

Supplemental materials: Variation across space, species and methods in models of spring phenology

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Methods S1: Using simulations to test Bayesian models in Rstan

To test all models, we used data simulations but simulation data can only take us so far in model interpretation. We first needed to be certain our models were operating correctly. To test our model function, we built test data and manipulated the effects of the parameters to make sure the models were reporting this information accurately. As building such data can be critical to testing models and better understanding them we provide a Shiny App and GitHub repository for this purpose for the models presented here.

Methods S2: Data analysis and model equations

Using Bayesian hierarchical models, we estimated the effects of site (i.e., ‘forest’ sites modeled as ‘0’ versus ‘urban’ sites modeled as a ‘1’), method (i.e., HOB0 logger climate data modeled as ‘0’ and weather station climate data modeled as ‘1’) and the interaction between site and method effects as predictors with species modeled hierarchically as grouping factors:

$$y_i = \alpha_{species[i]} + \beta_{site_{species[i]}} X_{site} + \beta_{method_{species[i]}} X_{method} + \beta_{sitexmethod_{species[i]}} X_{sitexmethod} + \epsilon_i \quad (1)$$

$$\epsilon_i \sim N(0, \sigma_y)$$

The α and each of the five β coefficients are modeled at the species level, as follows:

$$\begin{aligned}
\alpha_{species} &\sim N(\mu_{\alpha}, \sigma_{\alpha}) \\
\beta_{site_{species}} &\sim N(\mu_{site}, \sigma_{site}) \\
\beta_{method_{species}} &\sim N(\mu_{method}, \sigma_{method}) \\
\beta_{site_{method}_{species}} &\sim N(\mu_{site_{method}}, \sigma_{site_{method}})
\end{aligned}$$

where i represents each unique observation, $species$ is the species, α represents the intercept, β terms represent slope estimates, and y is the number of growing degree days.

Supplemental tables and figures

Tables

Table S1: **Estimates from urban simulations.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable. See main text methods and Fig 1 for more details.

| | mean | 25% | 75% | 2.5% | 97.5% |
|--------------------------|--------|--------|--------|--------|--------|
| μ_{α} | 307.40 | 303.75 | 310.96 | 296.83 | 318.49 |
| μ_{site} | 20.67 | 20.08 | 21.25 | 19.01 | 22.30 |
| μ_{method} | 0.23 | -0.35 | 0.80 | -1.49 | 1.97 |
| $\mu_{site_{method}}$ | -0.36 | -1.19 | 0.38 | -2.57 | 2.01 |
| σ_{site} | 1.18 | 0.56 | 1.65 | 0.06 | 2.93 |
| σ_{method} | 1.09 | 0.46 | 1.57 | 0.05 | 2.84 |
| $\sigma_{site_{method}}$ | 0.75 | 0.28 | 1.06 | 0.02 | 2.28 |
| σ_{α} | 21.49 | 18.37 | 23.99 | 14.82 | 31.44 |
| σ_y | 15.57 | 15.44 | 15.69 | 15.18 | 15.97 |
| N_{sp} | 15.00 | | | | |

Table S2: **Estimates from provenance latitude simulations.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable. See main text methods and Fig 1 for more details.

| | mean | 25% | 75% | 2.5% | 97.5% |
|--------------------------|--------|--------|--------|--------|--------|
| μ_{α} | 307.61 | 304.40 | 310.79 | 296.64 | 318.14 |
| μ_{site} | -4.80 | -5.38 | -4.22 | -6.47 | -3.05 |
| μ_{method} | -0.29 | -0.69 | 0.11 | -1.50 | 0.90 |
| $\mu_{site_{method}}$ | -0.54 | -1.41 | 0.32 | -3.03 | 1.96 |
| σ_{site} | 0.94 | 0.39 | 1.35 | 0.04 | 2.61 |
| σ_{method} | 0.77 | 0.33 | 1.09 | 0.03 | 2.13 |
| $\sigma_{site_{method}}$ | 1.58 | 0.72 | 2.23 | 0.08 | 4.08 |
| σ_{α} | 20.54 | 17.57 | 22.71 | 14.07 | 30.22 |
| σ_y | 15.57 | 15.43 | 15.71 | 15.19 | 15.96 |
| N_{sp} | 15.00 | | | | |

Table S3: **Estimates from microclimate simulations.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable. See main text methods and Fig 1 for more details.

| | mean | 25% | 75% | 2.5% | 97.5% |
|------------------------|--------|--------|--------|--------|--------|
| μ_α | 322.94 | 318.50 | 327.45 | 310.33 | 335.58 |
| μ_{site} | -0.32 | -0.91 | 0.30 | -2.11 | 1.42 |
| μ_{method} | -6.78 | -8.07 | -5.50 | -10.55 | -3.07 |
| $\mu_{sitexmethod}$ | 1.05 | 0.26 | 1.85 | -1.33 | 3.38 |
| σ_{site} | 1.14 | 0.47 | 1.65 | 0.06 | 3.12 |
| σ_{method} | 6.82 | 5.63 | 7.72 | 4.26 | 10.92 |
| $\sigma_{sitexmethod}$ | 1.23 | 0.46 | 1.77 | 0.04 | 3.60 |
| σ_α | 24.85 | 21.32 | 27.48 | 17.17 | 36.72 |
| σ_y | 16.73 | 16.59 | 16.87 | 16.32 | 17.14 |
| N_{sp} | 15.00 | | | | |

Table S4: **Estimates from noisy weather station simulations.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable. See main text methods and Fig 1 for more details.

| | mean | 25% | 75% | 2.5% | 97.5% |
|------------------------|--------|--------|--------|--------|--------|
| μ_α | 307.45 | 303.99 | 310.89 | 297.13 | 318.19 |
| μ_{site} | 0.07 | -0.50 | 0.66 | -1.54 | 1.69 |
| μ_{method} | 4.93 | 2.35 | 7.60 | -3.09 | 12.52 |
| $\mu_{sitexmethod}$ | -0.39 | -1.16 | 0.36 | -2.81 | 1.84 |
| σ_{site} | 0.68 | 0.26 | 0.98 | 0.02 | 1.93 |
| σ_{method} | 14.63 | 12.37 | 16.33 | 9.81 | 22.36 |
| $\sigma_{sitexmethod}$ | 0.86 | 0.33 | 1.23 | 0.03 | 2.59 |
| σ_α | 21.79 | 18.43 | 24.37 | 14.47 | 33.19 |
| σ_y | 15.55 | 15.42 | 15.67 | 15.16 | 15.95 |
| N_{sp} | 15.00 | | | | |

Table S5: **Estimates from noisy HOBO logger simulations.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable. See main text methods and Fig 1 for more details.

| | mean | 25% | 75% | 2.5% | 97.5% |
|------------------------|--------|--------|--------|--------|--------|
| μ_α | 316.41 | 311.01 | 321.54 | 299.27 | 333.71 |
| μ_{site} | -1.20 | -1.78 | -0.62 | -2.89 | 0.51 |
| μ_{method} | -6.41 | -9.15 | -3.68 | -14.64 | 1.86 |
| $\mu_{sitexmethod}$ | 2.15 | 1.36 | 2.91 | -0.10 | 4.47 |
| σ_{site} | 1.00 | 0.42 | 1.43 | 0.03 | 2.73 |
| σ_{method} | 15.14 | 12.73 | 17.02 | 10.11 | 23.17 |
| $\sigma_{sitexmethod}$ | 1.20 | 0.48 | 1.70 | 0.04 | 3.31 |
| σ_α | 31.87 | 27.47 | 35.30 | 22.11 | 46.96 |
| σ_y | 15.05 | 14.91 | 15.19 | 14.67 | 15.46 |
| N_{sp} | 15.00 | | | | |

Table S6: **Estimates from empirical urban versus rural model.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable.

| | mean | 25% | 75% | 2.5% | 97.5% |
|-------------------------------|--------|--------|--------|--------|--------|
| μ_α | 437.88 | 426.93 | 449.53 | 401.77 | 469.66 |
| μ_{site} | -40.75 | -50.73 | -31.31 | -69.71 | -10.23 |
| μ_{method} | 1.47 | -5.42 | 8.27 | -18.47 | 20.36 |
| $\mu_{site \times method}$ | -43.53 | -51.04 | -35.53 | -68.06 | -20.23 |
| σ_{site} | 42.80 | 34.12 | 50.79 | 19.11 | 71.77 |
| σ_{method} | 17.13 | 7.86 | 24.52 | 0.79 | 42.11 |
| $\sigma_{site \times method}$ | 24.96 | 15.15 | 33.60 | 2.26 | 54.65 |
| σ_α | 53.65 | 44.60 | 61.17 | 33.01 | 83.36 |
| σ_y | 71.69 | 69.77 | 73.51 | 66.49 | 77.74 |
| N_{sp} | 17.00 | | | | |

Table S7: **Estimates from empirical provenance latitude model.** We present posterior means, as well as 50% and 95% uncertainty intervals from models in which the predictors have been standardized so that they are comparable.

| | mean | 25% | 75% | 2.5% | 97.5% |
|-------------------------------|--------|--------|--------|--------|--------|
| μ_α | 399.53 | 389.19 | 410.24 | 365.67 | 430.54 |
| μ_{site} | 16.17 | 9.37 | 23.01 | -3.96 | 36.13 |
| μ_{method} | -5.70 | -10.01 | -1.49 | -18.72 | 7.46 |
| $\mu_{site \times method}$ | -2.44 | -9.26 | 3.99 | -20.62 | 16.73 |
| σ_{site} | 14.45 | 6.36 | 20.02 | 0.58 | 41.27 |
| σ_{method} | 9.13 | 3.69 | 13.09 | 0.38 | 24.77 |
| $\sigma_{site \times method}$ | 12.89 | 5.50 | 18.39 | 0.48 | 36.13 |
| σ_α | 59.46 | 50.36 | 66.66 | 37.73 | 89.76 |
| σ_y | 84.57 | 82.47 | 86.53 | 78.88 | 91.01 |
| N_{sp} | 17.00 | | | | |

Figures

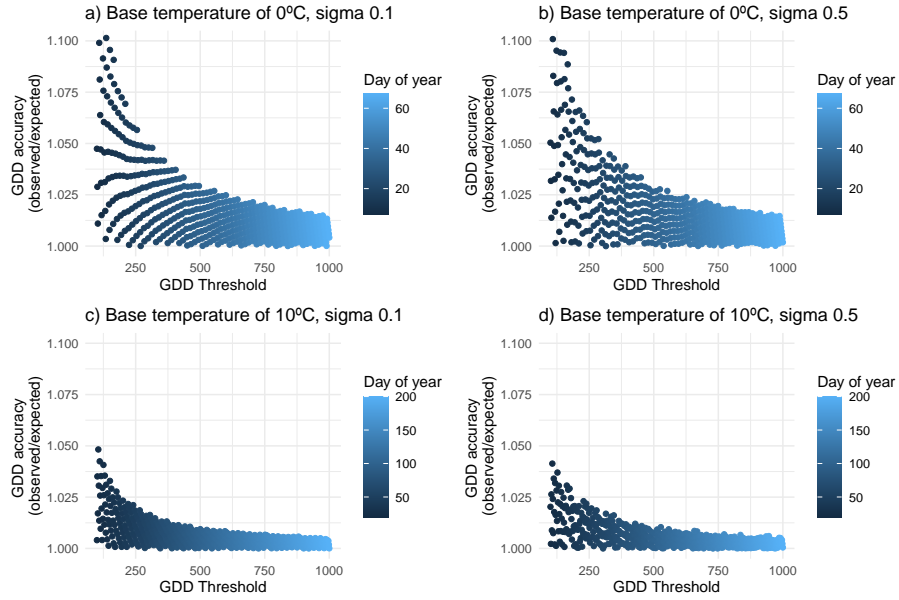


Figure S1: Using simulated data, we show how GDD measurement accuracy changes along varying GDD thresholds using a base temperature of (a) 0°C and a sigma of 0.1°C, (b) 0°C and a sigma of 0.5°C, (c) 10°C and a sigma of 0.1°C and (d) 10°C and a sigma of 0.5°C. GDD accuracy is measured as the observed GDD divided by the expected GDD.

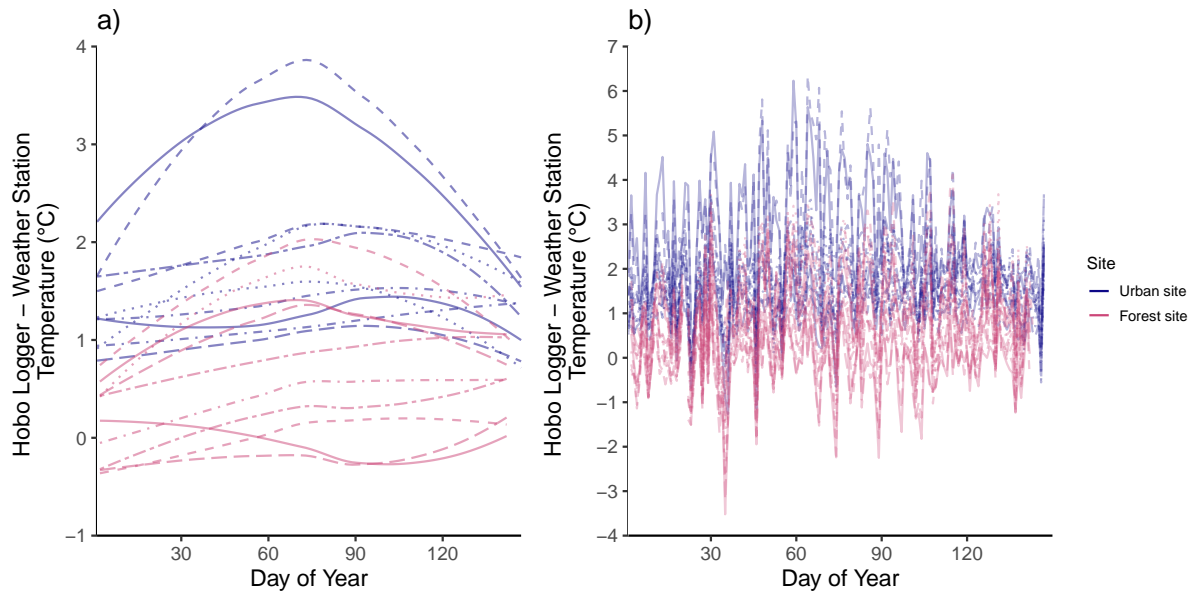


Figure S2: Here we show a breakdown of the mean temperature differences in data across the two sites between the two methods with darker lines representing weather station data and the lighter, more transparent lines of varying line types representing the HOBOLogger: a) a series of smoothing splines of mean temperature differences measured as HOBOLogger minus weather station and b) actual mean temperature differences measured as HOBOLogger minus weather station.

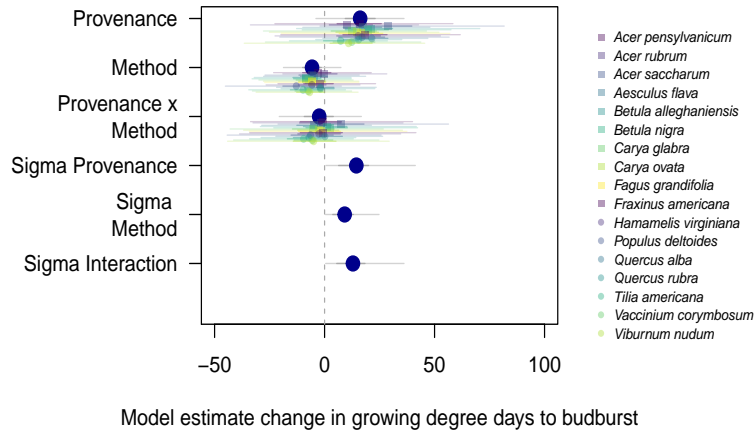


Figure S3: Empirical Data: Using real data to test provenance latitude, we show the effects of provenance latitude and climate data method (weather station versus HOBOLogger) on GDDs until budburst. The intercept represents the HOBOLogger data for the rural forested site. More positive values indicate more GDDs are required for budburst whereas more negative values suggest fewer GDDs are required. Dots and thin lines show means and 90% uncertainty intervals and thicker lines show 50% uncertainty intervals. See Table S7 for full model output.

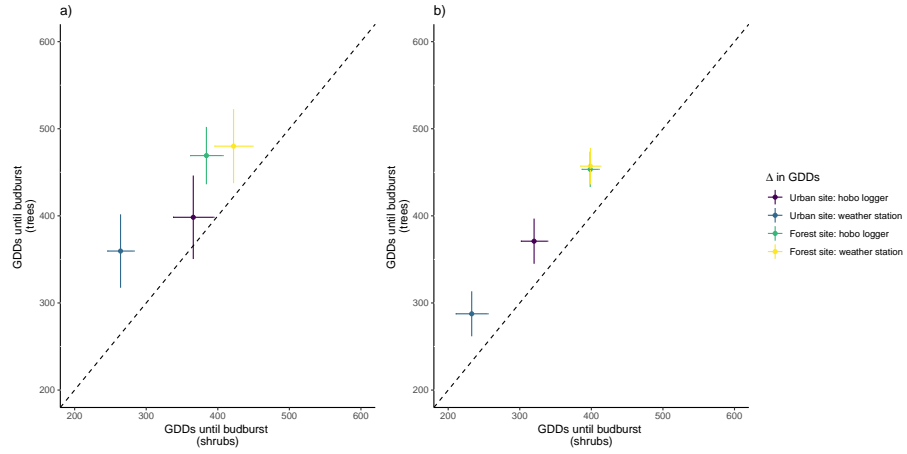


Figure S4: Empirical Data: Using real data, we show (a) the effects of site (urban versus rural) and climate data method (weather station versus HOBO logger) on GDDs until budburst between shrubs versus tree species used in the study. We also show model output for the same relationship in (b). The 1:1 (dashed) line helps visualize that shrubs generally require fewer GDDs until budburst than trees.

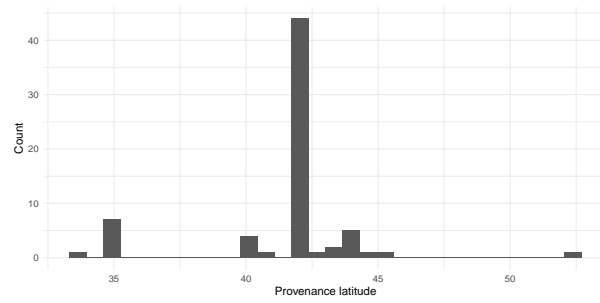


Figure S5: Histogram of provenance latitude data at the urban arboretum site.