \\ &\frac{1984.31}{A} \leq \frac{0.5\sigma_f}{n} \\ &\frac{1984.31}{\frac{\pi}{4} \ensuremath{\emptyset}^2} \leq \frac{0.5\sigma_f}{2} \end{split}$$

$$\sqrt{\frac{(4)(2)(1984.31)}{\pi(0.5)(2500)}} \le \emptyset$$
$$2.0106[cm] \le \emptyset$$

$$\emptyset \ge 20.11[mm]$$

$$\emptyset = \frac{13''}{16}$$

b) Diámetro de los pernos ($\sigma_f=2100[kg/cm^2]$):

$$\begin{split} &\sigma_{\mathsf{max}} \leq \bar{\sigma} \\ &\frac{3283.35}{4A} \leq \frac{\sigma_f}{n} \\ &\frac{3283.35}{4\frac{\pi}{4} \varnothing^2} \leq \frac{\sigma_f}{2} \\ &\sqrt{\frac{(2)(3283.35)}{\pi(2100)}} \leq \varnothing \\ &0.9977[cm] \leq \varnothing \end{split}$$

$$\emptyset \ge 9.98[mm]$$

$$\emptyset = \frac{13''}{32}$$

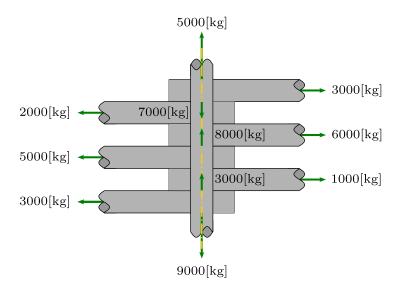
$$\begin{split} &\tau_{\mathsf{max}} \leq \bar{\tau} \\ &\frac{1984.31}{4A} \leq \frac{0.5\sigma_f}{n} \\ &\frac{1984.31}{4\frac{\pi}{4} \varnothing^2} \leq \frac{0.5\sigma_f}{2} \\ &\sqrt{\frac{(2)(1984.31)}{\pi(0.5)(2100)}} \leq \varnothing \\ &1.0969[cm] \leq \varnothing \end{split}$$

$$\emptyset \ge 10.97[mm]$$

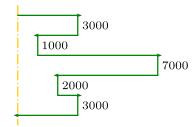
$$\emptyset = \frac{7}{16}''$$

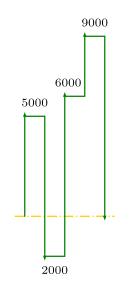
PROBLEMA 8:

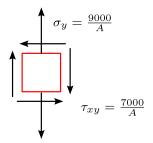
a) Hallar el diámetro del eje para $\sigma_f=4500[kg/cm^2]$ y n=2.



Solución:

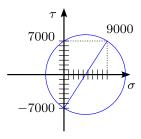






Circulo de Mohr:

$$\begin{split} \sigma_x &= 0 [\text{kg/cm}^2] \\ \sigma_y &= \frac{9000}{A} [\text{kg/cm}^2] \\ \tau_{xy} &= \frac{7000}{A} [\text{kg/cm}^2] \end{split}$$



 σ_{\max} , σ_{\min} , α y β .

$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{0 + \frac{9000}{A}}{2} = \frac{4500}{A} [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{0 - \frac{9000}{A}}{2} = -\frac{4500}{A} [\text{kg/cm}^2] \\ b &= \tau_{xy} = \frac{7000}{A} [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{\left(-\frac{4500}{A}\right)^2 + \left(\frac{7000}{A}\right)^2} = \frac{\sqrt{69250000}}{A} \\ \sigma_{\text{max}} &= \sigma_0 + R = \frac{12821.66}{A} [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = -\frac{3821.66}{A} [\text{kg/cm}^2] \\ \tau_{\text{max}} &= R = \frac{8321.66}{A} [\text{kg/cm}^2] \\ \tan 2\alpha &= \frac{b}{a} = \frac{7000}{-4500} = -\frac{14}{9} \\ \alpha &= \frac{\tan^{-1}(-0.4444)}{2} = -28.63^\circ \end{split}$$

$$2\alpha + 2\beta = 90^{\circ}$$

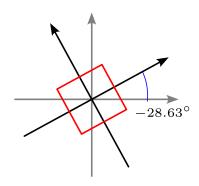
$$\beta = \frac{90 - 2\alpha}{2} = 73.63^{\circ}$$

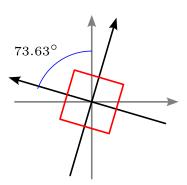
$$\sigma_{\rm max} = \frac{12821.66}{A} [{\rm kg/cm^2}]$$

$$\sigma_{\rm min} = -\frac{3821.66}{A} [{\rm kg/cm^2}]$$

$$\alpha = -28.63^\circ$$

$$\beta = 73.63^\circ$$





a) Diámetro del eje ($\sigma_f=4500[kg/cm^2]$):

$$\begin{split} \sigma_{\text{max}} &\leq \bar{\sigma} \\ \frac{12821.66}{A} &\leq \frac{\sigma_f}{n} \\ \frac{12821.66}{\frac{\pi}{4} \ensuremath{\emptyset}^2} &\leq \frac{\sigma_f}{2} \end{split}$$

$$\sqrt{\frac{(4)(2)(12821.66)}{\pi(4500)}} \le \emptyset$$
$$2.6936[cm] \le \emptyset$$

$$\emptyset \ge 26.94[mm]$$

$$\emptyset = 1\frac{1}{16}''$$

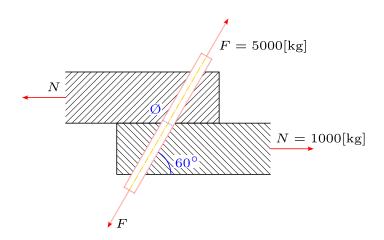
$$\begin{aligned} \tau_{\mathsf{max}} &\leq \bar{\tau} \\ \frac{8321.66}{A} &\leq \frac{0.5\sigma_f}{n} \\ \frac{8321.66}{\frac{\pi}{4} \varnothing^2} &\leq \frac{0.5\sigma_f}{2} \\ \sqrt{\frac{(4)(2)(8321.66)}{\pi(0.5)(4500)}} &\leq \varnothing \\ 3.069[cm] &\leq \varnothing \end{aligned}$$

$$\emptyset \ge 30.69[mm]$$

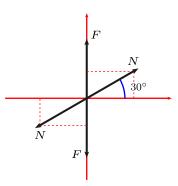
$$\emptyset = 1\frac{13}{64}''$$

PROBLEMA 9:

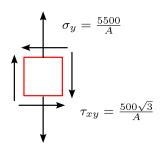
a) Hallar el diámetro del remache para un SAE1045 y $n=2.\,$



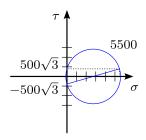
Solución:



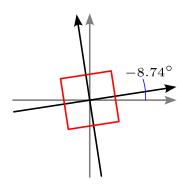
$$\begin{split} \sigma_x &= 0 [\text{kg/cm}^2] \\ \sigma_y &= \frac{F + Nsen(30^\circ)}{A} = \frac{5000 + 1000 \, sen(30^\circ)}{A} = \frac{5500}{A} [\text{kg/cm}^2] \\ \tau_{xy} &= \frac{Ncos(30^\circ)}{A} = \frac{1000 \, cos(30^\circ)}{A} = \frac{500\sqrt{3}}{A} [\text{kg/cm}^2] \end{split}$$

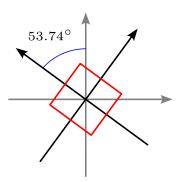


Circulo de Mohr:



$$\begin{split} \sigma_0 &= \frac{\sigma_x + \sigma_y}{2} = \frac{0 + \frac{5500}{A}}{2} = \frac{2750}{A} [\text{kg/cm}^2] \\ a &= \frac{\sigma_x - \sigma_y}{2} = \frac{0 - \frac{5500}{A}}{2} = -\frac{2750}{A} [\text{kg/cm}^2] \\ b &= \tau_{xy} = \frac{500\sqrt{3}}{A} [\text{kg/cm}^2] \\ R &= \sqrt{a^2 + b^2} = \sqrt{\left(-\frac{2750}{A}\right)^2 + \left(\frac{500\sqrt{3}}{A}\right)^2} = \frac{\sqrt{8312500}}{A} \\ \sigma_{\text{max}} &= \sigma_0 + R = \frac{5633.14}{A} [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= \sigma_0 - R = -\frac{133.14}{A} [\text{kg/cm}^2] \\ \tan 2\alpha &= \frac{b}{a} = \frac{500\sqrt{3}}{-2750} = -\frac{2\sqrt{3}}{11} \\ \alpha &= \frac{\tan^{-1}(-0.3149)}{2} = -8.74^{\circ} \\ 2\alpha + 2\beta &= 90^{\circ} \\ \beta &= \frac{90 - 2\alpha}{2} = 53.74^{\circ} \\ \hline \sigma_{\text{max}} &= \frac{5633.14}{A} [\text{kg/cm}^2] \\ \sigma_{\text{min}} &= -\frac{133.14}{A} [\text{kg/cm}^2] \\ \alpha &= -8.74^{\circ} \\ \beta &= 53.74^{\circ} \end{split}$$





a) Diámetro del remache ($\sigma_f=4500[kg/cm^2]$):

$$\begin{split} \sigma_{\mathsf{max}} &\leq \bar{\sigma} \\ \frac{5633.14}{A} &\leq \frac{\sigma_f}{n} \\ \frac{5633.14}{\frac{\pi}{4}} &\leq \frac{\sigma_f}{2} \\ \sqrt{\frac{(4)(2)(5633.14)}{\pi(4500)}} &\leq \varnothing \\ 1.7854[cm] &\leq \varnothing \end{split}$$

$$\emptyset \ge 17.84[mm]$$

$$\emptyset = \frac{11}{16}''$$

$$\begin{split} & \tau_{\mathsf{max}} \leq \bar{\tau} \\ & \frac{2883.14}{A} \leq \frac{0.5\sigma_f}{n} \\ & \frac{2883.14}{\frac{\pi}{4} \ensuremath{\emptyset}^2} \leq \frac{0.5\sigma_f}{2} \end{split}$$

$$\sqrt{\frac{(4)(2)(2883.14)}{\pi(0.5)(4500)}} \le \emptyset$$
$$1.8064[cm] \le \emptyset$$

$$\emptyset \ge 18.06[mm]$$

$$\emptyset = \frac{23''}{32}$$