

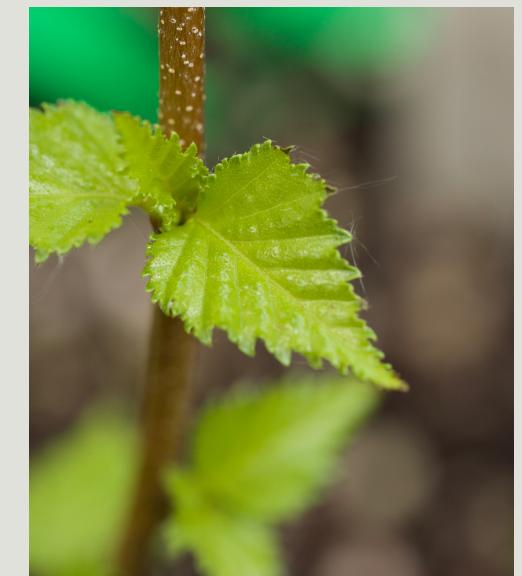
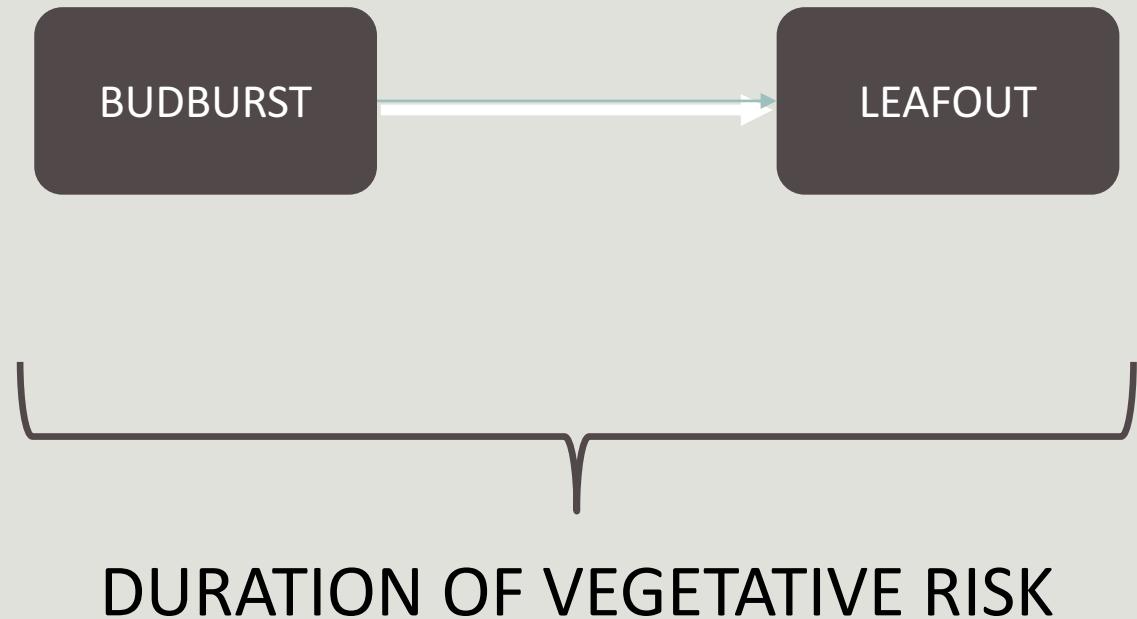
Buds Experiment

FALSE SPRING EVENTS

CATHERINE CHAMBERLAIN

False Spring Risk

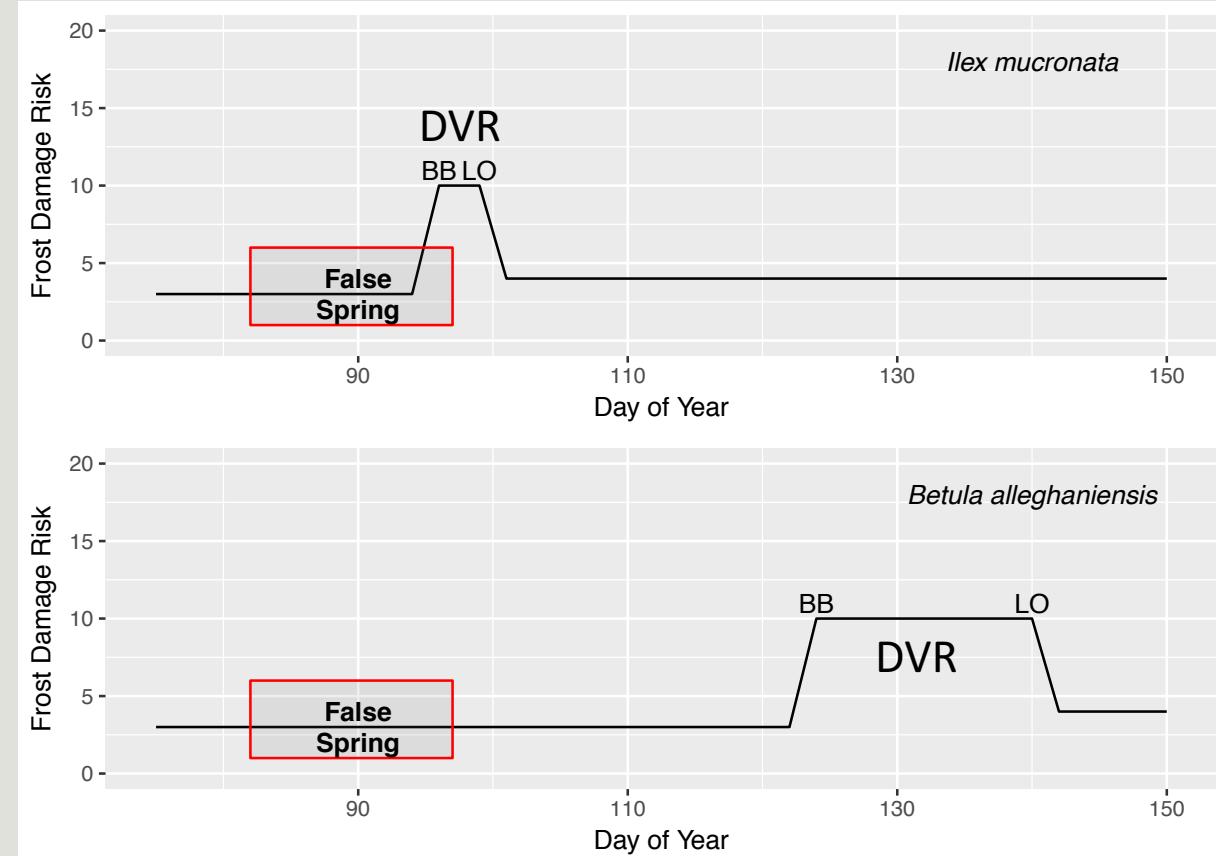
Interested in time between leaf budburst and leafout,
when frost tolerance is lowest but risk is still relatively high.



Betula populifolia - leafout

STRATEGIES:

Avoidance



Tolerance



Trichomes
on young
leaves

Serrations
along
leave
margins

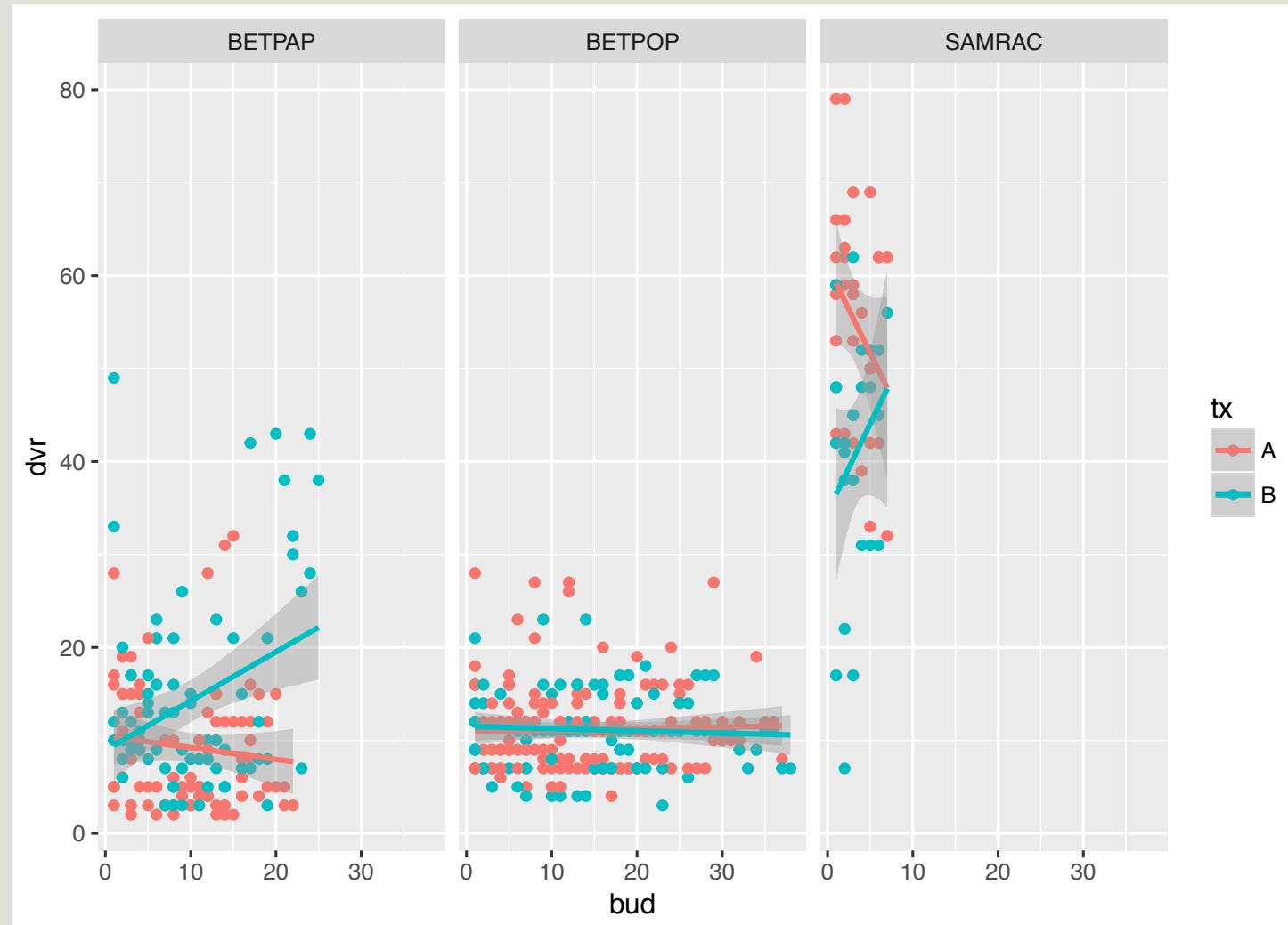
Buds Experiment

Freezing Experiment with greenhouse individuals

Put individuals in growth chamber at
-3degC between budburst and leafout







Sambucus racemosa hit by
pests...

Species: 2-3 -- BETPAP, BETPOP, SAMRAC (?)

Individuals: 14-18

Buds: 6-36

TX: Control vs. Freeze

$$\text{dvr} \sim \text{tx} + \text{species} + (1 | \text{individual})$$

DVR: Duration of Vegetative Risk

FAKE DATA: 2 ways (still testing...)

Apply Version

```
nrep <- 22
nind <- 7; ind_sd<-0.1
nsp <- 2; sp_sd<-0.3
ntx <- 2; tx_sd<-1

## Generate Random Y Response Data that follows studies nesting structure
rep_means <- rnorm(nrep, mean = 11, sd = 3)
ind_means <- lapply(rep_means, function(x) rnorm(nind, mean = x, sd = ind_sd))
sp_means <- lapply(ind_means, function(x) rnorm(nsp, mean = x, sd = sp_sd) )
tx_means <- lapply(unlist(sp_means), function(x) rnorm(ntx, mean = x, sd = tx_sd))

## Put Together X Predictor Matrix
ntot <- nsp * ntx * nind * nrep
x_mat <- data.frame(buds = rep(1:(nrep), each = ntot/nrep),
                      species = rep(1:(nsp), each = nrep*nind*nsp),
                      tx = rep(1:(ntx), each=nsp*nind),
                      ind = rep(1:(nind), each=nrep))

## Add in response for full fake dataset
x_mat <- x_mat[order(x_mat$species, x_mat$tx, x_mat$ind),]
#x_mat$dvr<-rnorm(n_pops, mean = 11, sd = 5)
x_mat$dvr <- unlist(tx_means)
fake_data <- x_mat

# now fix the levels to 0/1 (not 1/2) as R does
fake_data$tx <- as.numeric(fake_data$tx)
fake_data$tx[fake_data$tx==1] <- 0
fake_data$tx[fake_data$tx==2] <- 1
```

Looping

```
##### Again, now with individuals.

baseinter = 11 # baseline intercept across all individuals
spint <- baseinter + c(1:nind)-mean(1:nind) # different intercepts by individual

fake <- vector()

for(i in 1:nind){ # loop over individual (random effect)

  # Give individuals different difference values, drawn from normal
  coeff <- c(spint[i],
              rnorm(1, spdiff, spdiff.sd),
              rnorm(1, txdiff, txdiff.sd)
  )

  dvr <- rnorm(n = length(tx), mean = mm %*% coeff, sd = 0.1)

  fakex <- data.frame(dvr, ind = i, sp, tx)

  fake <- rbind(fake, fakex)
}

summary(lm(dvr ~ (sp+tx)^2, data = fake)) # sanity check
```

Stan_glmer (dvr ~ tx + species + (1 | ind))

Fake: apply version

```
stan_glmer
family: gaussian [identity]
formula: dvr ~ tx + species + (1 | ind)
-----
Estimates:
      Median MAD_SD
(Intercept) 10.0    0.4
tx          -0.2    0.3
species      0.2    0.3
sigma        3.3    0.1
```

Error terms:

Groups	Name	Std.Dev.
ind	(Intercept)	0.19
Residual		3.33

Num. levels: ind 7

Sample avg. posterior predictive distribution of y (X = xbar):

	Median	MAD_SD
mean_PPD	10.2	0.2

Fake: loop version

```
stan_glmer
family: gaussian [identity]
formula: dvr ~ tx + sp + (1 | ind)
-----
Estimates:
      Median MAD_SD
(Intercept) 10.5    0.7
tx          2.7    0.1
sp          0.5    0.1
sigma        0.7    0.0
```

Error terms:

Groups	Name	Std.Dev.
ind	(Intercept)	1.94
Residual		0.73

Num. levels: ind 7

Sample avg. posterior predictive distribution of y (X = xbar):

	Median	MAD_SD
mean_PPD	12.6	0.0

Real!

```
stan_glmer
family: gaussian [identity]
formula: dvr ~ tx + sp + (1 | ind)
-----
Estimates:
      Median MAD_SD
(Intercept) 10.5    1.8
tx          1.5    0.6
sp          0.4    0.7
sigma        6.3    0.2
```

Error terms:

Groups	Name	Std.Dev.
ind	(Intercept)	3.7
Residual		6.3

Num. levels: ind 8

Sample avg. posterior predictive distribution of y (X = xbar):

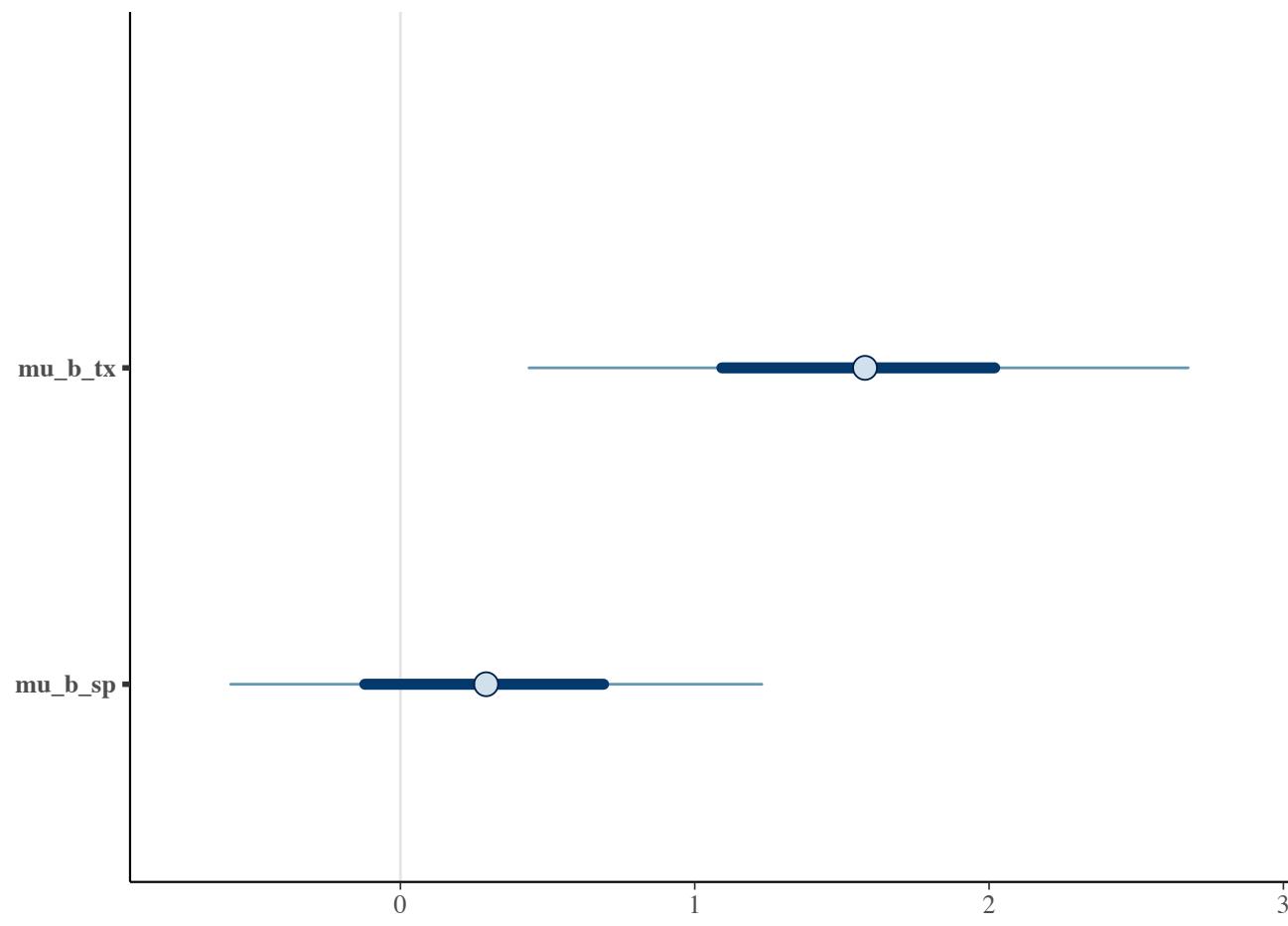
	Median	MAD_SD
mean_PPD	11.4	0.4

Stan Model

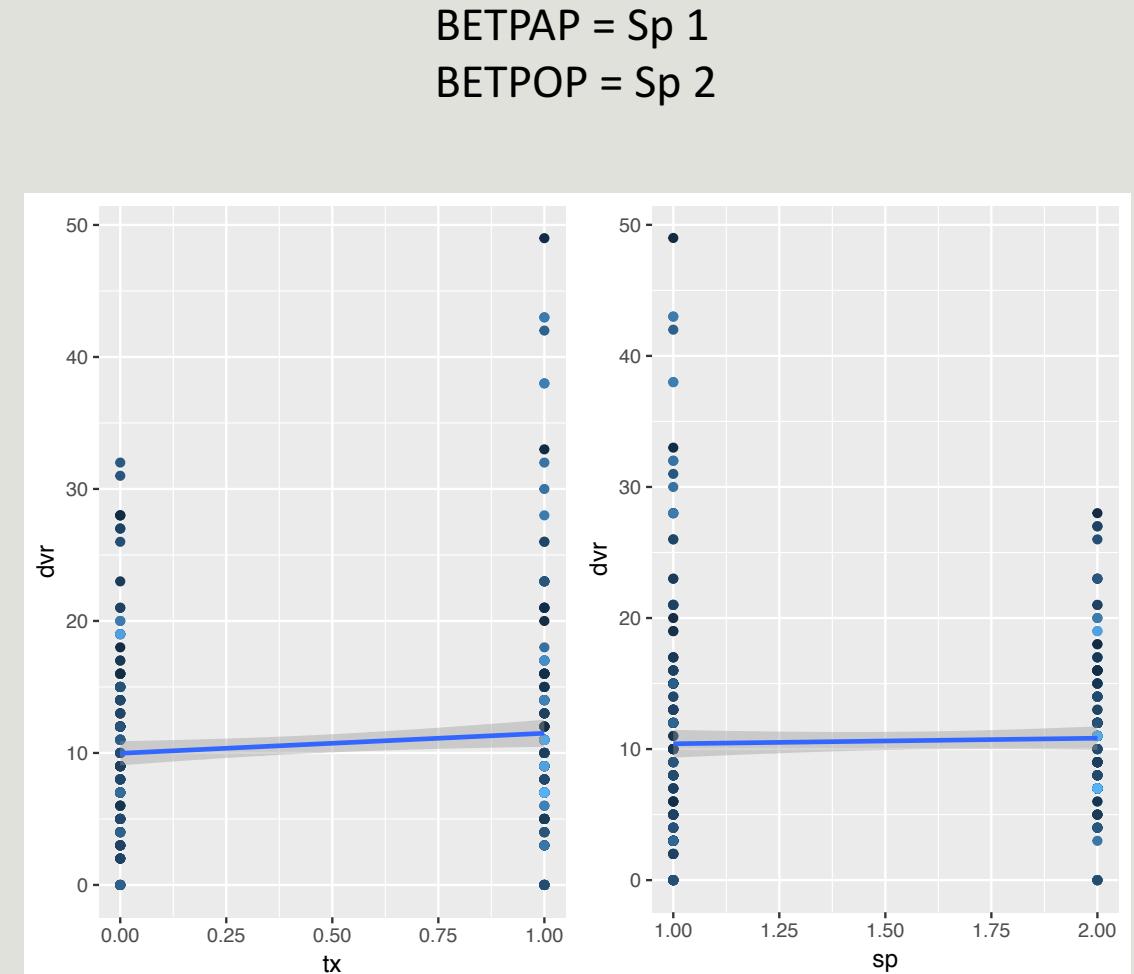
```
data {  
    int<lower=0> N;  
    int<lower=0> n_ind;  
    int<lower=0> n_sp;  
    int<lower=1, upper=n_ind> ind[N];  
    vector[N] dvr;  
    vector[N] tx;  
    vector[N] sp;  
}  
  
parameters {  
    vector[n_ind] a_ind;  
    vector[n_ind] b_tx;  
    vector[n_ind] b_sp;  
  
    real mu_a;  
    real mu_b_tx;  
    real mu_b_sp;  
  
    real<lower=0> sigma_b_tx;  
    real<lower=0> sigma_b_sp;  
  
    real<lower=0> sigma_a;  
  
    real<lower=0> sigma_y;  
}
```

```
transformed parameters {  
    vector[N] y_hat;  
  
    for(i in 1:N){  
        y_hat[i] = a_ind[ind[i]] +  
            b_sp[ind[i]] * sp[i] +  
            b_tx[ind[i]] * tx[i]  
    }  
}  
  
model {  
    // Priors. Make them flat  
    mu_b_tx ~ normal(0, 5);  
    mu_b_sp ~ normal(0, 2);  
  
    sigma_b_tx ~ normal(0, 1);  
    sigma_b_sp ~ normal(0, .5);  
  
    a_ind ~ normal(mu_a, sigma_a); |  
    b_tx ~ normal(mu_b_tx, sigma_b_tx);  
    b_sp ~ normal(mu_b_sp, sigma_b_sp);  
  
    dvr ~ normal(y_hat, sigma_y);  
}
```

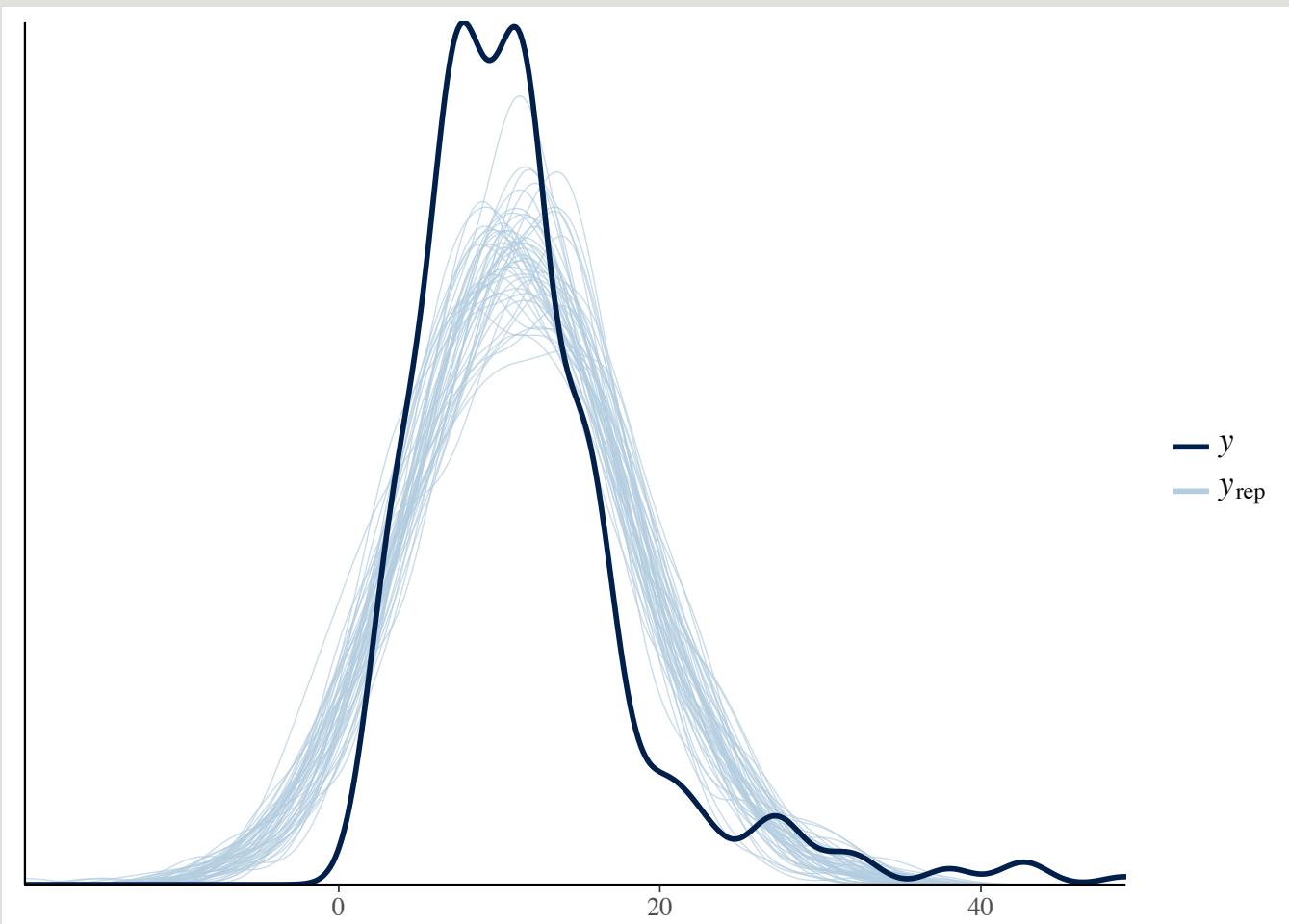
Real Data Output



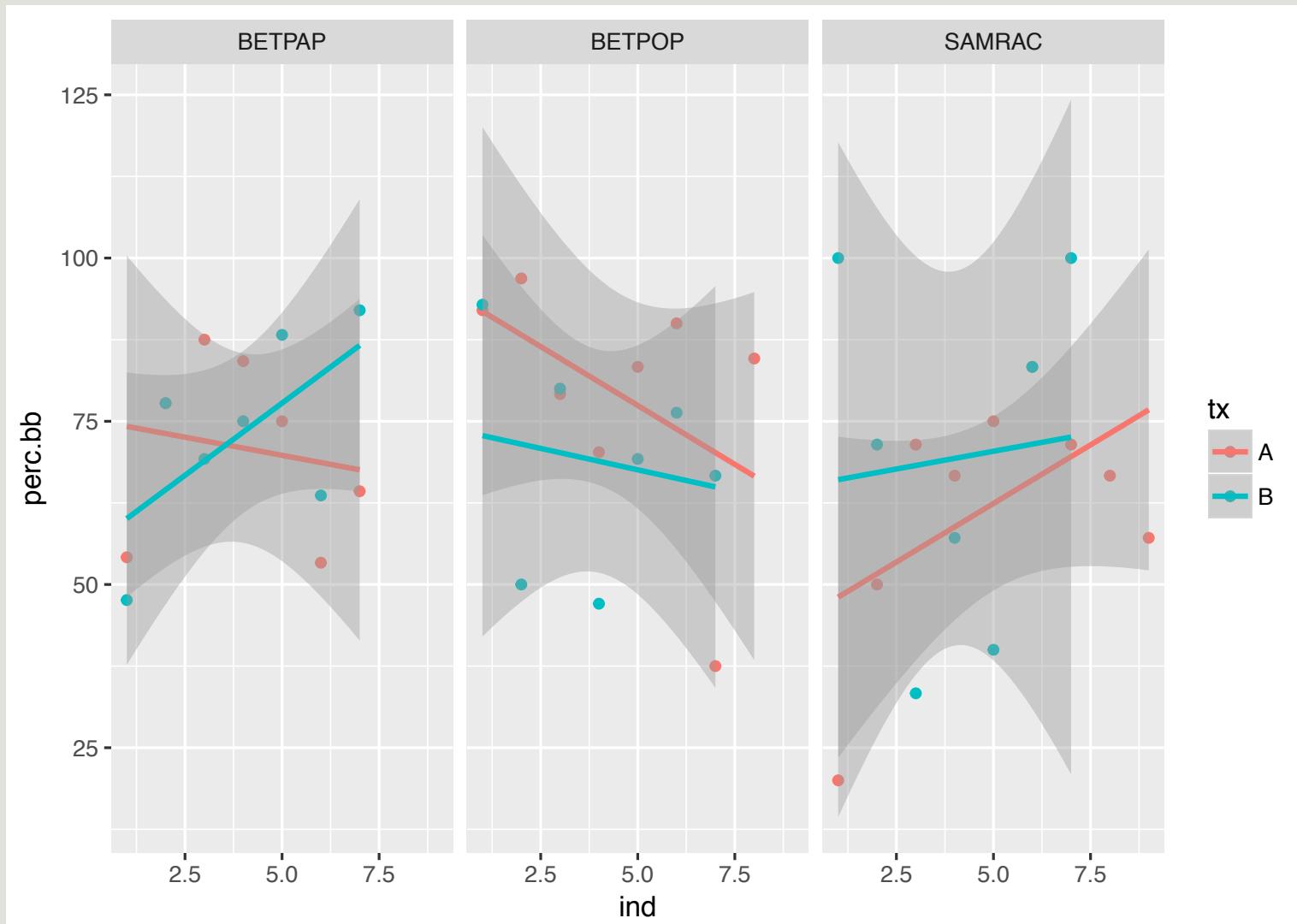
$dvr \sim tx + \text{species} + (1|\text{individual})$



PP_Check



Percent Budburst Model: percBB ~ tx + species

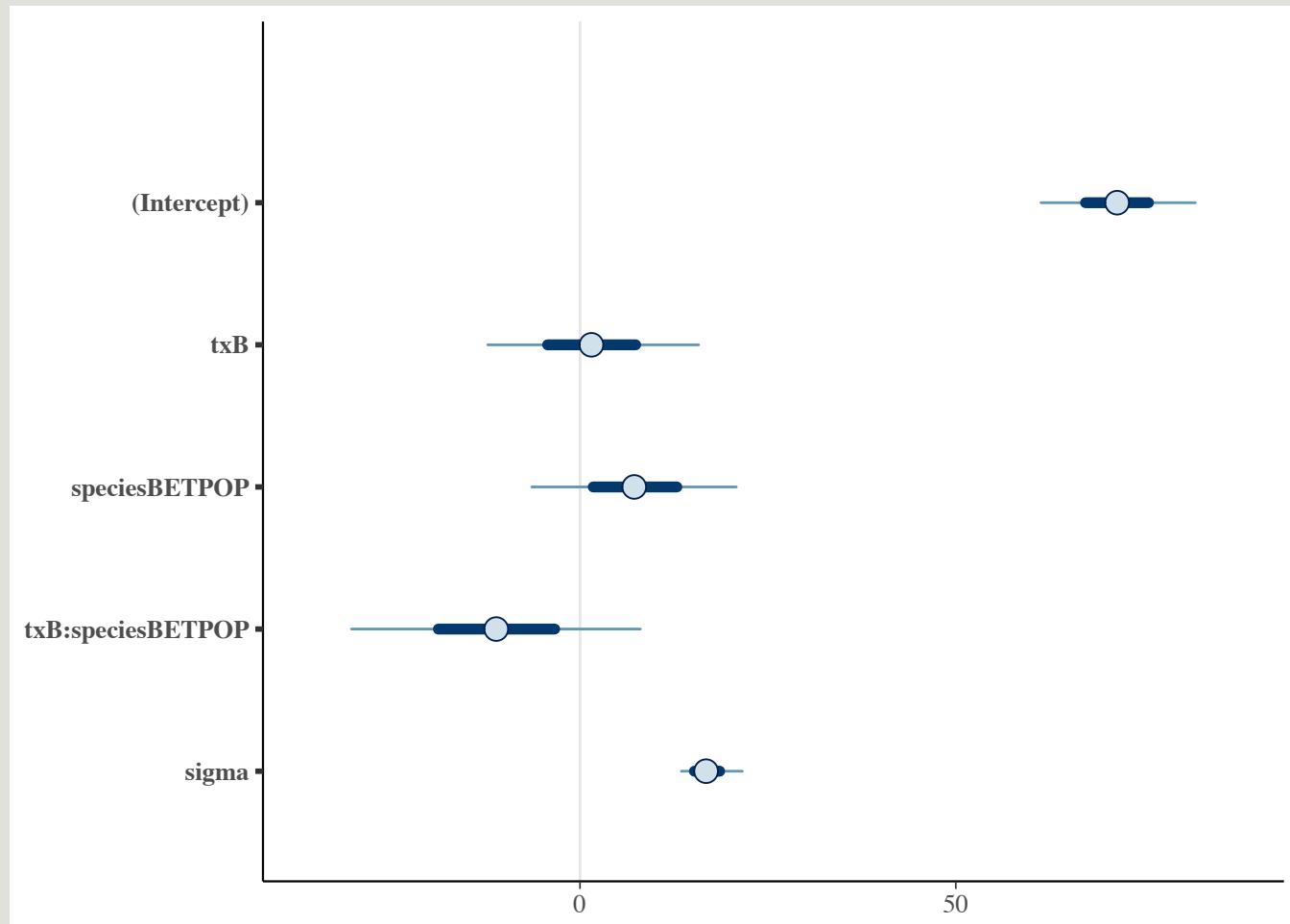


Dove straight into the Real data...

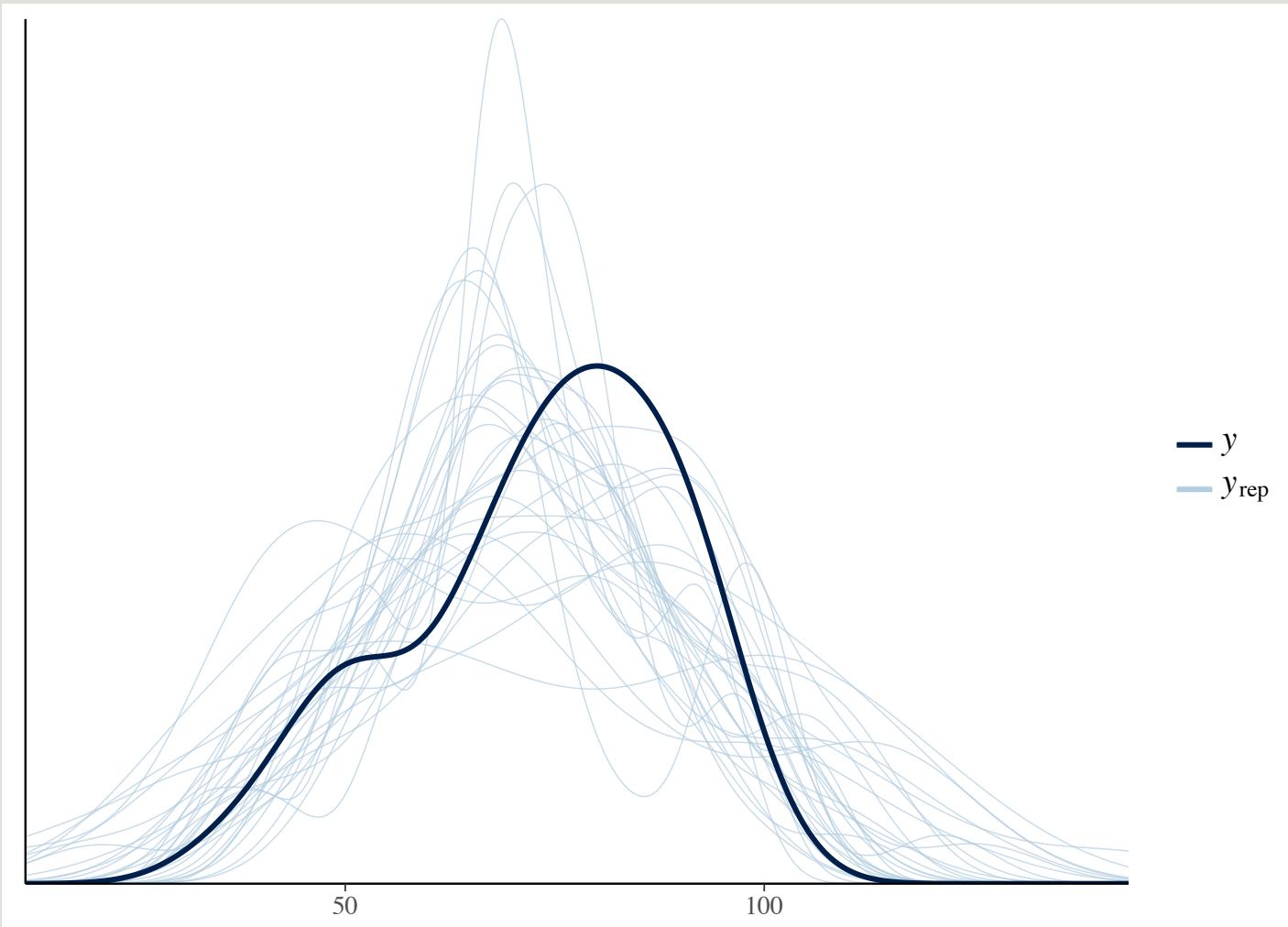
- ** Need to make fake data and start learning about Beta Distribution models
- ** Not including *Sambucus racemosa*

```
stan_glm
  family: gaussian [identity]
  formula: perc.bb ~ tx + species
-----
Estimates:
      Median MAD_SD
(Intercept) 74.1   5.4
txB        -3.9   6.2
speciesBETPOP 2.0   6.2
sigma       16.8   2.3

Sample avg. posterior predictive
distribution of y (X = xbar):
      Median MAD_SD
mean_PPD 73.3   4.4
```



PP_check



Next Steps...

1. Make models for each species: incorporate *Sambucus racemosa*
2. Work on Posterior Predictive Checks
3. Try to learn about Beta Distribution models
 - a) $\% \text{ budburst} \sim \text{tx} + \text{species} + (1 | \text{individual})$
4. Somehow evaluate both models