

## **Practice Set 7 Supply Chain Management**

### ***Question 1***

A supplier produces a product at per unit cost \$35 and sells it to a retailer at the wholesale price \$75. The retailer decides how many units to order ( $q$ ) before the sales season. The demand of customers is normally distributed with mean 250 and standard deviation of 125. The retail price is \$115 and each unit of leftover inventory has salvage value of \$15. Which of the following statements is false?

- a. The retailer should order less than 250 units
- b. If the wholesale price decreases from \$75 to \$65, the retailer would order more than 250 units
- c. If the retailer price increases from \$115 to \$145, the retailer would order more than 250 units
- d. If the wholesale price decreases from \$75 to \$35, the total profit earned in the supply chain would be maximized

### ***Question 2***

A supplier produces a product at per unit cost \$35 and sells it to a retailer at the wholesale price \$75. The retailer decides how many units to order ( $q$ ) before the sales season. The demand of customers is normally distributed with mean 250 and standard deviation of 125. The retail price is \$115 and each unit of leftover inventory has salvage value of \$15. Which of the following statements is false?

- a. The retailer should order less than 250 units
- b. If the wholesale price decreases from \$75 to \$85, the retailer would order less than 250 units
- c. If the retailer price decreases from \$115 to \$105, the retailer would order more than 250 units
- d. If the wholesale price decreases from \$75 to \$35, the total profit earned in the supply chain would be maximized

### ***Question 3***

A supplier produces a product at per unit cost \$35 and sells it to a retailer at the wholesale price \$75. The retailer decides how many units to order ( $q$ ) before the sales season. The demand of customers is normally distributed with mean 250 and standard deviation of 125. The retail price is \$115 and each unit of leftover inventory has salvage value of \$25. Which of the following statements is false?

- a. The retailer should order less than 250 units
- b. If the wholesale price decreases from \$75 to \$65, the retailer would order more than 250 units
- c. If the retailer price decreases from \$115 to \$105, the retailer would order more than 250 units

d. If the wholesale price decreases from \$75 to \$35, the total profit earned in the supply chain would be maximized

#### Question 4

Umbra Visage (UV) is a retailer of Zamatia, an upscale maker of eyewear. UV purchases each pair of sunglasses from Zamatia for \$75 and sells them for \$115. Zamatia's production cost per pair is \$35. At the end of the season, UV offers deep discounts to sell remaining inventory. The estimate is each pair will only have \$25 salvage value if not sold by the end of the season. UV's forecasting department believes the demand for this pair of sunglasses is:

Demand	800	1,000	1,200	1,400	1,600	1,800
Probability	0.11	0.11	0.28	0.22	0.18	0.10
<b>Cumulative Probability</b>	<b>0.11</b>	<b>0.22</b>	<b>0.50</b>	<b>0.72</b>	<b>0.90</b>	<b>1.00</b>

(a) What is the **optimal order quantity for UV**?

$$C_u = 115 - 75 = 40$$

$$C_o = 75 - 25 = 50$$

$$\text{Prob} = C_u / (C_u + C_o) = 40 / 90 = 0.444$$

$$Q = 1200$$

(b) What is **UV's expected profit** under its optimal order quantity in part (a)?

$$\text{UV Profit} = \text{revenue} + \text{salvage value collected} - \text{purchase cost}$$

$$= E[p * \min(D, Q) + s * \max(Q - D, 0) - w * Q]$$

$$= E[115 * \min(D, 1200) + 25 * \max(1200 - D, 0) - 75 * 1200]$$

$$= 115 * [800 * 0.11 + 1000 * 0.11 + 1200 * 0.78] + 25 * [400 * 0.11 + 200 * 0.11] - 75 * 1200$$

$$= 42,060$$

(c) What is **Zamatia's expected profit** when UV orders its optimal order quantity in part (a)?

$$\text{Zamatia Profit} = (w - c) * Q = (75 - 35) * 1200 = 48,000$$

(d) What is the **supply chain's total profit** (that is the sum of UV and Zamantia's profits) when UV orders its optimal order quantity in part (a)?

$$\text{Supply Chain Profit} = 42060 + 48000 = 90,060$$

- (e) What would be the **integrated supply chain's optimal order quantity** if there's a centralized decision maker?

Optimal order quantity under Integrated centralized supply chain:

$$C_u = 115 - 35 = 80$$

$$C_o = 35 - 25 = 10$$

$$\text{Prob} = C_u / (C_u + C_o) = 8/9 = 0.888$$

$$Q = 1,600$$

- (f) What would be the **integrated supply chain's total profit** under the optimal order quantity in part (e)?

Integrated SC Profit

$$= E[p * \min(D, Q) + s * \max(Q - D, 0) - c * Q]$$

$$= E[115 * \min(D, 1600) + 25 * \max(1600 - D, 0) - 35 * 1600]$$

$$= 115 * (800 * 0.11 + 1000 * 0.11 + 1200 * 0.28 + 1400 * 0.22 + 1600 * 0.28) \\ + 25 * (800 * 0.11 + 600 * 0.11 + 400 * 0.28 + 200 * 0.22) - 35 * 1600$$

$$= 100,100$$