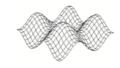


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QUESTION 5.2

(a)
$$\cos ADB = \frac{12^2 + 20^2 - 28^2}{2(12)(20)}$$
 (MI)(AI)

Notes: Award (M1) for substituted cosine rule formula, (A1) for correct substitutions.

$$\angle ADB = 120^{\circ}$$
 (A1)(G2) [3 marks]

(b) Area =
$$\frac{(12)(20)\sin 120^{\circ}}{2}$$
 (M1)(A1)(ft)

Notes: Award (M1) for substituted area formula, (A1)(ft) for their correct substitutions.

$$=104 \text{ cm}^2 \quad (103.923...\text{cm}^2)$$
 (A1)(ft)(G2) [3 marks]

Note: The final answer is 104 cm^2 , the units are required. Accept 100 cm^2 .

(c)
$$\frac{\sin BCD}{12} = \frac{\sin 60^{\circ}}{13}$$
 (A1)(ft)(M1)(A1)

Note: Award (AI)(ft) for their 60 seen, (MI) for substituted sine rule formula, (AI) for correct substitutions.

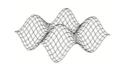
$$BCD = 53.1^{\circ}$$
 (53.0736...) (A1)(G3) [4 marks]

Note: Accept 53, do not accept 50 or 53.0.

continued...



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Question 5.2 continued

(d) Using triangle ABC

$$\frac{\sin BAC}{13} = \frac{\sin 53.1^{\circ}}{28}$$

(M1)(A1)(ft)

OR

Using triangle ABD

$$\frac{\sin BAD}{12} = \frac{\sin 120^{\circ}}{28}$$

(M1)(A1)(ft)

Note: Award (MI) for substituted sine rule formula (one of the above), $(AI)(\mathbf{ft})$ for their correct substitutions. Follow through from (a) or (c) as appropriate.

$$BAC = BAD = 21.8^{\circ}$$
 (21.7867...)

(A1)(ft)(G2)

Notes: Accept 22, do not accept 20 or 21.7.

Accept equivalent methods, for example cosine rule.

$$180^{\circ} - (53.1^{\circ} + 21.8^{\circ}) \neq 90^{\circ}$$
, hence triangle ABC is not right angled

(R1)(AG)

OR

$$\frac{\text{CD}}{\sin 66.9^{\circ}} = \frac{13}{\sin 60^{\circ}}$$

(M1)(A1)(ft)

Note: Award (M1) for substituted sine rule formula, (A1)(ft) for their correct substitutions. Follow through from (a) and (c).

$$CD = 13.8 \quad (13.8075...)$$

(A1)(ft)

$$13^3 + 28^2 \neq 33.8^2$$
, hence triangle ABC is not right angled.

(R1)(ft)(AG) [4 marks]

Note: The complete statement is required for the final (*R1*) to be awarded.

Total [14 marks]