



**iTMO**

**TEST 2**

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# Preliminary

The test consists of 10 questions with answers (5 points max)



You have 1 attempt.

Any new attempt gives you 0,5-point penalty.

In the case of anonymous answer (like «Name – 1, HDU ID – 1 .....»)  
ALL students will receive 0,5-point penalty for each case.

All questions are in this presentation.  
Form with answers can be filled here:

<https://forms.yandex.ru/u/67cdd0b0eb61469181a62610/>



## Question 1

Consider the follows mechanical system:

$T_M$  – the torque of the motor

$\omega_M$  – the velocity of the motor

$N_1$  – number of teeth of the first gear

$N_2$  – number of teeth of the second gear

$D_c$  – diameter of the cylinder

$m_c$  – mass of the cylinder

$m_L$  – mass of the load

$v_L$  – speed of the load

$$N_1 = 5$$

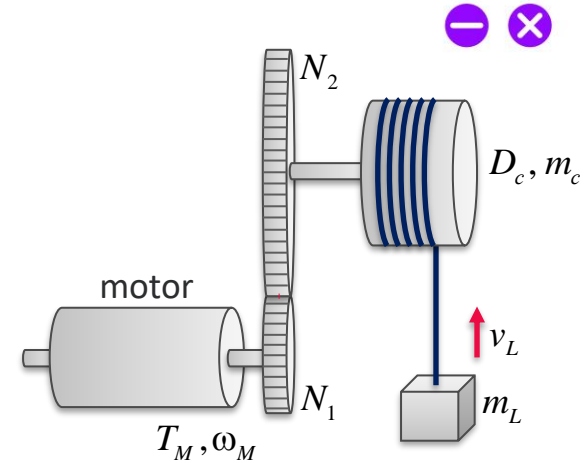
$$N_2 = 15$$

$$D_c = 0.2 \text{ m}$$

$$m_c = 50 \text{ kg}$$

$$v_L = 0.25 \text{ m/s}$$

$$m_L = 200 \text{ kg}$$



Find the equivalent inertia of the mass  $m_L$  converted to the motor side

a)  $J_{Le} \approx 2 \text{ kg} \cdot \text{m}^2$

b)  $J_{Le} \approx 0.67 \text{ kg} \cdot \text{m}^2$

c)  $J_{Le} \approx 0.28 \text{ kg} \cdot \text{m}^2$

d)  $J_{Le} \approx 18 \text{ kg} \cdot \text{m}^2$

e)  $J_{Le} \approx 0.22 \text{ kg} \cdot \text{m}^2$

f) not enough data to answer

## Question 2

Consider the follows mechanical system:

$T_M$  – the torque of the motor

$\omega_M$  – the velocity of the motor

$N_1$  – number of teeth of the first gear

$N_2$  – number of teeth of the second gear

$D_c$  – diameter of the cylinder

$m_c$  – mass of the cylinder

$m_L$  – mass of the load

$v_L$  – speed of the load

$$N_1 = 15$$

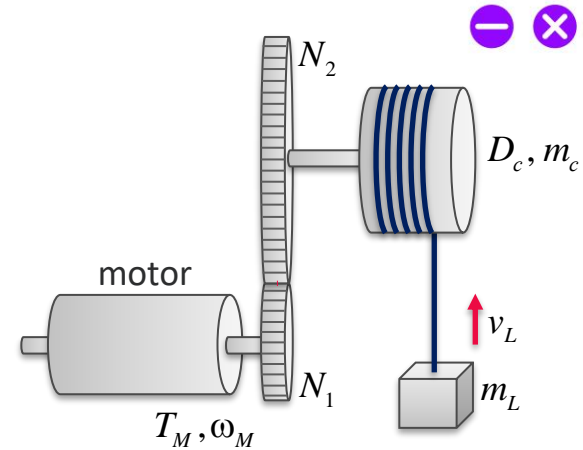
$$N_2 = 60$$

$$D_c = 0.3 \text{ m}$$

$$m_c = 20 \text{ kg}$$

$$v_L = 0.4 \text{ m/s}$$

$$m_L = 150 \text{ kg}$$



Find the torque of the motor that is needed to lift the load of mass  $m$  with the speed  $v$

a)  $T_M \approx 220.7 \text{ Nm}$

b)  $T_M \approx 13.8 \text{ Nm}$

c)  $T_M \approx 1.4 \text{ Nm}$

d)  $T_M \approx 55.2 \text{ Nm}$

e)  $T_M \approx 3.4 \text{ Nm}$

f) not enough data to answer

## Question 3

Consider the follows mechanical system:

$T_M$  – the torque of the motor

$\omega_M$  – the velocity of the motor

$N_1$  – number of teeth of the first gear

$N_2$  – number of teeth of the second gear

$D_c$  – diameter of the cylinder

$m_c$  – mass of the cylinder

$m_L$  – mass of the load

$v_L$  – speed of the load

$$N_1 = 10$$

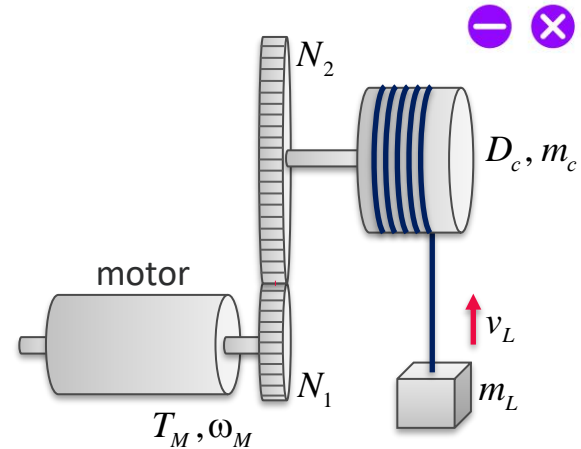
$$N_2 = 50$$

$$D_c = 0.4 \text{ m}$$

$$m_c = 25 \text{ kg}$$

$$v_L = 0.5 \text{ m/s}$$

$$m_L = 300 \text{ kg}$$



Find the full inertia of the load converted to motor side (assume the inertia of motor's shaft and inertias of gears are equal to zero)

a)  $J_e \approx 0.02 \text{ kg} \cdot \text{m}^2$

b)  $J_e \approx 0.48 \text{ kg} \cdot \text{m}^2$

c)  $J_e \approx 0.5 \text{ kg} \cdot \text{m}^2$

d)  $J_e \approx 12.02 \text{ kg} \cdot \text{m}^2$

e)  $J_e \approx 0.98 \text{ kg} \cdot \text{m}^2$

f) not enough data to answer

## Question 4

Consider the follows mechanical system:

$T_M$  – the torque of the motor

$\omega_M$  – the velocity of the motor

$N_1$  – number of teeth of the first gear

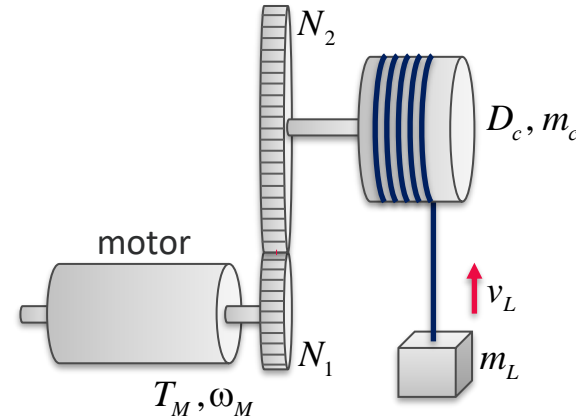
$N_2$  – number of teeth of the second gear

$D_c$  – diameter of the cylinder

$m_c$  – mass of the cylinder

$m_L$  – mass of the load

$v_L$  – speed of the load



How will change the power of the motor if the number of teeth of the second gear ( $N_2$ ) increases twice but speed of the load ( $v_L$ ) will stay the same?

a) increases twice

b) decreases twice

c) increases 4 times

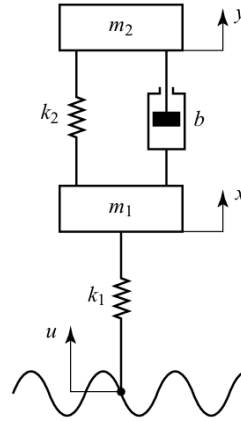
d) decreases 4 times

e) doesn't change

f) not enough data to answer

## Question 5

Consider the follows mechanical system:

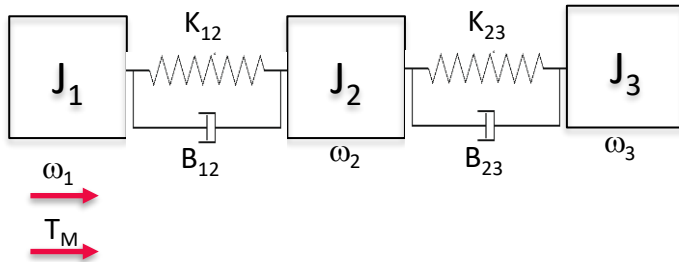


Choose the right differential equation for  $m_2$

- a)  $m_2\ddot{y} = k_2(y - x) + b(\dot{y} - \dot{x})$     b)  $m_2\ddot{y} = -k_1(u - x) - b(\dot{y} - \dot{x})$     c)  $m_2\ddot{y} = -k_2(y - x) - b(\dot{y} - \dot{x}) + u$
- d)  $m_2\ddot{y} = -k_2(y - x) - b(\dot{y} - \dot{x})$     e)  $m_2\ddot{y} = -k_2(y - x)$     f)  $m_2\ddot{y} = k_1(u - x)$

## Question 6

Consider the follows mechanical system:



Choose the right differential equation for  $J_2$

- a)  $J_2 \frac{d\omega_2}{dt} = T_{s12} + b_{12}(\omega_1 - \omega_2) - T_{s23} - b_{23}(\omega_2 - \omega_3) - T_{L2},$
- b)  $J_2 \frac{d\omega_2}{dt} = T_{s12} - b_{12}(\omega_1 - \omega_2) - T_{s23} + b_{23}(\omega_2 - \omega_3) - T_{L2},$
- c)  $(J_1 + J_2) \frac{d\omega_2}{dt} = T_{s12} + b_{12}(\omega_1 - \omega_2) - T_{s23} - b_{23}(\omega_2 - \omega_3) - T_{L2},$
- d)  $J_2 \frac{d\omega_2}{dt} = -T_{s12} + b_{12}(\omega_1 - \omega_2) + T_{s23} - b_{23}(\omega_2 - \omega_3) - T_{L2},$
- e)  $J_2 \frac{d\omega_2}{dt} = T_{s12} + b_{12}(\omega_1 + \omega_2) - T_{s23} - b_{23}(\omega_2 + \omega_3) - T_{L2},$
- f)  $(J_2 + J_3) \frac{d\omega_2}{dt} = T_{s12} + b_{12}(\omega_1 - \omega_2) - T_{s23} - b_{23}(\omega_2 - \omega_3) - T_{L2},$



## Question 7

Consider the mechanical system, that is described by the follows differential equations:

$$\begin{cases} 0.05 \frac{d\omega_1}{dt} = T_M - T_{s12} - 2(\omega_1 - \omega_2) - 3, \\ \frac{dT_{s12}}{dt} = 500(\omega_1 - \omega_2) \\ 0.2 \frac{d\omega_2}{dt} = T_{s12} + 2(\omega_1 - \omega_2) - 1. \end{cases}$$

Calculate the resonant frequency of the mechanical system

a) 111.8 rad/s

b) 55.9 rad/s

c) 17.8 rad/s

d) 4.5 rad/s

e) 223.6 rad/s

f) not enough data to answer

## Question 8

Consider the mechanical system, that is described by the follows differential equations:



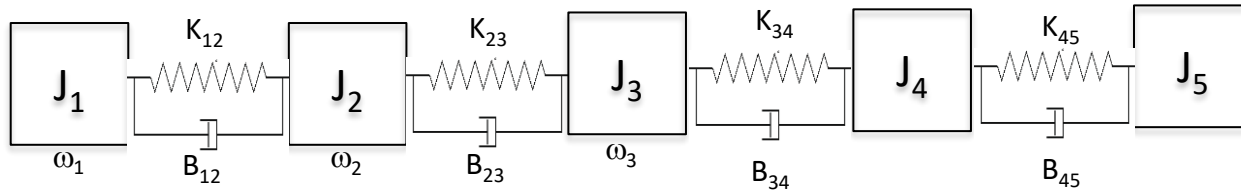
$$\begin{cases} J_1 \frac{d\omega_1}{dt} = T_M - T_{s12} - b_{12}(\omega_1 - \omega_2) - T_{L1}, \\ \frac{dT_{s12}}{dt} = K_{12}(\omega_1 - \omega_2) \\ J_2 \frac{d\omega_2}{dt} = T_{s12} + b_{12}(\omega_1 - \omega_2) - T_{L2}. \end{cases}$$

How will resonant frequency change if load torque  $T_{L2}$  increases twice

- |                      |                    |                              |
|----------------------|--------------------|------------------------------|
| a) increases twice   | b) decreases twice | c) increases 4 times         |
| d) decreases 4 times | e) doesn't change  | f) not enough data to answer |

## Question 9

How many differential equations of the first order we need to describe the dynamic behavior of the velocities of the follows mechanical system:



a) 5

b) 7

c) 9

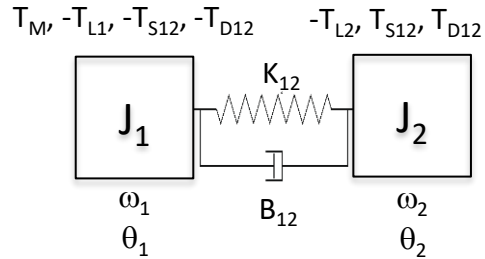
d) 3

e) 1

f) not enough data to answer

## Question 10

Consider the follows mechanical system:



How will change the resonant frequency of the system if  $K_{12}$  decreases twice

- a) increases twice      b) decreases twice      c) doesn't change
- d) decreases  $\sqrt{2}$  times      e) increases  $\sqrt{2}$  times      f) not enough data to answer

**THANK YOU  
FOR YOUR TIME!**

**it's** **MO** *re than a*  
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