



# Laboratory Work 3

## Active filter circuits design and simulation

Nikolai Poliakov

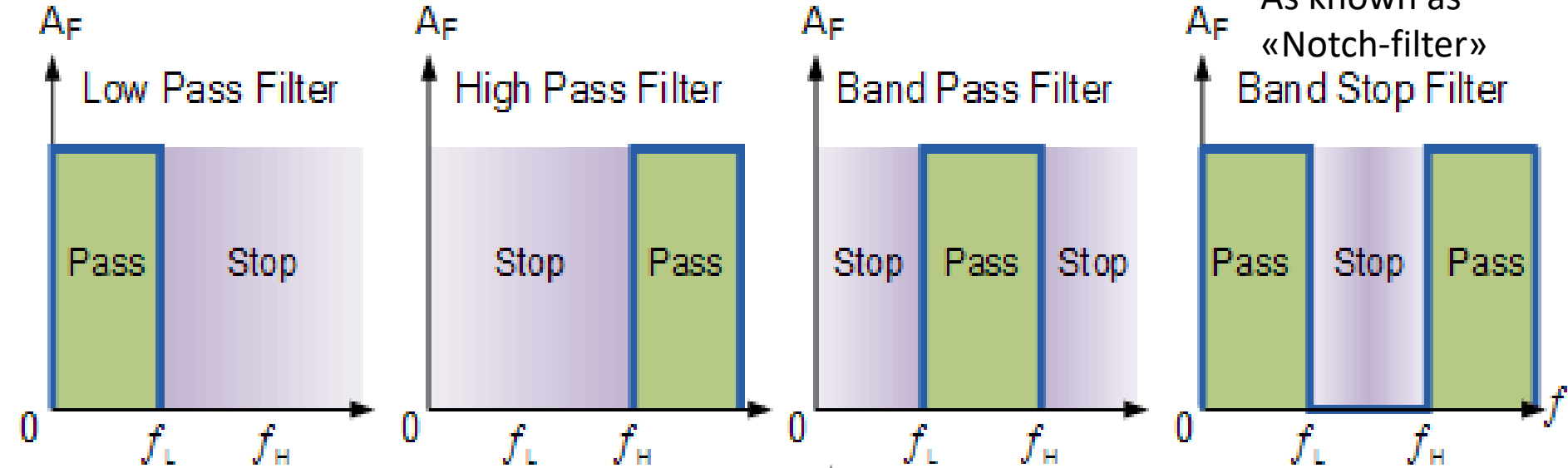
(polyakov\_n\_a@itmo.ru)

Arina Arbuzina

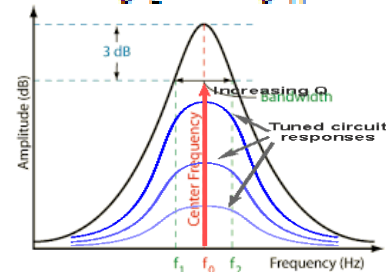
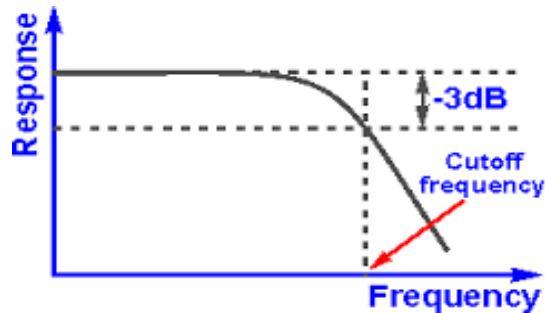
(arbyzina99@gmail.com)

1. Filter approximation theory review
2. Laboratory work 3: ideal and real amplifier comparison
3. Active filter circuits design
4. Second Order Filters
5. Frequency Transformation
6. Step 1: check of scheme gain
7. Step 2: time domain simulation
8. Step 3: Step response (time domain simulation)
9. Step 4: frequency domain simulation)
10. Results and conclusions
11. Uploading report

# Ideal Filter Response Curves



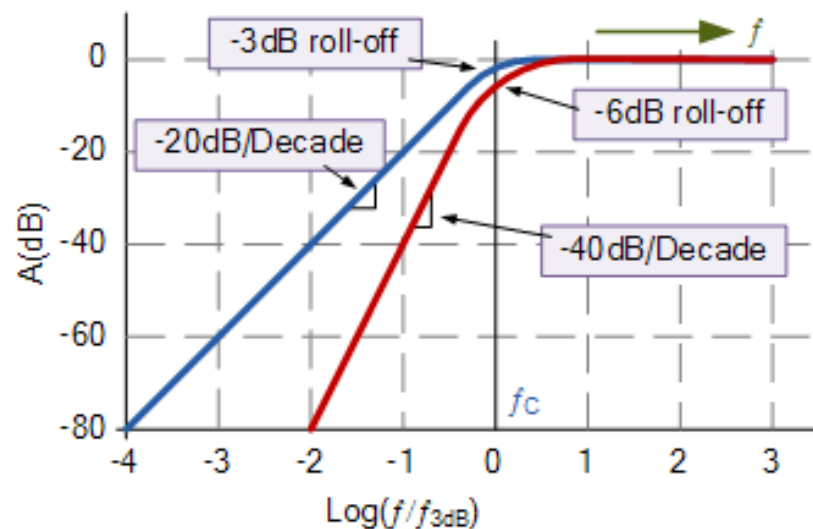
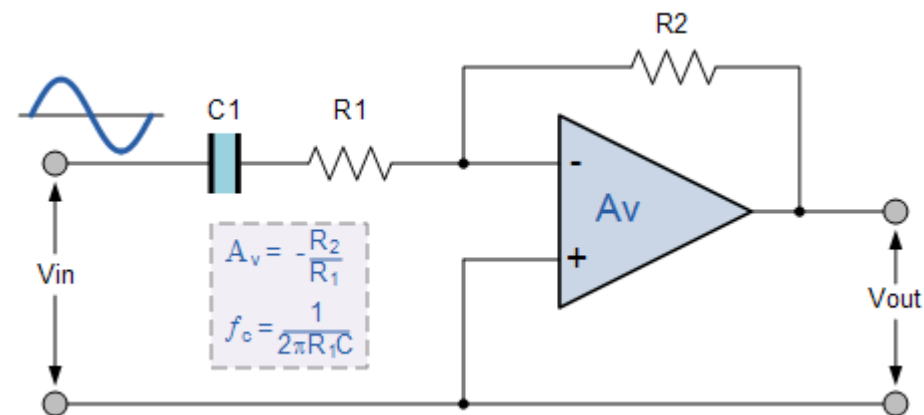
As known as  
«Notch-filter»  
Band Stop Filter



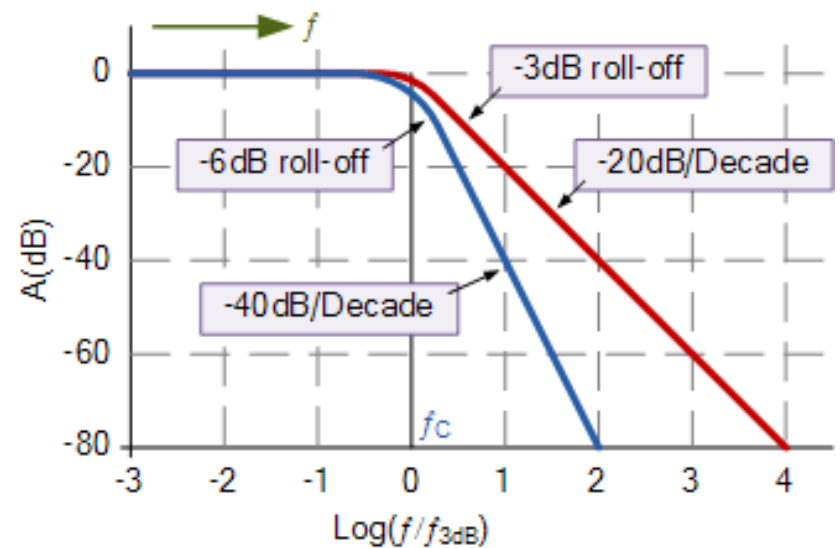
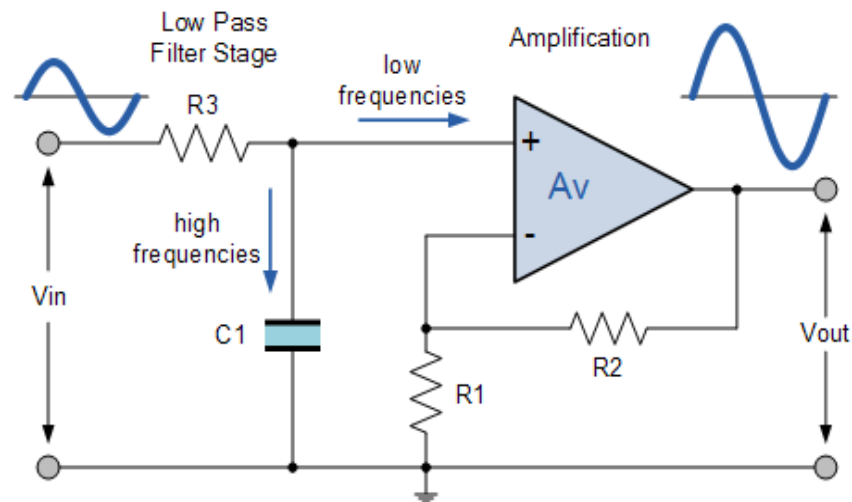
$$Q = \frac{f_c}{f_1 - f_2} = \frac{\text{center frequency}}{\text{3 dB bandwidth}}$$

# Active High Pass Filter

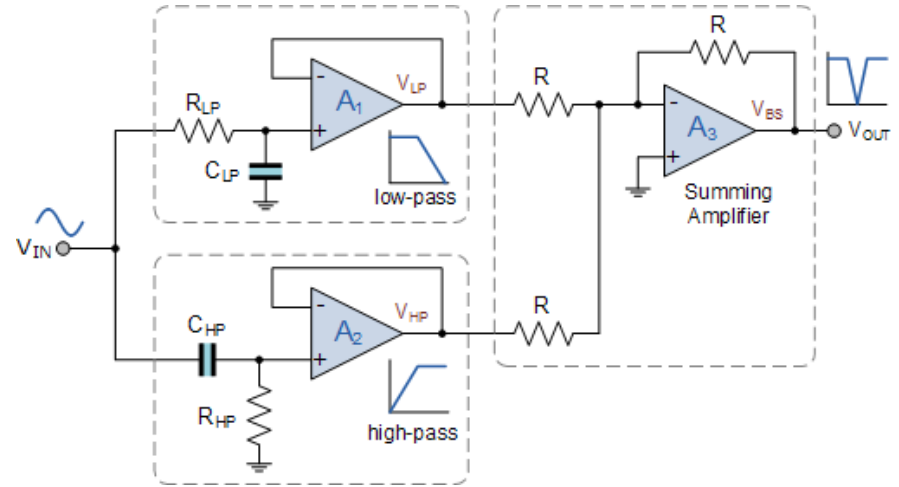
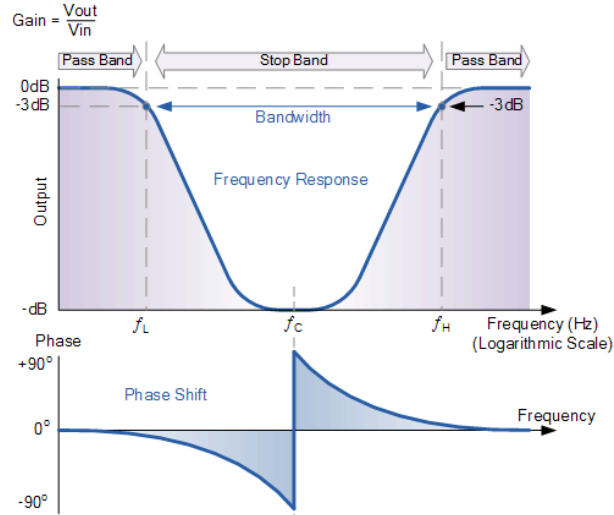
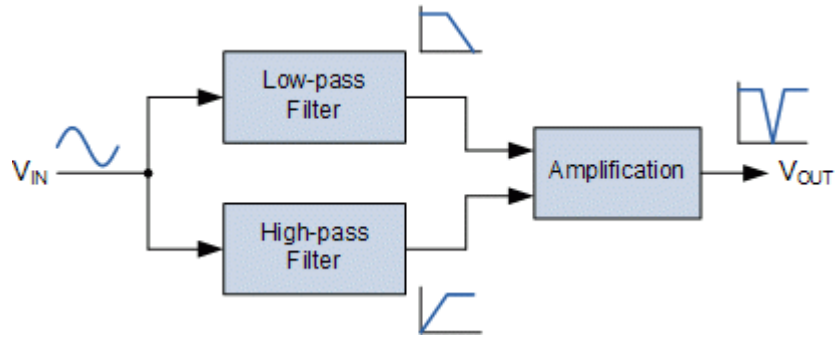
## First-order Filter



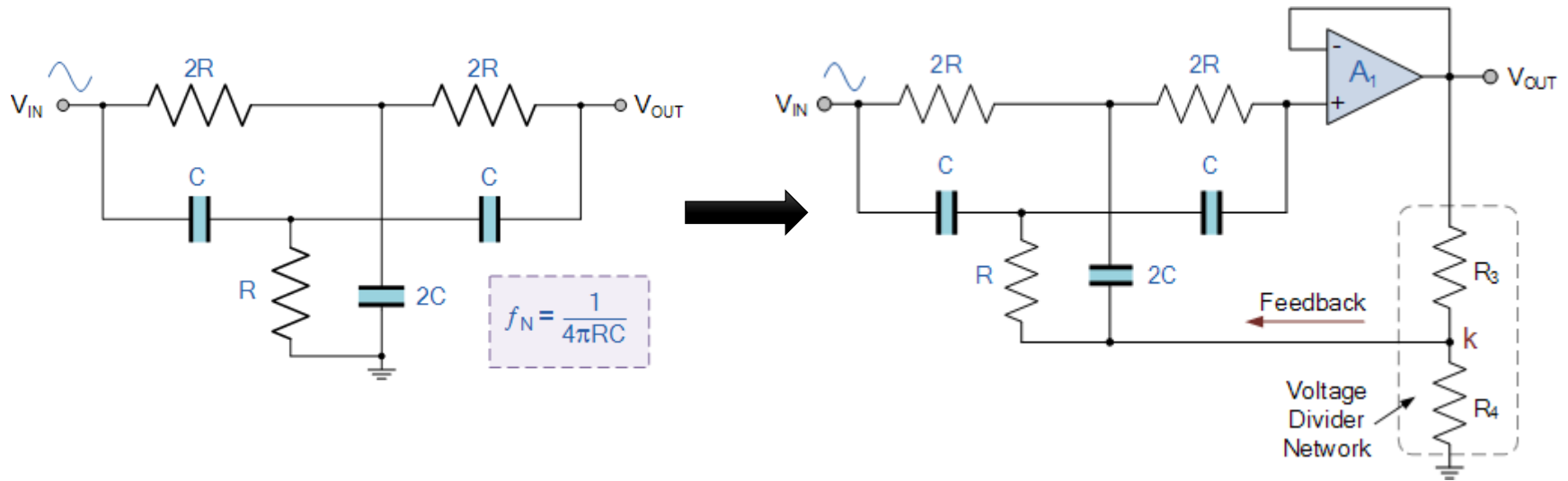
## First-order Filter



# Band Stop Filter



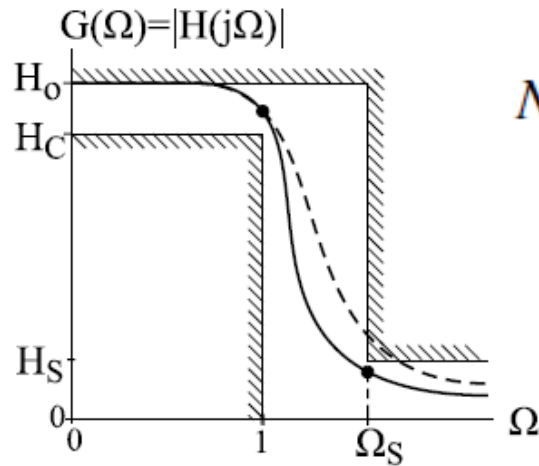
# Notch Filters



# The Butterworth Approximation

$$G(\Omega) = \frac{H_o}{\sqrt{1 + \beta^2 \Omega^{2N}}}$$

$$G(\Omega_S) = \frac{H_o}{\sqrt{1 + \beta^2 \Omega_S^{2N}}} \leq H_S$$



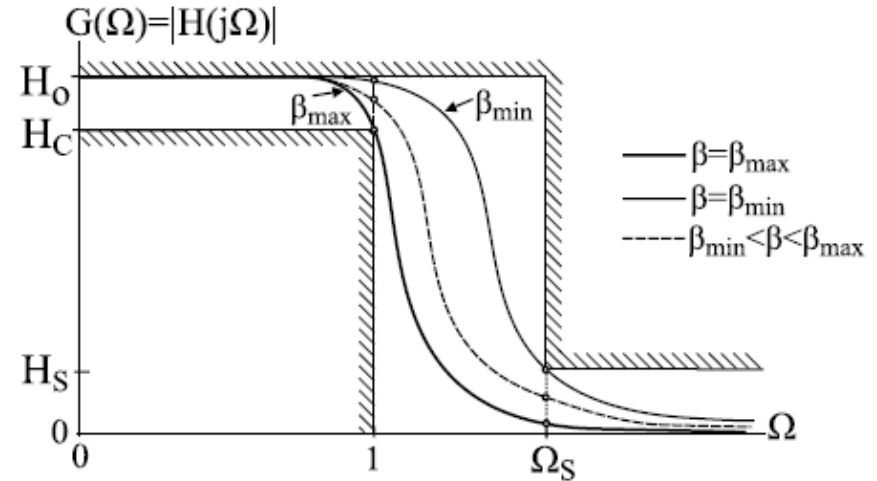
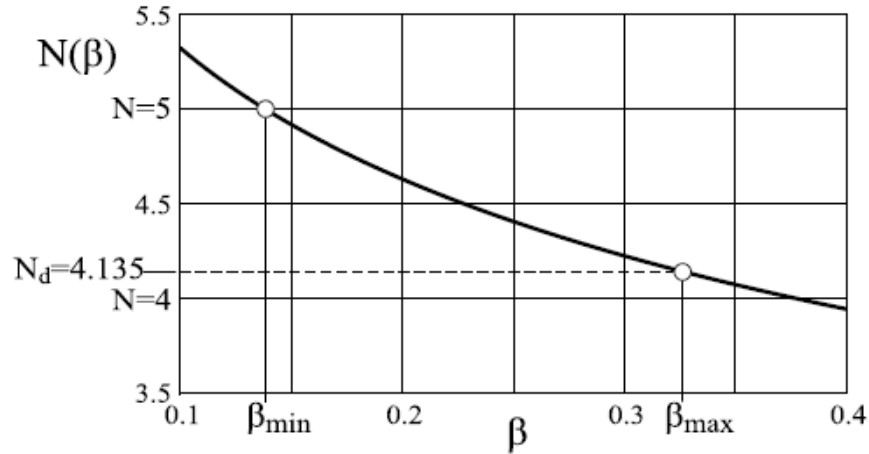
$$N \geq \frac{\log\left(\frac{(H_o/H_S)^2 - 1}{\beta^2}\right)}{2 \log \Omega_S}$$

$$N \geq N_d = \frac{\log\left(\frac{(H_o/H_S)^2 - 1}{\beta^2}\right)}{2 \log \Omega_S}$$

$$n_{f \min} = \frac{\log\left(\frac{\frac{H_o^2}{H_S^2} - 1}{\frac{H_o^2}{H_C^2} - 1}\right)}{2 \log \Omega_S} = \frac{\log\left(\frac{10^{\frac{a_{\min}}{10}} - 1}{10^{\frac{a_{\max}}{10}} - 1}\right)}{2 \log \Omega_S}$$



# The Butterworth Approximation



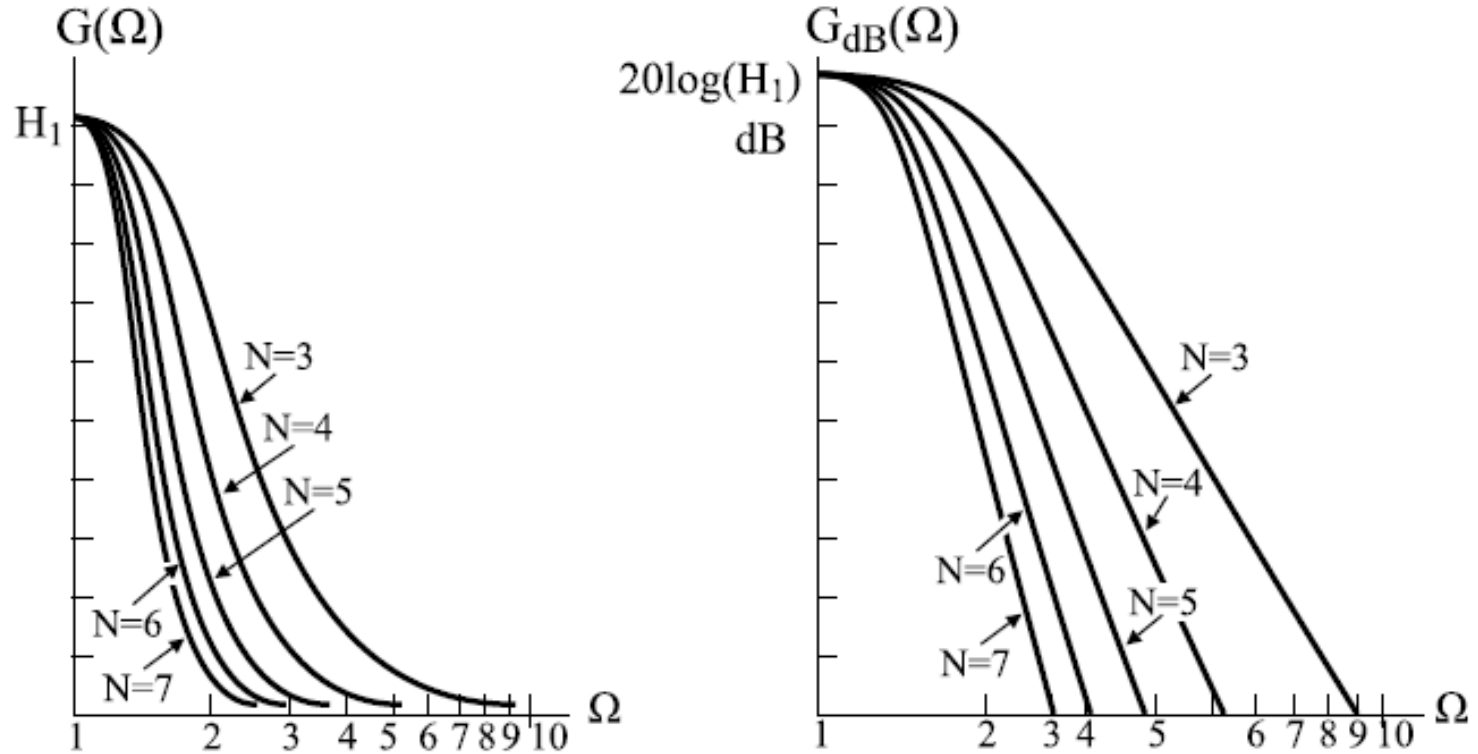
filter designed with normalized specifications

$H_o = 1$ ,  $H_C = 0.95$ ,  $H_S = 0.05$  and  $\Omega_S = 2.7$

$$\beta_{\min} = \frac{\sqrt{\frac{H_o^2}{H_S^2} - 1}}{\Omega_S^N} \leq \beta \leq \sqrt{\frac{H_o^2}{H_C^2} - 1} = \beta_{\max}$$

$$\beta_{\min} = \frac{\sqrt{10^{\frac{\alpha_{\min}}{10}} - 1}}{\Omega_S^N} \leq \beta \leq \sqrt{10^{\frac{\alpha_{\max}}{10}} - 1} = \beta_{\max}$$

# The Butterworth Approximation



$$G_{CH}(\Omega) = \frac{H_o}{\sqrt{1 + \varepsilon^2 C_N^2(\Omega)}}$$

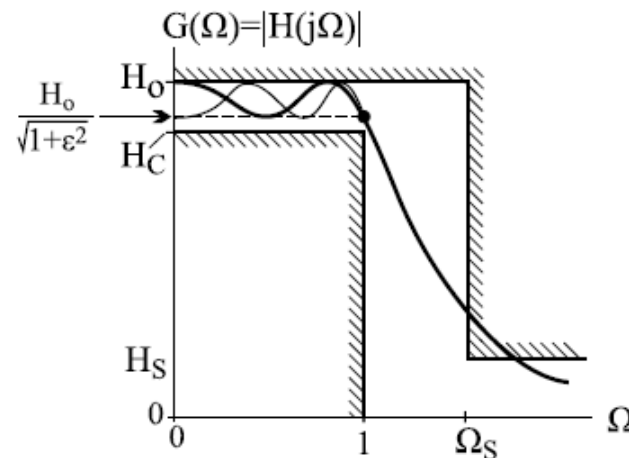
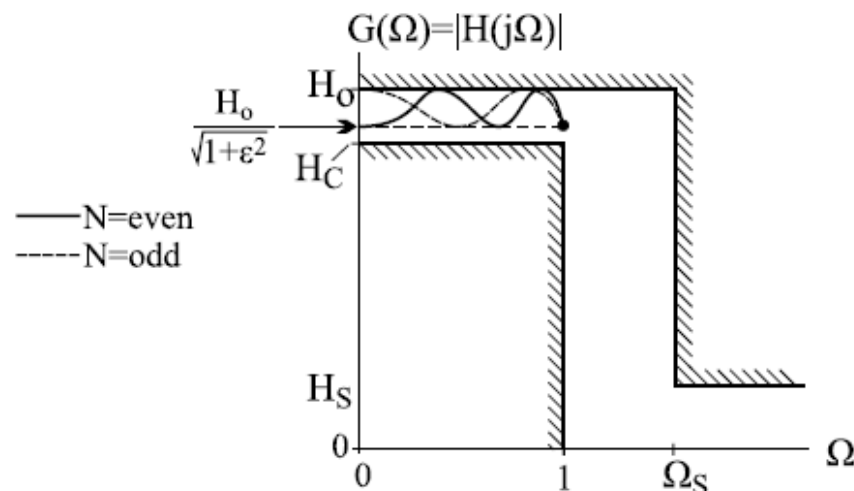
$$\varepsilon \leq \sqrt{\frac{H_o^2}{H_C^2} - 1} = \sqrt{10^{\frac{\alpha_{\max}}{10}} - 1} = \varepsilon_{\max}$$

For  $\varepsilon \leq \varepsilon_{\max}$

$$H_o \geq G_{CH}(\Omega) \geq \frac{H_o}{\sqrt{1 + \varepsilon^2}} \geq H_C$$

For  $\Omega = 1$

$$G_{CH}(1) = \frac{H_o}{\sqrt{1 + \varepsilon^2}} \geq H_C$$



$$G_{CH}(\Omega_S) = \frac{H_o}{\sqrt{1 + \varepsilon^2 C_N^2(\Omega_S)}} \leq H_S$$

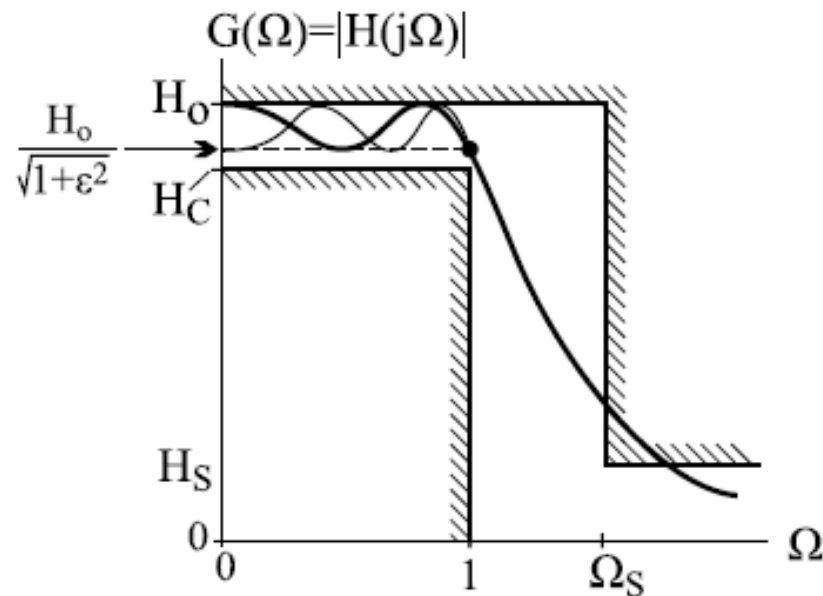
$$\Leftrightarrow C_N^2(\Omega_S) \geq \frac{(H_o/H_S)^2 - 1}{\varepsilon^2}$$

$$\Leftrightarrow N \cosh^{-1}(\Omega_S) \geq \cosh^{-1} \sqrt{\frac{(H_o/H_S)^2 - 1}{\varepsilon^2}}$$

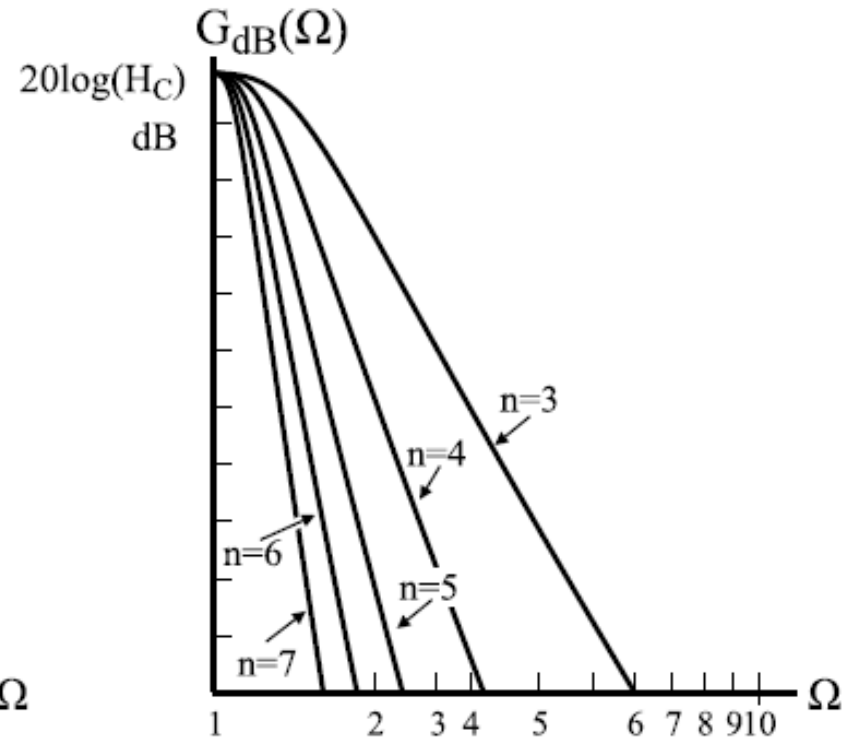
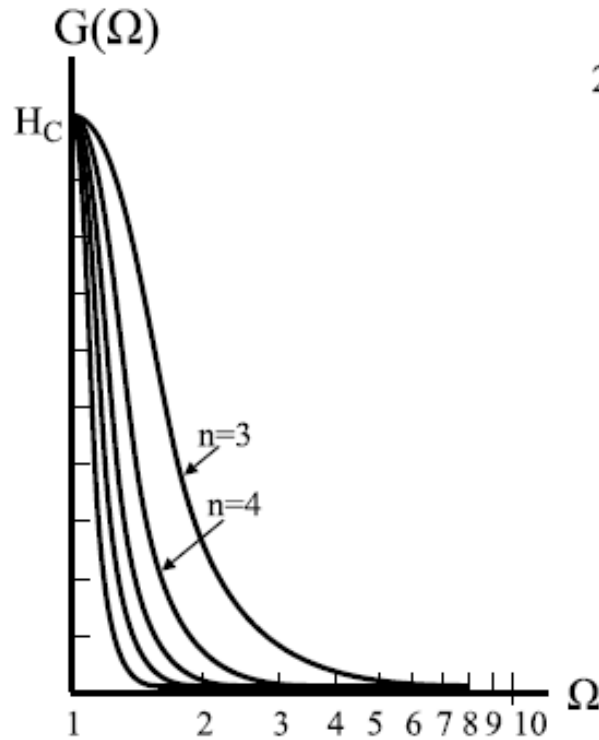
for N:  $N \geq N_d = \frac{\cosh^{-1}(\sqrt{\frac{(H_o/H_S)^2 - 1}{\varepsilon^2}})}{\cosh^{-1}(\Omega_S)}$

$$N \geq N_d = \frac{\cosh^{-1}(\sqrt{\frac{(H_o/H_S)^2 - 1}{\varepsilon_{\max}^2}})}{\cosh^{-1}(\Omega_S)} = \frac{\cosh^{-1}(\sqrt{\frac{(H_o/H_S)^2 - 1}{(H_o/H_C)^2 - 1}})}{\cosh^{-1}(\Omega_S)}$$

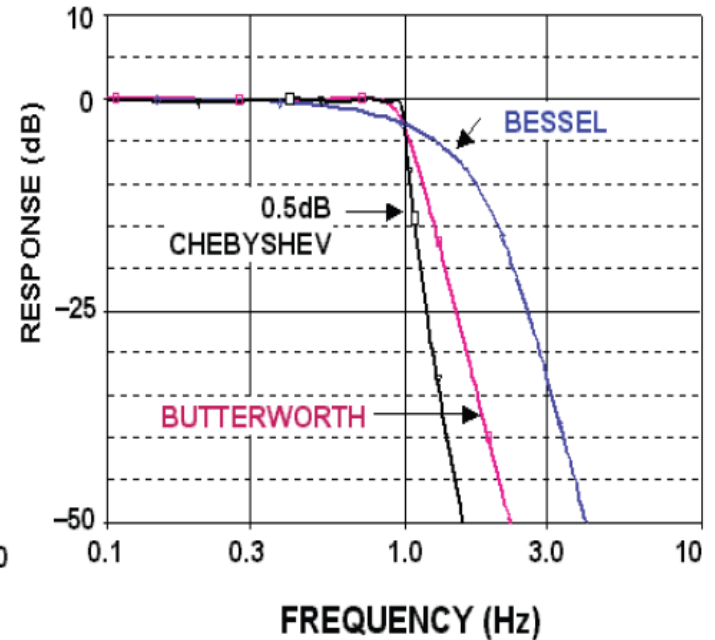
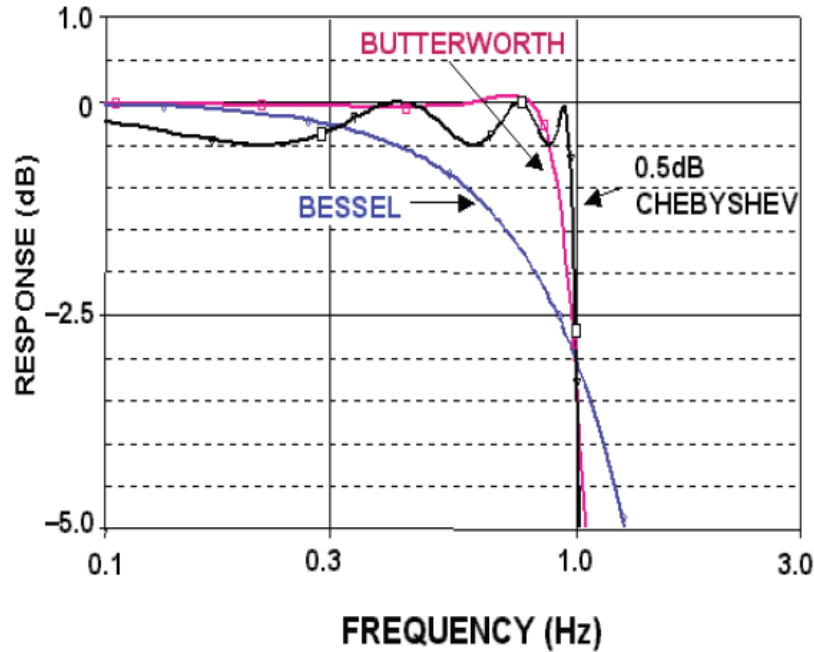
logarithmic gain  
specifications



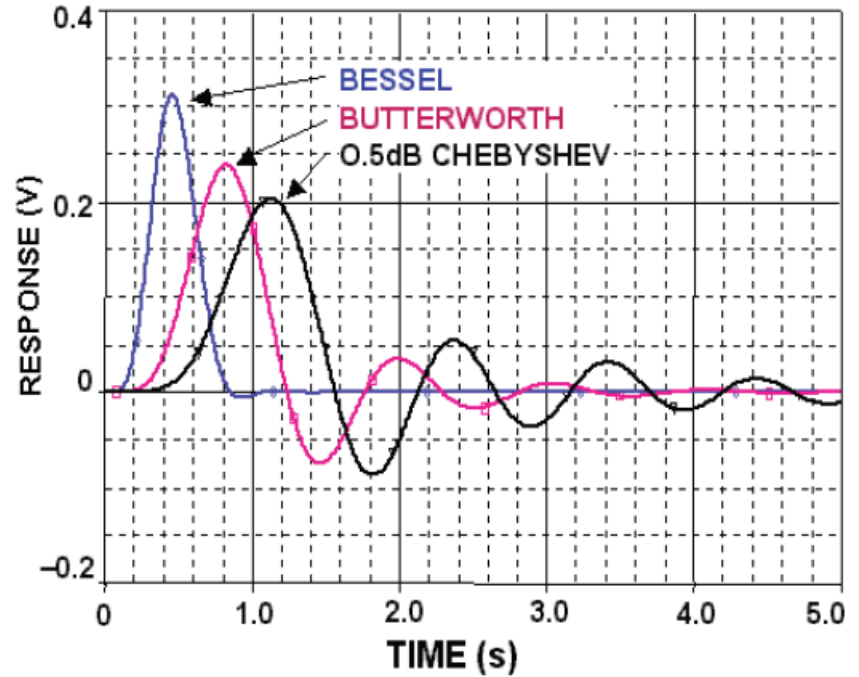
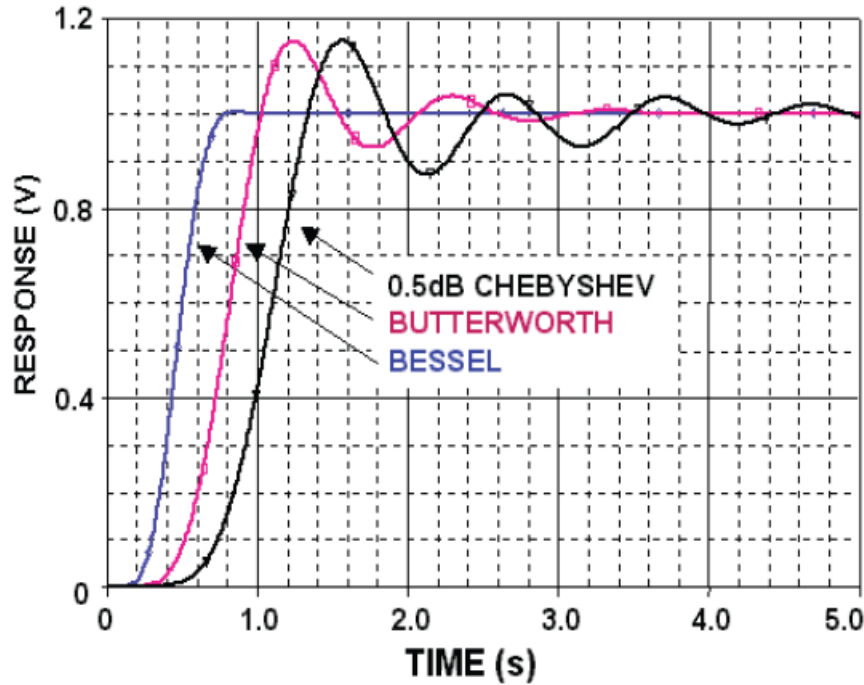
$$N \geq N_d = \frac{\cosh^{-1}(\sqrt{\frac{10^{\frac{\alpha_{\min}}{10}} - 1}{10^{\frac{\alpha_{\max}}{10}} - 1}})}{\cosh^{-1}(\Omega_S)}$$



## Comparison of Amplitude Response



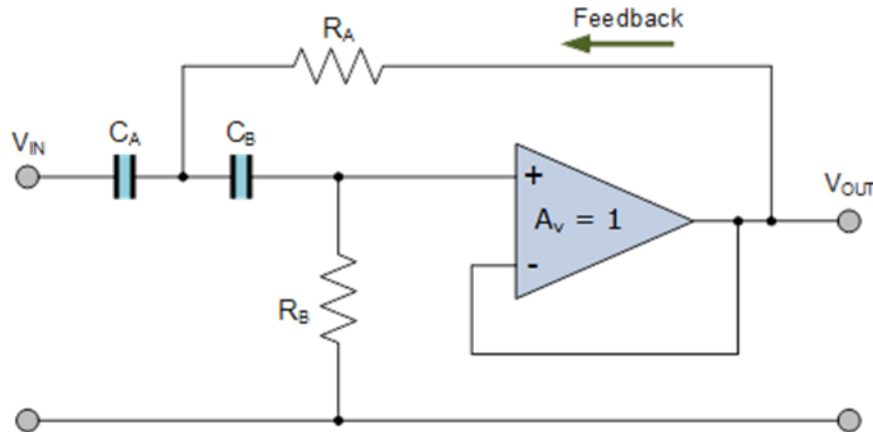
## Comparison of Step and Impulse Responses



# Butterworth VS Chebyshev

|                  | Butterworth Filter   | Chebyshev Filter  |
|------------------|--|---|
| Order of Filter  | The order of the Butterworth filter is higher than the Chebyshev filter for the same desired specifications. | The order of the Chebyshev filter is less compared to the Butterworth filter for the same desired specifications. |
| Hardware         | It requires more hardware.   | It requires less hardware.  |
| Ripple           | There is no ripple in passband and stopband of frequency response.   | There is either ripple in passband or stopband.   |
| Poles            | All poles lie on a circle having a radius of the cutoff frequency.   | All poles lie on ellipse having major axis $R$ , $\xi$ , minor axis $r$ .   |
| Transition band  | The Butterworth filter has a wider transition band compared to the Chebyshev filter.                         | The Chebyshev filter has a narrow transition band compared to the Butterworth filter.                             |
| Types            | It doesn't have any types.   | It has two types; type-1 and type-2.  |
| Cutoff Frequency | The cutoff frequency of this filter is not equal to the passband frequency.                                  | The cutoff frequency of this filter is equal to the passband frequency.   |

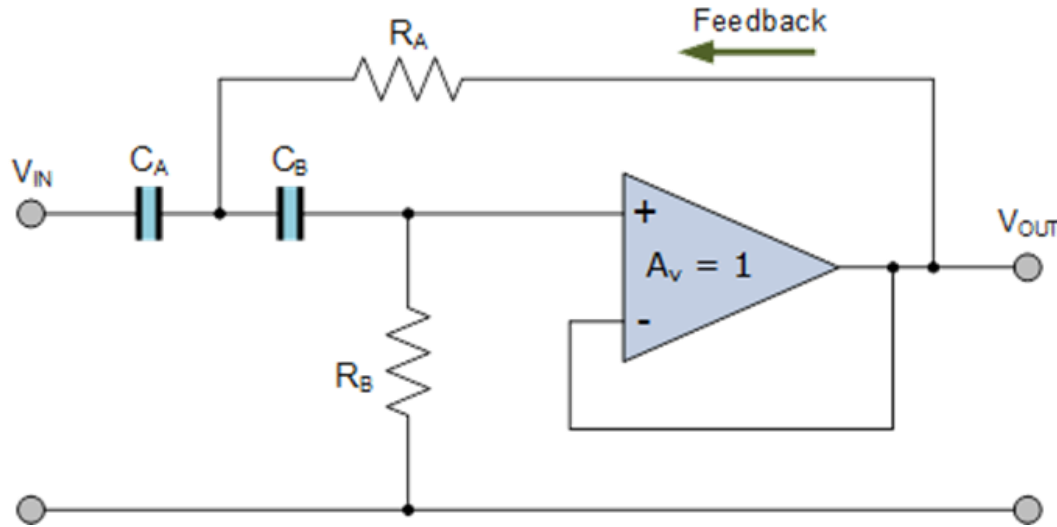




The main advantages of the Sallen-key filter design are:

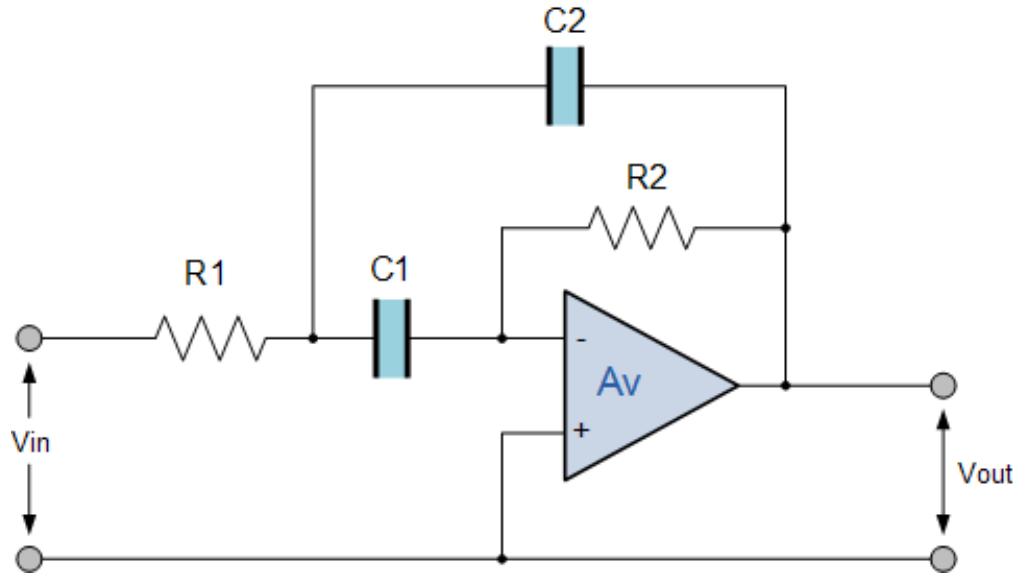
- Simplicity and Understanding of their Basic Design
- The use of a Non-inverting Amplifier to Increase Voltage Gain
- First and Second-order Filter Designs can be Easily Cascaded Together
- Low-pass and High-pass stages can be Cascaded Together
- Each RC stage can have a different Voltage Gain
- Replication of RC Components and Amplifiers
- Second-order Sallen-key Stages have Steep 40dB/decade roll-off than cascaded RC

# Sallen-key High Pass Filter Circuit



$$f_c = \frac{1}{2\pi\sqrt{R_A C_A R_B C_B}}$$

## Multiple Feedback Band Pass Active Filter



infinite-gain multiple-feedback (IGMF) band pass filter

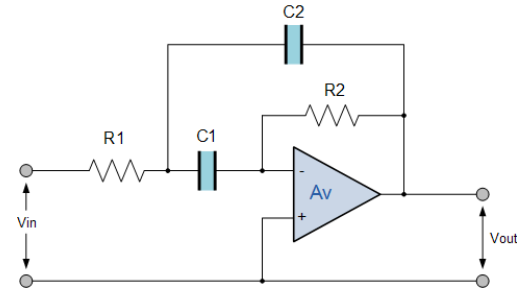
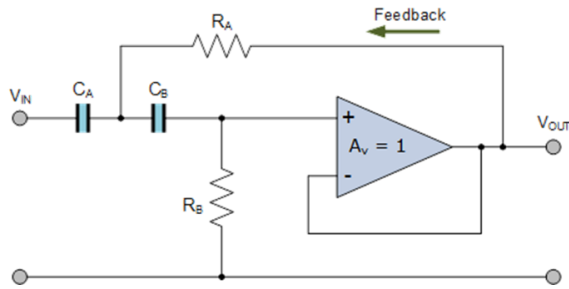
the characteristics of the IGMF filter

$$f_r = \frac{1}{2\pi\sqrt{R_1 C_1 R_2 C_2}}$$

$$Q = \frac{f_r}{BW_{-3dB}} = \frac{1}{2} \sqrt{\frac{R_2}{R_1}}$$

$$\text{Max gain} \sim -\frac{R_2}{2R_1} = 2Q^2$$

# Sallen-Key Filter VS Multiple Feedback Filter **ITMO**



## Sallen-Key

Non-inverting

Very precise DC-gain of 1

Less components for gain = 1

Op-amp input capacitance must possibly be taken into account

Resistive load for sources even in high-pass filters

## Multiple Feedback

Inverting

Any gain is dependent on the resistor precision

Less components for gain  $> 1$  or  $< 1$

Op-amp input capacitance has almost no effect

Capacitive loads can become very high for sources in high-pass filters

The background features a dark gray grid pattern. In the top right and bottom left corners, there are decorative wavy lines in a bright purple color, creating a modern, abstract aesthetic.

**iTMO**

# **Frequency Transformation**

| Type of Transformation  | Frequency transform  |
|---|--|
| The Lowpass to Highpass (LP-HP)<br>Frequency<br>Transformation    | $s \Leftrightarrow \frac{1}{s}$ $H_{HP}(s) = H_{LP}\left(\frac{1}{s}\right)$                                   |
| The Lowpass to Bandpass (LP-BP)<br>Frequency<br>Transformation    | $s \Leftrightarrow \frac{s^2 + \omega_0^2}{sBW}$ $H_{BP}(s) = H_{LP}\left(\frac{s^2 + \omega_0^2}{sBW}\right)$ |
| The Lowpass to Band-Reject (LP-BR)<br>Frequency<br>Transformation | $s \Leftrightarrow \frac{sBW}{s^2 + \omega_0^2}$ $H_{BR}(s) = H_{LP}\left(\frac{sBW}{s^2 + \omega_0^2}\right)$ |

<https://forms.yandex.com/cloud/63548180c417f37fd24e9ec2/>

<https://clck.ru/32Sksd>



1. Sarma M. S. Introduction to electrical engineering. – New York : Oxford University Press, 2001. – C. 715-716.
2. Boylestad, Robert L. Electronic devices and circuit theory / Robert L. Boylestad, Louis Nashelsky.—11th ed.
3. ISBN 978-0-13-262226-4 Scherz P., Monk S. Practical electronics for inventors. – McGraw-Hill Education, 2016.
4. Horowitz, Paul, and Winfield Hill. "The Art of Electronics. 3rd." *New York, NY, USA: University of Cambridge* (2015).
5. All about circuits (<https://www.allaboutcircuits.com/>)
6. <https://www.electronics-tutorials.ws/>
7. <https://en.wikipedia.org/>





# Laboratory Work 3

## Active filter circuits design and simulation

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# Second Order Filters

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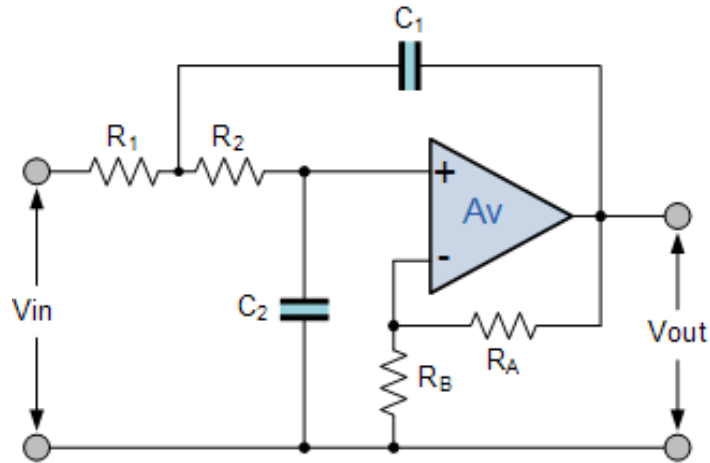
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# Second Order Low Pass Filter



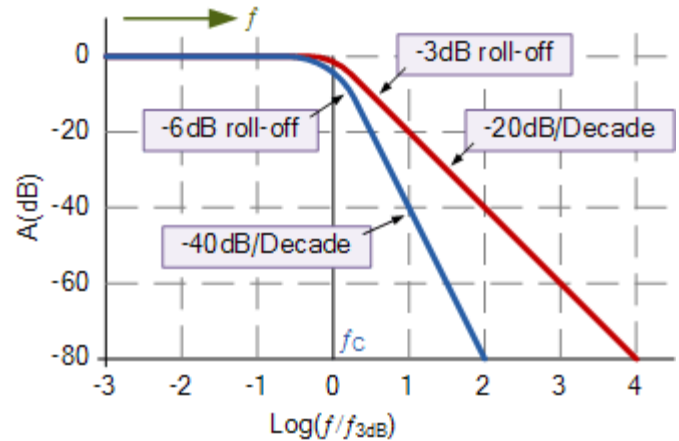
$$\text{Gain } (A_v) = 1 + \frac{R_A}{R_B}$$

If Resistor and Capacitor values are different:

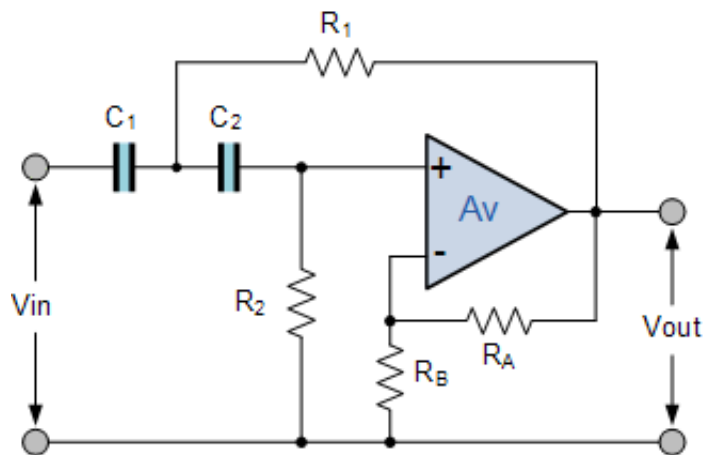
$$f_c = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

If Resistor and Capacitor values are the same:

$$f_c = \frac{1}{2\pi RC}$$



# Second Order High Pass Filter



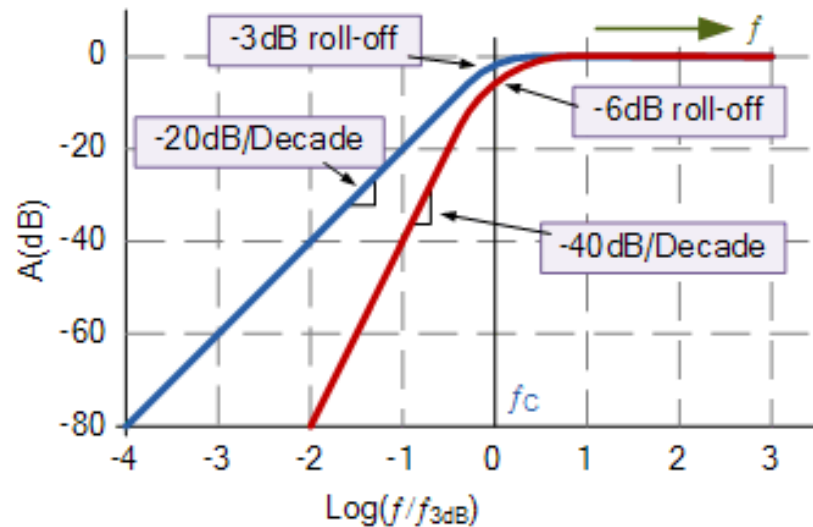
$$\text{Gain } (A_v) = 1 + \frac{R_A}{R_B}$$

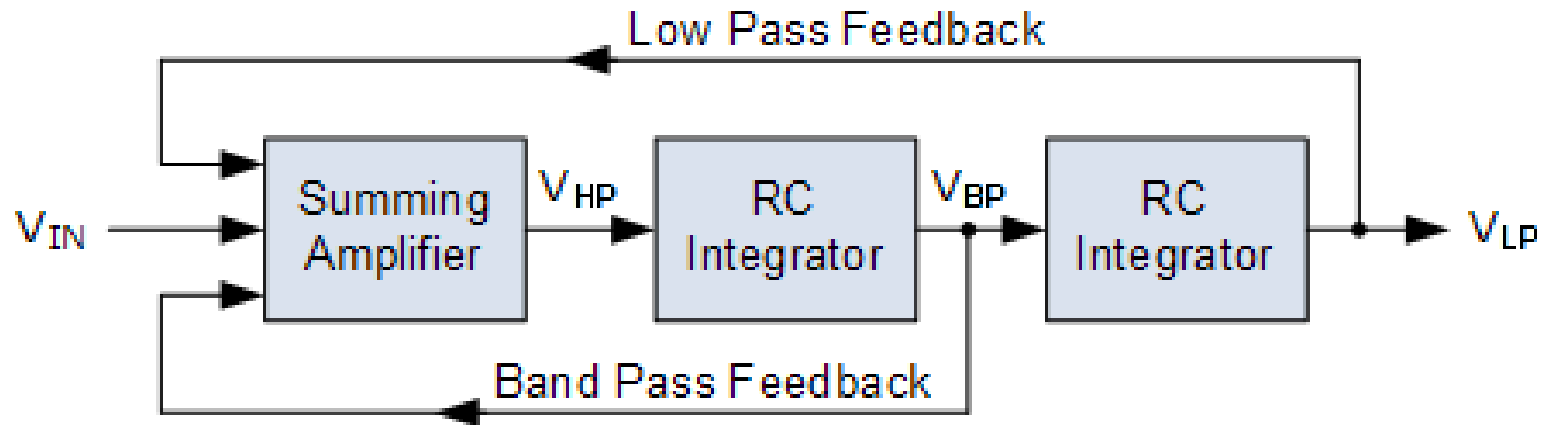
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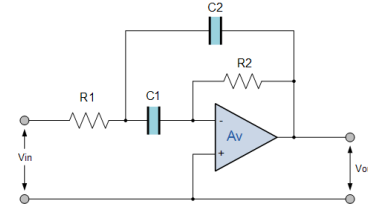
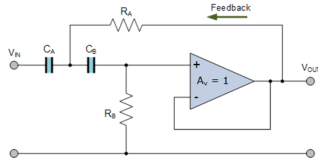
$$f_c = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

If Resistor and Capacitor values are the same:

$$f_c = \frac{1}{2\pi RC}$$







## Sallen-Key

Non-inverting

Very precise DC-gain of 1

Less components for gain = 1

Op-amp input capacitance must possibly be taken into account

Resistive load for sources even in high-pass filters

## Multiple Feedback

Inverting

Any gain is dependent on the resistor precision

Less components for gain  $> 1$  or  $< 1$

Op-amp input capacitance has almost no effect

Capacitive loads can become very high for sources in high-pass filters



# Frequency Transformation

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# Typical values of low-pass filter parameters

$$H_{LP}(f) := \frac{K}{b_1 \cdot \left( \left( \frac{2 \cdot \pi \cdot f \cdot i}{\omega_p} \right)^2 \right) + a_1 \cdot \frac{(2 \cdot \pi \cdot f \cdot i)}{\omega_p} + 1}$$

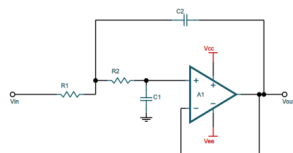
| $n$                | $i$ | $a_i$  | $b_i$  | $f_B/f_S$ | $Q_i$ |
|--------------------|-----|--------|--------|-----------|-------|
| <b>Butterworth</b> |     |        |        |           |       |
| 1                  | 1   | 1.0000 | 0.0000 | 1.000     | –     |
| 2                  | 1   | 1.4142 | 1.0000 | 1.000     | 0.71  |
| 3                  | 1   | 1.0000 | 0.0000 | 1.000     | –     |
|                    | 2   | 1.0000 | 1.0000 | 1.272     | 1.00  |
| 4                  | 1   | 1.8478 | 1.0000 | 0.719     | 0.54  |
|                    | 2   | 0.7654 | 1.0000 | 1.390     | 1.31  |
| 5                  | 1   | 1.0000 | 0.0000 | 1.000     | –     |
|                    | 2   | 1.6180 | 1.0000 | 0.859     | 0.62  |
|                    | 3   | 0.6180 | 1.0000 | 1.448     | 1.62  |
| 6                  | 1   | 1.9319 | 1.0000 | 0.676     | 0.52  |
|                    | 2   | 1.4142 | 1.0000 | 1.000     | 0.71  |
|                    | 3   | 0.5176 | 1.0000 | 1.479     | 1.93  |
| 7                  | 1   | 1.0000 | 0.0000 | 1.000     | –     |
|                    | 2   | 1.8019 | 1.0000 | 0.745     | 0.55  |
|                    | 3   | 1.2470 | 1.0000 | 1.117     | 0.80  |
|                    | 4   | 0.4450 | 1.0000 | 1.499     | 2.25  |
| 8                  | 1   | 1.9616 | 1.0000 | 0.661     | 0.51  |
|                    | 2   | 1.6629 | 1.0000 | 0.829     | 0.60  |
|                    | 3   | 1.1111 | 1.0000 | 1.206     | 0.90  |
|                    | 4   | 0.3902 | 1.0000 | 1.512     | 2.56  |
| 9                  | 1   | 1.0000 | 0.0000 | 1.000     | –     |
|                    | 2   | 1.8794 | 1.0000 | 0.703     | 0.53  |
|                    | 3   | 1.5321 | 1.0000 | 0.917     | 0.65  |
|                    | 4   | 1.0000 | 1.0000 | 1.272     | 1.00  |
|                    | 5   | 0.3473 | 1.0000 | 1.521     | 2.88  |
| 10                 | 1   | 1.9754 | 1.0000 | 0.655     | 0.51  |
|                    | 2   | 1.7820 | 1.0000 | 0.756     | 0.56  |
|                    | 3   | 1.4142 | 1.0000 | 1.000     | 0.71  |
|                    | 4   | 0.9080 | 1.0000 | 1.322     | 1.10  |
|                    | 5   | 0.3129 | 1.0000 | 1.527     | 3.20  |

| $n$              | $i$ | $a_i$   | $b_i$   | $f_B/f_S$ | $Q_i$ |
|------------------|-----|---------|---------|-----------|-------|
| <b>Chebyshev</b> |     |         |         |           |       |
| 1                | 1   | 1.0000  | 0.0000  | 1.000     | –     |
| 2                | 1   | 1.0650  | 1.9305  | 1.000     | 1.30  |
| 3                | 1   | 3.3496  | 0.0000  | 0.299     | –     |
|                  | 2   | 0.3559  | 1.1923  | 1.396     | 3.07  |
| 4                | 1   | 2.1853  | 5.5339  | 0.557     | 1.08  |
|                  | 2   | 0.1964  | 1.2009  | 1.410     | 5.58  |
| 5                | 1   | 5.6334  | 0.0000  | 0.178     | –     |
|                  | 2   | 0.7620  | 2.6530  | 0.917     | 2.14  |
|                  | 3   | 0.1172  | 1.0686  | 1.500     | 8.82  |
| 6                | 1   | 3.2721  | 11.6773 | 0.379     | 1.04  |
|                  | 2   | 0.4077  | 1.9873  | 1.086     | 3.46  |
|                  | 3   | 0.0815  | 1.0861  | 1.489     | 12.78 |
| 7                | 1   | 7.9064  | 0.0000  | 0.126     | –     |
|                  | 2   | 1.1159  | 4.8963  | 0.670     | 1.98  |
|                  | 3   | 0.2515  | 1.5944  | 1.222     | 5.02  |
|                  | 4   | 0.0582  | 1.0348  | 1.527     | 17.46 |
| 8                | 1   | 4.3583  | 20.2948 | 0.286     | 1.03  |
|                  | 2   | 0.5791  | 3.1808  | 0.855     | 3.08  |
|                  | 3   | 0.1765  | 1.4507  | 1.285     | 6.83  |
|                  | 4   | 0.0448  | 1.0478  | 1.517     | 22.87 |
| 9                | 1   | 10.1759 | 0.0000  | 0.098     | –     |
|                  | 2   | 1.4585  | 7.8971  | 0.526     | 1.93  |
|                  | 3   | 0.3561  | 2.3651  | 1.001     | 4.32  |
|                  | 4   | 0.1294  | 1.3165  | 1.351     | 8.87  |
|                  | 5   | 0.0348  | 1.0210  | 1.537     | 29.00 |
| 10               | 1   | 5.4449  | 31.3788 | 0.230     | 1.03  |
|                  | 2   | 0.7414  | 4.7363  | 0.699     | 2.94  |
|                  | 3   | 0.2479  | 1.9952  | 1.094     | 5.70  |
|                  | 4   | 0.1008  | 1.2638  | 1.380     | 11.15 |
|                  | 5   | 0.0283  | 1.0304  | 1.530     | 35.85 |

| $n$           | $i$ | $a_i$  | $b_i$  | $f_B/f_S$ | $Q_i$ |
|---------------|-----|--------|--------|-----------|-------|
| <b>Bessel</b> |     |        |        |           |       |
| 1             | 1   | 1.0000 | 0.0000 | 1.000     | –     |
| 2             | 1   | 1.3617 | 0.6180 | 1.000     | 0.58  |
| 3             | 1   | 0.7560 | 0.0000 | 1.323     | –     |
|               | 2   | 0.9996 | 0.4772 | 1.414     | 0.69  |
| 4             | 1   | 1.3397 | 0.4889 | 0.978     | 0.52  |
|               | 2   | 0.7743 | 0.3890 | 1.797     | 0.81  |
| 5             | 1   | 0.6656 | 0.0000 | 1.502     | –     |
|               | 2   | 1.1402 | 0.4128 | 1.184     | 0.56  |
|               | 3   | 0.6216 | 0.3245 | 2.138     | 0.92  |
| 6             | 1   | 1.2217 | 0.3887 | 1.063     | 0.51  |
|               | 2   | 0.9686 | 0.3505 | 1.431     | 0.61  |
|               | 3   | 0.5131 | 0.2756 | 2.447     | 1.02  |
| 7             | 1   | 0.5937 | 0.0000 | 1.684     | –     |
|               | 2   | 1.0944 | 0.3395 | 1.207     | 0.53  |
|               | 3   | 0.8304 | 0.3011 | 1.695     | 0.66  |
|               | 4   | 0.4332 | 0.2381 | 2.731     | 1.13  |
| 8             | 1   | 1.1112 | 0.3162 | 1.164     | 0.51  |
|               | 2   | 0.9754 | 0.2979 | 1.381     | 0.56  |
|               | 3   | 0.7202 | 0.2621 | 1.963     | 0.71  |
|               | 4   | 0.3728 | 0.2087 | 2.992     | 1.23  |
| 9             | 1   | 0.5386 | 0.0000 | 1.857     | –     |
|               | 2   | 1.0244 | 0.2834 | 1.277     | 0.52  |
|               | 3   | 0.8710 | 0.2636 | 1.574     | 0.59  |
|               | 4   | 0.6320 | 0.2311 | 2.226     | 0.76  |
|               | 5   | 0.3257 | 0.1854 | 3.237     | 1.32  |
| 10            | 1   | 1.0215 | 0.2650 | 1.264     | 0.50  |
|               | 2   | 0.9393 | 0.2549 | 1.412     | 0.54  |
|               | 3   | 0.7815 | 0.2351 | 1.780     | 0.62  |
|               | 4   | 0.5604 | 0.2059 | 2.479     | 0.81  |
|               | 5   | 0.2883 | 0.1665 | 3.466     | 1.42  |

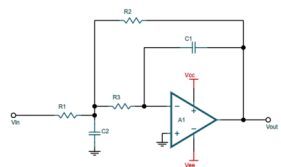


## Lowpass Filter



Sallen-Key

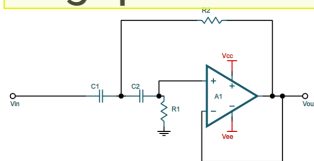
$$H_{LP\_SK}(f) := \frac{K}{(2 \cdot \pi \cdot f \cdot i)^2 \cdot R_{1LP} \cdot R_{2LP} \cdot C_{1LP} \cdot C_{2LP} + C_{2LP} \cdot (R_{1LP} + R_{2LP}) \cdot (2 \cdot \pi \cdot f \cdot i) + 1}$$



Multiple Feedback

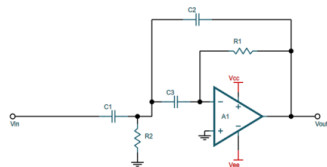
$$H_{LP\_MF}(f) := \frac{\frac{R_{2LP}}{R_{1LP}}}{(2 \cdot \pi \cdot f \cdot i)^2 \cdot R_{2LP} \cdot R_{3LP} \cdot C_{1LP} \cdot C_{2LP} + C_{1LP} \cdot \left( R_{2LP} + R_{3LP} + \frac{R_{2LP} \cdot R_{3LP}}{R_{1LP}} \right) \cdot (2 \cdot \pi \cdot f \cdot i) + 1}$$

## Highpass Filter



Sallen-Key

$$H_{HP\_SK}(f) := \frac{K}{\frac{1}{(2 \cdot \pi \cdot f \cdot i)^2 \cdot R_{1HP} \cdot R_{2HP} \cdot C_{1HP} \cdot C_{2HP}} + \frac{R_{2HP} \cdot (C_{1HP} + C_{2HP}) + (1 - K) \cdot R_{1HP} \cdot C_{2HP}}{R_{1HP} \cdot R_{2HP} \cdot C_{1HP} \cdot C_{2HP} \cdot 2 \cdot \pi \cdot f \cdot i} + 1}$$



Multiple Feedback

$$H_{HP\_MF}(f) := \frac{(2 \cdot \pi \cdot f \cdot i)^2 \cdot R_{1HP} \cdot R_{2HP} \cdot C_{1HP} \cdot C_{3HP}}{(2 \cdot \pi \cdot f \cdot i)^2 \cdot R_{1HP} \cdot R_{2HP} \cdot C_{2HP} \cdot C_{3HP} + R_{2HP} \cdot (C_{1HP} + C_{2HP} + C_{3HP}) \cdot (2 \cdot \pi \cdot f \cdot i) + 1}$$

| Type of Transformation  | Frequency transform  |
|---|--|
| The Lowpass to Highpass (LP-HP)<br>Frequency<br>Transformation    | $s \Leftrightarrow \frac{1}{s}$ $H_{HP}(s) = H_{LP}\left(\frac{1}{s}\right)$                                   |
| The Lowpass to Bandpass (LP-BP)<br>Frequency<br>Transformation    | $s \Leftrightarrow \frac{s^2 + \omega_0^2}{sBW}$ $H_{BP}(s) = H_{LP}\left(\frac{s^2 + \omega_0^2}{sBW}\right)$ |
| The Lowpass to Band-Reject (LP-BR)<br>Frequency<br>Transformation | $s \Leftrightarrow \frac{sBW}{s^2 + \omega_0^2}$ $H_{BR}(s) = H_{LP}\left(\frac{sBW}{s^2 + \omega_0^2}\right)$ |

# Typical values of High-pass filter parameters

$$H_{HP}(f) := \frac{K}{\frac{b_1}{\left(\frac{2 \cdot \pi \cdot f \cdot i}{\omega_p}\right)^2} + \frac{a_1}{\omega_p} + 1}$$

| $n$                | $i$ | $a_i$  | $b_i$  | $f_{\theta}/f_s$ | $Q_i$ |
|--------------------|-----|--------|--------|------------------|-------|
| <b>Butterworth</b> |     |        |        |                  |       |
| 1                  | 1   | 1,0000 | 0,0000 | 1,000            | –     |
| 2                  | 1   | 1,4142 | 1,0000 | 1,000            | 0,71  |
| 3                  | 1   | 1,0000 | 0,0000 | 1,000            | –     |
|                    | 2   | 1,0000 | 1,272  | 1,00             |       |
| 4                  | 1   | 1,8478 | 1,0000 | 0,719            | 0,54  |
|                    | 2   | 0,7654 | 1,0000 | 1,390            | 1,31  |
| 5                  | 1   | 1,0000 | 0,0000 | 1,000            | –     |
|                    | 2   | 1,6180 | 1,0000 | 0,859            | 0,62  |
|                    | 3   | 0,6180 | 1,0000 | 1,448            | 1,62  |
| 6                  | 1   | 1,9319 | 1,0000 | 0,676            | 0,52  |
|                    | 2   | 1,4142 | 1,0000 | 1,000            | 0,71  |
|                    | 3   | 0,5176 | 1,0000 | 1,479            | 1,93  |
| 7                  | 1   | 1,0000 | 0,0000 | 1,000            | –     |
|                    | 2   | 1,8019 | 1,0000 | 0,745            | 0,55  |
|                    | 3   | 1,2470 | 1,0000 | 1,117            | 0,80  |
|                    | 4   | 0,4450 | 1,0000 | 1,499            | 2,25  |
| 8                  | 1   | 1,9616 | 1,0000 | 0,661            | 0,51  |
|                    | 2   | 1,6629 | 1,0000 | 0,829            | 0,60  |
|                    | 3   | 1,1111 | 1,0000 | 1,206            | 0,90  |
|                    | 4   | 0,3902 | 1,0000 | 1,512            | 2,56  |
| 9                  | 1   | 1,0000 | 0,0000 | 1,000            | –     |
|                    | 2   | 1,8794 | 1,0000 | 0,703            | 0,53  |
|                    | 3   | 1,5321 | 1,0000 | 0,917            | 0,65  |
|                    | 4   | 1,0000 | 1,0000 | 1,272            | 1,00  |
|                    | 5   | 0,3473 | 1,0000 | 1,521            | 2,88  |
| 10                 | 1   | 1,9754 | 1,0000 | 0,655            | 0,51  |
|                    | 2   | 1,7820 | 1,0000 | 0,756            | 0,56  |
|                    | 3   | 1,4142 | 1,0000 | 1,000            | 0,71  |
|                    | 4   | 0,9080 | 1,0000 | 1,322            | 1,10  |
|                    | 5   | 0,3129 | 1,0000 | 1,527            | 3,20  |

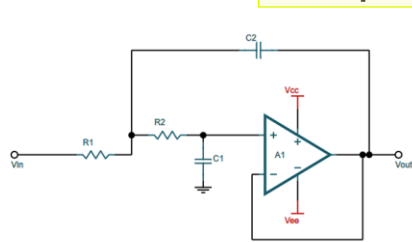
| $n$              | $i$ | $a_i$   | $b_i$   | $f_{\theta}/f_s$ | $Q_i$ |
|------------------|-----|---------|---------|------------------|-------|
| <b>Chebyshev</b> |     |         |         |                  |       |
| 1                | 1   | 1,0000  | 0,0000  | 1,000            | –     |
| 2                | 1   | 1,0650  | 1,9305  | 1,000            | 1,30  |
| 3                | 1   | 3,3496  | 0,0000  | 0,299            | –     |
|                  | 2   | 0,3559  | 1,1923  | 1,396            | 3,07  |
| 4                | 1   | 2,1853  | 5,5339  | 0,557            | 1,08  |
|                  | 2   | 0,1964  | 1,2009  | 1,410            | 5,58  |
| 5                | 1   | 5,6334  | 0,0000  | 0,178            | –     |
|                  | 2   | 0,7620  | 2,6530  | 0,917            | 2,14  |
|                  | 3   | 0,1172  | 1,0686  | 1,500            | 8,82  |
| 6                | 1   | 3,2721  | 11,6773 | 0,379            | 1,04  |
|                  | 2   | 0,4077  | 1,9873  | 1,086            | 3,46  |
|                  | 3   | 0,0815  | 1,0861  | 1,489            | 12,78 |
| 7                | 1   | 7,9064  | 0,0000  | 0,126            | –     |
|                  | 2   | 1,1159  | 4,8963  | 0,670            | 1,98  |
|                  | 3   | 0,2515  | 1,5944  | 1,222            | 5,02  |
|                  | 4   | 0,0582  | 1,0348  | 1,527            | 17,46 |
| 8                | 1   | 4,3583  | 20,2948 | 0,286            | 1,03  |
|                  | 2   | 0,5791  | 3,1808  | 0,855            | 3,08  |
|                  | 3   | 0,1765  | 1,4507  | 1,285            | 6,83  |
|                  | 4   | 0,0448  | 1,0478  | 1,517            | 22,87 |
| 9                | 1   | 10,1759 | 0,0000  | 0,098            | –     |
|                  | 2   | 1,4585  | 7,8971  | 0,526            | 1,93  |
|                  | 3   | 0,3561  | 2,3651  | 1,001            | 4,32  |
|                  | 4   | 0,1294  | 1,3165  | 1,351            | 8,87  |
|                  | 5   | 0,0348  | 1,0210  | 1,537            | 29,00 |
| 10               | 1   | 5,4449  | 31,3788 | 0,230            | 1,03  |
|                  | 2   | 0,7414  | 4,7363  | 0,699            | 2,94  |
|                  | 3   | 0,2479  | 1,9952  | 1,094            | 5,70  |
|                  | 4   | 0,1008  | 1,2638  | 1,380            | 11,15 |
|                  | 5   | 0,0283  | 1,0304  | 1,530            | 35,85 |

| $n$           | $i$ | $a_i$  | $b_i$  | $f_{\theta}/f_s$ | $Q_i$ |
|---------------|-----|--------|--------|------------------|-------|
| <b>Bessel</b> |     |        |        |                  |       |
| 1             | 1   | 1,0000 | 0,0000 | 1,000            | –     |
| 2             | 1   | 1,3617 | 0,6180 | 1,000            | 0,58  |
| 3             | 1   | 0,7560 | 0,0000 | 1,323            | –     |
|               | 2   | 0,9996 | 0,4772 | 1,414            | 0,69  |
| 4             | 1   | 1,3397 | 0,4889 | 0,978            | 0,52  |
|               | 2   | 0,7743 | 0,3890 | 1,797            | 0,81  |
| 5             | 1   | 0,6656 | 0,0000 | 1,502            | –     |
|               | 2   | 1,1402 | 0,4128 | 1,184            | 0,56  |
|               | 3   | 0,6216 | 0,3245 | 2,138            | 0,92  |
| 6             | 1   | 1,2217 | 0,3887 | 1,063            | 0,51  |
|               | 2   | 0,9686 | 0,3505 | 1,431            | 0,61  |
|               | 3   | 0,5131 | 0,2756 | 2,447            | 1,02  |
| 7             | 1   | 0,5937 | 0,0000 | 1,684            | –     |
|               | 2   | 1,0944 | 0,3395 | 1,207            | 0,53  |
|               | 3   | 0,8304 | 0,3011 | 1,695            | 0,66  |
|               | 4   | 0,4332 | 0,2381 | 2,731            | 1,13  |
| 8             | 1   | 1,1112 | 0,3162 | 1,164            | 0,51  |
|               | 2   | 0,9754 | 0,2979 | 1,381            | 0,56  |
|               | 3   | 0,7202 | 0,2621 | 1,963            | 0,71  |
|               | 4   | 0,3728 | 0,2087 | 2,992            | 1,23  |
| 9             | 1   | 0,5386 | 0,0000 | 1,857            | –     |
|               | 2   | 1,0244 | 0,2834 | 1,277            | 0,52  |
|               | 3   | 0,8710 | 0,2636 | 1,574            | 0,59  |
|               | 4   | 0,6320 | 0,2311 | 2,226            | 0,76  |
|               | 5   | 0,3257 | 0,1854 | 3,237            | 1,32  |
| 10            | 1   | 1,0215 | 0,2650 | 1,264            | 0,50  |
|               | 2   | 0,9393 | 0,2549 | 1,412            | 0,54  |
|               | 3   | 0,7815 | 0,2351 | 1,780            | 0,62  |
|               | 4   | 0,5604 | 0,2059 | 2,479            | 0,81  |
|               | 5   | 0,2883 | 0,1665 | 3,466            | 1,42  |

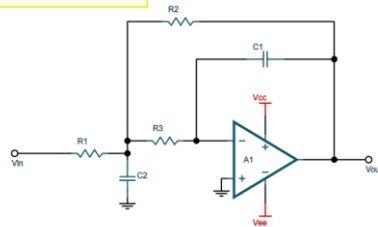
# Typical values of low-pass filter parameters

| Filter scheme                   | Filter type         | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [ $\Omega$ ] | Filter resistance, [ $\Omega$ ] |       |       | Resistor tolerance | Filter capacitance, [ $\Omega$ ] |          |          |                     |
|---------------------------------|---------------------|---------------------------------|----------|--|--------------------------------|--------------------------------|--------------------------------|-------------------------------|-------------------------------|---------------------------------|-------|-------|--------------------|----------------------------------|----------|----------|---------------------|
|                                 |                     | $V_{cc}$                        | $V_{ee}$ |  |                                |                                |                                |                               |                               | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    | Capacitor tolerance |
| Sallen-Key<br>Multiple Feedback | Lowpass<br>Highpass | 6                               | -6       | $ K_{NI} $   | $f_{test\_1}$                  | $f_{test\_2}$                  | $f_{test\_3}$                  | $V_{test\_AC} = V_{test}$     | $R_{Load}$                    | $R_1$                           | $R_2$ | $R_3$ |                    |                                  |          |          |                     |
| Sallen-Key                      | Lowpass             | 6                               | -6       | 1,000  | 50                             | 1000                           | 100000                         | 2,000                         | 1000000                       | 8200                            | 15000 | -     | 5%                 | 1e-9                             | 2,20E-09 | -        | 20%                 |
| Multiple Feedback               | Highpass            | 6                               | -6       | 1,000  | 60                             | 1200                           | 120000                         | 2,000                         | 1000000                       | 3300                            | 820   | -     | 5%                 | 1,50E-08                         | 1,50E-08 | 2,20E-08 | 20%                 |

## Lowpass Filter

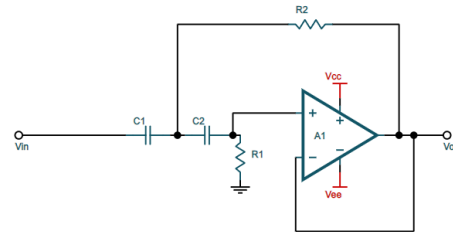


Sallen-Key

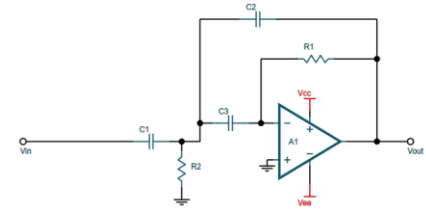


Multiple  
Feedback

## Highpass Filter



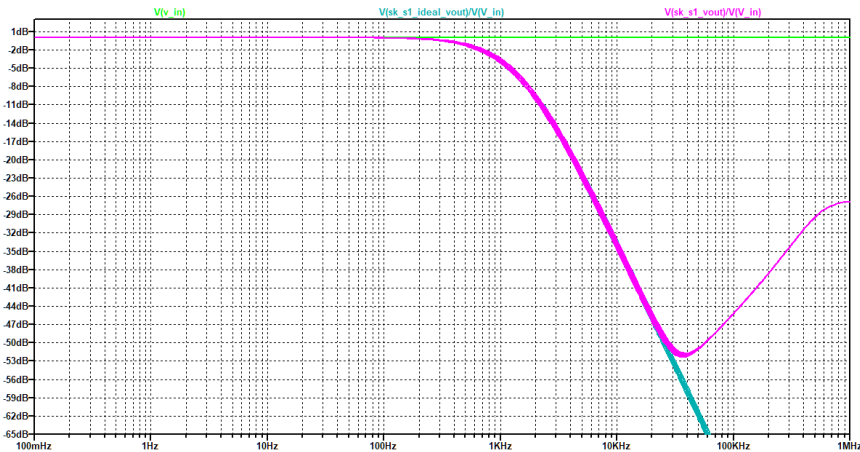
Sallen-Key



Multiple  
Feedback

# Define the filter approximation

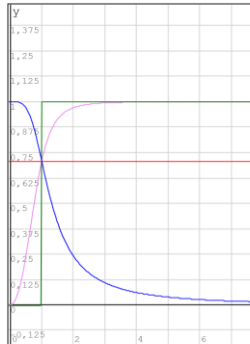
| Filter scheme                   | Filter type         | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] | Source voltage frequency , [Hz] | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [Ω] | Filter resistance, [Ω] |               |               | Resistor tolerance | Filter capacitance, [n] |                        |            |                     |
|---------------------------------|---------------------|---------------------------------|----------|--|--------------------------------|---------------------------------|--------------------------------|-------------------------------|----------------------|------------------------|---------------|---------------|--------------------|-------------------------|------------------------|------------|---------------------|
|                                 |                     | $V_{cc}$                        | $V_{ee}$ |  |                                |                                 |                                |                               |                      | $ K_{NT} $             | $f_{test\_1}$ | $f_{test\_2}$ |                    | $f_{test\_3}$           | $V_{test,AC}=V_{test}$ | $R_{Load}$ | $R_1$               |
| Sallen-Key<br>Multiple Feedback | Lowpass<br>Highpass | $V_{cc}$                        | $V_{ee}$ | $ K_{NT} $   | $f_{test\_1}$                  | $f_{test\_2}$                   | $f_{test\_3}$                  | $V_{test,AC}=V_{test}$        | $R_{Load}$           | $R_1$                  | $R_2$         | $R_3$         | Resistor tolerance | $C_1$                   | $C_2$                  | $C_3$      | Capacitor tolerance |
| Sallen-Key                      | Lowpass             | 6                               | -6       | 1,000  | 50                             | 1000                            | 100000                         | 2,000                         | 1000000              | 8200                   | 15000         | -             | 5%                 | 1e-9                    | 2,20E-09               | -          | 20%                 |
| Multiple Feedback               | Highpass            | 6                               | -6       | 1,000  | 60                             | 1200                            | 120000                         | 2,000                         | 1000000              | 3300                   | 820           | -             | 5%                 | 1,50E-08                | 1,50E-08               | 2,20E-08   | 20%                 |



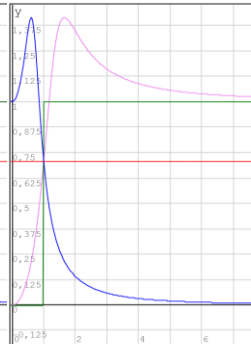
Butterworth

Chebyshev

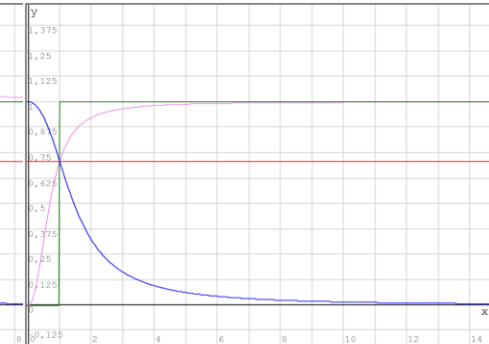
Bessel



$$\begin{cases} |H_{LP}(x)| \\ \frac{1}{\sqrt{2}} \\ \text{if } x < f \\ 0 \\ \text{else} \\ K \\ |H_{HP}(x)| \end{cases}$$



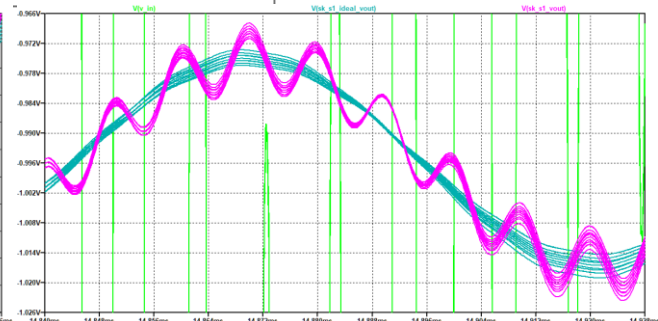
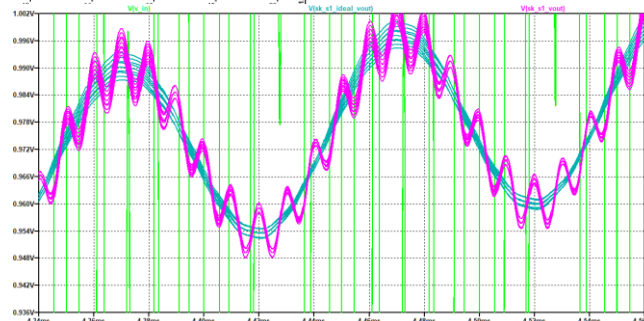
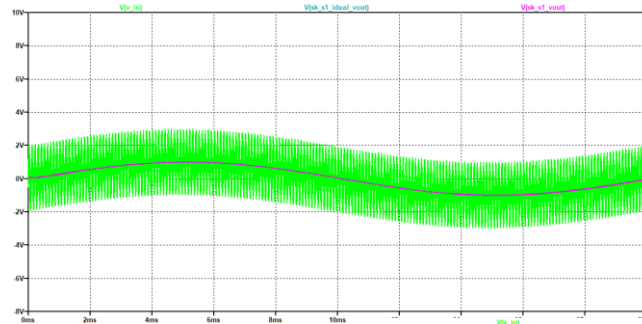
$$\begin{cases} |H_{LP}(x)| \\ \frac{1}{\sqrt{2}} \\ \text{if } x < f \\ 0 \\ \text{else} \\ K \\ |H_{HP}(x)| \end{cases}$$



$$\begin{cases} |H_{LP}(x)| \\ \frac{1}{\sqrt{2}} \\ \text{if } x < f \\ 0 \\ \text{else} \\ K \\ |H_{HP}(x)| \end{cases}$$

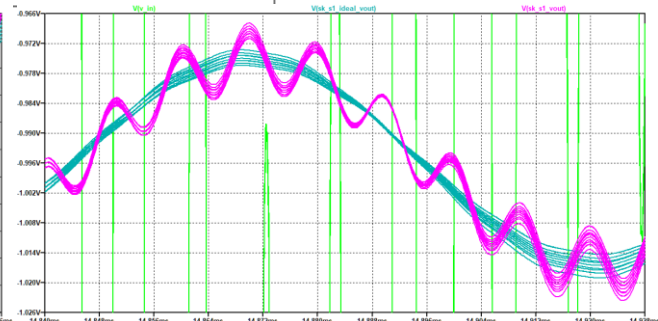
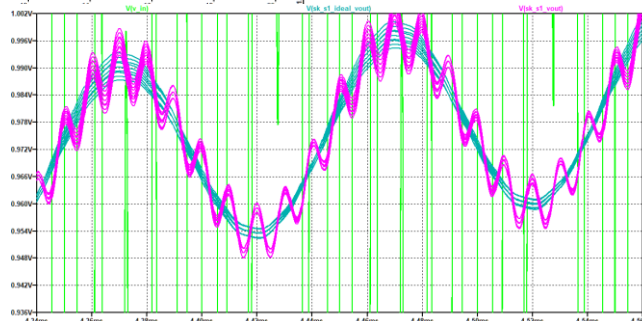
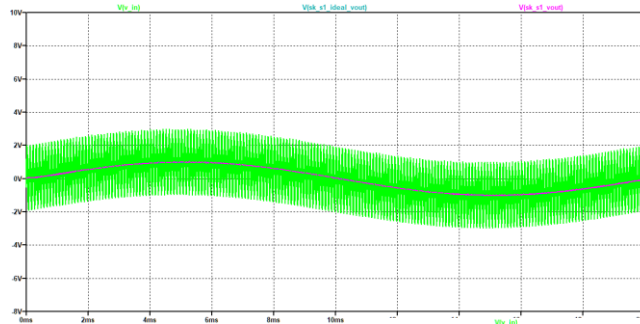
# Define the filter approximation

| Filter scheme                   | Filter type         | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] |               | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [ $\Omega$ ] | Filter resistance, [ $\Omega$ ] |       |       | Resistor tolerance | Filter capacitance, [ $\Omega$ ] |          |          | Capacitor tolerance |
|---------------------------------|---------------------|---------------------------------|----------|--|--------------------------------|---------------|--------------------------------|--------------------------------|-------------------------------|-------------------------------|---------------------------------|-------|-------|--------------------|----------------------------------|----------|----------|---------------------|
|                                 |                     | $V_{cc}$                        | $V_{ee}$ |  | $f_{test\_1}$                  | $f_{test\_2}$ |                                |                                |                               |                               | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    |                     |
| Sallen-Key<br>Multiple Feedback | Lowpass<br>Highpass | $V_{cc}$                        | $V_{ee}$ | $ K_{NT} $   | $f_{test\_1}$                  | $f_{test\_2}$ | $f_{test\_3}$                  | $V_{testAC}=V_{test}$          | $R_{Load}$                    |                               | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    |                     |
| Sallen-Key                      | Lowpass             | 6                               | -6       | 1,000  | 50                             | 1000          | 100000                         | 2,000                          | 1000000                       |                               | 8200                            | 15000 | -     | 5%                 | 1e-9                             | 2,20E-09 | -        | 20%                 |
| Multiple Feedback               | Highpass            | 6                               | -6       | 1,000  | 60                             | 1200          | 120000                         | 2,000                          | 1000000                       |                               | 3300                            | 820   | -     | 5%                 | 1,50E-08                         | 1,50E-08 | 2,20E-08 | 20%                 |



# Define the filter approximation

| Filter scheme                   | Filter type         | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [ $\Omega$ ] | Filter resistance, [ $\Omega$ ] |       |       | Resistor tolerance | Filter capacitance, [ $\Omega$ ] |          |          | Capacitor tolerance |
|---------------------------------|---------------------|---------------------------------|----------|--|--------------------------------|--------------------------------|--------------------------------|-------------------------------|-------------------------------|---------------------------------|-------|-------|--------------------|----------------------------------|----------|----------|---------------------|
| Sallen-Key<br>Multiple Feedback | Lowpass<br>Highpass | $V_{cc}$                        | $V_{ee}$ | $ K_{NT} $   | $f_{test\_1}$                  | $f_{test\_2}$                  | $f_{test\_3}$                  | $V_{testAC}=V_{test}$         | $R_{Load}$                    | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    |                     |
| Sallen-Key                      | Lowpass             | 6                               | -6       | 1,000  | 50                             | 1000                           | 100000                         | 2,000                         | 1000000                       | 8200                            | 15000 | -     | 5%                 | 1e-9                             | 2,20E-09 | -        | 20%                 |
| Multiple Feedback               | Highpass            | 6                               | -6       | 1,000  | 60                             | 1200                           | 120000                         | 2,000                         | 1000000                       | 3300                            | 820   | -     | 5%                 | 1,50E-08                         | 1,50E-08 | 2,20E-08 | 20%                 |



# Define the step response

| Filter scheme                | Filter type      | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [ $\Omega$ ] | Filter resistance, [ $\Omega$ ] |       |       | Resistor tolerance | Filter capacitance, [ $\Omega$ ] |          |          | Capacitor tolerance |
|------------------------------|------------------|---------------------------------|----------|--|--------------------------------|--------------------------------|--------------------------------|-------------------------------|-------------------------------|---------------------------------|-------|-------|--------------------|----------------------------------|----------|----------|---------------------|
| Sallen-Key Multiple Feedback | Lowpass Highpass | $V_{cc}$                        | $V_{ee}$ | $ K_{NZ} $   | $f_{test\_1}$                  | $f_{test\_2}$                  | $f_{test\_3}$                  | $V_{testAC}=V_{test}$         | $R_{Load}$                    | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    |                     |
| Sallen-Key                   | Lowpass          | 6                               | -6       | 1,000  | 50                             | 1000                           | 100000                         | 2,000                         | 1000000                       | 8200                            | 15000 | -     | 5%                 | 1e-9                             | 2,20E-09 | -        | 20%                 |
| Multiple Feedback            | Highpass         | 6                               | -6       | 1,000  | 60                             | 1200                           | 120000                         | 2,000                         | 1000000                       | 3300                            | 820   | -     | 5%                 | 1,50E-08                         | 1,50E-08 | 2,20E-08 | 20%                 |

Edit Simulation Command

Transient AC Analysis DC sweep Noise DC Transfer DC op pnt

Perform a non-linear, time-domain simulation.

Stop time:

Time to start saving data:

Maximum Timestep:

Start external DC supply voltages at 0V: ☐

Stop simulating if steady state is detected: ☐

Don't reset T=0 when steady state is detected: ☐

Step the load current source: ☐

Skip initial operating point solution: ☒

Syntax: `tran <Tprint> <Tstop> [<Tstart> [<Tmaxstep>]] [<option> [<option>] ...]`

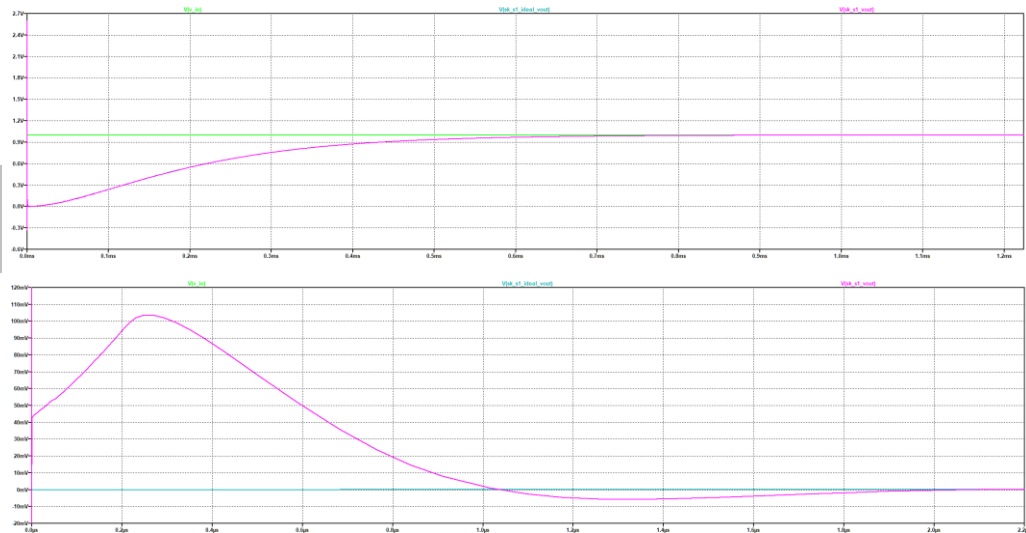
`tran 0 {1*1/f_test_1} {0*1/f_test_2} {1/f_test_3/50} uic`

Cancel OK

$V_{step}=1$

$V_{test}=0$

```
Signal source voltage step(D0)      parameter V_step=1
Step source voltage step(D0)       parameter V_step=1
Signal test frequency 1 [Hz]       parameter f_test_1=50
Signal test frequency 2 [Hz]       parameter f_test_2=1000
Signal test frequency 3 [Hz]       parameter f_test_3=100000
AC sweep source 1 parameters       parameter AC1=1 1000000
Signal source voltage step(D0)      parameter V_step=1
```





| Filter scheme                   | Filter type         | Voltage source power supply [V] |          | Required absolute gain of amplifier (sign of the gain is not considered) | Source voltage frequency, [Hz] |               | Source voltage frequency, [Hz] | Source voltage amplitude, [V] | Load resistance, [ $\Omega$ ] | Filter resistance, [ $\Omega$ ] |       |       | Resistor tolerance | Filter capacitance, [ $\Omega$ ] |          |          | Capacitor tolerance |
|---------------------------------|---------------------|---------------------------------|----------|--|--------------------------------|---------------|--------------------------------|-------------------------------|-------------------------------|---------------------------------|-------|-------|--------------------|----------------------------------|----------|----------|---------------------|
|                                 |                     | $V_{cc}$                        | $V_{ee}$ |  | $f_{test\_1}$                  | $f_{test\_2}$ |                                |                               |                               | $R_1$                           | $R_2$ | $R_3$ |                    | $C_1$                            | $C_2$    | $C_3$    |                     |
| Sallen-Key<br>Multiple Feedback | Lowpass<br>Highpass | $V_{cc}$                        | $V_{ee}$ | $ K_{NT} $   | $f_{test\_1}$                  | $f_{test\_2}$ | $f_{test\_3}$                  | $V_{testAC}=V_{test}$         | $R_{Load}$                    | $R_1$                           | $R_2$ | $R_3$ | Resistor tolerance | $C_1$                            | $C_2$    | $C_3$    | Capacitor tolerance |
| Sallen-Key                      | Lowpass             | 6                               | -6       | 1,000  | 50                             | 1000          | 100000                         | 2,000                         | 1000000                       | 8200                            | 15000 | -     | 5%                 | 1e-9                             | 2,20E-09 | -        | 20%                 |
| Multiple Feedback               | Highpass            | 6                               | -6       | 1,000  | 60                             | 1200          | 120000                         | 2,000                         | 1000000                       | 3300                            | 820   | -     | 5%                 | 1,50E-08                         | 1,50E-08 | 2,20E-08 | 20%                 |

Conclusions should contain:

- Which filter type were used?
- What was the bandwidth?
- What was the maximum/minimum gain relation in the passband?

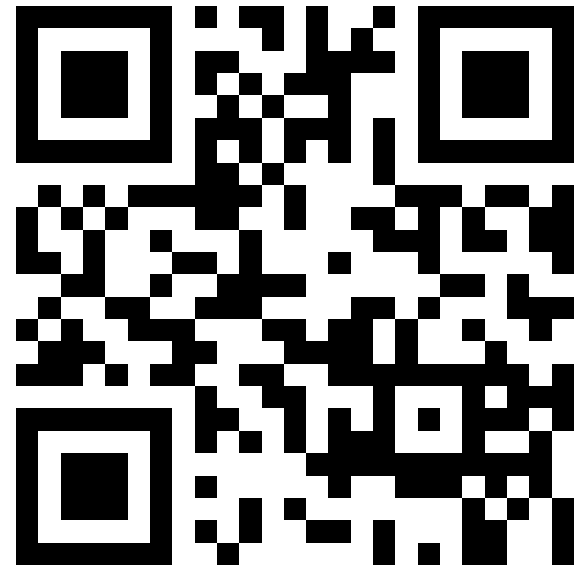
# Lab 3 submission form

<https://forms.yandex.com/cloud/637a65df5d2a068973e26fba/>

<https://clck.ru/32jqcy>

**1<sup>st</sup> deadline: 11.11.2024 10:00 (GMT +8)**

| Task              | Deadline #1 (extra score)                       | Deadline #2 (No extra score)                    | Deadline #3 (No extra score)  |
|-------------------|---|---|---|
|                   | The results will be published before 15.11.2024 | The results will be published before 20.11.2024 | The results will be published with the results of the final test (final scores) |
| Lab 1, Practice 1 | 28.10.24 10:00                                  | 11.11.24 10:00                                  | 20.11.24 10:00  |
| Practice 2        | 28.10.24 22:00                                  | 11.11.24 10:00                                  | 20.11.24 10:00  |
|                   |   |   |   |
| Lab 2             | 04.11.24 10:00                                  | 11.11.24 10:00                                  | 20.11.24 10:00  |
| Practice 3        | 04.11.24 10:00                                  | 11.11.24 10:00                                  | 20.11.24 10:00  |
|                   |   |   |   |
| Lab 3             | 11.11.24 10:00                                  | 15.11.24 10:00                                  | 20.11.24 10:00  |
| Practice 4        | 11.11.24 10:00                                  | 15.11.24 10:00                                  | 20.11.24 10:00  |



The background features a dark gray grid pattern. In the top right and bottom left corners, there are decorative wavy lines in a bright purple color, creating a modern, abstract aesthetic.

# iTMO

Thanks for your attention!