

Suppose Bob has made an important discovery.

He wants to record publicly what he has done, but he does not want anyone else to know.

Goal allow Alice to sign a document without knowing its contents.

- | Alice                                  | Bob   |
|--|---|
| 1. execute $\text{RSA.KeyGen}(1^n)$ .  |   |
| $pk = (n, e_A)$ , $sk = (p, q, d_A)$   |   |
|  | 2. choose a random $r \xleftarrow{\$} \mathbb{Z}_n$         |
|  | with $\gcd(r, n) = 1$ .                                     |
|  | compute $t \equiv r^{e_A} m \pmod{n}$                       |
| 3. compute $s \equiv t^{d_A} \pmod{n}$ | reveals no information of $m$ .<br>( $\because r$ : random) |
|  | 4. compute $\sigma := s/r$                                  |

$$\text{Since } s/r \equiv t^{d_A}/r \equiv (r^{e_A} m)^{d_A}/r \equiv m^{d_A} \pmod{n},$$

$\sigma$  is a signed message of  $m$ .

### Dangers of RSA Blind Signature

Suppose Bob has a ciphertext  $c = \text{Enc}(m)$  encrypted through RSA.

$$\text{In step 2, } t \equiv r^e c \equiv (m^e \pmod{n}) r^e \equiv (mr)^e \pmod{n}$$

$$\text{In step 3, } s \equiv t^d \equiv (mr)^{ed} \equiv mr \pmod{n}$$

$$\text{In step 4, } \sigma = s/r \equiv m \pmod{n} \text{ since } \gcd(r, n) = 1$$