# Quick Sort Sorting Algorithm

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#### Table of Contents

Introduction

**Quick Sort Examples** 

Demonstration

**Conclusion Questions** 

# Introduction

# Why would we ever want to sort anything?

# Sorting: arranging objects in some sort of order

- ▶ Integers: in numerical order, e.g., 1, 2, 3, 4, 5
- Characters: in alphabetical order, e.g. A, B, C, D, E
- Students: in class rank order
- Movies: in review order, highest to lowest
- ▶ Dates: ???

### A motivational example

How do you finding a name in a large directory?

What if the names are not sorted?

Do you start at the beginning and search until you find the name you are looking for?

What if there are 1,000,000 names in the directory?

The complexity of bisection search is  $O = \log_2 n$ 

- 4 guesses to find an item in a list of size 10
- 7 guesses in a list of size 100
- ▶ 10 guesses in a list of size 1000
- ▶ 20 guesses in a list of size 1000000
- ▶ 30 guesses in a list of size 1000000000
- ▶ 40 guesses in a list of size 1000000000000

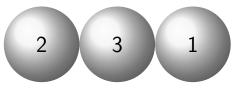
### Brief Description of QuickSort

- QuickSort is a recursive algorithm based on the "divide and conquer" technique. It works by placing the "middle" element in the proper place, i.e., in the "middle", and then doing the same thing for the left and right halves. This "middle" element is known as the PIVOT.
- ▶ Think of sorting a stack of books by number of pages. Pick a book at random (the pivot, or "middle"), and place all the books with fewer pages on the left, and all the books with more pages on the right. Repeat for the left and right sides.
- Question: How would you do this for a deck of cards?

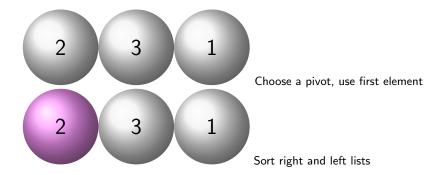
#### Description of QuickSort

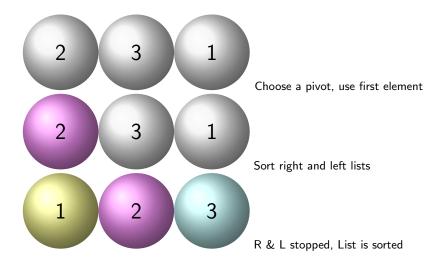
- 1. Call the QuickSort() procedure, passing a perhaps unsorted list as the only parameter.
- Start with the list parameter. Pick one element of the list to be the pivot. (First, last, middle, random — it doesn't matter.)
- 3. Iterate through the list placing all elements less than the pivot on the left and all elements greater than the pivot on the right. (Equal elements can go either on the left, right, or in my demonstration in the middle.)
- 4. Continue the same process for the left and right sides. Call the same procedure passing the left or right side as the parameter. This is the recursive step.
- 5. Stop the recursion when a list has one or zero elements and return the list. This stops the recursion.

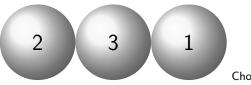
# Quick Sort Examples



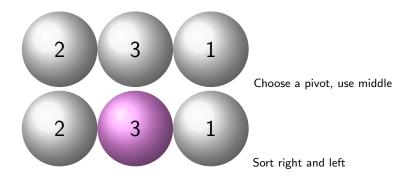
Choose a pivot, use first element

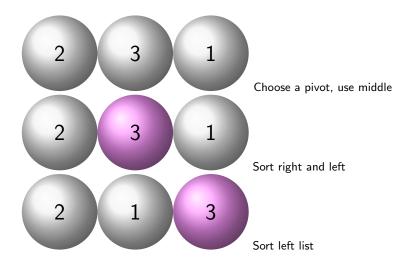






Choose a pivot, use middle



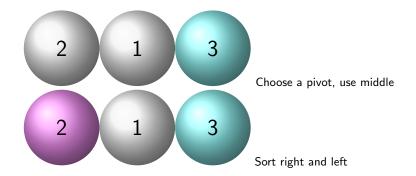


#### Example 2, continued

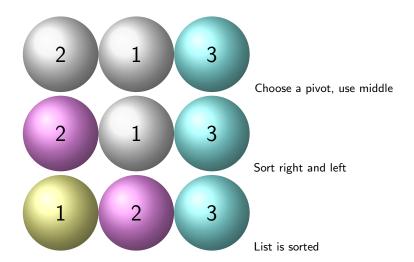


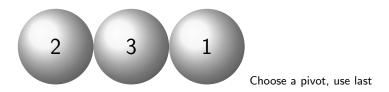
Choose a pivot, use middle

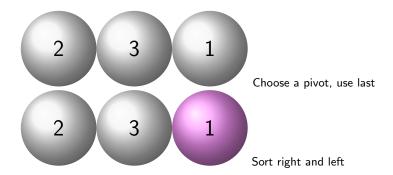
### Example 2, continued

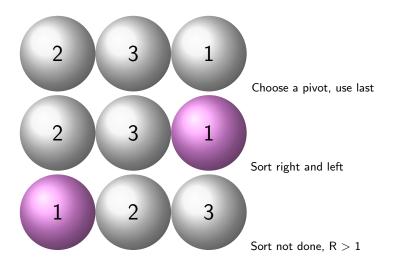


#### Example 2, continued

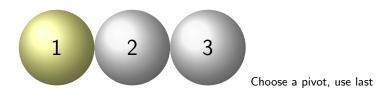




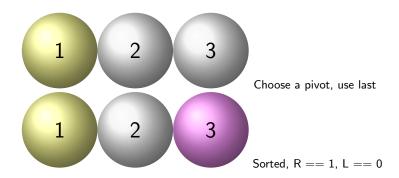




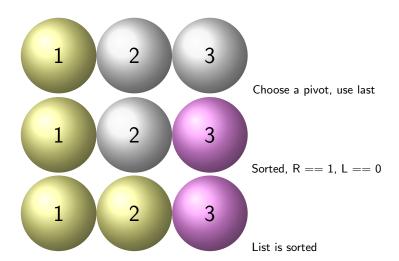
### Example 3, continued



# Example 3, continued

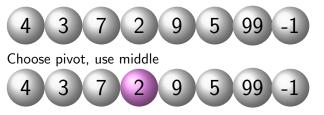


#### Example 3, continued

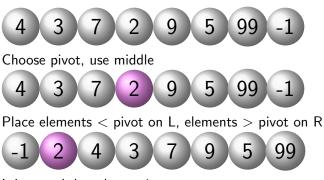




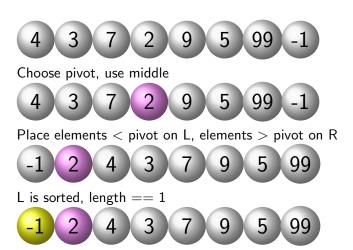
Choose pivot, use middle



Place elements < pivot on L, elements > pivot on R

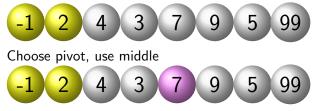


L is sorted, length == 1

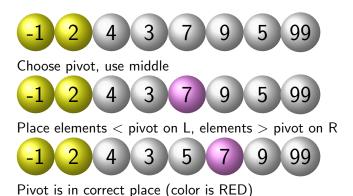


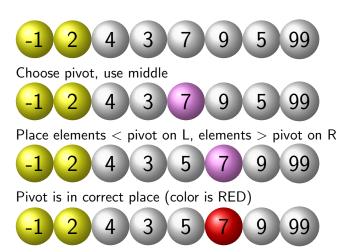


Choose pivot, use middle



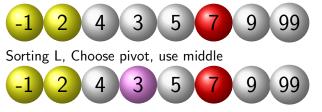
Place elements < pivot on L, elements > pivot on R



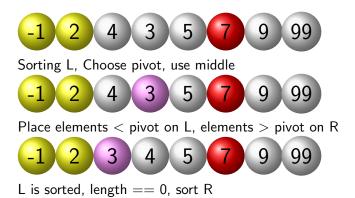


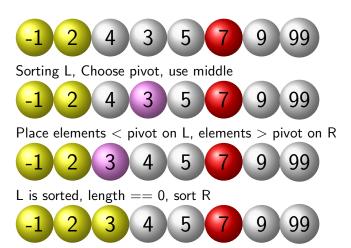


Sorting L, Choose pivot, use middle



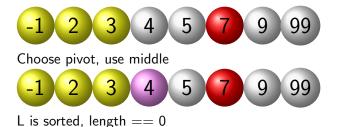
Place elements < pivot on L, elements > pivot on R

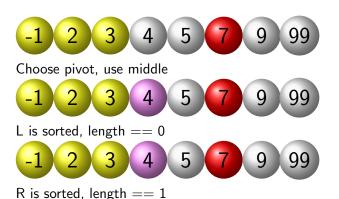


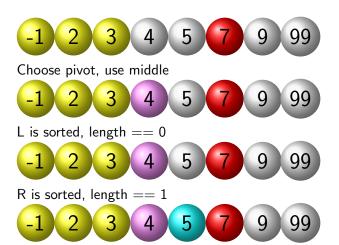




Choose pivot, use middle

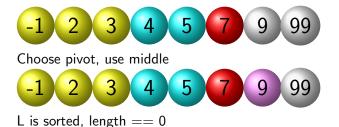


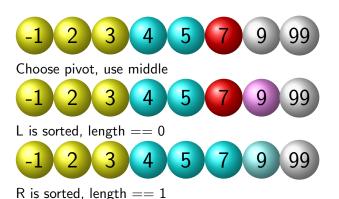


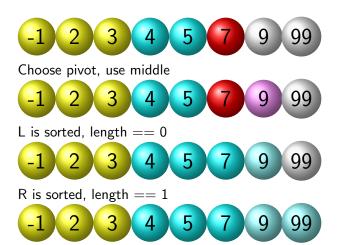




Choose pivot, use middle







# Demonstration

```
def quick_sort(arr):
    less = \Pi
    equal = []
    more = []
    if len(arr) <= 1:
        return arr
    else:
        pivot = arr[(len(arr)-1) // 2]
        for i in arr:
            if i < pivot:
                less.append(i)
            elif i > pivot:
                more.append(i)
            else:
                equal.append(i)
        less = quick_sort(less)
        more = quick_sort(more)
        return less + equal + more
```

#### Python code comments, declare variables

```
def quick_sort(arr):
    less = []
    equal = []
    more = []
```

Declare a function named *quick\_sort* that takes one parameter, a list, which presumably is unsorted.

Declare a *less* list to hold the lesser-than items, a *more* list to hold the greater-than items, and an *equal* lost to hold the equal-to items.

```
if len(arr) <= 1:
    return arr
else:</pre>
```

If the length of the parameter list is 1 or 0, you are done. Stop the recursion. Else, continue the recursion.

```
pivot = arr[(len(arr)-1) // 2] #select the middle element
for i in arr:
    if i < pivot:
        less.append(i)
    elif i > pivot:
        more.append(i)
    else:
        equal.append(i)
```

Select a pivot. It could be the first element (arr[0]), the last element (arr[-1]), the middle element (arr[len(arr)-1 // 2]), or a random element.

Iterate through the parameter list, placing all lesser-than elements on the left, and all greater than elements on the right.

```
#recursive calls for the right and left lists
less = quick_sort(less)
more = quick_sort(more)

#return the left, middle, and right lists glued together
return less + equal + more
```

Call the function recursively on the left and right sides, passing each as a parameter. Return the three lists glued together.

```
initial list is [4, 3, 7, 2, 9, 5, 99, -1]
calling quick_sort([4, 3, 7, 2, 9, 5, 99, -1])
  else branch, list is [4, 3, 7, 2, 9, 5, 99, -1]
  for: i = 4 and pivot = 2, i > pivot, more = [4]
  for: i = 3 and pivot = 2, i > pivot, more = [4, 3]
  for: i = 7 and pivot = 2, i > pivot, more = [4, 3, 7]
  for: i = 2 and pivot = 2, i == pivot, equal = [2]
  for: i = 9 and pivot = 2, i > pivot, more = [4, 3, 7, 9]
  for: i = 5 and pivot = 2, i > pivot, more = [4, 3, 7, 9, 5]
  for: i = 99 and pivot = 2, i > pivot, more = [4, 3, 7, 9, 5, 99]
  for: i = -1 and pivot = 2, i < pivot, less = [-1]</pre>
```

```
calling quick_sort([-1])
   DONE if list length <= 1, returning [-1]
calling quick_sort([4, 3, 7, 9, 5, 99])
   else branch, list is [4, 3, 7, 9, 5, 99]
   for: i = 4 and pivot = 7, i < pivot, less = [4]
   for: i = 3 and pivot = 7, i < pivot, less = [4, 3]
   for: i = 7 and pivot = 7, i == pivot, equal = [7]
   for: i = 9 and pivot = 7, i > pivot, more = [9]
   for: i = 5 and pivot = 7, i < pivot, less = [4, 3, 5]
   for: i = 99 and pivot = 7, i > pivot, more = [9, 99]
```

```
calling quick_sort([4, 3, 5])
  else branch, list is [4, 3, 5]
    for: i = 4 and pivot = 3, i > pivot, more = [4]
    for: i = 3 and pivot = 3, i == pivot, equal = [3]
    for: i = 5 and pivot = 3, i > pivot, more = [4, 5]
calling quick_sort([])
  DONE if list length <= 1, returning []
calling quick_sort([4, 5])
  else branch, list is [4, 5]
    for: i = 4 and pivot = 4, i == pivot, equal = [4]
    for: i = 5 and pivot = 4, i > pivot, more = [5]
calling quick_sort([])
  DONE if list length <= 1, returning []</pre>
```

```
calling quick_sort([5])
   DONE if list length <= 1, returning [5]
<<re>turning [] + [4] + [5]
<<returning [] + [3] + [4, 5]
calling quick_sort([9, 99])
    else branch, list is [9, 99]
       for: i = 9 and pivot = 9, i == pivot, equal = [9]
       for: i = 99 and pivot = 9, i > pivot, more = [99]
calling quick_sort([])
   DONE if list length <= 1, returning []
calling quick_sort([99])
   DONE if list length <= 1, returning [99]
<<returning [] + [9] + [99]
<<re>turning [3, 4, 5] + [7] + [9, 99]
<<re>turning [-1] + [2] + [3, 4, 5, 7, 9, 99]
end list is [-1, 2, 3, 4, 5, 7, 9, 99]
```

# Conclusion and Questions

# Time complexity of QuickSort

Best case

$$O = n \log_2 n \tag{1}$$

Worst case

$$O=n^2 \tag{2}$$

# Questions