Vector Semantics

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Announcements

• Individual assignment 1 deadline: 03/03, 23:59

Overview

- Vector semantics
- Matrix representations
- Calculating vectors
- 4 Similarity measures
- 5 Evaluation

Vector semantics

The quest for meaning

- The realm of *lexical semantics*.
- A lemma can be associated with multiple word senses (e.g., "mouse (N)".
- The many facets of 'meaning':
 - Propositional synonymity: two words (senses) are synonyms if the truth conditions of a sentence do not change when we swap them.
 - Word similarity: some features are shared, but no synonyms. E.g., 'cat' and 'dog'.
 - Word relatedness: no features are shared, but there is a relationship. E.g., 'water' and 'bottle'.
 - Semantic frames or topics: topical structure in documents. E.g., 'sport' and 'politics'.
 - Connotations, e.g., sentiment (positive, negative), tone (formal or not).

Denotational vs distributional approaches

- Denotational approach: define (dictionary) meaning then apply definition. Meaning as dictionary index.
- Distributional approach: look at data to come up with meaning.
 Distributional hypothesis: "the amount of meaning difference between two words corresponds roughly to the amount of difference in their environments" (contexts of appearance). Harris, 1954.

Vector Semantics

"The meaning of a word is its use in the language." Wittgenstein, 1953.

- 1 ??? is best when cooked just right.
- ② I prefer my ??? with abundant tomato sauce.
- 3 I eat ??? for lunch.
- Would you like tomato sauce on your pizza?
- We went to a pizza place for lunch.
- Pizza should not be too cooked: it burns!

Can you guess ???

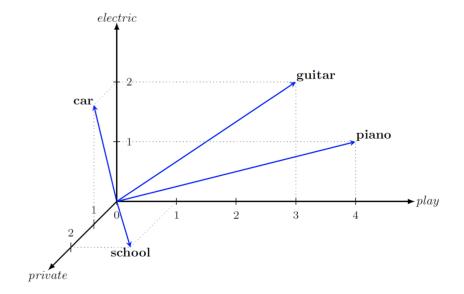
Vector Semantics

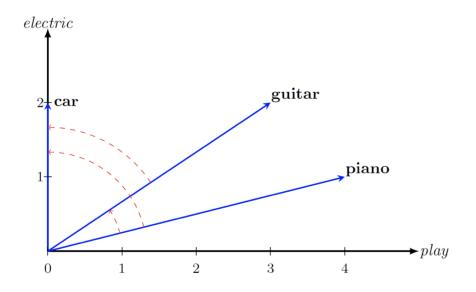
"The meaning of a word is its use in the language." Wittgenstein, 1953.

- Pasta is best when cooked just right.
- Pizza should not be too cooked: it burns!
- Vector semantics combines two intuitions:
 - ▶ **Distributional approach**: define a word by the contexts it occurs into.
 - Vectorize it: use vectors to represent word meaning, as a point in space.
- Feature engineering for NLP: word vectors are increasingly used as features for other tasks.
- (Word) vectors are usually referred as (word) embeddings in modern neural network literature.

```
...ound and sonic power of a [new electric
                                              guitar
                                                      played through] a guitar amp has play...
                          ...[Some electric
                                              guitar
                                                      models featurel piezoelectric pickups...
                                 ...[Playing
                                              guitar
                                                      with a] pick produces a bright sound ...
...ings, he is known for [playing fretless
                                              guitar
                                                      in his] performances...
                ...the neck of [a classical
                                              guitar
                                                      is too] wide and the normal position ...
...t in the centre of Bristol [playing the
                                                      , I was] punched in the head while, a...
                                              piano
...r in Houston, Texanstagram [playing the
                                              piano
                                                      in his] flooded home after Hurrican H...
... some supplies, he stopped to [play the
                                              piano
                                                      that was] sitting in knee-high water ...
...te and one black, who [played classical
                                              piano
                                                      together]...
                     ...The [first electric
                                              pianos
                                                      from thel late 1920s used metal strin...
...technologies, for example [the electric
                                               car
                                                      and thel integration of mobile commun...
...study had each driver of [each electric
                                               car
                                                      drive unimpeded], perform a task whil...
...Honda to commence testing of [their new
                                               car
                                                      and thel American was no doubt more t...
...mary design considerations for [the new
                                                      were "safety] innovations, performanc...
                                               car
...would be possible if almost [all private
                                                      requiring drivers], which are not in ...
                                               cars
... who donate to groups [providing private
                                                      scholarships have] written pieces att...
                                              school
... that students participating [in private
                                              school
                                                      choice programs] graduate high school...
...s in the establishment of this [new high
                                              school.
                                                       , named the | Gavirate Business School...
         ...Anna heads into her [final high
                                              school
                                                      vear beforel university wanting somet...
... but he can prevent them from [playing at school]
```

	play	electric	classical	private	high	 the	new
guitar	3	2	1	0	0	 0	1
piano	4	1	1	0	0	 4	0
car	0	2	0	1	0	 4	2
school	1	0	0	2	2	 1	1





Matrix representations

Word-Document matrix

• We have a set of documents D and a vocabulary V. X is a $|V| \times |D|$ matrix with word occurrences in documents.

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	1	0	7	13
good	114	80	62	89
fool	36	58	1	4
wit	20	15	2	3

Figure 6.2 The term-document matrix for four words in four Shakespeare plays. Each cell contains the number of times the (row) word occurs in the (column) document.

Word-Document matrix

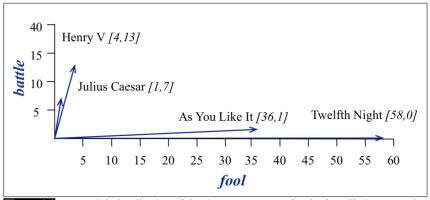


Figure 6.4 A spatial visualization of the document vectors for the four Shakespeare play documents, showing just two of the dimensions, corresponding to the words *battle* and *fool*. The comedies have high values for the *fool* dimension and low values for the *battle* dimension.

Word-Context matrix

- We have a set of words V and a set of contexts they occur into C, taken from our corpus of documents. X in this case is a $|V| \times |C|$ matrix with word occurrences in contexts.
- The most intuitive context are co-occurrences with other words in V, within a certain **window**. In this case, X would be a $|V| \times |V|$ matrix.

	aardvark	 computer	data	pinch	result	sugar	
apricot	0	 0	0	1	0	1	
pineapple	0	 0	0	1	0	1	
digital	0	 2	1	0	1	0	
information	0	 1	6	0	4	0	

Figure 6.5 Co-occurrence vectors for four words, computed from the Brown corpus, showing only six of the dimensions (hand-picked for pedagogical purposes). The vector for the word *digital* is outlined in red. Note that a real vector would have vastly more dimensions and thus be much sparser.

Word-Context matrix

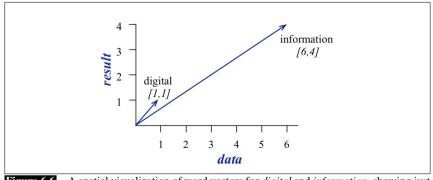


Figure 6.6 A spatial visualization of word vectors for *digital* and *information*, showing just two of the dimensions, corresponding to the words *data* and *result*.

Types of co-occurrences

Surface co-occurrence:

- ▶ a contextual word co-occurs with the target word as many times as the former appears in a collocational span (window) surrounding the latter.
- ► The span may be symmetric ([-5w, +5w]) or asymmetric ([-5w, 0]).

Textual co-occurrence:

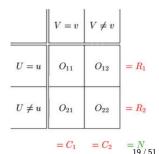
- words co-occur if they appear in the same text segment (e.g., a sentence, a paragraph, a web page ...).
- It usually does not matter how many times each word occur in each document

Syntactic co-occurrence:

count word co-occurrences in a specific syntactic relation (e.g., verb-object, adjective-noun ...).

Contingency tables

- Tabular representation of the observed frequencies between the variable whose values are reported in rows and the variable whose values are reported in columns.
- Intermediate step for some calculations we will see.
- If *u* is our target word and *v* is a contextual word:
 - ▶ O_{11} observed frequency of u and v (i.e., f(u, v)).
 - $ightharpoonup R_1$, R_2 , C_1 , C_2 marginal frequencies.
 - $ightharpoonup R_1$ absolute frequency of u (i.e. f(u)).
 - $ightharpoonup C_1$ absolute frequency of v (i.e. f(v)).
 - $ightharpoonup N = O_{11} + O_{12} + O_{21} + O_{22}$ sample size.



Contingency tables – Surface co-occurrences

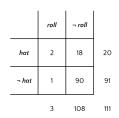
- w1 = ``hat''; w2 = ``roll''.
- Collocational span: ± 4 words (i.e. [-4w, +4w]).
- Spans cannot cross sentence boundaries.

A vast deal of coolness and a peculiar degree of judgement, are [requisite in catching a hat]. A man must not be precipitate, or he runs over it; he must not rush into the opposite extreme, or he loses it altogether. There was a fine gentle [wind, and Mr. Pickwick's hat rolled sportively before it]. The wind puffed, and Mr. [Pickwick puffed, and the hat rolled over and over] as merrily as a lively porpoise in a strong tide; and on it might have rolled, far beyond Mr. Pickwick's reach, had not its course been providentially stopped, just as that gentleman was on the point of resigning it to its fate.

Contingency tables – Surface co-occurrences

- w1 = "hat"; w2 = "roll".
- Collocational span: ± 4 words (i.e. [-4w, +4w]).
- Spans cannot cross sentence boundaries.

observed frequencies



NOTE: N equals the number of tokens in the corpus

Contingency tables – Textual co-occurrences

- w1 = "hat"; w2 = "over".
- Unit is sentence (multiple occurrence is the same unit are ignored).

A vast deal of coolness and a peculiar degree of judgement, are requisite in catching a hat	hat	
A man must not be precipitate, or he runs <i>over</i> it		over
he must not rush into the opposite extreme, or he loses it altogether		
There was a fine gentle wind, and Mr. Pickwick's halt rolled sportively before it	hat	
The wind puffed, and Mr. Pickwick puffed, and the hat rolled over and over as merrily as a lively porpoise in a strong tide	hat	over

Contingency tables – Textual co-occurrences

- w1 = "hat"; w2 = "over".
- Unit is sentence (multiple occurrence is the same unit are ignored).

observed frequencies

		over	¬over	
•	hat	1	2	3
•	¬ hat	1	1	2
		2	3	5

NOTE: *N* equals the number of text units

Calculating vectors

Families of vectors

- **Sparse vectors**: many zero values and high-dimensional spaces. E.g., weighted co-occurrence matrices (this class).
- Dense vectors: no zero values and smaller-dimensional spaces.
 - ▶ Dimensionality reduction (Latent Semantic Analysis or truncated Singular Value Decomposition, Principal Component Analysis, Non-negative Matrix Factorization, and many more): mostly we skip, there is a little in the next lab.
 - ▶ Neural-networks (Skigp-gram, CBOW, GloVe): next class.

(Better) quantifying association

Raw co-occurrence frequency is often not the optimal measure of association between a word and a context:

- we need a way to estimate to what extent a context word is particularly informative about a target word;
- frequencies are very skewed.
- A couple of solutions: tf-idf and PPMI.

Term frequency - Inverse document frequency

- Tf-idf is the standard weighting scheme for term-document matrices.
- It is likely the most used weighting scheme in Information Retrieval.
- **Term frequency** tf(t, d) = the number of times term t occurs in document d. M any variants exist (e.g., using a log transform). It accounts for how frequent t is within the document collection.
- Inverse document frequency $idf(t) = log\left(\frac{|D|}{|D_t|}\right)$; where D is the collection of documents and D_t is the subset where term t appears once or more. It accounts for how 'discriminative' t is with respect to the document collection.

$$tfidf(t, d) = tf(t, d) \times idf(t)$$

Term frequency - Inverse document frequency

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	1	0	7	13
good	114	80	62	89
fool	36	58	1	4
wit	20	15	2	3

Figure 6.2 The term-document matrix for four words in four Shakespeare plays. Each cell contains the number of times the (row) word occurs in the (column) document.

Word	df	idf
Romeo	1	1.57
salad	2	1.27
Falstaff	4	0.967
forest	12	0.489
battle	21	0.074
fool	36	0.012
good	37	0
sweet	37	0

Term frequency - Inverse document frequency

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	1	0	7	13
good	114	80	62	89
fool	36	58	1	4
wit	20	15	2	3

Figure 6.2 The term-document matrix for four words in four Shakespeare plays. Each cell contains the number of times the (row) word occurs in the (column) document.

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	0.074	0	0.22	0.28
good	0	0	0	0
fool	0.019	0.021	0.0036	0.0083
wit	0.049	0.044	0.018	0.022

Figure 6.8 A tf-idf weighted term-document matrix for four words in four Shakespeare plays, using the counts in Fig. 6.2. Note that the idf weighting has eliminated the importance of the ubiquitous word *good* and vastly reduced the impact of the almost-ubiquitous word *fool*.

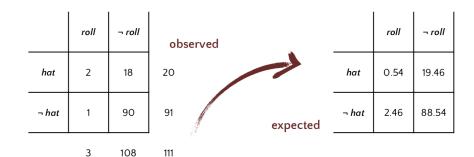
Intuition: in order to discriminate between informative and uninformative word-context associations, let us take the expected frequency into account as a baseline.

- The expected frequency of a (word, context) pair is a measure of how often a word would occur in a context if the two linguistic entities were statistically independent (i.e., if they were occurring by chance).
- The expected frequency can be estimated from the marginals in the contingency table:

$$E_{11} = \frac{f(u)f(v)}{N}$$

	V = v	$V \neq v$
U = u	$E_{11} = \frac{R_1 C_1}{N}$	$E_{12} = \frac{R_1 C_2}{N}$
$U \neq u$	$E_{21} = \frac{R_2 C_1}{N}$	$E_{22} = \frac{R_2 C_2}{N}$

		roll	¬ roll	observed	
	hat	2	18	20	
•	¬ hat	1	90	91	
		3	108	111	



 Mutual Information provides a measure of independence of two random variables X and Y:

$$MI(X,Y) = \sum_{x \in X} \sum_{y \in Y} P(x,y) log \frac{P(x,y)}{P(x)P(y)}$$

 Pointwise Mutual Information is the part related to two outcomes x and y:

$$PMI(x, y) = log \frac{P(x, y)}{P(x)P(y)}$$

• Us, we are interested in a word-context pair, w and c:

$$PMI(w, c) = log \frac{P(w, c)}{P(w)P(c)}$$

 We are not interested in joint events more unlikely than independent ones, thus we usually just consider the positive values of PPMI:

$$PPMI(w, c) = max(0, log \frac{P(w, c)}{P(w)P(c)})$$

- Many variants to account for minor issues:
 - ▶ **Positive Local Mutual Information**: deals with the tendency of PPMI to emphasize rare events over frequent ones:

$$PLMI(w, c) = max(0, f(w, c) \times PMI(w, c))$$

PPMI

p(w,context)						
	computer	data	pinch	result	sugar	p(w)
apricot	0	0	0.05	0	0.05	0.11
pineapple	0	0	0.05	0	0.05	0.11
digital	0.11	0.05	0	0.05	0	0.21
information	0.05	.32	0	0.21	0	0.58
p(context)	0.16	0.37	0.11	0.26	0.11	

Figure 6.9 Replacing the counts in Fig. 6.5 with joint probabilities, showing the marginals around the outside.

	computer	data	pinch	result	sugar
apricot	0	0	2.25	0	2.25
pineapple	0	0	2.25	0	2.25
digital	1.66	0	0	0	0
information	0	0.57	0	0.47	0

Figure 6.10 The PPMI matrix showing the association between words and context words, computed from the counts in Fig. 6.5 again showing five dimensions. Note that the 0 ppmi values are ones that had a negative pmi; for example pmi(information,computer) = $\log 2(.05/(.16*.58)) = -0.618$, meaning that information and computer co-occur in this mini-corpus slightly less often than we would expect by chance, and with ppmi we replace negative values by zero. Many of the zero ppmi values had a pmi of $-\infty$, like pmi(apricot,computer) = $\log 2(0/(0.16*0.11)) = \log 2(0) = -\infty$.

Example: Collostructions in linguistics

```
an accident waiting to happen - Idioms by The Free Diction
                  accident waiting to happen Definition from Wiktionary.
. News 'This is a Ferguson waiting to happen:' Activists speak out again:
se > Idioms > A > Accident waiting to happen Idiom: Accident waiting to }
                  Trouble Waiting to Happen From Wikipedia, the free end
26 April 2015. 'Nightmare Waiting to Happen': Quake Experts Gathered in
at Start reading Accidents Waiting to Happen on the free Kindle Reading A
Earthquake Was "Nightmare Waiting to Happen" Slate Sign In Sign Up Slate
gions Disasters 'Nightmare waiting to happen': Experts gathered in Nepal
an></span></div> A tragedy waiting to happen By Colin Stark Updated 1759
cal quake was a "nightmare waiting to happen" Breaking News US Secretary
Vepal quake was 'nightmare waiting to happen' Major earthquakes hit Nepa:
umph of Life Contact Tarot Waiting to Happen - A Tarot Deck by Andrew McC
nergy Solution or Accident Waiting to Happen: The Public and Nuclear Power
/ Angela Weight and Sanity Waiting to Happen don't live here anymore. Cor
of Things Is a Revolution Waiting to Happen The challenge of the IoT is
arthquake was a 'nightmare waiting to happen' says lead scientist Expert:
     Angela Weight Sanity Waiting to Happen Skip to content Home Book(s)
tos Games Music En Deadman Waiting To Happen by nProcess Random Animation
              an accident waiting to happen - definition in the British
Bhui-temblorA catastrophe waiting to happen? The author has posted comme
grade Winter Meeting trade waiting to happen between M's. Rockies JP More
2 Author Savs Disaster Was Waiting to Happen Don't Miss Out - Follow us
earthquake was a disaster waiting to happen Sitting on one of the most (
gallery 10 Sports Injuries Waiting to Happen of Advertisement Skip this a
en Noun (plural disasters waiting to happen) Something potentially very
1st Classic FAILs accident waiting to happen Share on Facebook- Featured
```

What is generally waiting to happen?

Example: Collostructions in linguistics

	accident	¬ accident	Row totals
[N waiting to happen]	14	21	35
¬ [N waiting to happen]	8,606	10,197,659	10,206,265
Column totals	8,620	10,197,680	10,206,300

Table: Contingency table from Stefanowitsch & Gries (2003) for the noun accident in the [N waiting to happen] construction

$$P(accident, waiting to happen) = \frac{14}{10,206,300} \\ P(accident) = \frac{8,606}{10,206,300} \\ P(waiting to happen) = \frac{35}{10,206,300} \\ PMI(accident, waiting to happen) = log \frac{0.00000137}{0.000843*0.00000342} = 474.38 \\ Independence when PMI is 0, association when PMI > 0$$

Associations in Dutch Google N-grams corpus: https://urd2.let.rug.nl/~gosse/bin/Web1T5_assoc.perl

Similarity measures

Comparing vectors: the dot product

- Now we know how to calculate the first-order associations between words and how to use this information to create a distributional representation of each word.
- **Similarity measures** can be used to quantify the distance between two vectors in a space, and this can be used to estimate how similar the represented words are.
- Most vector similarity measure are based on the dot (inner) product:

$$\vec{u} \cdot \vec{v} = \sum_{i=1}^{d} u_i v_i = u_1 v_1 + u_2 v_2 + \dots + u_d v_d$$

Comparing vectors: Euclidean distance

- When used as a similarity metric, the dot product has a problem: it favors vectors with higher values (e.g., frequencies).
- It is the same issue you have with the Euclidean norm:

$$||\vec{v}|| = \sqrt{\sum_{i=1}^d v_i^2}$$

• from which the Euclidean distance stems:

$$d(\overrightarrow{u},\overrightarrow{v}) = ||\overrightarrow{u} - \overrightarrow{v}|| = \sqrt{\sum_{i=1}^d (u_i - v_i)^2}$$

 A similarity measure that is sensitive to frequency can sometimes work, yet other times it is the direction of vectors which is more important.

Comparing vectors: Cosine distance

 A solution is to use the cosine of the angle between the two vectors:

$$cosine(\vec{u}, \vec{v}) = \frac{\vec{u} \cdot \vec{v}}{||\vec{u}||||\vec{v}||} = \frac{\sum_{i=1}^{d} u_i v_i}{\sqrt{\sum_{i=1}^{d} u_i^2} \sqrt{\sum_{i=1}^{d} v_i^2}}$$

• The cosine ranges between 1 and -1, taking value 0 for orthogonal vectors. Due to the fact that PPMIs and other frequencies are always non-negative, cosine ranges from 0 to 1 (identically directed vectors).

Cosine

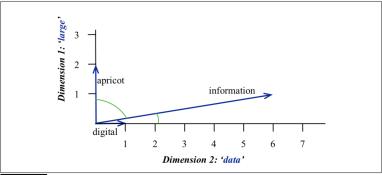


Figure 6.7 A graphical demonstration of cosine similarity, showing vectors for three words (apricot, digital, and information) in the two dimensional space defined by counts of the words data and large in the neighborhood. Note that the angle between digital and information is smaller than the angle between apricot and information. When two vectors are more similar, the cosine is larger but the angle is smaller; the cosine has its maximum (1) when the angle between two vectors is smallest (0°) ; the cosine of all other angles is less than 1.

Credit: J&M, ch. 6.

Cosine similarity

```
Similarity in Quine philosophy corpus
('epistemology', 1.0)
('naturalized', 0.6133719682693481)
('normative', 0.4007303714752197)
('doctrinal', 0.39382827281951904)
('epistemological', 0.37758421897888184)
('evolutionary', 0.34609323740005493)
('dominates', 0.3314409852027893)
('traces', 0.3263438642024994)
('irreducibility', 0.3175702691078186)
('psychological', 0.3145177364349365)
```

Comparing vectors: Probabilistic measures

- The Euclidean and cosine distances are geometric measures.
 Sometimes is more convenient to see vectors as probability distributions (after appropriate normalization).
- Many measures exists to compare two probability distributions, for example the Kullback-Leibler divergence (non-symmetric) or the (symmetric) Jensen-Shannon divergence:

$$D_{KL}(\overrightarrow{u}||\overrightarrow{v}) = \sum_{i=1}^{d} u_i log\left(\frac{u_i}{v_i}\right)$$

$$D_{JS}(\overrightarrow{u}||\overrightarrow{v}) = \frac{1}{2}D_{KL}(\overrightarrow{u}||\overrightarrow{m}) + \frac{1}{2}D_{KL}(\overrightarrow{v}||\overrightarrow{m})$$

where
$$m = \frac{(\vec{u} + \vec{v})}{2}$$

Evaluation

Association/Similarity

Two words or a word and a context, may have two kinds of associations:

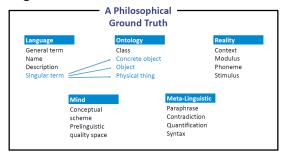
- **Syntagmatic associations** (first-order co-occurrence): how much two words appear one next to the other.
 - 1 E.g., the association between a verb and its typical complements;
 - what is represented in a co-occurrence matrix.
- Paradigmatic associations (second-order co-occurrence) is similarity
 of context: how similar are the neighbors of the two words.
 - E.g., the association between two synonyms, or "wrote", "said", "remarked".
 - what is estimated by calculating (first-order) vectors similarity.

Evaluation of vectors

- The most common evaluation is to test their performance on similarity tasks.
- Correlation between algorithm and human word similarity ratings:
 - WordSim-353: 353 noun pairs rated on a 0-10 scale. sim("plane", "car") = 5.77.
 - SimLex-999: similarity of noun, adjectives and adjectives pairs. Assignment 3.
- Taking TOEFL multiple-choice vocabulary tests
 - Levied is closest in meaning to: imposed, believed, requested, correlated.
- Judgments in context
 - Stanford Contextual Word Similarity (SCWS) dataset: human judgments on 2,003 pairs of nouns, verbs, and adjectives in their sentence context.

Intrinsic evaluation of vectors

- Comparison to human word similarity ratings
- Comparison to gold standard



Post-hoc evaluation

Intrinsic evaluation of vectors

- Comparison to human word similarity ratings
- Comparison to gold standard
- Post-hoc evaluation
 - Synonym detection task

word is i	nost related to illiornation :	
a) Learning	b) Reductions	
c) Collateral	d) Application	
e) Ordered Pair	f) None of these words is	
•	even remotely related	
Coherence task		
What word de	oes not belong to the group?	
a) Numbers	b) Pronouns	
c) Subtraction	d) Actually	
e) No coherent group ca	n be formed from these words	
	·	

What word is most related to 'Information'?

Extrinsic evaluation of vectors

- Use vectors to perform some other task
- For example: Information retrieval

```
4. (0.8002) 9783772804557_sect82_sent1247 context query [enfach 0.33][enfachen 0.16][zusammengesetzt 0.17]

Alle Begriffe sind entweder einfach, oder aus mehreren einfachen zusammengesetzt.

5. (0.7994) Wissenschaftslehre_sect370_para2287_sent14029 context query [zusammengesetzt 0.17][einfach 0.33]

Ein solcher Beweis mag zusammengesetzt, ein anderer einfach heißen.
```

Use cosine similarity to rank results and evaluate those results

Lab

- Extracting Co-occurrences
- Sparse Vectors
- Calculating Cosine Similarities
- Visualizing Similarities
- Evaluating your Model
- Working with Dense Vectors