



# iTMO

## Actuators

### Lab 5. DC drive PWM converters

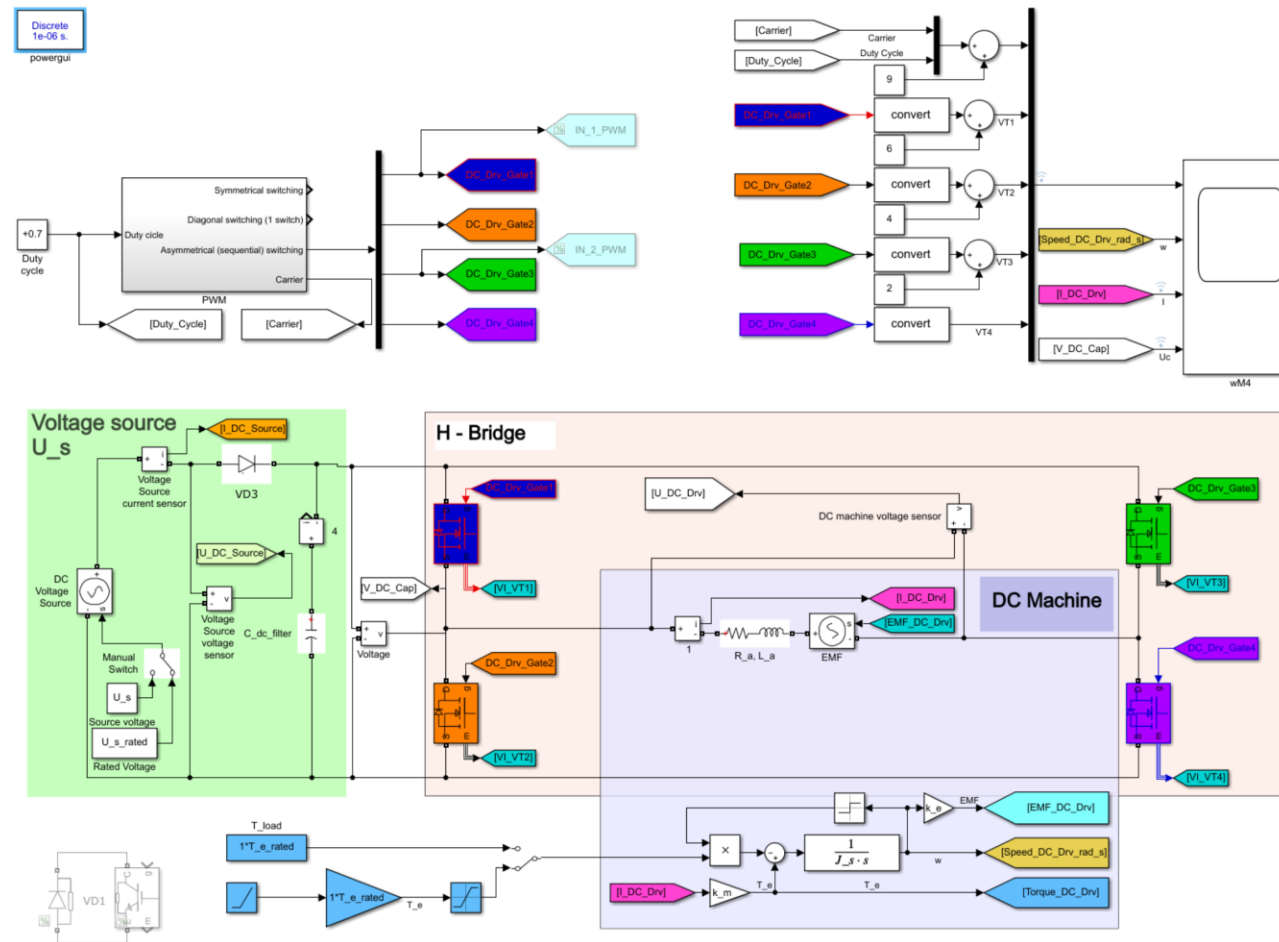
Asc. Prof. Nikolai Poliakov

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Asc. Prof. Dmitry Lukichev

# Efficiency analysis of DC drive with PWM converter

<https://clck.ru/34SRNH>



**Deadline is the 9<sup>th</sup> of April  
(Beijing 23:59 GMT+8 )**

**09/ 04 /2024**

## Step 1.

**HDU\_ID\_XXXXXXX.** Lab 5. Research on DC drive PWM converters

Please ensure yourself that **XXXXXXX** is your **HDU ID number**

Use the **Actuators\_Lab\_5\_R20XX.mlx** to evaluate missing parameters.

Drive data should be used from your variant in

**Actuators - Bachelor - Automation - Lab 5.xlsx**

### Lab 3. Research on DC drive PWM converters

Student name: \_\_\_\_\_ Date of submission \_\_\_\_\_  
 HDU ID \_\_\_\_\_ Student ITMO ID \_\_\_\_\_

#### Part 1. Evaluate missing parameters

Open **Actuators\_Lab3\_PWM\_R202\_.slx** model and **Actuators\_Lab3\_R202\_.mlx**  
**Drive parameters**

$U_{s\_rated}$  = - Rated source voltage, V;  
 $n_{rated}$  = - Rated rotating speed, rpm;  
 $f_{sw}$  = - PWM frequency, Hz;  
 $R_a$  = - Resistance of DC machine winding,  $\Omega$ ;  
 $L_a$  = - Armature inductance, H;  
 $J_s$  = - Moment of inertia,  $kg \cdot m^2$ ;  
 $I_{a\_rated}$  = - Anchor rated current of DC machine, A;  
 $k_{lim} = \frac{T_{e\_max}}{T_{e\_rated}}$  = - Maximum current limit, A.

#### Evaluations:

$P = U_{s\_rated} \cdot I_{a\_rated}$  = - Power, W;  
 $I_{a\_sc} = \frac{U_{s\_rated}}{R_a}$  = - Short circuit current, A;  
 $\omega_{m\_rated} = \frac{2 \cdot \pi \cdot n_{rated}}{60}$  = - Rated rotating speed, rad/s;  
 $k_e = \frac{(U_{s\_rated} - R_a \cdot I_{a\_rated})}{\omega_{m\_rated}}$  = - EMF constant, V\*s/rad;  
 $k_m = k_e$  = - Electromechanical constant,  $N \cdot m / A$ ;  
 $T_{e\_rated} = k_m \cdot I_{a\_rated}$  = - Rated Torque of the DC machine,  $N \cdot m$ ;  
 $T_{e\_max} = k_{lim} \cdot T_{e\_rated}$  = - Maximum torque,  $N \cdot m$ ;  
 $I_{lim} = k_{lim} \cdot I_{a\_rated}$  = - Maximum current,  $N \cdot m$ ;  
 $T_{e\_st} = k_m \cdot I_{a\_sc}$  = - Starting torque,  $N \cdot m$ ;  
 $K_{eff\_rated} = \frac{\omega_{m\_rated} \cdot T_{e\_rated}}{P} \cdot 100\%$  = - Rated efficiency, %;  
 $\tau_e = \frac{L_a}{R_a}$  = - Electromagnetic time constant, s;  
 $\omega_0 = \frac{U_{s\_rated}}{k_e}$  = - Idle speed, rad/s;

Automation (bachelor 2021)						Drive parameters									Transistor switch parameters								
Semester 2, Year (2023/2024)						Source rated voltage	Rated rotating speed	PWM frequency	Resistance of DC machine winding	Armature inductance	Moment of inertia	Anchor rated current of DC machine	Duty cycles	Maximum current limit coefficient	Forward voltage	Forward voltage $V_{dt}$ at current $I_a=I_{lim}$	Shubler capacitance	Shubler resistance	Internal (antiparallel) diode forward voltage $V_d$	Internal (antiparallel) diode forward voltage $V_{dt}$ at current $I_{lim}$	switch-on (rise) time of the transistor	switch-off (fall) time of the transistor	
Course name		Actuators				[V]	[rpm]	[Hz]	[Ω]	[mH]	[kg·m²]	[A]			[V]	[V]	[nF]	[kΩ]	[V]	[V]	[μs]	[μs]	
No. In ITMO	Surname, First name in Russian	No. In HDU	Surname, First name in English	Surname, First name in Chinese	Gender	$U_{s\_rated}$	$n_{rated}$	$f_{sw}$	$R_a$	$L_a$	$J_s$	$I_{a\_rated}$	$\gamma_{max}$	$k_{L\_lim}$	$V_{L\_st}$	$V_{L\_st, Ia}$	$C_s$	$R_s$	$V_{L\_st}$	$V_{L\_st, Ia}$	$t_s$	$t_f$	

```

U_s Rated = 220; % - Rated source voltage, V;
n Rated = 750; % - Rated rotating speed, rpm;
f_sw = 5000; % - PWM frequency, Hz;
R_a = 27.20; % - Resistance of DC machine winding (armature),  $\Omega$ ;
L_a = 0.128; % - Anchor inductance, H, %tau_e=La/Ra;
J_s = 0.004; % - Moment of inertia,  $kg \cdot m^2$ ;
I_a Rated = 170/220; % - Anchor rated current of DC machine, A;
k_lim = 3.5; % - Maximum current limit coefficient
    
```

## Part 2. Evaluate parameters of the system with PWM

### Transistor switched on circuit parameters

$V_{fvt} = 0$	- IGBT Forward voltage $V_f$ at current $I_a \approx 0$ , V (For MOSFET may be considered equal to 0);
$V_{fvtIa} = 1.3$	- Forward voltage $V_f$ at current $I_a = I_{lim} = I_{a\_rated} \cdot k_{lim}$ , V;
$R_{onvt} = \frac{(V_{fvtIa} - V_{fvt})}{I_{lim}} =$	- MOSFET / IGBT resistance $R_{on}$ , $\Omega$ ;

### Snubber circuit parameters

$C_S = 330e-9$	- Snubber capacitance, F;
$R_S = 1e6$	- Snubber resistance, $\Omega$ ;

### Reverse (antiparallel) diode parameters

$V_{frd} = 0.65$	- Internal (antiparallel) diode forward voltage $V_f$ at current $I_a \approx 0$ , V;
$V_{frdIa} = 0.75$	- Internal (antiparallel) diode forward voltage at current $I_{lim}$ , V;
$R_{onrd} = \frac{(V_{frdIa} - V_{frd})}{I_{lim}} =$	- Internal (antiparallel) diode resistance $R_d$ , $\Omega$ ;

## Step 2.

Change the transistor parameters in the section to the new ones from your variant data

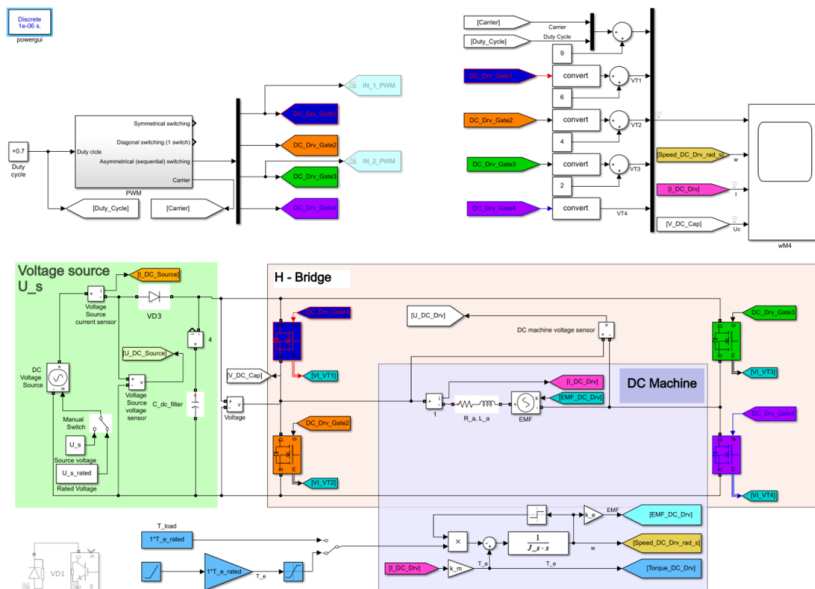


Figure 1 – DC drive system under test

### Transistor parameters

#### Transistor switched on circuit parameters

$V_{f\_vt}$	$= 0;$	% - Forward voltage $V_f$ (V) (For MOSFET may be considered equal to 0)
$V_{f\_vtIa}$	$= 1.3;$	% - Forward voltage $V_f$ at rated current $I_{lim}$ (V)
$R_{on\_vt}$	$= (V_{f\_vtIa} - V_{f\_vt}) / I_{lim};$	% - MOSFET / IGBT resistance $R_{on}$ ( $\Omega$ )

#### Snubber circuit parameters

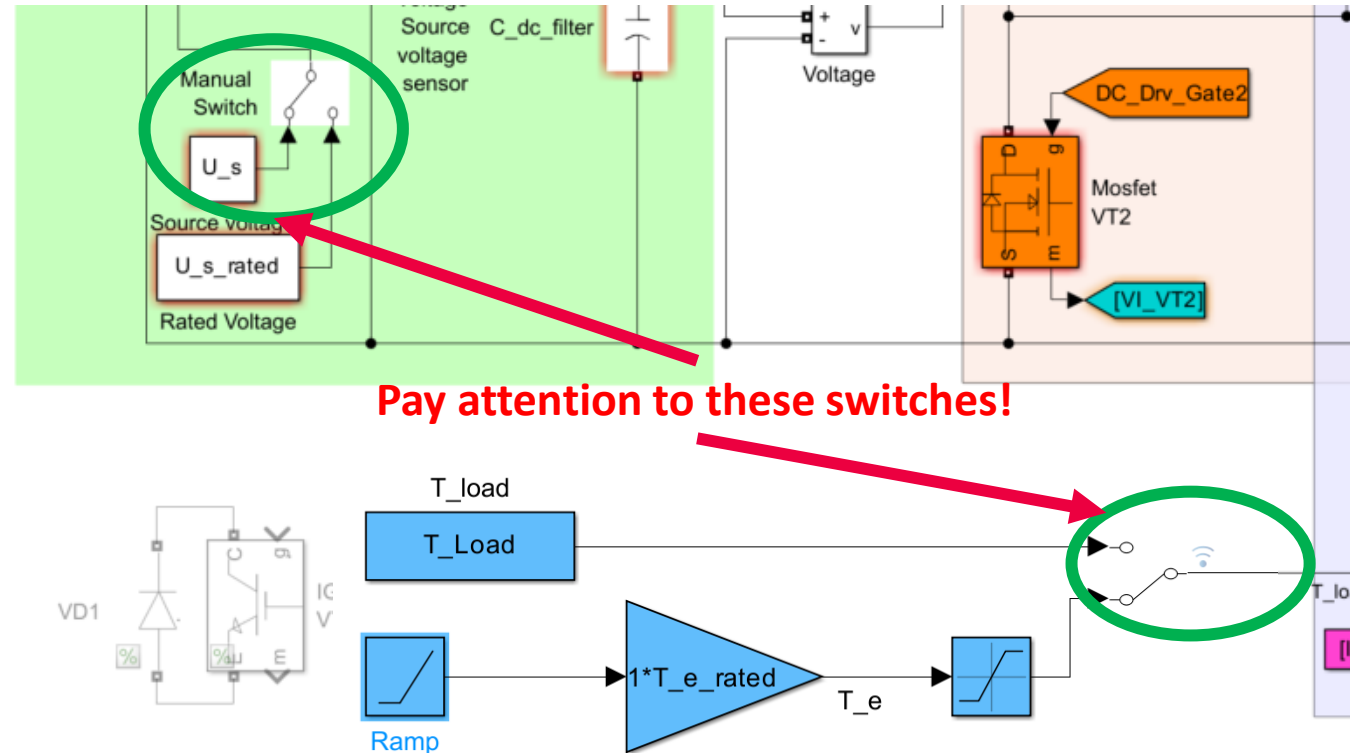
$C_{s\_vt}$	$= 330e-9;$	% - Snubber resistance $R_s$ ( $\Omega$ )
$R_{s\_vt}$	$= 1e6;$	% - Snubber capacitance $C_s$ (F)

#### Reverse (antiparallel) diode parameters

$V_{f\_rd}$	$= 0.65;$	% - Internal (antiparallel) diode forward voltage $V_f$ (V)
$V_{f\_rdIa}$	$= 0.75;$	% - Internal (antiparallel) diode forward voltage at rated current $I_{lim}$ (V)
$R_{on\_rd}$	$= (V_{f\_rdIa} - V_{f\_rd}) / I_{lim};$	% - Internal (antiparallel) diode resistance $R_d$ ( $\Omega$ )

## Step 3

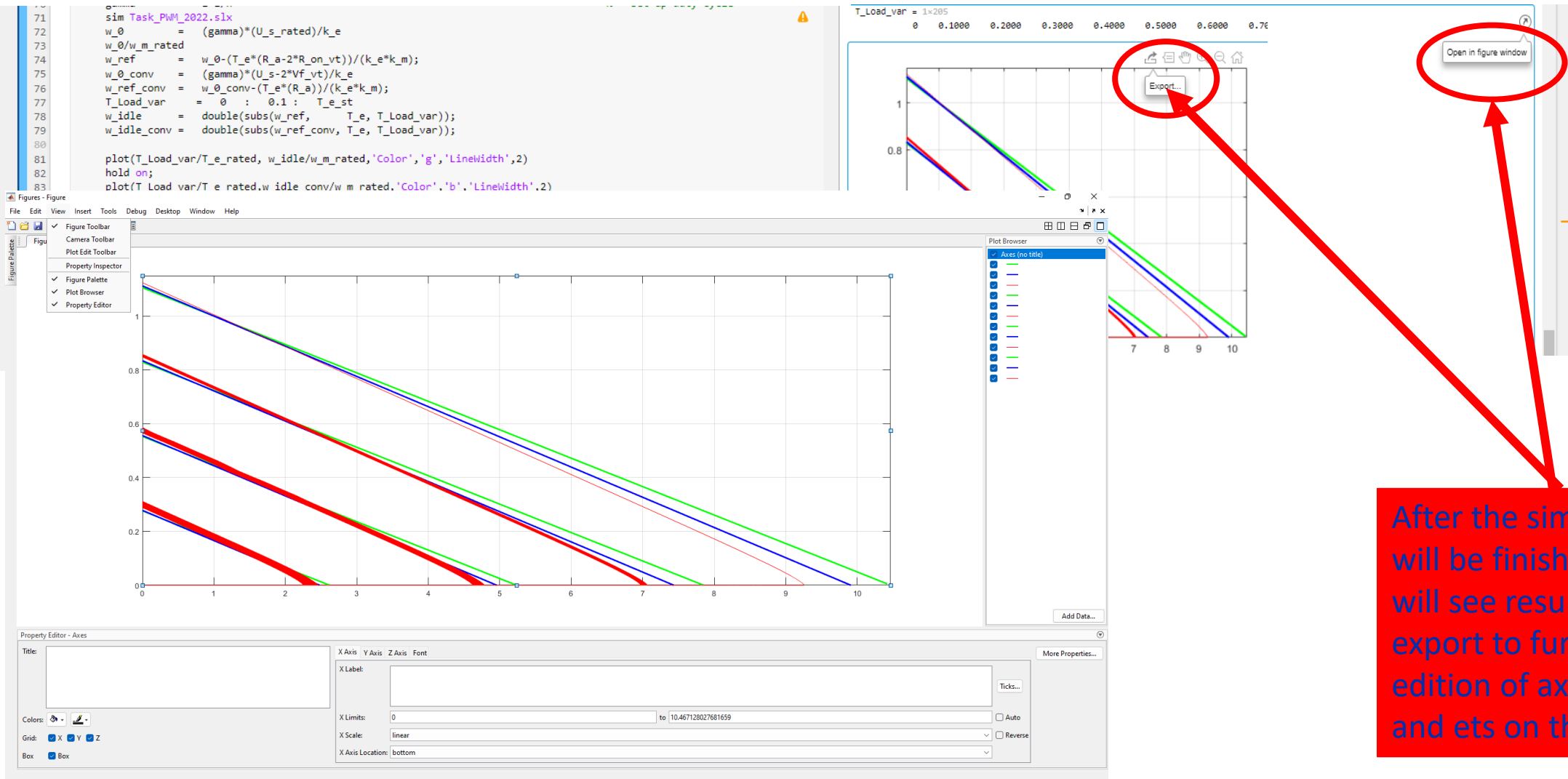
```
figure
syms T_e
for i = 1 : 1 : n
    gamma = i*1/n; % - set up duty cycle
    sim Actuators_Lab3_PWM_R2022b.slx % - this file should be in the same folder with Lab3.mlx
    w_0 = (gamma)*(U_sRated)/k_e;
    w_ref = w_0-(T_e*(R_a))/(k_e*k_m);
    w_0_conv = (gamma)*(U_s-2*V_f_vt)/k_e;
    w_ref_conv = w_0_conv-(T_e*(R_a+2*R_on_vt))/(k_e*k_m);
    T_load_var = 0 : 0.1 : T_e_st;
    w_idle = double(subs(w_ref, T_e, T_load_var));
    w_idle_conv = double(subs(w_ref_conv, T_e, T_load_var));
    plot(T_load_var/T_eRated, w_idle/w_mRated, 'Colon', 'g', 'LineWidth', 2);
    hold on;
    plot(T_load_var/T_eRated, w_idle_conv/w_mRated, 'Colon', 'b', 'LineWidth', 2);
    hold on;
    plot(Current_speed.signals(3).values*k_m/T_eRated, Current_speed.signals(2).values/w_mRated, 'Colon', 'r', 'LineWidth', 0.5);
    hold on;
end
grid on;
if f_sw==f_sw_opt_s_sw
    SW_type='Symmetric';
elseif f_sw==f_sw_opt_n_sw
    SW_type='Asymmetric';
else
    SW_type='Not set'
end
xlim([0 T_e_st/T_eRated])
ylim([0 1.15])
xlabel('T_e / T_eRated')
ylabel('omega / omega_mRated')
legend('DC Drive theoretical characteristic', 'DC Drive with power converter', 'DC Drive with PWM simulation', 'Location', 'northoutside')
v=axis;
text(T_e_st/T_eRated-4, 0.7, {
    strcat('U_sRated', num2str(U_sRated, '%3.2f'), ' [V] ');...
    strcat('U_s', num2str(U_s, '%3.2f'), ' [V] ');...
    strcat('f_sw', num2str(f_sw, '%3.2f'), ' [Hz] ');...
    strcat('Switching type: ', SW_type);...
    strcat('f_sw_opt_s_sw', num2str(f_sw_opt_s_sw, '%3.2f'), ' [Hz] ');...
    strcat('f_sw_opt_n_sw', num2str(f_sw_opt_n_sw, '%3.2f'), ' [Hz] ');...
    strcat('I_aRated', num2str(I_aRated, '%3.1f'), ' [A] ');...
    strcat('T_eRated', num2str(T_eRated, '%3.1f'), ' [Nm] ');...
    strcat('k_lim', num2str(k_lim, '%3.1f'), ' ');...
});...
'BackgroundColor', [1 1 1])
% hold off;
```



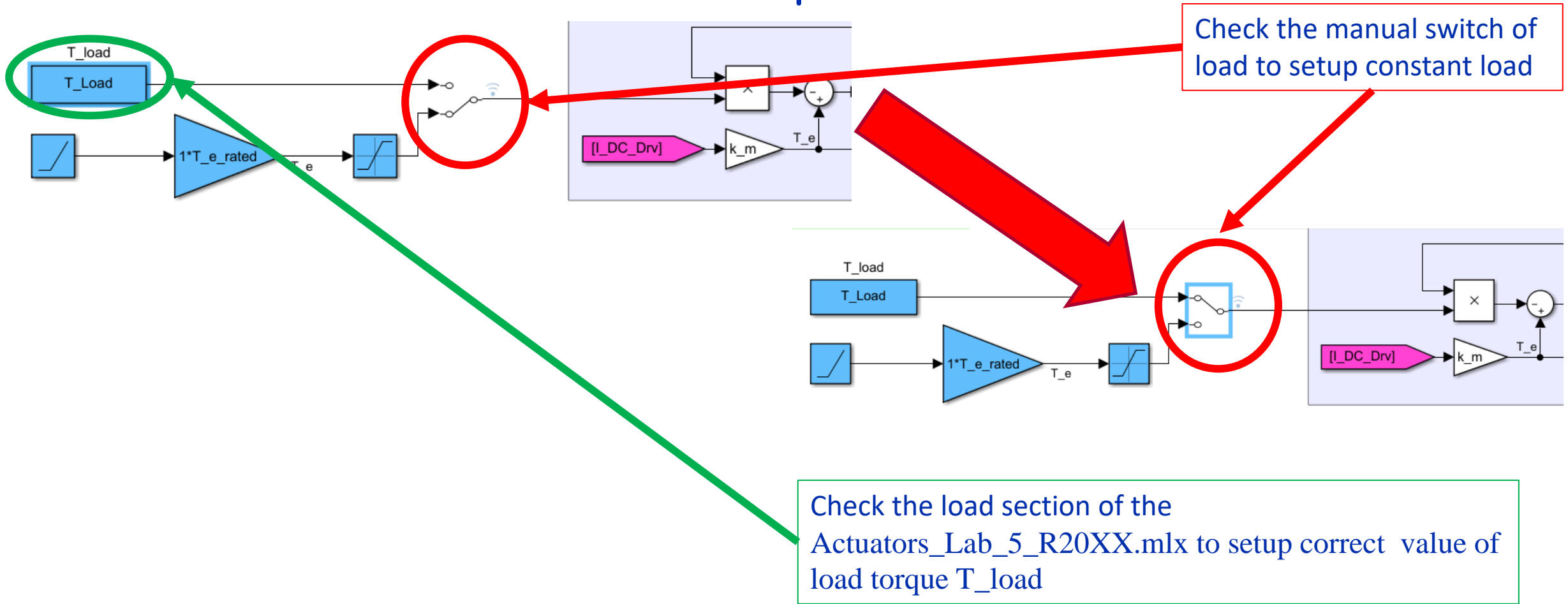
Pay attention to this settings. To obtain a group of characteristics it is recommended to select appropriate switching method. In this case you will get results as 4 characteristics, one of them will be for duty cycle  $\gamma = 0.5$

But after this experiment it recommended to setup  $\gamma = \gamma_{all}(n)$  to perform correct efficiency analysis

## Step 3



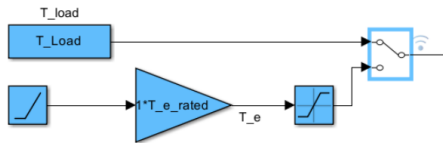
## Step 4





## Step 4

Set up  $\gamma = 0.5$  and  $T_{load} = T_{e\_rated}$  and comment "Ctrl+R" lines 94 - 140 for energy efficiency experiment



You may uncomment frequency required and evaluate this selection only with F9

```
gamma = 0.5;
Stop_time = 30*tau_m;
% f_sw for symmetric switching
% f_sw for asymmetric sequential and diagonal switching
T_sw = 1/f_sw;
% Reassigned switching period, s
T_load = k_i_lim * T_e_rated;
% - Load torque set up as constant load;
sim(ModelName);
% - uncomment this line to do the efficiency experiment
```

or

```
gamma = 0.5;
Stop_time = 30*tau_m;
f_sw = f_sw_opt_s_sw;
% f_sw for symmetric switching
% f_sw for asymmetric sequential and diagonal switching
T_sw = 1/f_sw;
% Reassigned switching period, s
T_load = k_i_lim * T_e_rated;
% - Load torque set up as constant load;
sim(ModelName);
% - uncomment this line to do the efficiency experiment
```

```
141 gamma = 0.5;
142 Stop_time = 30*tau_m;
143 % f_sw = f_sw_opt_s_sw;
144 % f_sw = f_sw_opt_n_sw;
145 T_sw = 1/f_sw;
146 T_load = k_i_lim * T_e_rated;
147 sim(ModelName);
```

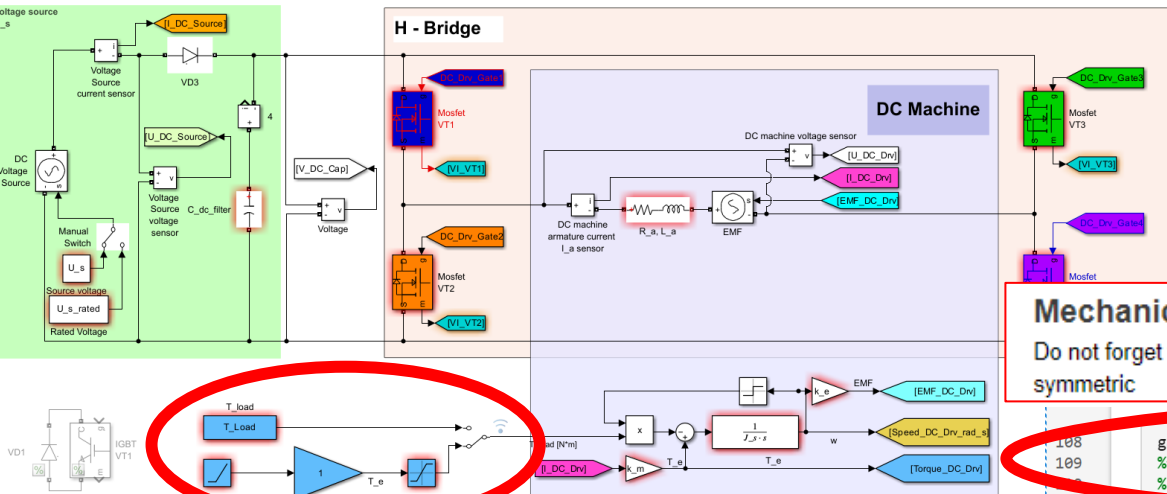
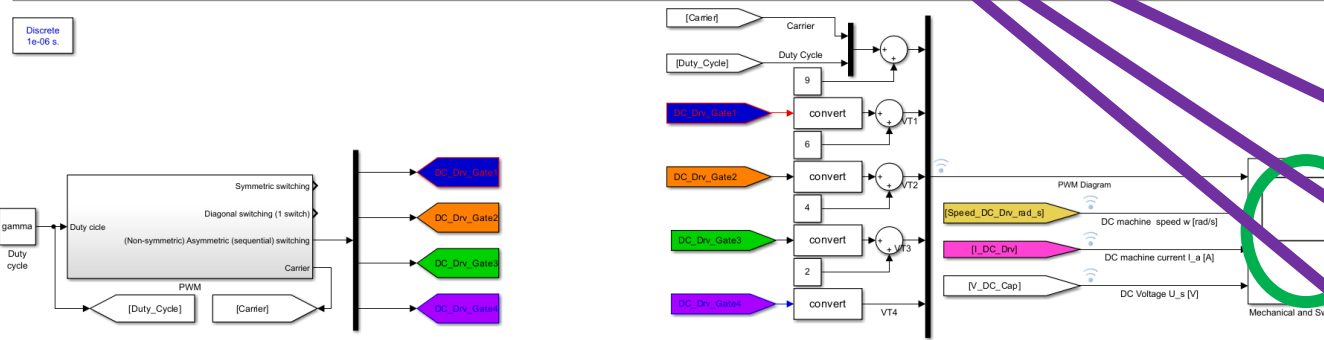
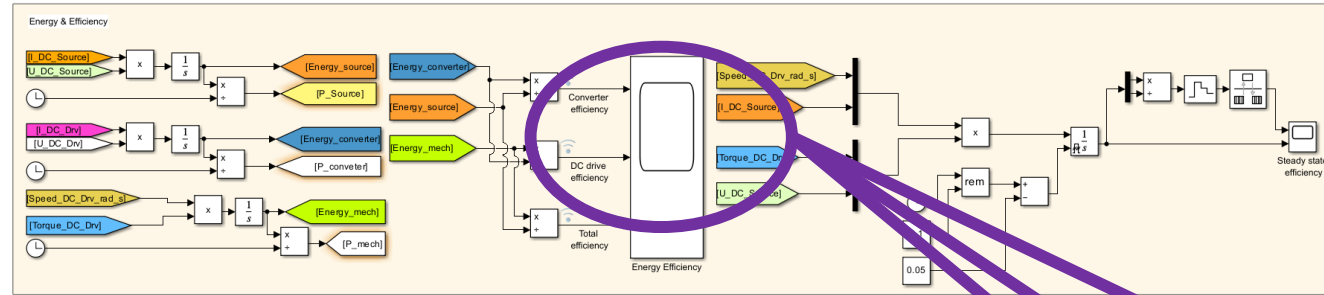
Evaluate Selection in Command Window F9	
Open Selection	Ctrl+D
Help on Selection	F1
Copy Output	
Copy All Output	
Cut	Ctrl+X
Copy	Ctrl+C
Paste	Ctrl+V
Wrap Comments	
Comment	Ctrl+J
Uncomment	Ctrl+R
Duplicate Line(s)	Ctrl+Shift+R
Convert Between Code and Text	Ctrl+Shift+C
Change Case	Ctrl+E
Smart Indent	Ctrl+Shift+A
Convert to Function	Ctrl+I
Convert to Local Function	

```
% figure
% syms T_e
% for i = 1 : 1 : n
%     gamma = gamma_all(i)
% - set up duty cycle
%
% sim(ModelName)
% - this file should be in the same folder with Lab3.mlx
%
% w_0 = (gamma)*(U_s_rated)/k_e;
% w_ref = w_0-(T_e*(R_a))/(k_e*k_m);
% w_0_conv = (gamma)*(U_s-2*f_vt)/k_e;
% w_ref_conv = w_0_conv-(T_e*(R_a+2*R_on_vt))/(k_e*k_m);
% T_load_var = 0 : 0.1 : T_e_st;
% w_idle = double(subs(w_ref, T_e, T_load_var));
% w_idle_conv = double(subs(w_ref_conv, T_e, T_load_var));
% plot(T_load_var/T_e_rated, w_idle/w_m_rated, 'Color', 'g', 'LineWidth', 2);
% hold on;
% plot(T_load_var/T_e_rated, w_idle_conv/w_m_rated, 'Color', 'b', 'LineWidth', 2);
% hold on;
% plot(Current_speed.signals(3).values*k_m/T_e_rated, Current_speed.signals(2).values/w_m_rated, 'Color', 'r', 'LineWidth', 0.5);
% hold on;
% end
% R_a = R_a-2*R_on_vt
% - Full active resistance of armature circuit (Ohm)
% grid on;
% if f_sw==f_sw_opt_s_sw
%     SW_type='Symmetric';
% elseif f_sw==f_sw_opt_n_sw
%     SW_type='Asymmetric';
% else
%     SW_type='Not set'
% end
% xlim([0 T_e_st/T_e_rated])
% ylim([0 1.15])
% xlabel('T_e / T_e_r_a_t_e_d')
% ylabel('\omega / \omega_m_r_a_t_e_d')
% legend('DC Drive theoretical characteristic', 'DC Drive with power converter', 'DC Drive with PWM simulation', 'Location', 'northoutside')
% v=axis;
% text(T_e_st/T_e_rated-4, 0.7, { strcat('U_s_r_a_t_e_d=', num2str(U_s_rated, '%3.2f'), ' [V] ');...
%     strcat('U_s=', num2str(U_s, '%3.2f'), ' [V] ');...
%     strcat('f_sw=', num2str(f_sw, '%3.2f'), ' [Hz] ');...
%     strcat('Switching type: ', SW_type, ' ');...
%     strcat('f_sw_o_p_t_s_sw=', num2str(f_sw_opt_s_sw, '%3.2f'), ' [Hz] ');...
%     strcat('f_sw_o_p_t_n_sw=', num2str(f_sw_opt_n_sw, '%3.2f'), ' [Hz] ');...
%     strcat('I_a_r_a_t_e_d=', num2str(I_a_rated, '%3.1f'), ' [A] ');...
%     strcat('T_e_r_a_t_e_d=', num2str(T_e_rated, '%3.1f'), ' [Nm] ');...
%     strcat('k_i_lim=', num2str(k_i_lim, '%3.1f'), ' ') },...
%     'BackgroundColor', [1 1 1])
%
%
% hold off;
```

Pay attention to this settings. You may comment lines 64-107 and run selection 108-113

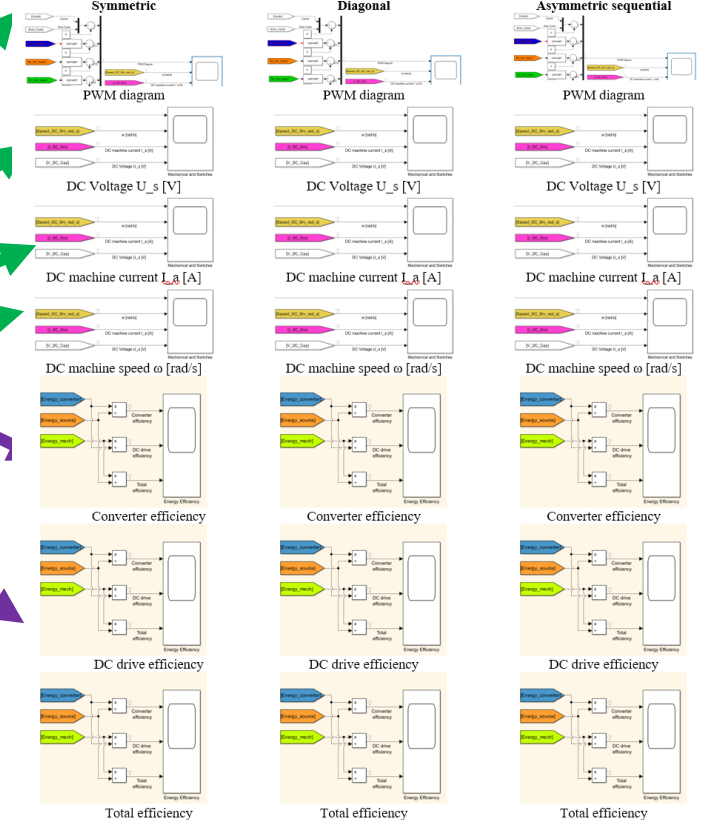
Do not forget to switch T\_load to constant block





### Part 4. Simulation results

- Analyze drive parameters with different pulse width with duty cycle  $\gamma = 0.75$  and  $T_{load} = k_{tim} \cdot T_{e\_rated}$



### Mechanical characteristic

Do not forget to change switching frequency  $f_{sw}$  when changing switching method from Symetric to any other or vice versa any asymmetric to symmetric

```

108 gamma = 0.75;
109 %f_sw = f_sw_opt_s_sw; % f_sw for symmetric switching
110 %f_sw = f_sw_opt_n_sw; % f_sw for asymmetric sequential and diagonal switching
111 %f_sw = 1/f_sw; % Reassigned switching period, s
112 T_Load = k_tlm * T_e_rated; % Load torque set up as constant load;
113 %sim Actuators_Lab3_PWM_R020b.slx % - uncomment this line to do the efficiency experiment
    
```

Fulfill the template and upload it: <https://clck.ru/34SRNH>

**1<sup>st</sup> Deadline is the 9<sup>th</sup> of April (Beijing 23:59 GMT+8 )**  
**09/ 04 /2025**



Student name: \_\_\_\_\_ Date of submission \_\_\_\_\_  
HDU ID \_\_\_\_\_ Student ITMO ID \_\_\_\_\_

### Part 1. Evaluate missing parameters

Open **Actuators\_Lab3\_PWM\_R202\_slx** model and **Actuators\_Lab3\_R202\_mlx** Drive parameters

$U_{s,rated}$  = \_\_\_\_\_ - Rated source voltage, V;  
 $n_{rated}$  = \_\_\_\_\_ - Rated rotating speed, rpm;  
 $f_{sw}$  = \_\_\_\_\_ - PWM frequency, Hz;  
 $R_a$  = \_\_\_\_\_ - Resistance of DC machine winding,  $\Omega$ ;  
 $L_a$  = \_\_\_\_\_ - Armature inductance, H;  
 $J_s$  = \_\_\_\_\_ - Moment of inertia,  $kg \cdot m^2$ ;  
 $I_{a,rated}$  = \_\_\_\_\_ - Anchor rated current of DC machine, A;  
 $k_{lim} = \frac{T_{e,max}}{T_{e,rated}}$  = \_\_\_\_\_ - Maximum current limit, A.

### Evaluations:

$P = U_{s,rated} \cdot I_{a,rated}$  = \_\_\_\_\_ - Power, W;  
 $I_{a,sc} = \frac{U_{s,rated}}{R_a}$  = \_\_\_\_\_ - Short circuit current, A;  
 $\omega_{m,rated} = \frac{2 \cdot \pi \cdot n_{rated}}{60}$  = \_\_\_\_\_ - Rated rotating speed, rad/s;  
 $k_e = \frac{(U_{s,rated} - R_a I_{a,rated})}{\omega_{m,rated}}$  = \_\_\_\_\_ - EMF constant, V\*s/rad;  
 $k_m = k_e$  = \_\_\_\_\_ - Electromechanical constant, N · m / A;  
 $T_{e,rated} = k_m \cdot I_{a,rated}$  = \_\_\_\_\_ - Rated Torque of the DC machine, N · m;  
 $T_{e,max} = k_{lim} \cdot T_{e,rated}$  = \_\_\_\_\_ - Maximum torque, N · m;  
 $I_{lim} = k_{lim} \cdot I_{a,rated}$  = \_\_\_\_\_ - Maximum current, N · m;  
 $T_{s,st} = k_m \cdot I_{a,sc}$  = \_\_\_\_\_ - Starting torque, N · m;  
 $\eta_{eff,rated} = \frac{\omega_{m,rated} T_{e,rated}}{P} \cdot 100\%$  = \_\_\_\_\_ - Rated efficiency, %;  
 $\tau_e = \frac{L_a}{R_a}$  = \_\_\_\_\_ - Electromagnetic time constant, s;  
 $\omega_0 = \frac{U_{s,rated}}{k_e}$  = \_\_\_\_\_ - Idle speed, rad/s;  
 $\tau_m = \frac{J_s \omega_0}{T_{s,st}}$  = \_\_\_\_\_ - Electromechanical time constant, s

### Part 2. Evaluate parameters of the system with PWM

Transistor switched on circuit parameters  
 $V_{gt} = 0$  - IGBT Forward voltage  $V_f$  at current  $I_a \approx 0$ , V (For MOSFET may be considered equal to 0);  
 $V_{fcsa} = 1.3$  - Forward voltage  $V_f$  at current  $I_a = I_{a,rated} \cdot k_{lim}$ , V;  
 $R_{onst} = \frac{(V_{fcsa} - V_{fcs})}{I_{lim}}$  = \_\_\_\_\_ - MOSFET / IGBT resistance  $R_{on}$ ,  $\Omega$ ;  
Snubber circuit parameters  
 $C_s = 330e-9$  - Snubber capacitance, F;  
 $R_s = 1e6$  - Snubber resistance,  $\Omega$ ;  
Reverse (antiparallel) diode parameters  
 $V_{fcd} = 0.65$  - Internal (antiparallel) diode forward voltage  $V_f$  at current  $I_a \approx 0$ , V;  
 $V_{fcds} = 0.75$  - Internal (antiparallel) diode forward voltage at current  $I_{lim}$ , V;  
 $R_{onrd} = \frac{(V_{fcds} - V_{fcd})}{I_{lim}}$  = \_\_\_\_\_ - Internal (antiparallel) diode resistance  $R_d$ ,  $\Omega$ ;

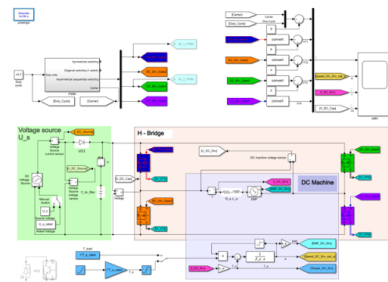


Figure 1 – DC drive system under test

### Part 3. Simulation results

- Compare diagonal (one switch) and symmetric switching. Optimal switching frequency evaluation (symmetrical switching)

$$\alpha_K = \frac{I_{lim}}{I_a} = \frac{0.332 \cdot \sqrt{\frac{R_{on}}{L_a}}}{\sqrt{L_a}(\tau_{on} + \tau_{off})} \text{ Hz}$$

$$f_{sw,opt} = 0.26 \cdot \sqrt{\frac{R_{on}}{L_a}(\tau_{on} + \tau_{off})} \text{ Hz}$$

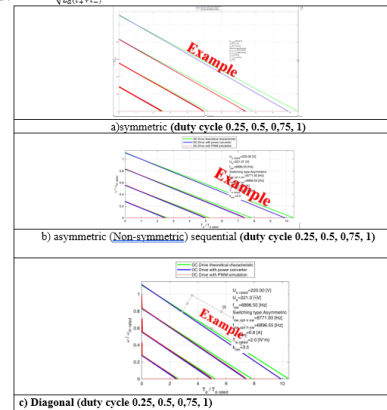


Figure 2 – DC drive mechanical characteristics  
NB! with new parameters your result will be slightly different!

### Part 4. Simulation results

- Analyze drive parameters with different pulse width with duty cycle  $\gamma = 0.75$  and  $I_{load} = k_{lim} \cdot T_{e,rated}$

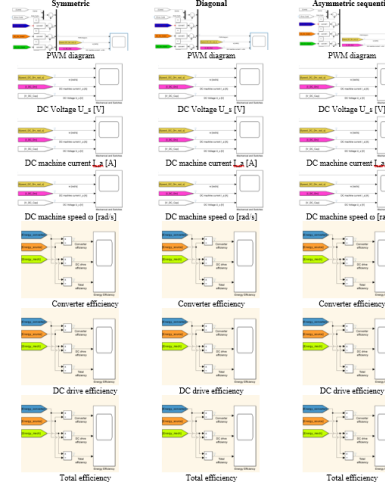


Figure 3 – DC drive energy efficiency characteristics

### EXAMPLE:

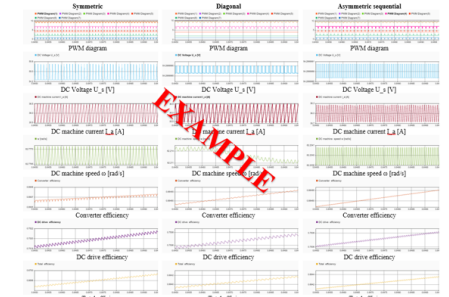


Figure 3 – DC drive energy efficiency characteristics

- Analyze drive parameters with different pulse width with duty cycle ( $\gamma = 0.75$  and  $I_{load} = k_{lim} \cdot T_{e,rated}$ )

### Conclusions

Results of comparison efficiency, current and speed ripple in case of symmetrical, diagonal, and sequential switching.