

SERIE TRIGONOMÉTRICA DE *FOURIER*:

$$f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} [a_n \cos(n\omega_0 t) + b_n \operatorname{sen}(n\omega_0 t)]$$

$$a_0 = \frac{2}{T} \int_0^T f(t) dt$$

$$a_n = \frac{2}{T} \int_0^T f(t) \cos(n\omega_0 t) dt$$

$$b_n = \frac{2}{T} \int_0^T f(t) \operatorname{sen}(n\omega_0 t) dt$$

FORMULAS ÚTILES:

$$\operatorname{sen}(\pi n) = 0; \quad n \in \mathbb{N}$$

$$\cos(\pi n) = (-1)^n; \quad n \in \mathbb{N}$$

$$\operatorname{sen}(2\pi n) = 0; \quad n \in \mathbb{N}$$

$$\cos(2\pi n) = 1; \quad n \in \mathbb{N}$$

DERIVADAS ÚTILES:

$$\frac{d}{dt} [\arctan(t)] = \frac{1}{t^2 + 1} t'$$

$$\frac{d}{dt} [\ln(t)] = \frac{1}{t} t'$$

INTEGRALES ÚTILES:

$$\int e^{at} dt = \frac{1}{a} e^{at}$$

$$\int t e^{at} dt = \frac{t}{a} e^{at} - \frac{1}{a^2} e^{at}$$

$$\int t^2 e^{at} dt = \frac{t^2}{a} e^{at} - \frac{2t}{a^2} e^{at} + \frac{2}{a^3} e^{at}$$

$$\int \operatorname{sen}(at) dt = -\frac{\cos(at)}{a}$$

$$\int t \operatorname{sen}(at) dt = -\frac{t}{a} \cos(at) + \frac{1}{a^2} \operatorname{sen}(at)$$

$$\int t^2 \operatorname{sen}(at) dt = -\frac{t^2}{a} \cos(at) + \frac{2t}{a^2} \operatorname{sen}(at) + \frac{2}{a^3} \cos(at)$$

$$\int \cos(at) dt = \frac{\operatorname{sen}(at)}{a}$$

$$\int t \cos(at) dt = \frac{t}{a} \operatorname{sen}(at) + \frac{1}{a^2} \cos(at)$$

$$\int t^2 \cos(at) dt = \frac{t^2}{a} \operatorname{sen}(at) + \frac{2t}{a^2} \cos(at) - \frac{2}{a^3} \operatorname{sen}(at)$$

$$\int \frac{1}{t^2 + a^2} dt = \frac{1}{a} \arctan\left(\frac{t}{a}\right)$$

$$\int \frac{1}{t^2 - a^2} dt = \frac{1}{2a} \ln \left(\frac{t - a}{t + a} \right)$$

$$\int \frac{t}{t^2 + a^2} dt = \frac{1}{2} \ln(t^2 + a^2)$$

$$\int \frac{t}{t^2 - a^2} dt = \frac{1}{2} \ln(t^2 - a^2)$$

$$\int \ln(t) dt = t \ln |t| - t$$

$$\int e^{at} \sin(bt) dt = \frac{e^{at}}{a^2 + b^2} [a \sin(bt) - b \cos(bt)]$$

$$\int e^{at} \cos(bt) dt = \frac{e^{at}}{a^2 + b^2} [a \cos(bt) + b \sin(bt)]$$

SIMETRÍAS DE ONDA:

| | a_0 | a_n | b_n |
|--------------|------------------------------------|---|---|
| PAR | $\frac{4}{T} \int_0^{T/2} f(t) dt$ | $\frac{4}{T} \int_0^{T/2} f(t) \cos(n\omega_0 t) dt$ | 0 |
| IMPAR | 0 | 0 | $\frac{4}{T} \int_0^{T/2} f(t) \sin(n\omega_0 t) dt$ |
| S.M.O. | 0 | $\begin{cases} \text{p: } a_n = 0 \\ \text{i: } a_n = \frac{4}{T} \int_0^{T/2} f(t) \cos(n\omega_0 t) dt \end{cases}$ | $\begin{cases} \text{p: } b_n = 0 \\ \text{i: } b_n = \frac{4}{T} \int_0^{T/2} f(t) \sin(n\omega_0 t) dt \end{cases}$ |
| S.C.O. PAR | 0 | $\begin{cases} \text{p: } a_n = 0 \\ \text{i: } a_n = \frac{8}{T} \int_0^{T/4} f(t) \cos(n\omega_0 t) dt \end{cases}$ | 0 |
| S.C.O. IMPAR | 0 | 0 | $\begin{cases} \text{p: } b_n = 0 \\ \text{i: } b_n = \frac{8}{T} \int_0^{T/4} f(t) \sin(n\omega_0 t) dt \end{cases}$ |

SERIE COMPLEJA DE FOURIER:

$$e^{j\theta} = \cos(\theta) + j \sin(\theta)$$

$$e^{-j\theta} = \cos(\theta) - j \sin(\theta)$$

$$e^{\pm j2\pi n} = 1$$

$$e^{\pm j\pi} = -1$$

$$e^{\pm j\pi n} = \cos(\pi n)$$

$$\cos(\theta) = \frac{e^{j\theta} + e^{-j\theta}}{2}$$

$$\sin(\theta) = \frac{e^{j\theta} - e^{-j\theta}}{2j}$$

$$f(t) = \sum_{n=-\infty}^{\infty} c_n e^{jn\omega_0 t}$$

$$c_n = \frac{1}{T} \int_0^T f(t) e^{-jn\omega_0 t} dt$$

$$c_0 = \frac{1}{T} \int_0^T f(t) dt$$

$$a_n = 2 \operatorname{Re}\{c_n\}$$

$$b_n = -2 \operatorname{Im}\{c_n\}$$

FUNCIÓN IMPULSO:

$$\int_{-\infty}^{\infty} \delta(t - t_0) dt = 1$$

$$\int_{-\infty}^{\infty} \phi(t) \delta(t - t_0) dt = \phi(t_0)$$

$$\int_{-\infty}^{\infty} \phi(t) \delta^{(n)}(t - t_0) dt = (-1)^n \phi^{(n)}(t_0)$$

$$\delta(at) = \frac{1}{|a|} \delta(t)$$

$$t^n \delta(t) = 0; n \in \mathbb{N}$$

$$u'(t - t_0) = \delta(t - t_0)$$

$$\phi(t) \delta(t) = \phi(0) \delta(t)$$

$$\delta(-t) = \delta(t)$$

SERIE DE *FOURIER* POR DIFERENCIACIÓN:

$$c_n = c'_n + c''_n + \dots + c_n^{(k)}$$

$$\gamma'_n = \frac{1}{T} \int_0^T f'(t) e^{-jn\omega_0 t} dt$$

$$c'_n = \frac{\gamma'_n}{jn\omega_0}$$

$$\gamma''_n = \frac{1}{T} \int_0^T f''(t) e^{-jn\omega_0 t} dt$$

$$c''_n = \frac{\gamma''_n}{(jn\omega_0)^2}$$

$$\gamma_n^{(n)} = \frac{1}{T} \int_0^T f^{(k)}(t) e^{-jn\omega_0 t} dt$$

$$c_n^{(k)} = \frac{\gamma_n^{(k)}}{(jn\omega_0)^k}$$

TEOREMA DE LA MULTIPLICACIÓN:

$$\frac{1}{T} \int_0^T f_1(t) f_2(t) dt = \sum_{n=-\infty}^{\infty} c_1(n) c_2(-n) = \sum_{n=-\infty}^{\infty} c_1(-n) c_2(n)$$

TEOREMA DE *PARSEVAL*:

$$\frac{1}{T} \int_0^T f^2(t) dt = c_0^2 + \frac{1}{2} \sum_{n=1}^{\infty} (a_n^2 + b_n^2)$$

TRANSFORMADA DE *FOURIER*:

$$\mathcal{F}\{f(t)\} = F(\omega) = \int_{-\infty}^{\infty} f(t)e^{-j\omega t} dt$$

$$F(\omega) = R(\omega) + jX(\omega)$$

$$|F(\omega)| = \sqrt{R^2(\omega) + X^2(\omega)}$$

$$\Theta(\omega) = \arctan\left(\frac{X(\omega)}{R(\omega)}\right)$$

PROPIEDADES DE LA TRANSFORMADA DE *FOURIER*:

| | | |
|---|----------------------------|---|
| 1 | Linealidad | $\mathcal{F}\{a_1 f_1(t) + a_2 f_2(t)\} = a_1 F_1(\omega) + a_2 F_2(\omega)$ |
| 2 | Cambio de escala | $\mathcal{F}\{f(at)\} = \frac{1}{ a } F\left(\frac{\omega}{a}\right)$ |
| 3 | Desplazamiento en ω | $\mathcal{F}\{f(t)e^{jat}\} = F(\omega - a)$ |
| 4 | Desplazamiento en t | $\mathcal{F}\{f(t - a)\} = F(\omega)e^{-ja\omega}$ |
| 5 | Simetría | $\mathcal{F}\{F(t)\} = 2\pi f(-\omega)$ |
| 6 | Multiplicación | $\mathcal{F}\{t^n f(t)\} = j^n \frac{d^{(n)} F(\omega)}{d\omega^n}; \quad n \in \mathbb{N}$ |
| 7 | Derivada | $\mathcal{F}\{f^{(n)}(t)\} = (j\omega)^n F(\omega); \quad n \in \mathbb{N}$ |

FUNCIÓN SIGNO:

$$\text{sgn}'(t) = 2\delta(t)$$

$$|t|' = \text{sgn}(t)$$

$$\text{sgn}^2(t) = 1$$

TABLA DE TRANSFORMADAS DE *FOURIER*:

| | $f(t)$ | $F(\omega) = \mathcal{F}\{f(t)\}$ |
|----|------------------------------------|---|
| 1 | $u(t+a) - u(t-a)$ | $\frac{2 \operatorname{sen}(a\omega)}{\omega}$ |
| 2 | $\frac{\operatorname{sen}(at)}{t}$ | $\pi[u(\omega+a) - u(\omega-a)]$ |
| 3 | $e^{-at}u(t) \quad a > 0$ | $\frac{1}{a + j\omega}$ |
| 4 | $e^{at}u(-t) \quad a > 0$ | $\frac{1}{a - j\omega}$ |
| 5 | $e^{-a t } \quad a > 0$ | $\frac{2a}{a^2 + \omega^2}$ |
| 6 | $\frac{1}{t^2 + a^2}$ | $\frac{\pi}{a} e^{-a \omega }$ |
| 7 | $\delta(t-a)$ | $e^{-ja\omega}$ |
| 8 | e^{jat} | $2\pi\delta(\omega-a)$ |
| 9 | k | $2\pi k\delta(\omega)$ |
| 10 | $\operatorname{sen}(at)$ | $j\omega[\delta(\omega+a) - \delta(\omega-a)]$ |
| 11 | $\cos(at)$ | $\pi[\delta(\omega+a) + \delta(\omega-a)]$ |
| 12 | $t^n e^{-at}u(t)$ | $\frac{n!}{(a + j\omega)^{n+1}} \quad n \in \mathbb{N}$ |
| 13 | $u(t)$ | $\frac{1}{j\omega} + \pi\delta(\omega)$ |
| 14 | $\operatorname{sgn}(t)$ | $\frac{2}{j\omega}$ |
| 15 | $ t $ | $-\frac{2}{\omega^2}$ |
| 16 | $\frac{1}{t}$ | $-j\pi \operatorname{sgn}(\omega)$ |
| 17 | $\frac{1}{t^n}$ | $\frac{j^n \pi \omega^{n-1} \operatorname{sgn}(\omega)}{(-1)^n (n-1)!}$ |

FUNCIONES TRIGONOMÉTRICAS DE ARCO DOBLE:

$$\operatorname{sen}(2x) = 2 \operatorname{sen}(x) \cos(x)$$

$$\cos(2x) = 2 \cos^2(x) - 1$$

$$\cos(2x) = 1 - 2 \operatorname{sen}^2(x)$$

FUNCIONES TRIGONOMÉTRICAS DE ARCO TRIPLE:

$$\operatorname{sen}(3x) = 3 \operatorname{sen}(x) - 4 \operatorname{sen}^3(x)$$

$$\cos(3x) = 4 \cos^3(x) - 3 \cos(x)$$

FUNCIONES TRIGONOMÉTRICAS DE LA SUMA DE ARCOS:

$$\operatorname{sen}(a \pm b) = \operatorname{sen}(a) \cos(b) \pm \operatorname{sen}(b) \cos(a)$$

$$\cos(a \pm b) = \cos(a) \cos(b) \mp \operatorname{sen}(b) \cos(a)$$

FUNCIONES TRIGONOMÉTRICAS DE SUMA A PRODUCTO:

$$\operatorname{sen}(a) + \operatorname{sen}(b) = 2 \operatorname{sen}\left(\frac{a+b}{2}\right) \cos\left(\frac{a-b}{2}\right)$$

$$\operatorname{sen}(a) - \operatorname{sen}(b) = 2 \cos\left(\frac{a+b}{2}\right) \operatorname{sen}\left(\frac{a-b}{2}\right)$$

$$\cos(a) + \cos(b) = 2 \cos\left(\frac{a+b}{2}\right) \cos\left(\frac{a-b}{2}\right)$$

$$\cos(a) - \cos(b) = -2 \operatorname{sen}\left(\frac{a+b}{2}\right) \operatorname{sen}\left(\frac{a-b}{2}\right)$$

TRANSFORMADA INVERSA DE *FOURIER*:

$$\mathcal{F}\{f(t)\} = F(\omega) \rightarrow \mathcal{F}^{-1}\{F(\omega)\} = f(t)$$

TABLA DE TRANSFORMADAS INVERSAS DE *FOURIER*:

| | $F(\omega)$ | $f(t) = \mathcal{F}^{-1}\{F(\omega)\}$ |
|---|--|--|
| 1 | $\frac{1}{a + j\omega}$ | $e^{-at}u(t) \quad a > 0$ |
| 2 | $\frac{1}{a - j\omega}$ | $e^{at}u(-t) \quad a > 0$ |
| 3 | $\frac{2a}{a^2 + \omega^2}$ | $e^{-a t } \quad a > 0$ |
| 4 | $\frac{1}{\omega} \operatorname{sen}(a\omega)$ | $\frac{1}{2}[u(t+a) - u(t-a)]$ |
| 5 | k | $k\delta(t)$ |
| 6 | $\frac{1}{\omega}$ | $\frac{1}{2}j \operatorname{sgn}(t)$ |

PROPIEDADES DE LA TRANSFORMADA INVERSA DE *FOURIER*:

| | | |
|---|----------------------------|---|
| 1 | Linealidad | $\mathcal{F}^{-1}\{a_1 F_1(\omega) + a_2 F_2(\omega)\} = a_1 f_1(t) + a_2 f_2(t)$ |
| 2 | Desplazamiento en ω | $\mathcal{F}^{-1}\{F(\omega - a)\} = f(t)e^{jat}$ |
| 3 | Desplazamiento en t | $\mathcal{F}^{-1}\{F(\omega)e^{-ja\omega}\} = f(t - a)$ |

CONVOLUCIÓN:

$$f(t) = f_1(t) * f_2(t) = \int_{-\infty}^{\infty} f_1(\tau) f_2(t - \tau) d\tau$$

PROPIEDADES DE LA CONVOLUCIÓN:

| | | |
|---|--------------------------|--|
| 1 | Conmutatividad | $f_1(t) * f_2(t) = f_2(t) * f_1(t)$ |
| 2 | Asociatividad | $f_1(t) * [f_2(t) * f_3(t)] = [f_1(t) * f_2(t)] * f_3(t)$ |
| 3 | Distributividad | $f_1(t) * [f_2(t) + f_3(t)] = f_1(t) * f_2(t) + f_1(t) * f_3(t)$ |
| 4 | Función impulso | $f_1(t) * \delta(t - t_0) = f_1(t - t_0)$ |
| 5 | Función escalón unitario | $[f_1(t)u(t)] * [f_2(t)u(t)] = \int_0^t f_1(\tau) f_2(t - \tau) d\tau$ |

TRANSFORMADA DE *FOURIER* Y CONVOLUCIÓN:

$$\mathcal{F}\{f_1(t) * f_2(t)\} = F_1(\omega)F_2(\omega)$$

$$\mathcal{F}^{-1}\{F_1(\omega)F_2(\omega)\} = f_1(t) * f_2(t)$$

ECUACIONES DIFERENCIALES ORDINARIAS:

$$\mathcal{F}\{f'(t)\} = j\omega F(\omega)$$

$$\mathcal{F}\{f''(t)\} = (j\omega)^2 F(\omega)$$

$$\mathcal{F}\{f^{(n)}(t)\} = (j\omega)^n F(\omega)$$

TRANSFORMADA DE *LAPLACE*:

$$\mathcal{L}\{f(t)\} = F(s) = \int_0^{\infty} f(t)e^{-st} dt$$

PROPIEDADES DE LA TRANSFORMADA DE *LAPLACE*:

| | | |
|---|-----------------------|--|
| 1 | Linealidad | $\mathcal{L}\{a_1 f_1(t) + a_2 f_2(t)\} = a_1 F_1(s) + a_2 F_2(s)$ |
| 2 | Desplazamiento en s | $\mathcal{L}\{f(t)e^{at}\} = F(s - a)$ |
| 3 | Desplazamiento en t | $\mathcal{L}\{f(t - a)u(t - a)\} = F(s)e^{-as}$ $\mathcal{L}\{f(t)u(t - a)\} = e^{-as}\mathcal{L}\{f(t + a)\}$ |
| 4 | Multiplicación | $\mathcal{L}\{tf(t)\} = -\frac{dF(s)}{ds}$ $\mathcal{L}\{t^n f(t)\} = (-1)^n \frac{d^{(n)} F(s)}{ds^n}$ |
| 5 | División | $\mathcal{L}\left\{\frac{1}{t} f(t)\right\} = \int_s^{\infty} F(s) ds$ |
| 6 | Derivadas | $\mathcal{L}\{f'(t)\} = sF(s) - f(0)$ $\mathcal{L}\{f''(t)\} = s^2 F(s) - f(0)s - f'(0)$ $\mathcal{L}\{f'''(t)\} = s^3 F(s) - f(0)s^2 - f'(0)s - f''(0)$ |
| 7 | Integrales | $\mathcal{L}\left\{\int_0^t f(t) dt\right\} = \frac{1}{s} F(s)$ |

TABLA DE TRANSFORMADAS DE LAPLACE:

| | $f(t)$ | $F(s) = \mathcal{L}\{f(t)\}$ |
|----|------------------------------|--|
| 1 | k | $\frac{k}{s}$ |
| 2 | t^n | $\frac{n!}{s^{n+1}}; \quad n \in \mathbb{N}$ |
| 3 | e^{at} | $\frac{1}{s-a}$ |
| 4 | $\text{sen}(at)$ | $\frac{a}{s^2 + a^2}$ |
| 5 | $\cos(at)$ | $\frac{s}{s^2 + a^2}$ |
| 6 | $\text{senh}(at)$ | $\frac{a}{s^2 - a^2}$ |
| 7 | $\cosh(at)$ | $\frac{s}{s^2 - a^2}$ |
| 8 | $u(t-a)$ | $\frac{e^{-as}}{s}$ |
| 9 | $\delta(t-a)$ | e^{-as} |
| 10 | $\frac{1}{t} \text{sen}(at)$ | $\arctan\left(\frac{a}{s}\right)$ |

FUNCIÓN GAMMA:

$$\Gamma(n) = \int_0^\infty x^{n-1} e^{-x} dx$$

PROPIEDADES DE LA FUNCIÓN GAMMA:

| | | |
|---|-------------|---|
| 1 | Propiedad 1 | $\Gamma(n) = (n-1)\Gamma(n-1)$ $\Gamma(n) = (n-1)(n-2)(n-3)\dots(n-r)\Gamma(n-r)$ |
| 2 | Propiedad 2 | $\Gamma(n) = \frac{\Gamma(n+1)}{n}$ |
| 3 | Propiedad 3 | $\Gamma(n) = (n-1)!$ $0! = 1$ |
| 4 | Propiedad 4 | $\Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$ $\Gamma\left(-\frac{1}{2}\right) = -2\sqrt{\pi}$ |

TEOREMA DEL VALOR INICIAL Y FINAL:

$$f(0) = \lim_{t \rightarrow 0} f(t) = \lim_{t \rightarrow \infty} sF(s)$$

$$f(\infty) = \lim_{t \rightarrow \infty} f(t) = \lim_{t \rightarrow 0} sF(s)$$

TRANSFORMADA INVERSA DE LAPLACE:

$$\mathcal{L}^{-1}\{F(s)\} = f(t); \quad t > 0$$

TABLA DE TRANSFORMADAS INVERSAS DE LAPLACE:

| | $F(s)$ | $f(t) = \mathcal{L}^{-1}\{F(s)\}; t > 0$ |
|----|-----------------------------------|--|
| 1 | $\frac{k}{s}$ | k |
| 2 | $\frac{1}{s^n}$ | $\frac{t^{n-1}}{\Gamma(n)}$ |
| | | $\frac{t^{n-1}}{(n-1)!}; \quad n \in \mathbb{N}$ |
| 3 | $\frac{1}{s-a}$ | e^{at} |
| 4 | $\frac{1}{s^2+a^2}$ | $\frac{1}{a} \sin(at)$ |
| 5 | $\frac{s}{s^2+a^2}$ | $\cos(at)$ |
| 6 | $\frac{1}{s^2-a^2}$ | $\frac{1}{a} \sinh(at)$ |
| 7 | $\frac{s}{s^2-a^2}$ | $\cosh(at)$ |
| 8 | $\arctan\left(\frac{a}{s}\right)$ | $\frac{1}{t} \sin(at)$ |
| 9 | k | $k\delta(t)$ |
| 10 | e^{-as} | $\delta(t-a)$ |

PROPIEDADES DE LA TRANSFORMADA INVERSA DE LAPLACE:

| | | |
|---|-----------------------|--|
| 1 | Linealidad | $\mathcal{L}^{-1}\{a_1 F_1(s) + a_2 F_2(s)\} = a_1 f_1(t) + a_2 f_2(t)$ |
| 2 | Desplazamiento en s | $\mathcal{L}^{-1}\{F(s-a)\} = f(t)e^{at}$ |
| 3 | Desplazamiento en t | $\mathcal{L}^{-1}\{F(s)e^{-as}\} = f(t-a)u(t-a)$ |
| 4 | División por s | $\mathcal{L}^{-1}\left\{\frac{F(s)}{s}\right\} = \int_0^t f(t)dt$ |
| | | $\mathcal{L}^{-1}\left\{\frac{F(s)}{s^n}\right\} = \int_0^t \int_0^t \cdots \int_0^t f(t)dt \cdots dt$ |
| 5 | Derivada | $\mathcal{L}^{-1}\{F'(s)\} = -tf(t)$ |
| | | $\mathcal{L}^{-1}\{F^{(n)}(s)\} = (-1)^n t^n f(t)$ |

DESCOMPOSICIÓN EN FRACCIONES PARCIALES:

$$\frac{P(s)}{(s-a_1)(s-a_2)\cdots(s-a_n)} = \frac{A_1}{s-a_1} + \frac{A_2}{s-a_2} + \cdots + \frac{A_n}{s-a_n}$$

$$\frac{P(s)}{(s-a)^m(s-b)^n} = \frac{A_1}{s-a} + \frac{A_2}{(s-a)^2} + \cdots + \frac{A_m}{(s-a)^m} + \frac{B_1}{(s-b)} + \frac{B_2}{(s-b)^2} + \cdots + \frac{B_n}{(s-b)^n}$$

$$\frac{P(s)}{(s^2+a_1s+b_1)(s^2+a_2s+b_2)} = \frac{A_1s+B_1}{s^2+a_1s+b_1} + \frac{A_2s+B_2}{s^2+a_2s+b_2}$$

CONVOLUCIÓN:

$$f(t) = f_1(t) * f_2(t) = \int_0^t f_1(\tau)f_2(t-\tau)d\tau$$

TRANSFORMADA DE LAPLACE Y CONVOLUCIÓN:

$$\mathcal{L}\{f_1(t) * f_2(t)\} = F_1(s)F_2(s)$$

$$\mathcal{L}^{-1}\{F_1(s)F_2(s)\} = f_1(t) * f_2(t)$$

APLICACIONES DE LA TRANSFORMADA DE LAPLACE:

$$\mathcal{L}\{f'(t)\} = sF(s) - f(0)$$

$$\mathcal{L}\{f''(t)\} = s^2F(s) - f(0)s - f'(0)$$

$$\mathcal{L}\{f'''(t)\} = s^3F(s) - f(0)s^2 - f'(0)s - f''(0)$$

CIRCUITOS RLC:

$$L \left(\frac{d^2q}{dt^2} \right) + R \left(\frac{dq}{dt} \right) + \frac{1}{C}(q) = V(t)$$

$$L \left(\frac{di}{dt} \right) + R(i) + \frac{1}{C} \left(\int_0^t i dt \right) + V_C(0) = V(t)$$