



Wind kinetic energy climatology and effective resolution for the ERA5 reanalysis

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Abstract

ERA5 represents the state of the art for atmospheric reanalyses and is widely used in meteorological and climatological research. In this work, this dataset is evaluated using the wind kinetic energy spectrum. Seasonal climatologies are generated for 30° latitudinal bands in the Northern Hemisphere (periodic domain) and over the North Atlantic area (limited-area domain). The spectra are also assessed to determine the effective resolution of the reanalysis. The results present notable differences between the latitudinal domains, indicating that ERA5 is properly capturing the synoptic conditions. The seasonal variability is adequate too, being winter the most energetic, and summer the least energetic season. The limited area domain results introduce a larger energy density and range. Despite the good results for the synoptic scales, the reanalysis' spectra are not able to properly reproduce the dissipation rates at mesoscale. This is a source of uncertainties which needs to be taken into account when using the dataset. Finally, a cyclone tropical transition is presented as a case study. The spectrum generated shows a clear difference in energy density at every wavelength, as expected for a highly-energetic status of the atmosphere.

Keywords Energy spectrum · Effective resolution · Climatology · ERA5

1 State of the art

At the present time, most of the meteorological predictions and forecasting products are based on numerical weather prediction (NWP) models. For this reason, NWP is both a major tool and principal research field for meteorology and climatology, as well as for other earth physics sciences. As a consequence, the assessment and validation of models, their evolutions and applications constitute a permanent topic of study and discussion. One of the most important

variables to consider in the configuration of a model for a NWP experiment is resolution. Spatial and temporal resolutions play a major role in the model's outcome (Adlerman and Droege 2002; Bryan et al. 2003) but also in the computation power required to perform the task, so they need to be carefully considered before the simulation is run to be adequate to the subject of study. Moreover, thanks to the enhancement of computational resources, the constant increase of spatio-temporal resolution in NWP models has reached a challenging point for their own improvement, as nowadays limited-area mesoscalar model resolutions are verging on the microscale (Prósper et al. 2019; Siewert and Kroszczynski 2020). This represents an intrinsic problem, as it is obvious that mesoscale (400–4 km) models are not originally designed for microscale (below 4 km) simulation. Thus, we face the need for new adequate parametrizations and computations for those physical processes taking place in the microscale, which had been previously disregarded (Gramelsberger 2010; Hong et al. 2004; Muñoz-Esparza et al. 2017; Sun et al. 2013). These limits of the models render necessary to know the productive limit of the resolutions used before undertaking simulation (Bolgiani et al. 2020). This *effective resolution* is usually considered as the

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physical distance at which the model's behaviour is reliable when considering a particular variable.

Skamarock (2004) studied a simple method of effective resolution evaluation for NWP models. The author proposes the kinetic energy dissipation curve, or kinetic energy spectrum diagram, as an indicator for effective resolution. For this diagram, the model kinetic energy dissipation is computed from the spectral decomposition of the simulated wind speed field. At a certain point, NWP models stop computing the energy in the model and proceed to filter it through diffusion so as to comply with a proper turbulent kinetic energy closure (Knievel et al. 2006; Skamarock et al. 2008). The departure of the simulated kinetic energy curve from the observed curve indicates the effective resolution, which is usually around seven times the model's grid size ($7\Delta x$). It has to be remarked that the computation beyond the effective resolution is not wrong in terms of physics, but a considerable uncertainty is introduced in the simulation. We can assert that the simulation below the effective resolution is not completely adequate, but that does not render it useless. For example, Skamarock (2004) defends that a finer orographic resolution or land surface processes can improve the PBL simulation, as far as the errors in energy dissipation are acknowledged. Knowing the limits and uncertainties of the tools we use is one of the motivations for the present study.

It must be noted that, the kinetic energy spectra are often derived from the wind speed. However, others atmospheric variables have also been explored. Nastrom and Gage (1985) and Cho et al. (1999) use observational data of potential temperature as well as wind components to compute the energy spectra. They conclude the horizontal wind and potential temperature have a very similar behaviour and do not depart greatly from the curve expected. Furthermore, Cho et al. (1999) compute the energy spectra with other atmospheric and air quality variables (e.g., specific humidity, CO_2 , O_3 , CH_4). The spectra behaviour of these variables follows again the curve produced by the wind speed. According to the observations by Nastrom and Gage (1985), the kinetic energy associated with planetary and large-scale processes follows a theoretical dissipation curve proportional to k^{-3} (Kolmogorov 1941) while the mesoscale atmospheric energy dissipates proportionally to $k^{-5/3}$. These upper troposphere observations show the theoretical curves falling to the microscale limit, which is considered to be at around 4 km. In this context, Lindborg (1999, Eq. 71) uses these observations to demonstrate an equation describing the energy dissipation. Notice that the domain selected can promote differences in the observed spectrum curve due to several issues, e.g. the synoptic conditions, the geographical region of study or even the local topography (Ricard et al. 2013; Skamarock 2004). The distance of sampling will also mark the lower limit of the curve ($2\Delta x$ as per Nyquist 1928) and the longitude of the observation segment will define the

upper limit of it (as it effectively filters the maximum wavelength). These conditions to the curve are also present in NWP simulations due to grid and domain sizes, and limited-area models will introduce additional modifications to the curve (Skamarock 2004).

Several researchers have been able to adequately reproduce the observations in global and limited area NWP simulations (Abdalla et al. 2013; Koshyk and Hamilton 2001; Ricard et al. 2013; Skamarock 2004; Takahashi et al. 2006), proving the effective resolution of the respective models used. Hamilton et al. (2008) remarks that some General Circulation Models (GCM) present rather different performances at the transition from k^{-3} to $k^{-5/3}$. In particular, Palmer (2001) reports that the Integrated Forecasting System [IFS; ECMWF (2016)] shows a kinetic energy spectrum that steepens rather than shallows in the mesoscale, being outperformed by other GCMs which can simulate more realistic spectra (Koshyk and Hamilton 2001; Takahashi et al. 2006). However, later results by Abdalla et al. (2013) prove that the updated versions of the IFS have corrected this issue, producing a realistic spectrum deep into mesoscale. This disagreement is a direct example of effective resolution. Palmer (2001) uses the GCM with approximately 60 km grid resolution, which yields an effective resolution of ≈ 420 km, just verging out of the mesoscale, while Abdalla et al. (2013) use a version of the model at ≈ 16 km, with an effective resolution (≈ 109 km) able to capture the aforementioned transition. This is in line with previous results from Takahashi et al. (2006) which already show how the resolution affects the ability to capture the spectrum. Also, this shows the limitations of GCMs for the study of fine scale phenomena and the current value of limited-area high-resolution NWP models at the present state of the art.

GCMs are not only used for operational forecasts and as boundary conditions for high-resolution NWP, but are also the basis for reanalyses, which have become a major research tool due to the proven enhancement by observations assimilation (Al-Yahyai et al. 2010; Bengtsson et al. 2017; Dee et al. 2011; Done et al. 2004; Hersbach et al. 2020; Uppala et al. 2005). Thus, knowing the energy spectra and effective resolution expected for global models and reanalyses is of paramount necessity to understand the limitations and uncertainties of these tools. Among the different atmospheric reanalyses available, the ERA5 dataset is currently considered a major reference. It represents a considerable improvement over previous versions (Hersbach et al. 2020) and is not only used as initial and boundary conditions for limited-area models but also frequently considered as an observational database (Aboobacker et al. 2021; Gil Ruiz et al. 2021; Molina et al. 2021; Olauson 2018; Rodríguez and Bech 2021; Taszarek et al. 2020; Zhang et al. 2021). In line with this, the principal objective of this paper is to provide seasonal climatological curves for the wind energy

spectrum over the northern hemisphere and the North Atlantic area from the ERA5 data. This aims to procure basal curves for further studies where no observational data is available, and additionally to be used as a reference for high-resolution simulations.

Another discussion related to the mesoscale energy spectrum treats the origin of the additional energy which brings the curve slope from k^{-3} up to $k^{-5/3}$ (Hamilton et al. 2008; Takahashi et al. 2006). Some results suggest that non-linear downscale energy cascades force the mesoscalar spectrum to a higher energy state (Lindborg 2007; Lindborg and Cho 2001; Tulloch and Smith 2006; VanZandt 1982). In line with this, Arimitsu and Arimitsu (2005) conclude that the synoptic part of the curve is a result of the global structure of turbulence, which is then followed by an inertial range controlled by the dissipative structure in turbulence, both sections governing the flow of turbulence. Other works support the idea of the mesoscale being energized by an upscale non-linear motion transfer from microscale, produced mainly by moist convective processes and latent heat (Gage and Nastrom 1986; Lilly 1983; Vallis et al. 1997). This would be in line with the classical results by Van der Hoven (1957), which present a peak of energy at microscale most probably due to the turbulence derived from short-term high wind speeds. Idealized simulations by Hamilton et al. (2008) show a partial forcing from both mechanisms affecting the mesoscalar spectra. This suggests that major convective and latent heat processes should alter the energy curves in NWP simulations. Thus, a secondary objective of this article is to compare the climatological spectra with those produced for a case study, namely, a subtropical cyclone transitioning to a tropical cyclone in the North Atlantic area, where convective processes are prevalent in the evolution of the phenomenon.

This work is organized as follows: Sect. 2 presents the data used and methodology followed for producing the results, shown and discussed in Sect. 3, along with the case study; Sect. 4 yields the conclusions of this study.

2 Data and methodology

The ERA5 climate reanalysis (Hersbach et al. 2020) is the most updated dataset and constitutes the fifth-generation reanalysis created by the European Centre for Medium-Range Weather Forecasts (ECMWF). This atmospheric reanalysis represents the next step with respect to the previous ERA-40 (Uppala et al. 2005) and ERA-Interim (Dee et al. 2011) databases, improving the time coverage and spatial resolution. ERA5 is freely available through the EU-funded Copernicus Climate Change Service (CDS Copernicus 2020). The set is based on the IFS (Cy41r2) and holds quality-controlled uniform data from 1979 to present, with preliminary data available from 1950 to 1978. Also, work is in progress to

provide the reanalysis in almost real-time conditions; at the date of writing of this paper, the product is available up to five days prior to the current. The resolution of the ERA5 is a big enhancement from the previous reanalysis. The horizontal grid resolution is 0.25° (approximately 27.8 km in latitude), re-gridded from the 31 km resolution of the model. The vertical resolution includes 37 pressure levels, from 1000 hPa up to 1 hPa, interpolated from the 137 sigma-pressure hybrid levels provided by the IFS. The temporal resolution is of hourly outputs. Observations from both satellites and surface-based instruments are assimilated into the global estimate, enhancing the quality of the product. A complete description of the ERA5 dataset characteristics can be found in Hersbach et al. (2020).

In the present study, the two components of the horizontal wind field (u , v) are used from the 1979–2020 dataset at 00:00, 06:00, 12:00 and 18:00 Universal Time Coordinated (UTC). The geographical domains selected are three latitudinal bands, covering the whole longitude of the northern hemisphere (periodic domains): from 00° to 30° N, from 30° to 60° N and from 60° to 90° N. These are then limited in longitude to cover exclusively the North Atlantic area (non-periodic or limited-area domains): from 080° to 010° W for the tropical area, from 070° to 000° E for the mid-latitudes and from 070° to 020° E for the polar area (Fig. 1).

The kinetic energy spectra are computed following the procedure of Skamarock (2004) and Abdalla et al. (2013). The process can be outlined as follows:



Fig. 1 Domain of study (white area) for the kinetic energy spectra over the North Atlantic Ocean. Built as the sum of three latitudinal bands

- Wind speed field is derived using u and v components.
- Anomalies are computed by removing the average wind speed.
- In the case of limited-area domains, anomalies are also detrended, rendering the non-periodic data to periodic data for the spectral decomposition.
- Energy spectral decomposition (through Fourier Analysis) is accomplished longitudinal-wise using single vertical levels.
- The obtained energy spectra are averaged over latitude, yielding a single result for each time step.
- Plots are redimensioned into wave number and energy density for easier understanding (from frequency and variance), using the ERA5 latitudinal resolution.
- The energy spectra for each time step are then plotted together with the corresponding total average. The Lindborg (1999) energy dissipation curve is added for reference.

In preliminary results several levels and monthly curves were evaluated (not shown). The spectra for different isobaric surfaces perform as expected, in line with Skamarock (2004), showing more energy at synoptic scales for higher levels and shallower curves for lower levels. The curves for each month do not show important differences as to be presented individually. Therefore, seasonal climatologies are produced at 500 hPa, as these are considered the most representative ones for this study. Also, it is worth mentioning that, as we are evaluating the energy on single levels using a large domain, the potential energy differences can be overlooked, and the contribution of the kinetic energy can be nearly considered as the whole energy of the system. Finally, it has to be noted that the same methodology was applied to the ERA5 monthly averages for wind speed. The average curves produced by these (not shown) are very similar to those produced by the aforementioned 6-h data. Thus, it was

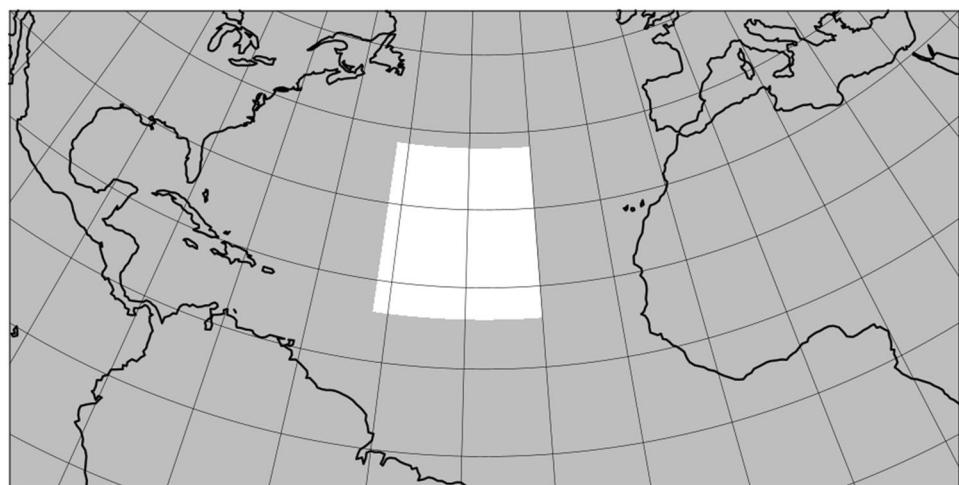
decided to show results of only the later dataset in attention to the high temporal resolution provided.

2.1 Case study

For the case study a highly active atmospheric system, a tropical storm formed by a tropical transition process (Davis and Bosart 2004), was selected due to the prominent convective activity and strong winds involved in the process. Among the multiple events available, storm Delta is to be evaluated (Beven 2005). This storm severely hit the Canary Islands archipelago in November 2005. Delta caused several casualties and many injuries, power outages, flooding and landslides. The system began to develop south-west of the Azores Islands on 19 NOV 2005 and gained subtropical cyclone characteristics on 22 NOV. By 23 NOV 2005 at 12:00 UTC the system underwent a tropical transition and continued intensifying until 27 NOV. The storm moved north-west and degraded to extratropical category with a warm-core just before hitting the Canary Islands on 28 NOV 2005 (Sánchez-Laulhé and Martin 2006). Storm Delta was detected by GPS measurements in the isle of La Palma and in the isle of Gran Canaria, showing an increase of rainfall and intensity of wind several hours prior to the effects of Delta on the ground (Seco et al. 2009). It is interesting to note, that during a tropical transition the cold-core cyclone is progressively losing its asymmetrical nature and is acquiring characteristics typical of warm-core symmetrical tropical cyclones. These transitions are of particular interest in terms of kinetic and thermodynamic atmospheric energy, expecting notable differences against the climatology in the energy spectra generated.

The data retrieved from the ERA5 dataset has a spatial domain (Fig. 2) restricted to $\pm 11^\circ$ from the approximate centre of the system at the moment of transition, 27° N 041° W. The time window considered is ± 36 h also centred at the

Fig. 2 Domain of case study (white area) of tropical storm Delta



approximate moment of transition, 12:00 UTC 23NOV2005. The energy spectra are obtained using the aforementioned procedure. Also the sea level pressure, 500 hPa geopotential height, and surface and 500 hPa wind speed and direction fields are plotted for assessment of the situation.

3 Results and discussion

The results for the North Hemisphere latitudinal bands are shown in Fig. 3, while the results for the North Atlantic are presented in Fig. 4. A seasonal comparison is shown in Fig. 5 and a latitudinal comparison in Fig. 6. These figures are analysed several times in the paper, as the results for the effective resolution and the climatologies are evaluated in separate subsections. The results for the case study are then shown in Fig. 8. For the sake of simplicity, in the discussion the seasons are named: DJF for December, January and February; MAM for March, April and May; JJA for June, July and August; SON for September, October and November. Also, the latitudinal band from 0° to 30° N is named Tropical, the band from 30° to 60° N is named Middle and the band from 60° to 90° N is named Polar.

Before initiating the discussion, it must be noted that the numerical differences between the average curves are computed and the Mann–Whitney U test (Mann and Whitney 1947) is used to check the statistical significance of these differences. This is a non-parametric test of null hypothesis, for populations with equal distribution, which are compared to check the independence of both groups. The p-value used is 0.01. Every test resulted statistically significant except for the Polar MAM and SON curves for the periodic domain which are not different enough ($p=0.10$).

Also, a short discussion on the behaviour of the spectra with altitude is worth considering. As mentioned in the methodology section, the results here presented are for 500 hPa wind speeds (Figs. 3 and 4), but preliminary results were also produced for 1000 hPa and 250 hPa wind speeds (not shown). When the 250 hPa spectra are compared with the 500 hPa results, different energy densities are only patent at synoptic scales. The upper troposphere spectra present higher densities at synoptic wavenumbers which, in turn, drive the dissipation above 10^{-5} rad m $^{-1}$ to a steeper rate. Nevertheless, the energy in the mesoscalar range does not vary much. When the 1000 hPa spectra are compared with the 500 hPa results, evident differences can be seen in both spatial ranges. The near-surface spectra show lower energy densities at synoptic scales, but there are higher energy densities at the larger mesoscalar wavenumbers (around $8 \cdot 10^{-5}$ rad m $^{-1}$), generating shallower dissipation rates along the major part of the curves. The results for 250 hPa are in accordance with those by Nastrom and Gage (1985) and Lindborg (1999), who work with observations

taken between 9 and 14 km of altitude, and also with those by Skamarock (2004) and Hamilton et al. (2008), who also show the increment of energy densities at higher altitudes. The curves at 1000 hPa are coincident with the conclusions derived by Van der Hoven (1957), who finds a secondary peak at microscale for near-surface wind spectra. However, it is known that upper troposphere spectra can be influenced by synoptic and planetary-scale waves, injecting energy in the system (Skamarock 2004). Also, ERA5 declares some reported issues with near-surface winds, i.e., a systematic jump in the boundary layer wind at the transition point for data assimilation, which can reflect on climatologies, and extremely large wind speeds (up to 300 m s^{-1}) near orographic features (Hersbach et al. 2020). As a consequence, we proceed only with the analysis for 500 hPa results.

3.1 Effective resolution

In this subsection, only the slope and shape of the curves will be assessed, disregarding the position or shape comparison with the theoretical dissipation curve.

All of the periodic domain climatological spectra (Fig. 3) seem very similar in terms of resolution. The curves present an initial shallow slope for the shortest wavenumbers, below 10^{-6} rad m $^{-1}$, coherent with the computation of the spectra in longitude and in line with those generated by Nastrom and Gage (1985), Takahashi et al. (2006) and Hamilton et al. (2008) for zonal winds. This does not match the results by Abdalla et al. (2013) for the satellite observations and the IFS, which present a decaying curve. However, as per the aforementioned authors, the decay seems to be associated with meridional winds. It is worth noting that most of the literature only evaluates the spectra down to 10^{-6} rad m $^{-1}$, so the curves beyond that point are mostly unknown. The climatological curves steepen when entering the synoptic scales, presenting an adequate energy dissipation close to k^{-3} between 10^{-6} and 10^{-5} rad m $^{-1}$ wavenumbers.

When mesoscale is reached, at about 10^{-5} rad m $^{-1}$, the curves do not show the expected shallower dissipation either. As aforementioned, this was already addressed by Palmer (2001) and Hamilton et al. (2008), reaching the conclusion that GCMs do not properly represent the energy spectrum for mesoscalar winds, however it is only a matter of grid resolution. Abdalla et al. (2013) can reproduce the change in regime due to the use of ≈ 16 km grid resolution (IFS version T1279). Nevertheless, ERA5 is based in a version of the IFS (T639) running at ≈ 31 km grid size (Hersbach et al. 2020; not to be confused with the ERA5 final delivery 0.25° grid size), with an effective resolution of ≈ 260 km, or $\approx 8\Delta x$ as per Abdalla et al. (2013). Thus, the reanalysis should in theory have the ability to reproduce the transition to $k^{-5/3}$. However, it is not seen in the spectra. On the contrary, the energy curves slightly steepen around $4 \cdot 10^{-5}$ rad m $^{-1}$, induced by

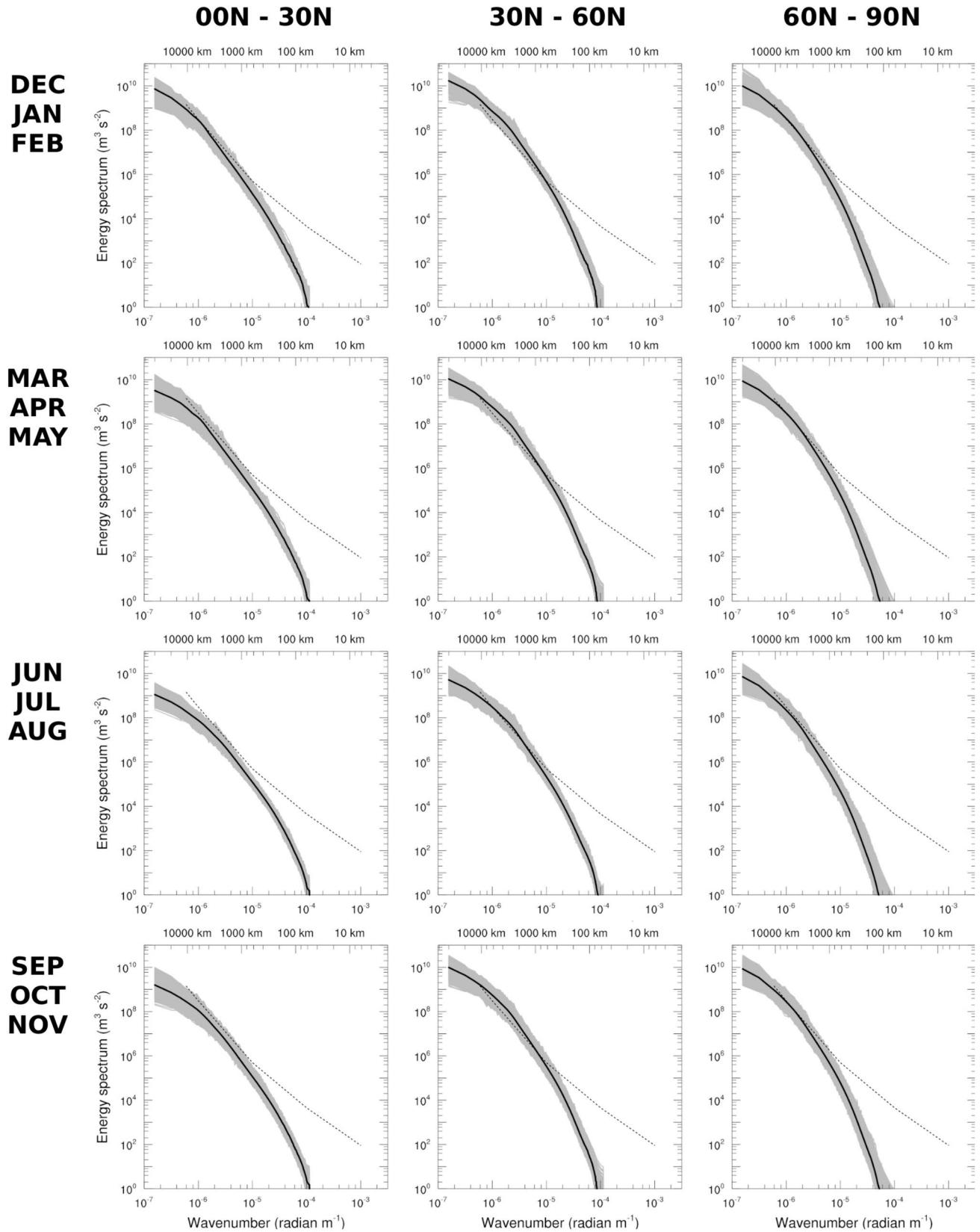


Fig. 3 Seasonal wind kinetic energy spectrum climatology for ERA5 North Hemisphere latitudinal bands. Data used in three bands: tropical (00° N– 30° N), Middle (30° N– 60° N) and Polar (30° N– 90° N).

Grey lines are individual spectra, black lines are averages, dashed lines correspond to the dissipation rate as per Lindborg (1999)

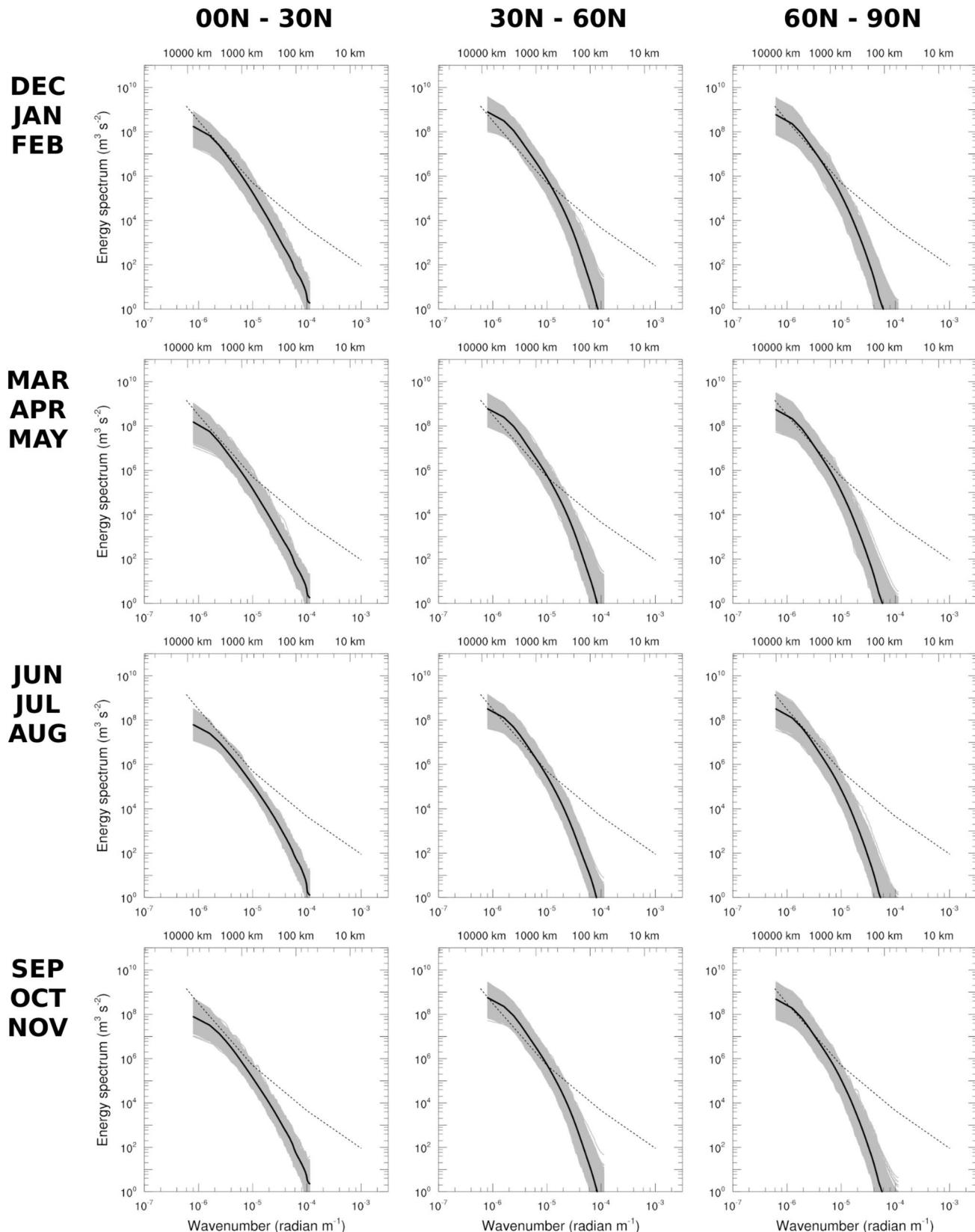


Fig. 4 Seasonal wind kinetic energy spectrum climatology for ERA5 in the North Atlantic domains described in Fig. 1. Grey lines are individual spectra, black lines are averages, dashed lines correspond to the dissipation rate as per Lindborg (1999)

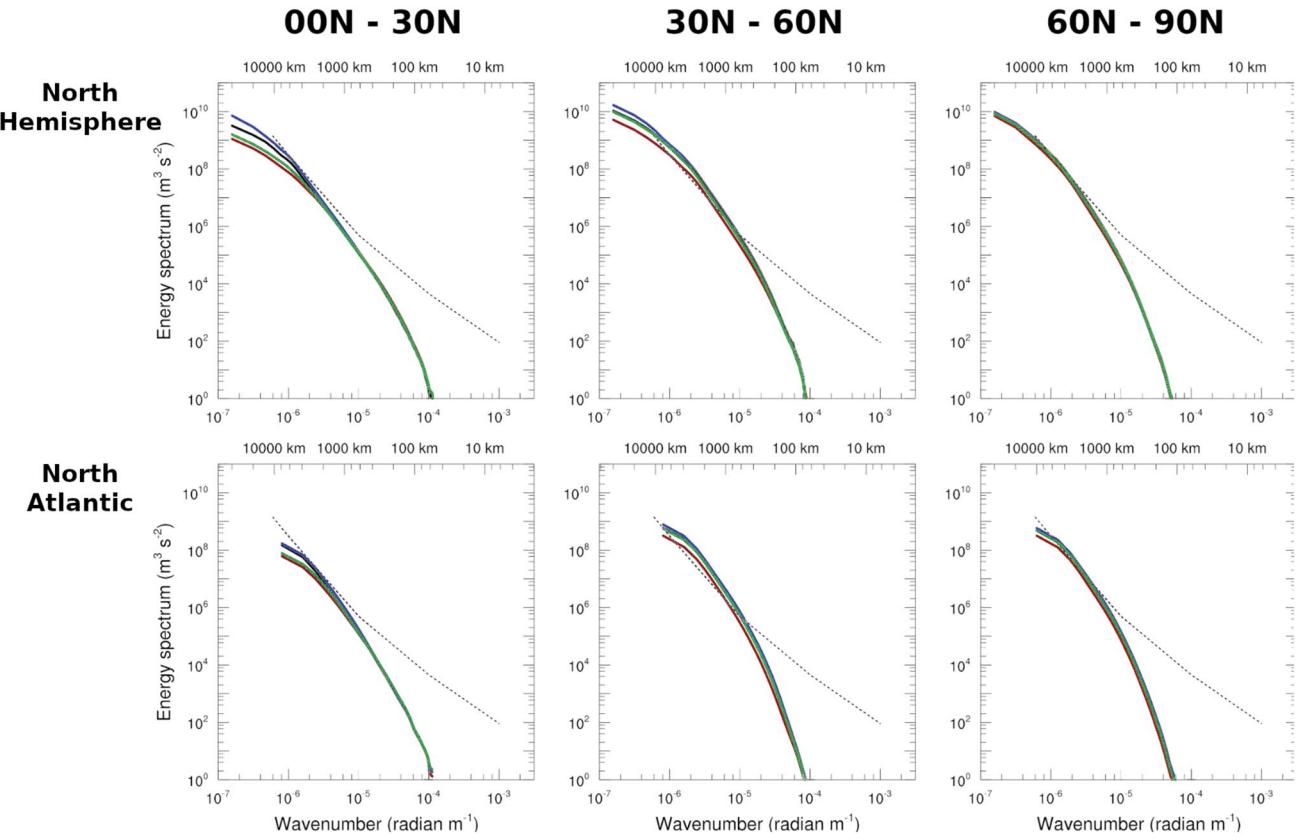


Fig. 5 Seasonal comparison of wind kinetic energy spectrum climatology for ERA5. Blue lines are DJF, black lines are MAM, red lines are JJA, green lines are SON, dashed lines correspond to the dissipation rate as per Lindborg (1999)

the damping of energy by the model and the divergence from the computed rate of dissipation. The curves end a little beyond 10^{-4} rad m^{-1} , or ≈ 50 km, as expected per $2\Delta x$.

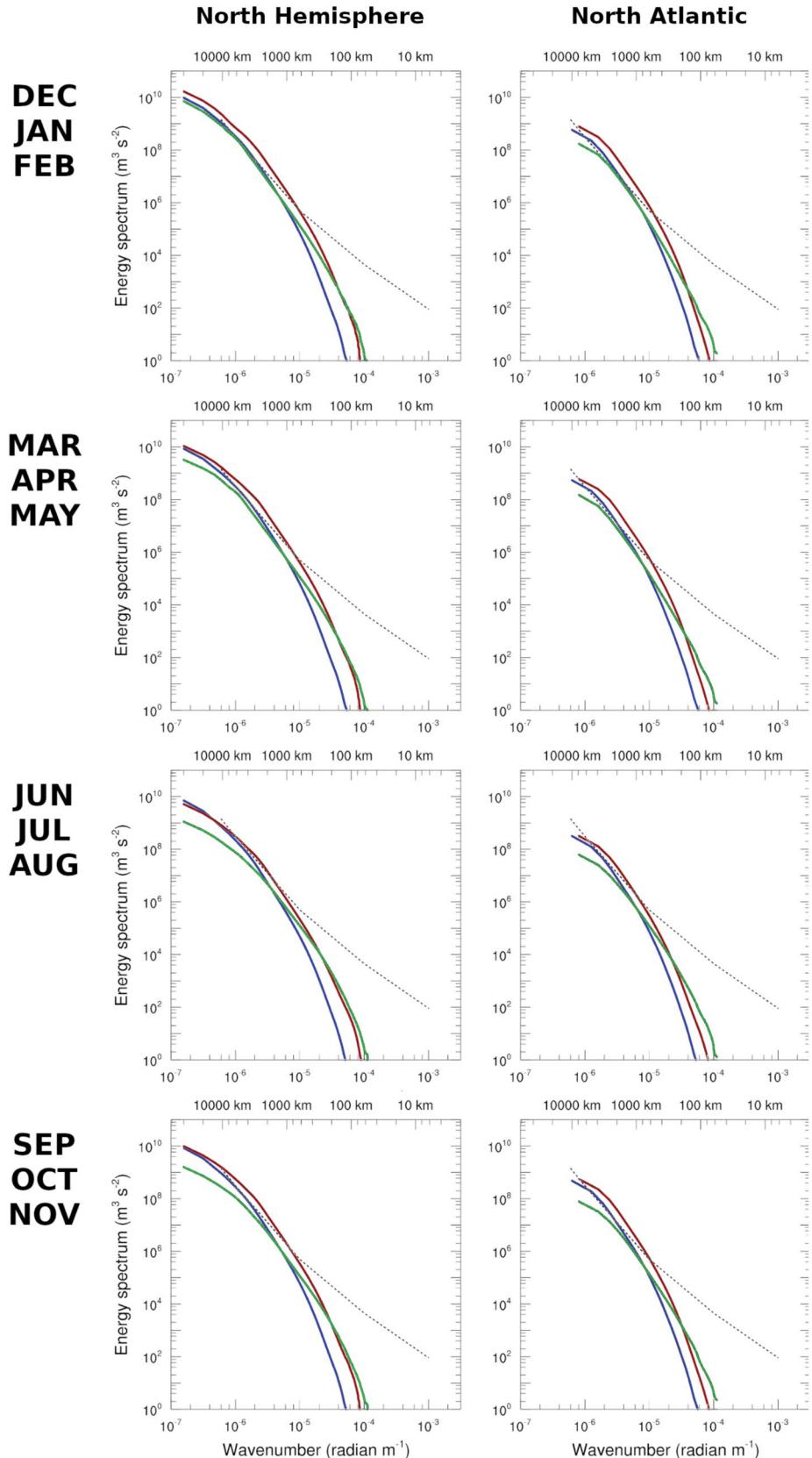
The previous results present a remarkable aspect of the effective resolution of the ERA5. As the spectra do not present a transition to $k^{-5/3}$, the reanalysis' effective resolution cannot be determined by the divergence to a steeper slope from the mesoscale curve. As a consequence, the limit has to be set on the point where the simulated curve diverges from the observation, as proposed by Skamarock (2004). That point is clearly seen at lower wavenumbers than expected for most spectra, approximately at 1300 km for the Tropical curves, at around 600 km for the Middle band and approximately at 1200 km for the Polar spectra (Fig. 5).

The results for the North Atlantic limited-area domains (Fig. 4) present spectra not reaching the 10,000 km wavelengths, as higher wavelengths are effectively filtered by the size of the domain. The curves are similar to those of the periodic domains in the global and synoptic scales, but present interesting differences at higher wavenumbers (Fig. 5). The divergence to steeper slopes is more pronounced for these results. The rates of dissipation are also higher, mostly for the Middle and Polar bands. Without a careful

assessment, the effective resolution for the limited-area seems to be closer to the mesoscale, but that is due to the larger spread of results in these domains. When the average curve is considered, the effective resolution may be defined approximately at 1100 km for the Tropical spectra, around 500 km for the Middle curves and approximately at 1000 km for the Polar area.

The poor results of the ERA5 in terms of effective resolution may be an interesting topic of research, albeit beyond the scope of this paper. Clearly, the grid and resolution changes from the IFS output to the ERA5 configuration take a toll on the effective resolution. Also, the assimilation of observations and the homogenization of data may affect the final effective resolution (Neyestani et al. 2021). Regardless of the source of it, the effective resolution marks the performance limits of the reanalysis and shows the necessity of using high-resolution NWP models for any research of mesoscalar phenomena (Bauer et al. 2015; Mass et al. 2002; Neyestani et al. 2021). It also presents the energetic uncertainties fed to those models when the dataset is used as initial and boundary conditions. In fact, the effective resolution of initial and boundary conditions should be considered when selecting the domain of study for a limited-area

Fig. 6 Latitudinal comparison of wind kinetic energy spectrum climatology for ERA5. Green lines are 00° N– 30° N, red lines are 30° N– 60° N, blue lines are 60° N– 90° N, dashed lines correspond to the dissipation rate as per Lindborg (1999)



high-resolution model. If the domain has any horizontal dimension smaller than the effective resolution, it will be resolving variables from initial and boundary data which is already energetically uncertain.

3.2 Latitudinal climatology

The ERA5 wind kinetic energy climatology for the North Hemisphere latitudinal bands or periodic domains is presented in Fig. 3. Here, the position and comparison against the observational curve (Lindborg 1999) is assessed. It is worth noting that initially the monthly results were considered (not shown); however a seasonal pattern was evident and the differences between months are not unalike enough to justify an individual analysis.

The Polar climatology (Fig. 3) shows very little differences among the seasons, as it can also seen in Fig. 5; in fact Polar MAM and SON for the North Hemisphere are the only curves which do not result statistically independent at 0.01. A slightly smaller energy content can be found for the JJA spectrum, and a somewhat larger one for the DJF spectrum; nevertheless, the four Polar curves are almost identical across the year. The spectra perform very well in terms of energy content for the synoptic scales, in wavelengths between 1000 and 10,000 km, being the average right on the expected curve at a wavenumber of 2.10^{-6} rad m $^{-1}$. Also, the four spectra present a high energy density at the lowest wavenumbers, $\approx 10^{10}$ m 3 s $^{-2}$, rapidly dissipating before reaching wavenumbers of 10 $^{-4}$ rad m $^{-1}$. This shows that the Polar climatology is dominated by very energetic and stable winds at synoptic scales with almost no energy produced by the convective and diabatic phenomena in the mesoscale, as expected.

On the other hand, the Tropical climatology (Fig. 3) presents rather different spectra. Even if the curves are underestimating the energy content in the mesoscale (due to the reasons presented in Sect. 3.1), the averages consistently reach a wavenumber of 10 $^{-4}$ rad m $^{-1}$ at the lowest energy density (Fig. 5) and present a shallower curve for the mesoscalar dissipation (Fig. 6). Thus indicating that the reanalysis properly captures the energy derived from convective processes at these latitudes. This work does not aim to shade light on the discussion about the downscale energy cascade or the upscale energy forcing from microscale phenomena, but both theories may be considered for the origin of the mentioned features of the spectra. For the synoptic scales, the Tropical climatology shows significant seasonal differences (Fig. 5). The JJA spectrum is clearly the less energetic season, presenting the lowest densities and a shallow dissipation from the global wavelengths down to 1000 km. The results for SON show a larger energy density than the previous, but still below the observed spectrum. The curve for MAM produces a notable increase at ≈ 4000 km, resulting

in a steeper curve. Finally, the spectrum for DJF is the most energetic one for the Tropical climatology, being very similar to the Polar curve at synoptic scales (Fig. 6). Comparing these two, is evident the influence of the mesoscale phenomena in the energy density and the rate of dissipation captured by the ERA5. The origin of the climatic variability of the spectra may be linked to the Inter-Tropical Convergence Zone (ITCZ), as this forces not only the trade winds and convection, affecting the mesoscale, but also the pattern of the tropical easterly jet, influencing the energy in the synoptic range (Ba and Nicholson 1998; Jackson et al. 2009; Mohr and Thorncroft 2006). The ITCZ will invade or leave the described Tropical band along the year bringing a large variation of winds, convection and latent heat processes (Ba and Nicholson 1998; Futyán and Del Genio 2007).

The climatology for the Middle latitudes (Fig. 3) is the most energetic. The energy content for each season behaves similar to the Tropical band, being from less to more energetic, JJA, SON, MAM and DJF (Fig. 5). The variability of the results may be somewhat lower than for the Tropical spectra, albeit being much larger than for the Polar band. Again, the summer season shows the lower density in the synoptic scales, nevertheless, this spectrum is very close to the observational curve. The curves for the other three seasons are clearly over-energetic, most probably forced by lows with associated fronts, jet streams and modes of low-frequency linking weather and climate anomalies over large distances across the globe (Barnston and Livezey 1987; Boer and Shepherd 1983; Martín et al. 2004; Santos-Muñoz et al. 2006; Tripoli et al. 2005; Valero et al. 2004). Regarding the mesoscale, the Middle spectra lie more or less in between the Tropical and the Polar ones, as expected (Fig. 6). Overall, the Middle latitudes produce the most adequate spectra, as the observed energy dissipation is within the range of simulated spectra for the entire synoptic scale (Kao and Wendell 1970).

3.3 North Atlantic climatology

The ERA5 energy spectrum climatology for the North Atlantic bands or limited-area domains is presented in Fig. 4. In terms of seasonal behaviour, the spectra show the same characteristics as the North Hemisphere latitudinal bands described in Sect. 3.2 (Fig. 5). JJA is the least energetic season while DJF presents the highest kinetic energy. The differences among the three different latitudinal bands are also in line with the previous results (Fig. 6). The North Atlantic Polar domain shows a very stable spectrum across the seasons, with little presence of energetic input from mesoscalar phenomena and a high density at synoptic wavenumbers. The Tropical domain for the North Atlantic presents a large variation during the year, with the lowest energy density for synoptic phenomena and the highest for mesoscalar. The

Middle latitudes in the North Atlantic Ocean also generate a large seasonal variability, with the largest energy input at low wavenumbers but still showing the influence of convection and latent heat at high wavenumbers.

Despite the similarities between Figs. 3 and 4, there are two large differences between the hemispheric bands and the North Atlantic domains. The first one is the dispersion of the spectra. The limited-area domains produce a wider range for the energy density, most notable at the higher wavenumbers. This can be partially influenced by the removal of the compensating mechanisms that may happen when evaluating global scales. Selecting only the North Atlantic area can remove the effects of continents and the Pacific Ocean into the wind, thus producing results more prone to variations due to the local situation, even if the issue is about climatic frames of time.

The second difference with the periodic domain results is found in the energy levels for the North Atlantic spectra. The kinetic energy density is higher at synoptic scales for almost every season and latitudinal band (Fig. 5). The Tropical domains are the most similar ones, with overlapping curves in the mesoscalar range and almost identical curves for JJA. However, for the other three seasons a slightly higher energy content is found above wavenumbers of 10^{-5} rad m $^{-1}$. The higher energy content is more pronounced at these wavenumbers for the Middle and Polar areas. Again, the origin of these differences may be found in the selection of the domain and the characteristics of the wind over it. On the other hand, the behaviour of the spectra for the mesoscale is different for each latitudinal band (Nastrom and Gage 1985; Stefanova and Krishnamurti 2011). The Tropical curves are almost identical below 10^{-5} rad m $^{-1}$ for both periodic and limited-area domains. Nevertheless, while the North Atlantic Polar results show higher energy contents than the periodic domain, the curves for the Middle latitudes tend to present lower contents and increased dissipation rates.

3.4 Case study

The synoptic situation of the storm Delta on 22 NOV (Fig. 7a, c, e) is initially characterized by a blocking configuration with a high over the British Islands and a cut-off low near the south-west of Iberia. A deep extratropical cyclone (Delta) with a trough at high upper levels is also located south-west of the Azores Islands. The blocking pattern allows the extratropical system to isolate from the general circulation. By 23 NOV (Fig. 7b, d, f), Delta is not solely governed by quasigeostrophic processes any more and begins to be sustained by a mixture of diabatic and baroclinic processes, general characteristics of a subtropical cyclone (Evans and Guishard 2009). The synoptic situation is characterized by an upper-level cut-off low around 30°N 040°W, the potential vorticity is vertically redistributed by

an important latent heat release (e.g., differential diabatic heat source; not shown) and, thus, a tropical cyclone at the surface purely governed by diabatic processes.

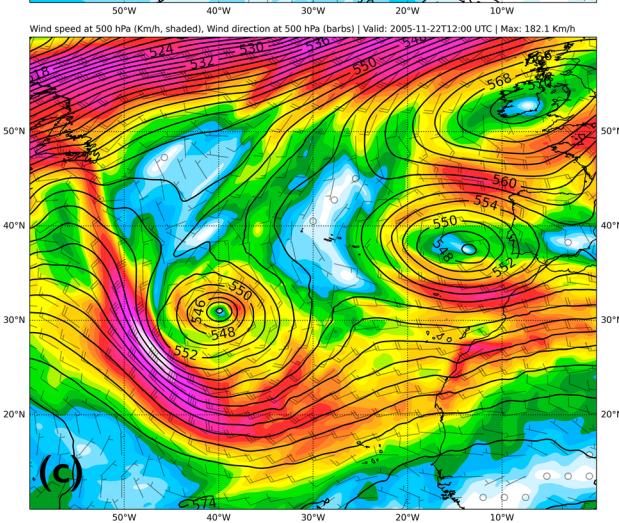
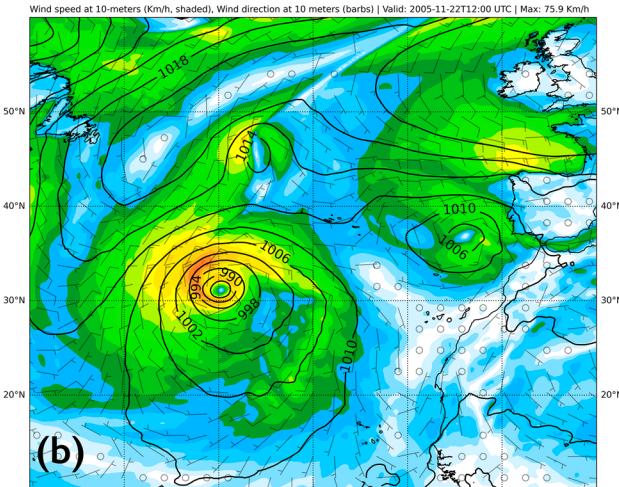
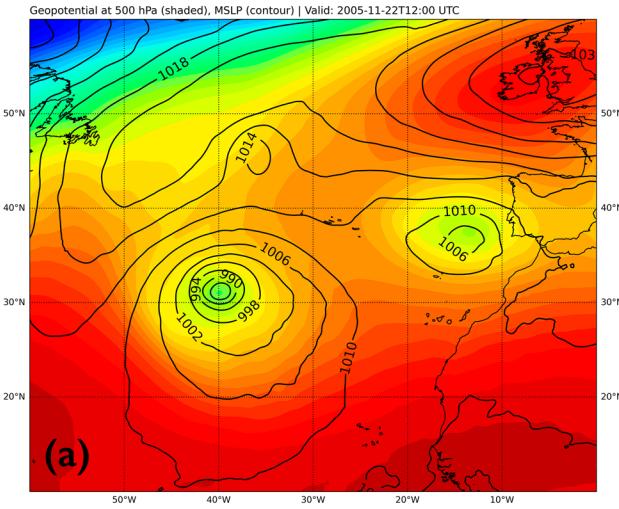
The surface wind speed field on 22 NOV (Fig. 7c) presents the characteristical asymmetry of subtropical cyclones with a predominance of values exceeding 80 km h $^{-1}$ in the north-west quadrant, sustained winds around 60 km h $^{-1}$ in the centre, and lower values in the south-east quadrant of the system. This is in line with the results by Quitián-Hernández et al. (2020, 2021), who already noted this asymmetry in similar systems. The winds at 500 hPa (Fig. 7e, f) show notably larger values than surface winds, clearly reinforced by a jet stream on the south-west quadrant. This is also frequent in this kind of systems, as the wind speed profile usually shows a reduction with height down to 3000 m, and increasing cyclonic winds aloft with two jets around 600 and 400 hPa (Evans and Guishard 2009).

The aforementioned situation indicates a state of high energy in the middle levels of the atmosphere, as expected for a subtropical storm (Evans and Guishard 2009), mainly forced by the jet stream present at 500 hPa (Fig. 7). This is clearly reflected for the synoptic scales in the kinetic energy spectrum (Fig. 8). At wavenumbers of 10^{-5} rad m $^{-1}$ the curve is well above by standard referenced observations (Lindborg 1999), clearly over-energized with respect to the SON Tropical climatology (Fig. 3) and the corresponding North Atlantic spectrum (Fig. 4). The excess of energy is shown into the mesoscale also, almost down to 100 km, albeit having a larger dissipation rate too. This is in line with previous results in this work indicating that ERA5 reanalysis is capturing the convective and latent heat processes involved (Hamilton et al. 2008; Nastrom and Gage 1985; Robertson et al. 2020; Rodríguez and Bech 2021). However, this is only partially achieved, as there is no sign of the transition to $k^{-5/3}$ and the amount of energy produced by convection in a tropical transition process is also above average. Overall, the resulting spectrum is according to the expectations and adequate to the atmospheric situation described, within the limitations of the ERA5. Nevertheless, these results are not appropriate enough to perform an in-depth study of a subtropical cyclone or any other atmospheric phenomena governed by mesoscalar processes. The uncertainties introduced by the dataset at mesoscalar ranges make it advisable to use a high-resolution NWP model for the simulation of this kind of meteorological systems.

4 Conclusions

The present study evaluates the climatology of wind kinetic energy for the ERA5 dataset following the energy spectrum methodology proposed by Skamarock (2004). The results have been generated using the 500 hPa u and v wind

12:00 UTC November 22



12:00 UTC November 23

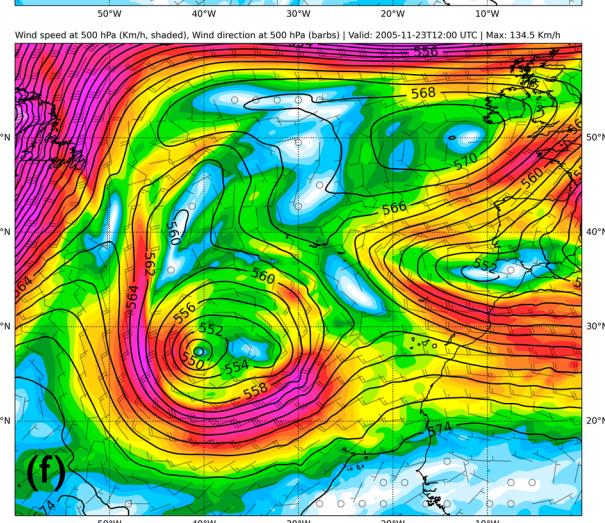
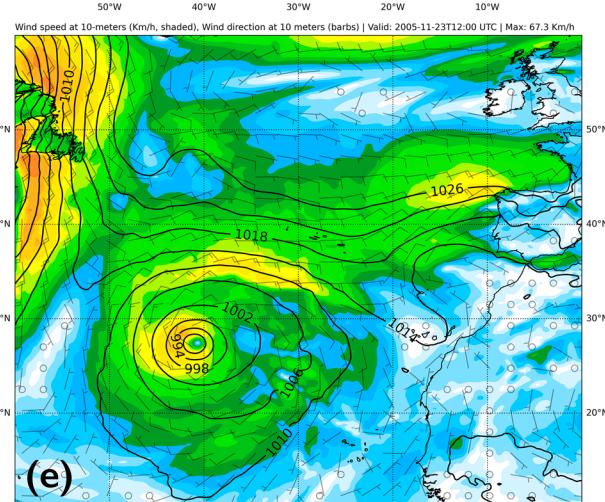
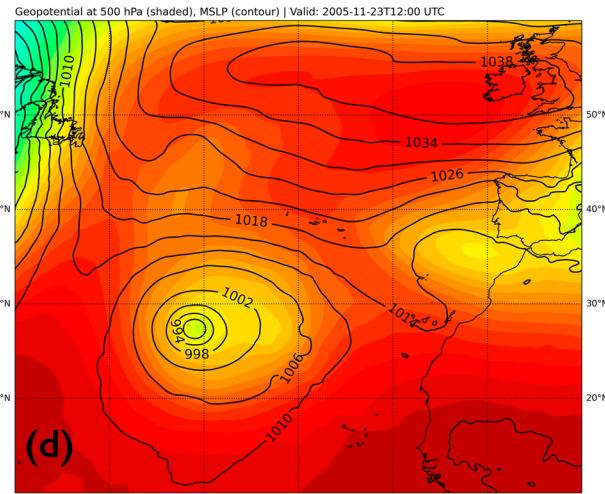


Fig. 7 **a, b** Mean sea level pressure (hPa, contours) and 500 hPa geopotential height (dm, shaded). **c, d** 10-m wind speed (km h^{-1} , shaded), direction (barbs) and mean sea level pressure (hPa, con-

tours). **e, f** 500 hPa wind speed (km h^{-1} , shaded), direction (barbs) and 500 hPa geopotential (gpm, contours)

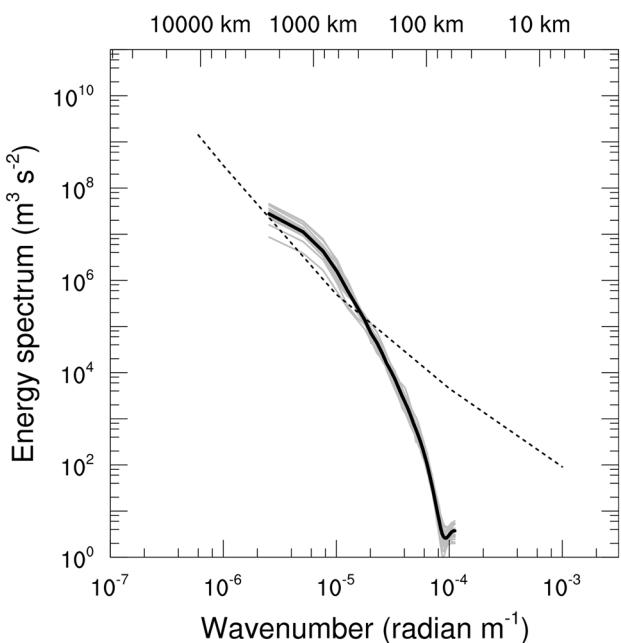


Fig. 8 ERA5 wind kinetic energy spectrum at 500 hPa for the domain of storm Delta from 00:00 UTC 22 NOV 2015 to 00:00 UTC 25 NOV 2015. Grey lines are individual spectra, the black line is the average, the dashed line corresponds to the dissipation rate as per Lindborg (1999)

components, from 1979 to 2020, with 6-hourly data outputs and 0.25° horizontal resolution. The climatologies are presented in 30° latitudinal bands, for the Northern Hemisphere and the North Atlantic areas. These spectra are also used to determine the effective resolution of the reanalysis. Finally, a case study for a tropical transition is presented, to assess the adequacy of the ERA5 to evaluate this type of phenomena. The major conclusions derived from the results are hereby presented:

- The ERA5 dataset is able to properly capture the synoptic scale kinetic energy spectrum, as defined from observations (Lindborg 1999; Nastrom and Gage 1985).
- The simulated spectra are not properly reproducing the energetic densities expected at mesoscalar ranges, in contradiction with previous studies on the IFS model (Abdalla et al. 2013). They do not show the dissipation rate transition from k^{-3} to $k^{-5/3}$ (Lindborg 1999) either. This is most probably due to the resolution changes and grid standardization processes involved in the reanalysis.
- The results drive the effective resolution to be defined between 1300 and 1100 km for the Tropical band, between 600 and 500 km for the Middle latitudes, and between 1200 and 1000 km for the Polar area, as per Skamarock (2004) methodology.
- The three latitudinal bands present characteristic differences, in the hemispherical and North Atlantic climatolo-

gies, indicating that the ERA5 is properly reproducing the synoptic conditions, in line with Nastrom and Gage (1985), and partially capturing the mesoscalar status of each latitude. The Middle bands presents a higher energy at synoptic levels, due to westerly winds. The Tropical domains show higher mesoscalar energy contents. The Polar latitudes are the most stable, with upper wind energies right in the expected levels and no convective activity.

- There are also seasonal differences, being DJF the most energetic period and JJA the season with the least energy density. These differences are almost negligible for the Polar domains.
- When comparing the results for the North Atlantic to the hemispheric ones, it can be seen that the limited-area domain introduces a wider energy range for each wavenumber. Also, the energy content is higher in the North Atlantic, mainly at synoptic scales.
- The results for an atmospheric high energetic status, namely, cyclone Delta tropical transition, show an over-energized spectrum. When compared with the corresponding climatology curve, the expected excess of energy is reproduced by the ERA5 at synoptic and mesoscales. Nevertheless, the dissipation rates produced by the spectra show that the reanalysis' curve is not adequate to evaluate phenomena with a large forcing from convection and latent heat processes.

Reanalyses derived from GCMs provide an excellent opportunity to expand the knowledge about climatic spectra. To the authors' knowledge, this is the only climatology published for wind kinetic energy spectra. Also, it's the first time spectra have been computed covering the whole hemisphere, reaching wavelengths up to 40,000 km. The value of ERA5 as a research tool is indisputable and here we provide a novel energetic climatology and spectral curves for future reference. The results may be used in the future to compare against different atmospheric configurations where energy may play a major role, as performed in the case study. This work may also help understanding better the adequacy and limitations of the reanalysis. Mainly for the type and scale of the atmospheric phenomena it should be used to research on. But also for the uncertainties it can introduce when used as initial and boundary conditions for high-resolution NWP models. The authors consider this later topic would be of interest for further studies. In addition, it would be worthwhile to deepen the study related to the performance of the dataset. The transformation from the GCM analysis to the final reanalysis seems to be deteriorating the results in terms of effective resolution, and this should be addressed.

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Author contributions PB contributed to the manuscript design, methodology preparation, data collection and analysis. CC-S contributed to the manuscript design, methodology preparation, data collection and analysis. JD-F contributed to the manuscript design and composition of the manuscript. LQ-H contributed to the manuscript design and composition of the manuscript. MS contributed to the manuscript design, methodology preparation, data collection and analysis. DS-M contributed to the manuscript design and composition of the manuscript. JIF contributed to the manuscript design, data collection and composition of the manuscript. JJG-A contributed to the manuscript design and composition of the manuscript. FV contributed to the manuscript design and composition of the manuscript. MLM contributed to the manuscript design, methodology preparation, data collection and analysis. All authors commented on the various previous versions of the manuscript. All authors read and approved the final manuscript.

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Availability of data and material The data used for this work is public and freely available through the EU-funded Copernicus Climate Change Service.

Code availability The main results of this work were obtained using the NCAR Command Language software. The scripts are available upon request.

Declarations

Conflict of interest The authors declare no conflict of interest. The funding sponsors have no participation in the execution of the experiment, the decision to publish the results, nor the writing of the manuscript.

Ethical approval Not applicable.

Consent to participate Not applicable.

Consent for publication Not applicable.

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