

Módulo V: Álgebra Lineal

- Manipulación de matrices.
- Solución de ecuaciones lineales.
- Valores y vectores propios.
- Funciones elementales.
- Gráficas básicas.

$$A = [1, 2; 3, 0]$$

$$A = \begin{matrix} 2 \times 2 \\ \begin{matrix} 1 & 2 \\ 3 & 0 \end{matrix} \end{matrix}$$

$$B = [3, -8; 0, 5]$$

$$B = \begin{matrix} 2 \times 2 \\ \begin{matrix} 3 & -8 \\ 0 & 5 \end{matrix} \end{matrix}$$

$$A + B$$

$$\text{ans} = \begin{matrix} 2 \times 2 \\ \begin{matrix} 4 & -6 \\ 3 & 5 \end{matrix} \end{matrix}$$

$$A * B$$

$$\text{ans} = \begin{matrix} 2 \times 2 \\ \begin{matrix} 3 & 2 \\ 9 & -24 \end{matrix} \end{matrix}$$

$$B * A$$

$$\text{ans} = \begin{matrix} 2 \times 2 \\ \begin{matrix} -21 & 6 \\ 15 & 0 \end{matrix} \end{matrix}$$

$$A . * B$$

$$\text{ans} = \begin{matrix} 2 \times 2 \\ \begin{matrix} 3 & -16 \\ 0 & 0 \end{matrix} \end{matrix}$$

$$B . * A$$

$$\text{ans} = \begin{matrix} 2 \times 2 \\ \begin{matrix} 3 & -16 \end{matrix} \end{matrix}$$

0 0

A^2

```
ans = 2x2
      7      2
      3      6
```

$A*A$

```
ans = 2x2
      7      2
      3      6
```

$A.^2$

```
ans = 2x2
      1      4
      9      0
```

A

```
A = 2x2
      1      2
      3      0
```

$AT = A'$

```
AT = 2x2
      1      3
      2      0
```

A/B

```
ans = 2x2
      0.3333      0.9333
      1.0000      1.6000
```

$A*inv(B)$

```
ans = 2x2
      0.3333      0.9333
      1.0000      1.6000
```

$A\backslash B$

```
ans = 2x2
      0      1.6667
      1.5000     -4.8333
```

$inv(A)*B$

```
ans = 2x2
      0      1.6667
      1.5000 -4.8333
```

Solución de ecuaciones lineales

Solucionar el sistema de ecuaciones lineales:

$$Ax = b$$

$$3x - 10y + z = 1$$

$$4w + x - 2z = 3$$

$$2w - x + \frac{1}{3}y = 14$$

$$5w + 3z = 0$$

Solución:

$$x = A^{-1}B$$

```
A = [ 0, 3, -10, 1;
      4, 1, 0, -2;
      2, -1, (1/3), 0;
      5, 0, 0, 3 ]
```

```
A = 4x4
      0      3.0000 -10.0000      1.0000
      4.0000      1.0000      0      -2.0000
      2.0000     -1.0000      0.3333      0
      5.0000      0      0      3.0000
```

```
B = [1; 3; 14; 0]
```

```
B = 4x1
      1
      3
     14
      0
```

```
x = inv( A )*B
```

```
x = 4x1
     1.9584
    -11.3615
```

```
-3.8349
-3.2640
```

```
R = [1, 2, 0.5;
      0.0, 3.2, 4.0;
      2, 5.1, 0.8]
```

```
R = 3x3
    1.0000    2.0000    0.5000
         0    3.2000    4.0000
    2.0000    5.1000    0.8000
```

```
[eivec, eival] = eig( R )
```

```
eivec = 3x3
   -0.2252   -0.8872   -0.2857
    0.5715    0.3739   -0.6936
   -0.7891   -0.2702   -0.6613
eival = 3x3
   -2.3228         0         0
         0    0.3094         0
         0         0    7.0135
```

Funciones elementales

Graficar:

$$y_1(t) = \cos(\omega t + \phi)$$

$$y_2(t) = \sin(\omega t)$$

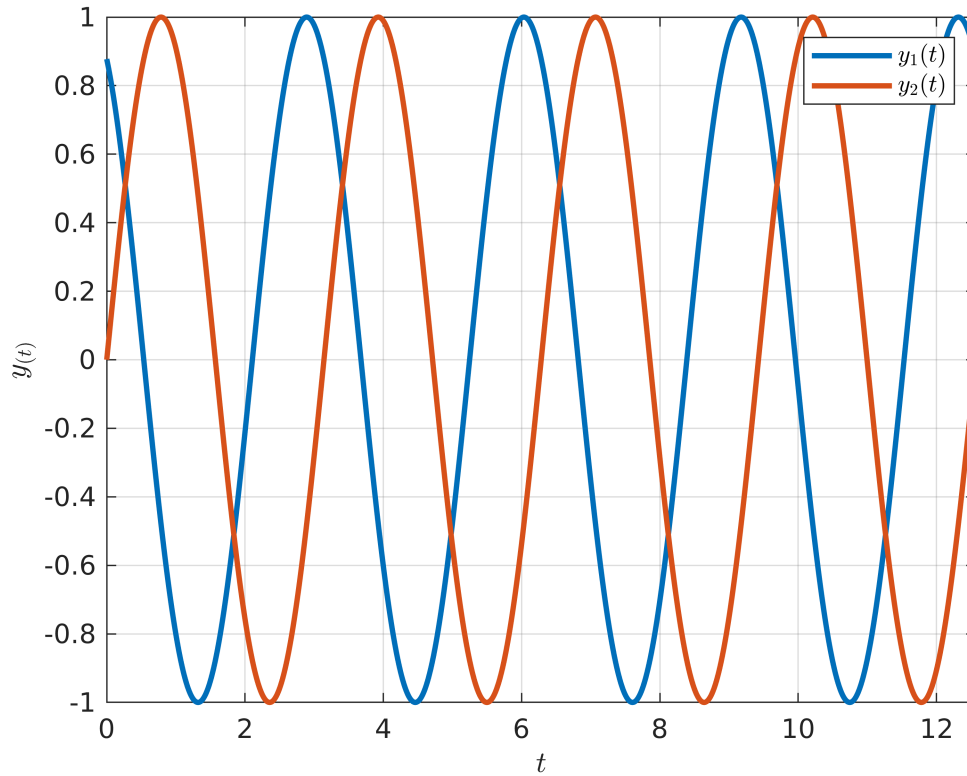
para $0 \leq t \leq 4\pi$

```
set(0, 'defaulttextInterpreter', 'latex')
set(0, 'defaultLegendInterpreter', 'latex')
t = 0 : 0.001 : 4*pi;
y_1 = cos( 2.*t + 0.5);
y_2 = sin( 2.*t )
```

```
y_2 = 1x12567
      0      0.0020      0.0040      0.0060      0.0080      0.0100      0.0120      0.0140 ...
```

```
figure(1)
clf
plot( t, y_1, 'Linewidth', 2 )
hold on
plot(t, y_2, 'Linewidth', 2)
grid on
xlim([0, 4*pi])
legend('$y_1(t)$', '$y_2(t)$')
```

```
xlabel('$t$')
ylabel('$y_{(t)}$')
```



Graficar:

$$y_3(t) = e^{(-at)}$$

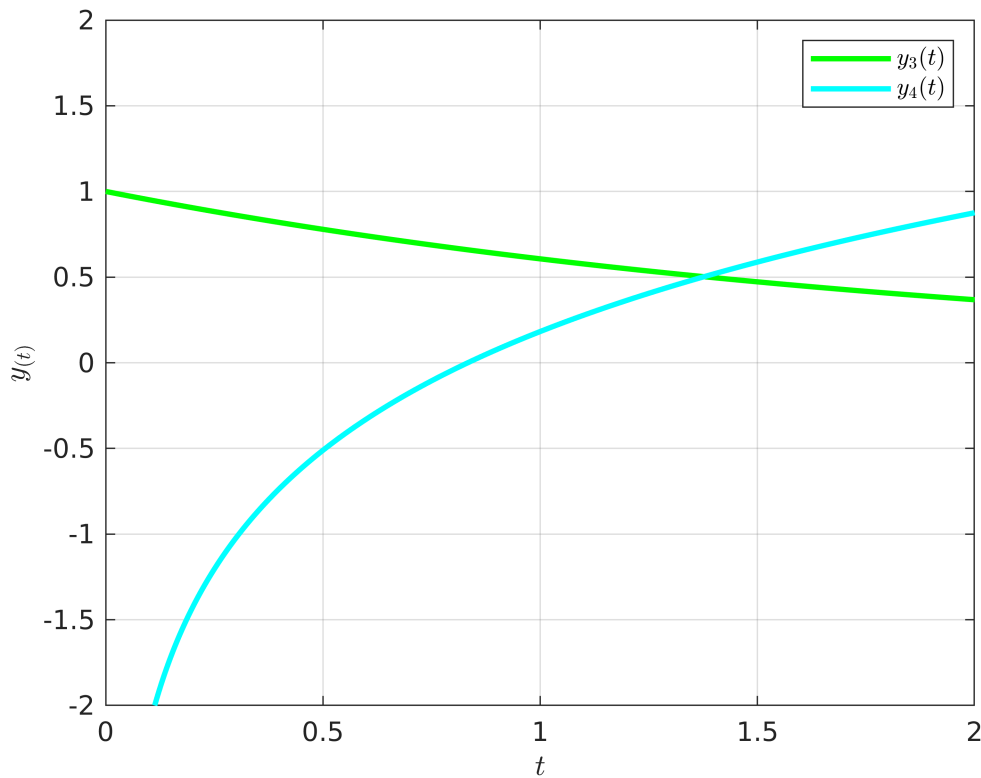
$$y_4(t) = \ln(bt)$$

```
t = 0 : 0.001 : 2;
a = 0.5;
b = 1.2;

y_3 = exp( -a.*t );
y_4 = log( b.*t );

figure(2)
clf
plot( t, y_3, 'color', 'g', 'Linewidth', 2 )
hold on
plot( t, y_4, 'color', 'c', 'Linewidth', 2 )
grid on
ylim([-2, 2])
legend('$y_3(t)$', '$y_4(t)$')
xlabel('$t$')
```

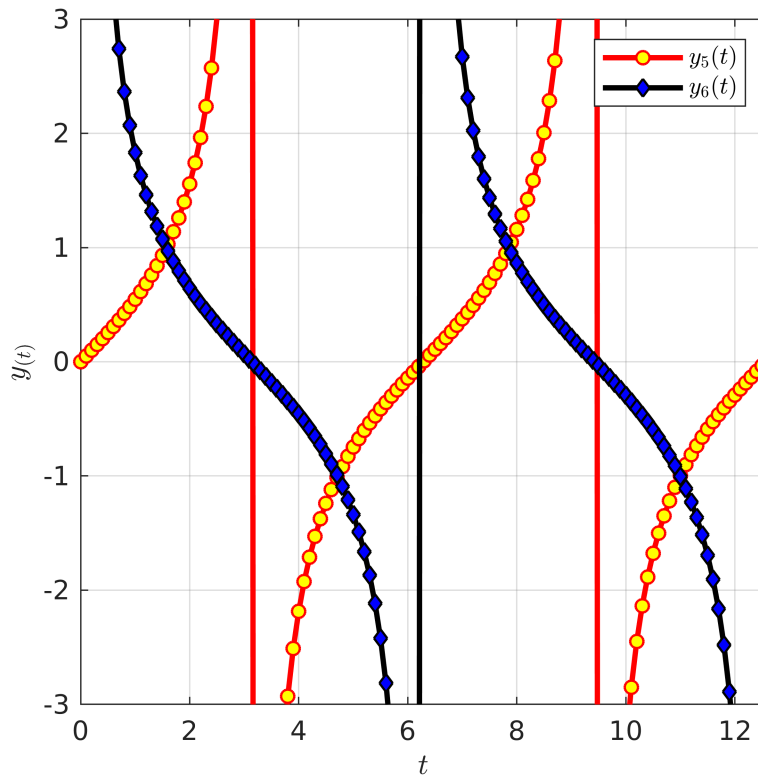
```
ylabel('$y_{(t)}$')
```



```
t = 0 : 0.1 : 4*pi;

y_5 = tan( 0.5.*t );
y_6 = cot( 0.5.*t );

figure(3)
clf
plot( t, y_5, 'color', 'r', 'Linewidth', 2, 'Marker', 'o', 'Markersize', 5,...
      'MarkerFaceColor', 'y')
hold on
plot( t, y_6, 'color', 'k', 'Linewidth', 2, 'Marker', 'd', 'Markersize', 5,...
      'MarkerFaceColor', 'b' )
grid on
ylim([-3, 3])
xlim([0, 4*pi])
legend('$y_5(t)$', '$y_6(t)$')
xlabel('$t$')
ylabel('$y_{(t)}$')
pbaspect([1 1 1])
print('tan_cot','-dpdf', '-fillpage')
```



```
t = -10 : 0.001 : 10;

y_7 = t.^3 + 5.*t.^2 + 7.*t + 2;
y_8 = t.^(1/3);

figure(4)
clf
plot( t, y_7, 'color', [1.0, 0.7, 0.0], 'Linewidth', 2 )
hold on
plot( t, y_8, 'color', 'm', 'Linewidth', 2 )
```

Warning: Imaginary parts of complex X and/or Y arguments ignored

```
grid on
ylim([-3, 3])
xlim([-4, 4])
legend('$y_7(t)$', '$y_8(t)$')
xlabel('$t$')
ylabel('$y_{(t)}$')
```

