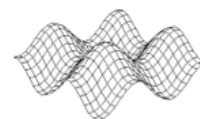




**GIMNASIO FEMENINO**  
**ÁREA DE MATEMÁTICAS**  
**4<sup>to</sup> CONCURSO NACIONAL DE MATEMÁTICAS IB**  
**PRUEBA 1 Y 2 – ESTUDIOS MATEMÁTICOS NM**  
**2017 – 2018**



7.4 (a)  $\frac{3}{4}(-2)^4 - (-2)^3 - 9(-2)^2 + 20$  (M1)

**Note:** Award (M1) for substituting  $x = -2$  in the function.

$= 4$  (A1)(G2) [2 marks]

**Note:** If the coordinates  $(-2, 4)$  are given as the answer award, at most, (M1)(A0). If no working shown award (G1). If  $x = -2$ ,  $y = 4$  seen then award full marks.

(b)  $3x^3 - 3x^2 - 18x$  (A1)(A1)(A1) [3 marks]

**Note:** Award (A1) for each correct term, award at most (A1)(A1)(A0) if extra terms seen.

(c)  $f'(3) = 3 \times (3)^3 - 3 \times (3)^2 - 18 \times 3$  (M1)

**Note:** Award (M1) for substitution in their  $f'(x)$  of  $x = 3$ .

$= 0$  (A1)

**OR**

$3x^3 - 3x^2 - 18x = 0$  (M1)

**Note:** Award (M1) for equating their  $f'(x)$  to zero.

$x = 3$  (A1)

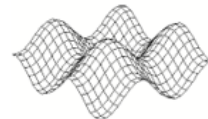
$f'(x_1) = 3 \times (x_1)^3 - 3 \times (x_1)^2 - 18 \times x_1 < 0$  where  $0 < x_1 < 3$  (M1)

**Note:** Award (M1) for substituting a value of  $x_1$  in the range  $0 < x_1 < 3$  into their  $f'$  and showing it is negative (decreasing).

$f'(x_2) = 3 \times (x_2)^3 - 3 \times (x_2)^2 - 18 \times x_2 > 0$  where  $x_2 > 3$  (M1)

**Note:** Award (M1) for substituting a value of  $x_2$  in the range  $x_2 > 3$  into their  $f'$  and showing it is positive (increasing).

continued...



Question 7.4 continued

**OR**

*With or without a sketch:*

Showing  $f(x_1) > f(3)$  where  $x_1 < 3$  and  $x_1$  is close to 3. **(M1)**

Showing  $f(x_2) > f(3)$  where  $x_2 > 3$  and  $x_2$  is close to 3. **(M1)**

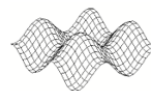
**Note:** If a sketch of  $f(x)$  is drawn **in this part of the question and**  $x = 3$  is identified as a stationary point on the curve, then  
 (i) award, at most, **(M1)(A1)(M1)(M0)** if the stationary point has been found;  
 (ii) award, at most, **(M0)(A0)(M1)(M0)** if the stationary point has not been previously found.

Since the gradients go from negative (decreasing) through zero to positive (increasing) it is a local minimum **(R1)(AG)**

**Note:** Only award **(R1)** if the first two marks have been awarded ie  $f'(3)$  has been shown to be equal to 0.

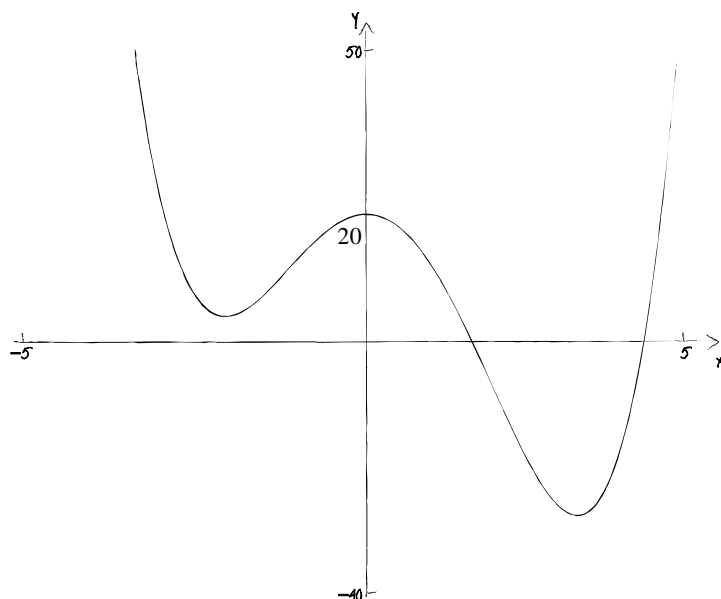
**[5 marks]**

*continued...*



Question 74 continued

(d)



(A1)(A1)(A1)(A1)

**Notes:** Award (A1) for labelled axes and indication of scale on both axes.  
Award (A1) for smooth curve with correct shape.  
Award (A1) for local minima in 2<sup>nd</sup> and 4<sup>th</sup> quadrants.  
Award (A1) for y intercept seen and labelled. Accept 20 on y-axis.  
Do **not** award the third (A1) mark if there is a turning point on the x-axis.  
If the derivative function is sketched then award, at most, (A1)(A0)(A0)(A0).  
For a smooth curve (with correct shape) there should be **ONE** continuous thin line, no part of which is straight and no (one to many) mappings of  $x$ .

[4 marks]

(e) (0, 20)

(G1)(G1)

**Note:** If parentheses are omitted award (G0)(G1).

**OR**

$$x = 0, y = 20$$

(G1)(G1) [2 marks]

**Note:** If the derivative function is sketched in part (d), award (G1)(ft)(G1)(ft) for  $(-1.12, 12.2)$ .

(f)  $f'(2) = 3(2)^3 - 3(2)^2 - 18(2)$

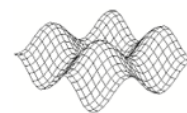
(M1)

**Notes:** Award (M1) for substituting  $x = 2$  into their  $f'(x)$ .

$$= -24$$

(A1)(ft)(G2) [2 marks]

continued...



Question 74 continued

(g) (i) Gradient of perpendicular =  $\frac{1}{24}$  (0.0417, 0.041666...) (AI)(ft)(GI)

**Note:** Follow through from part (f).

(ii)  $y + 12 = \frac{1}{24}(x - 2)$  (MI)(MI)

**Note:** Award (MI) for correct substitution of (2, -12), (MI) for correct substitution of their perpendicular gradient into equation of line.

**OR**

$$-12 = \frac{1}{24} \times 2 + d \quad (MI)$$

$$d = -\frac{145}{12}$$

$$y = \frac{1}{24}x - \frac{145}{12} \quad (MI)$$

**Note:** Award (MI) for correct substitution of (2, -12) and gradient into equation of a straight line, (MI) for correct substitution of the perpendicular gradient and correct substitution of  $d$  into equation of line.

$$b = -24, c = -290 \quad (AI)(ft)(AI)(ft)(G3) \quad [5 \text{ marks}]$$

**Note:** Follow through from parts (f) and g(i).  
 To award (ft) marks,  $b$  and  $c$  must be integers.  
 Where candidate has used 0.042 from g(i), award (AI)(ft) for -288.

**Total: [23 marks]**