

Problem1: Trailer hitch –

Q.1. a.

Diagram showing the trailer hitch assembly with forces and dimensions. The horizontal member is subjected to a force $F_T = 600 \text{ lbf}$ and a weight $W = 220 \text{ lbf}$. The dimensions are: horizontal distance $3''$, vertical distance $0.75''$, and member thickness $0.625''$. The cross-section B-B has a width of $2.5''$ and a height of $0.625''$.

FBD:

Equilibrium equations:

$$\sum F_x = 0 \Rightarrow S = F_T = 600 \text{ lbf}$$

$$\sum F_y = 0 \Rightarrow T = W = 220 \text{ lbf}$$

$$\sum M = 0 \Rightarrow M = F_T \times (1.616 + 0.625 + 0.75) + W(3 - 0.625)$$

$$\therefore M = 600 \times 2.991 + 220 \times 2.6875$$

$$\therefore M = 2385.85 \text{ lbf.in} \quad \text{--- (1)}$$

Area moment of Inertia at B-B:

$$I_{BB} = \frac{bd^3}{12} = \frac{2.5 \times 0.625^3}{12} \text{ in}^4 \quad \text{--- (2)}$$

Assuming neutral axis is at center:

$$y_{\max} = \frac{0.625}{2} \text{ in} \quad \text{--- (3)}$$

Bending moment at B-B:

$$\sigma_{\text{bending}} = \frac{My}{I_{BB}}$$

Let point 1 be at concave surface & point 2 at convex surface,

then, $\sigma_1 = \sigma_{\min}$ due to compression
& $\sigma_2 = \sigma_{\max}$ due to tension

$$\sigma_{\max/\min} = \pm \frac{My_{\max}}{I_{BB}} = \pm \frac{2385.85}{\frac{2.5 \times 0.625^3}{12}} \times \frac{0.625}{2}$$

$$\therefore \sigma_{\max/\min} = \pm 14658.6624 \text{ psi}$$

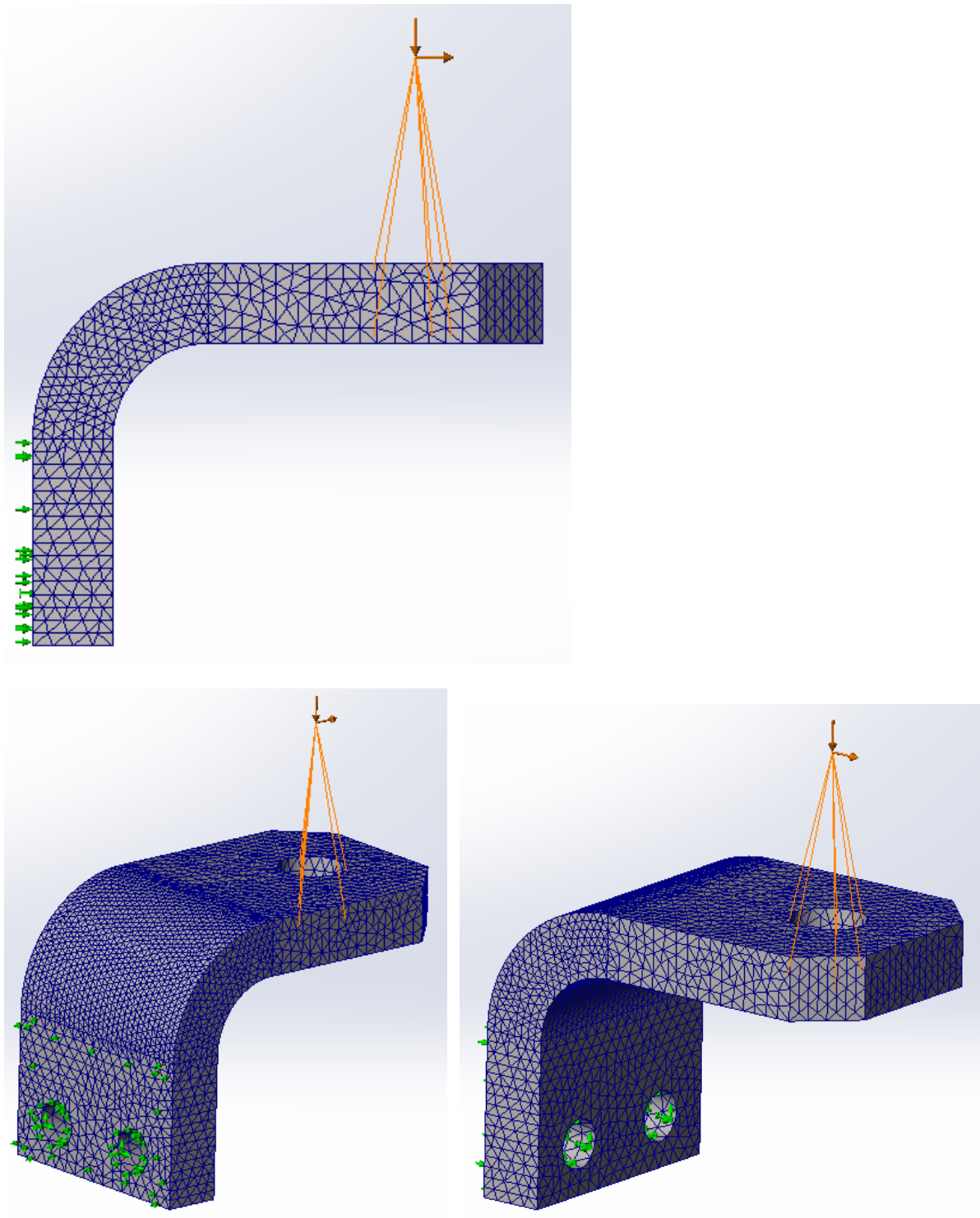
At concave surface,

$$\sigma_1 = \sigma_{\min} = -14658.6624 \text{ psi}$$

At convex surface,

$$\sigma_2 = \sigma_{\max} = +14658.6624 \text{ psi}$$

Q1.b. FEA model showing fixtures, remote loads, and mesh:

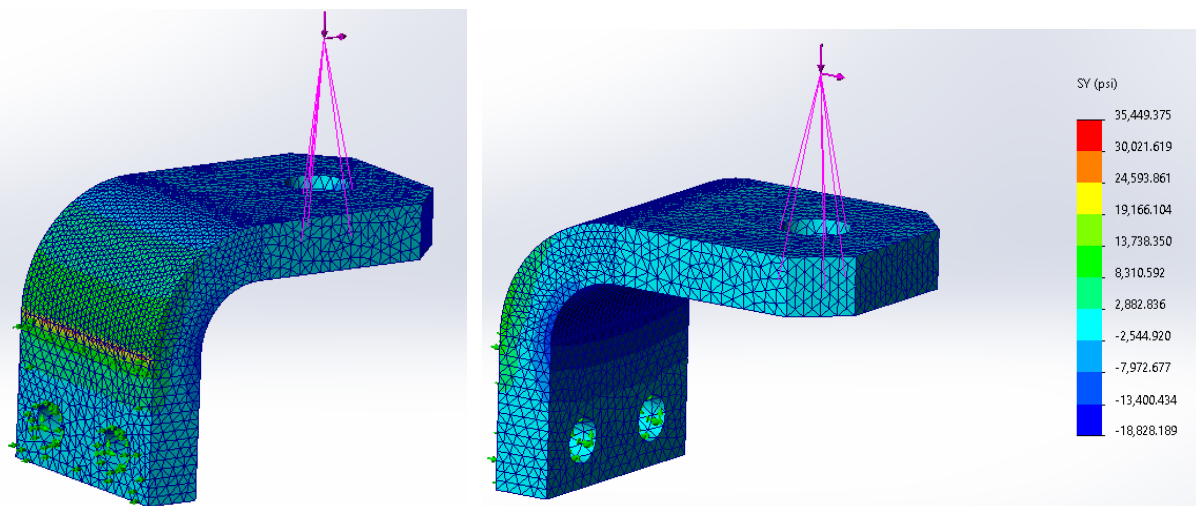
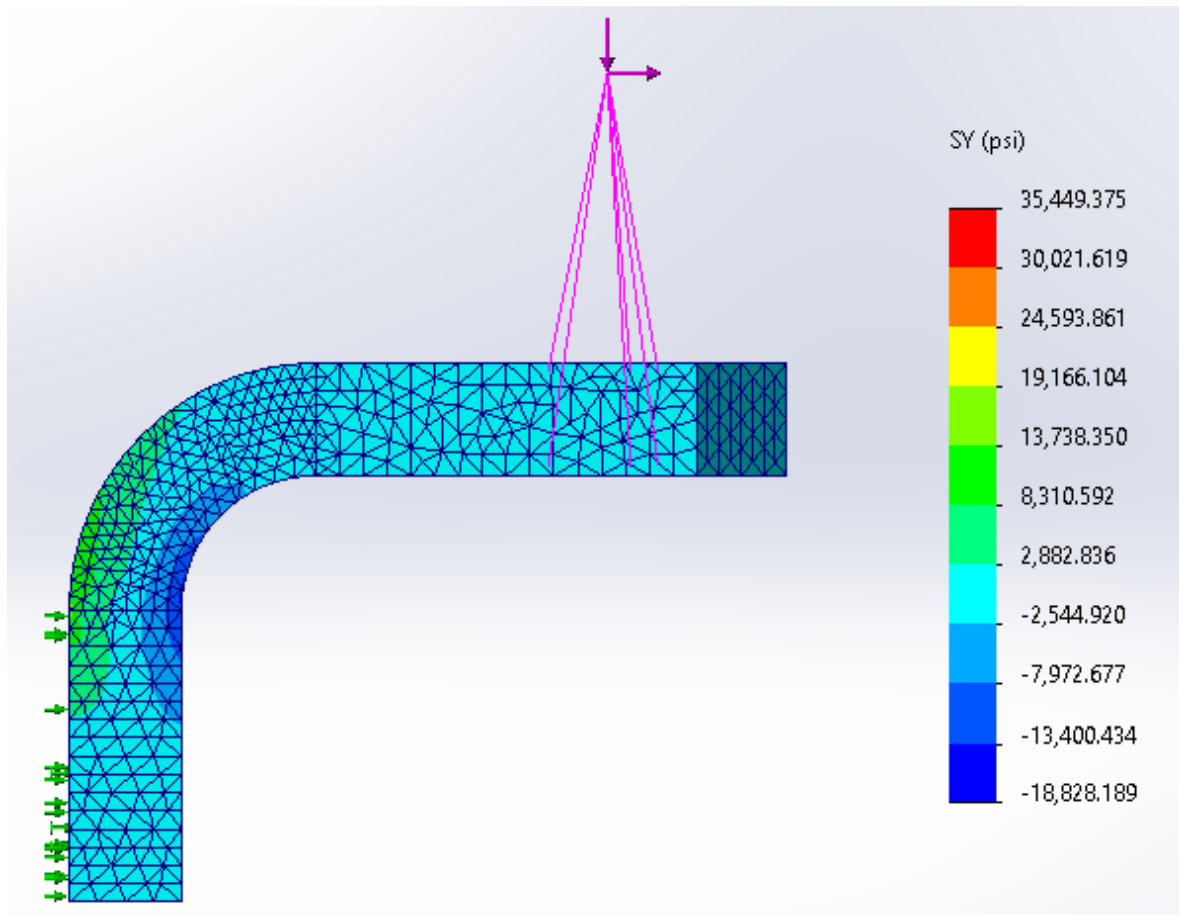


Fixtures: Fixed geometry on bolt hole walls & Roller support on side touching vehicle.

Remote load: Tow force = 600 lbf & Tongue weight = 220 lbf.

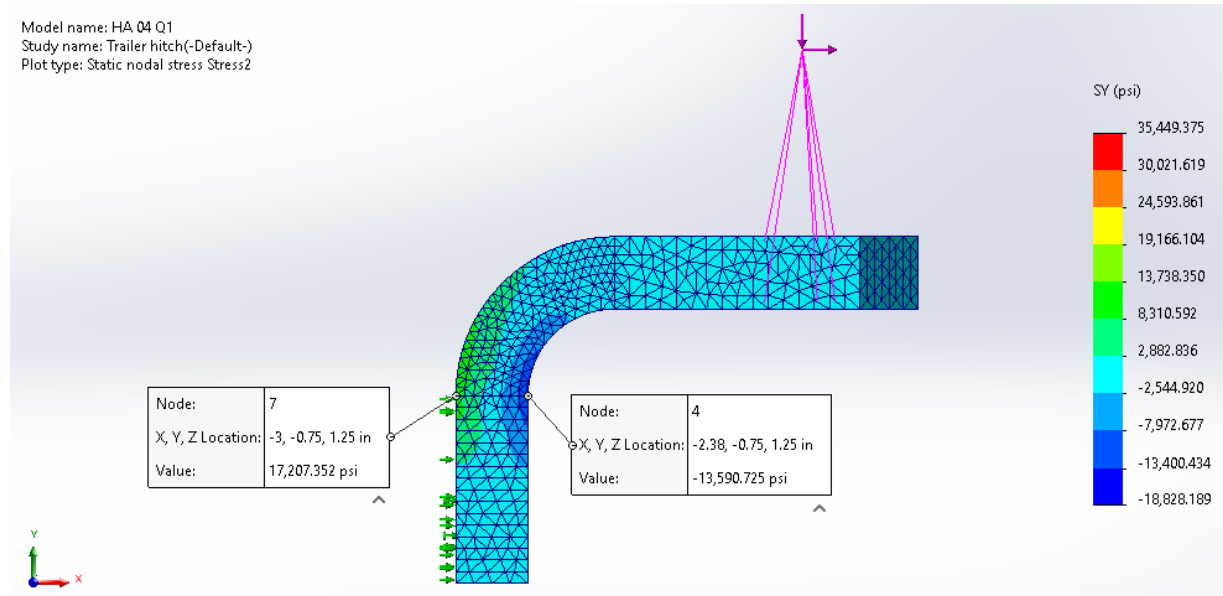
Q1.c.

Bending stress given by stress in Y-direction:



Q1.d.

Using probe to get values of bending stress at concave & convex sides of section B-B:



Q1.e. Comparing bending stress between FEA & classical:

At concave side,

Classical: $\sigma_1 = -14658.66 \text{ psi}$

FEA: $\sigma_1 = -13590.725 \text{ psi}$

Difference w.r.t. classical: 7.3%

At convex side,

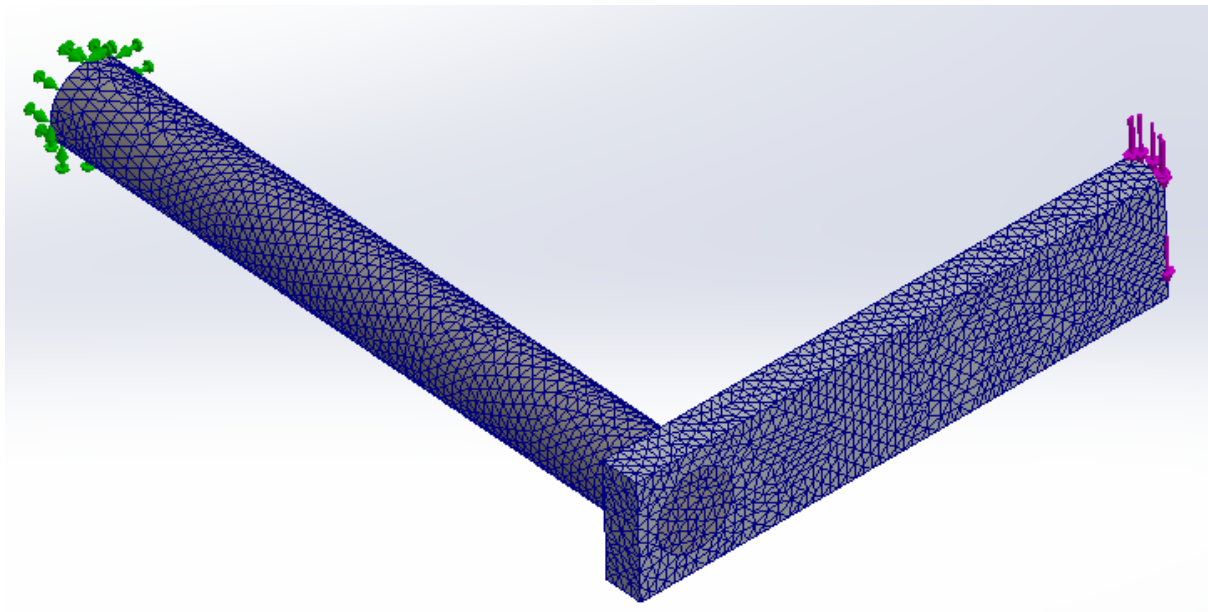
Classical: $\sigma_2 = 14658.66 \text{ psi}$

FEA: $\sigma_2 = 17207.352 \text{ psi}$

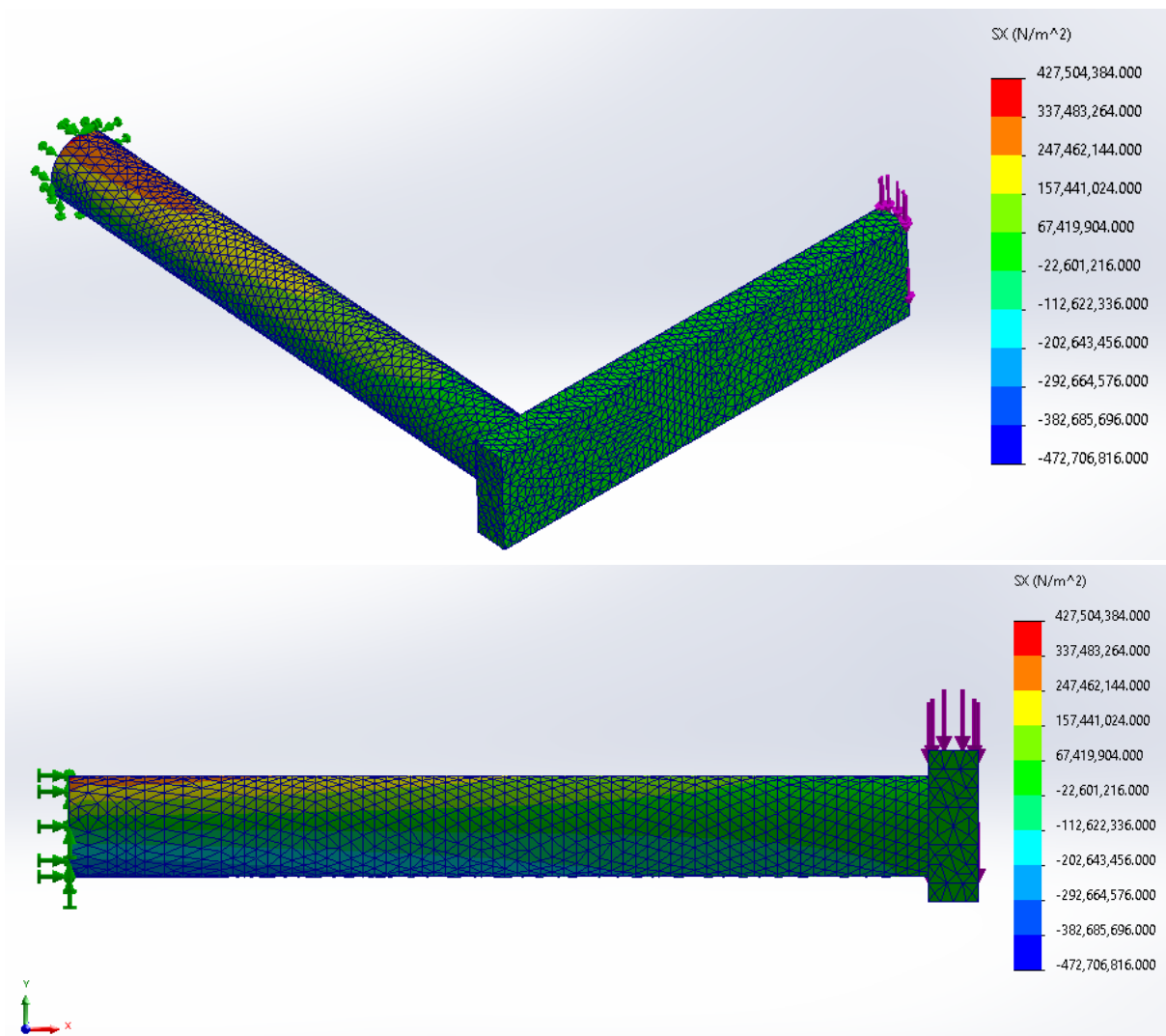
Difference w.r.t. classical: 17.4%

Conclusion: The FEA results are within 20% of the classical values for bending stress where we consider assumptions of 2D, uniform cross-section, neutral axis at centre. This can be taken care by considering a factor of safety of 1.2 or above for safe design in actual working conditions.

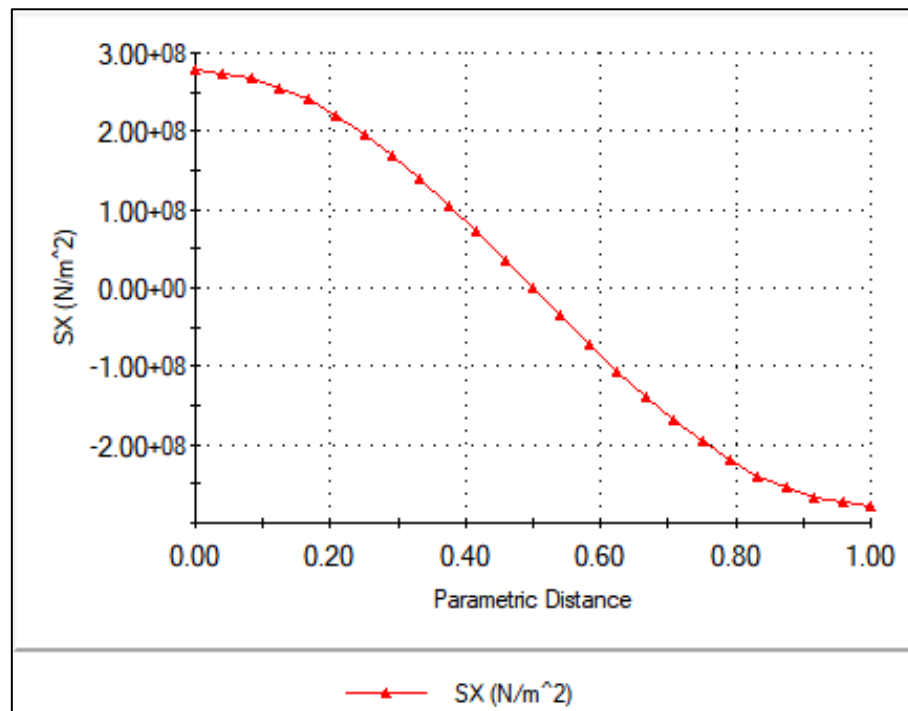
Problem 2: L-shaped cantilever beam –



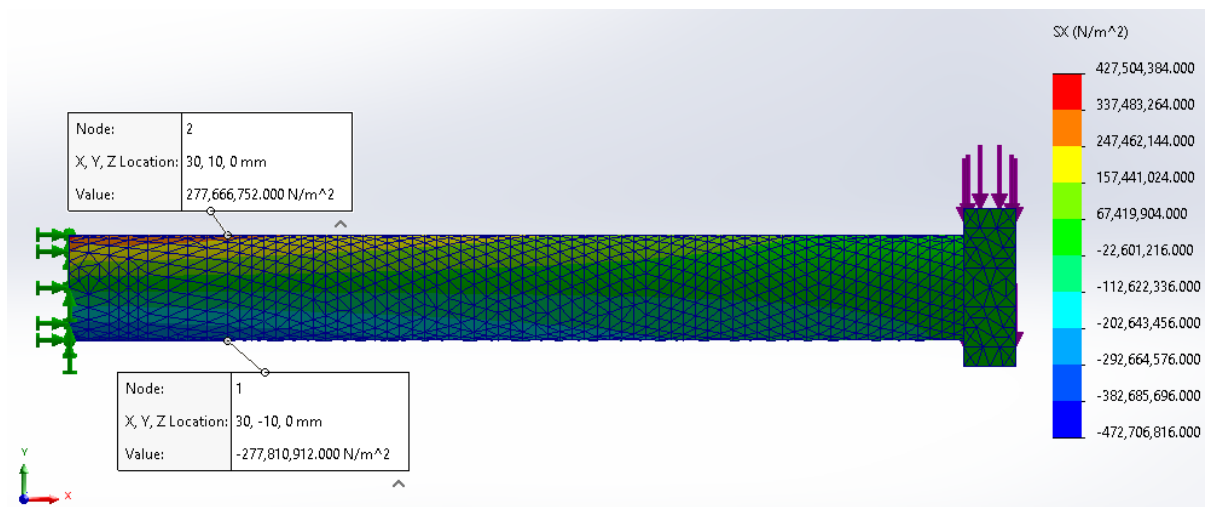
Q2.a. Bending stress given by stress in X-direction:



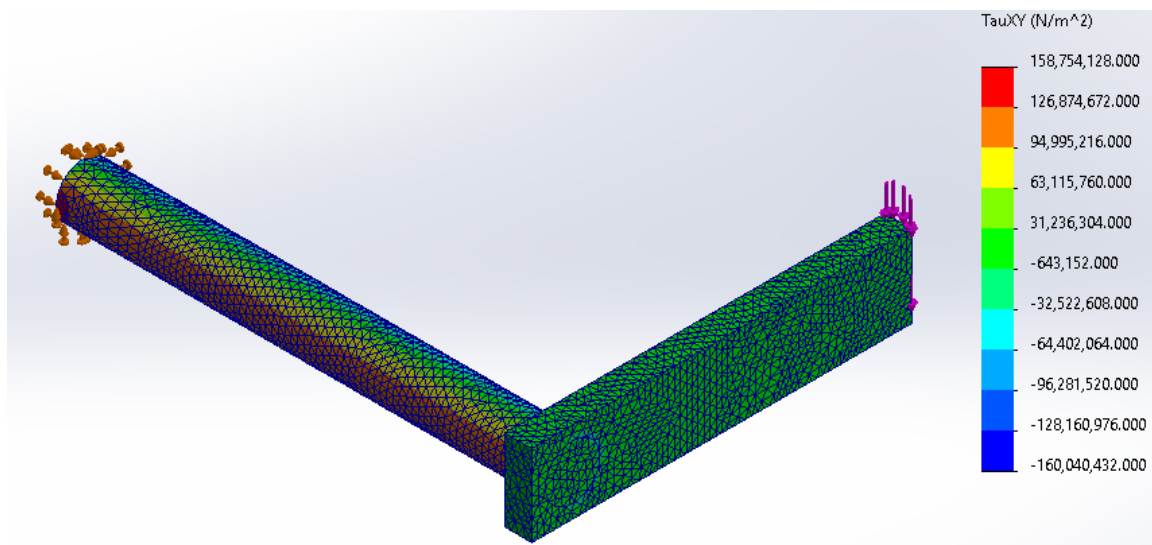
Q2.b. Using probe feature to create a XY plot of bending stress from the top to bottom of beam AB at section Z-Z:



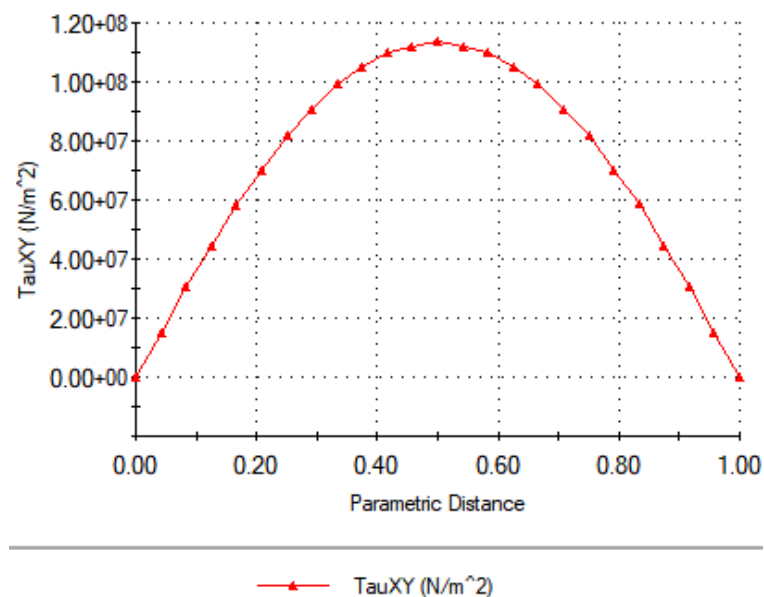
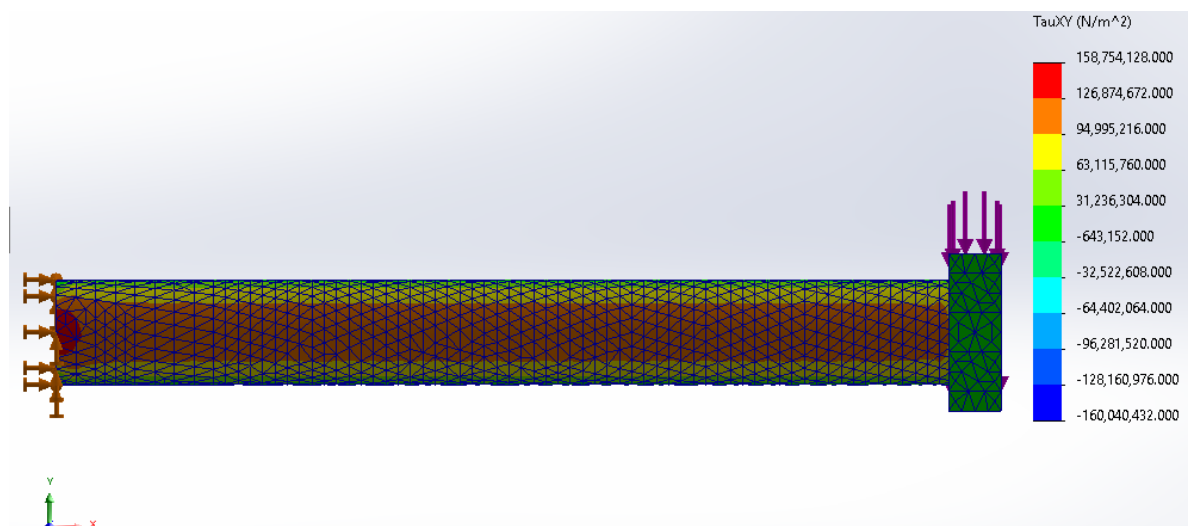
Using probe to get values of bending stress at top & bottom of section Z-Z:



Q2.c. Shear stress τ_{xy} :

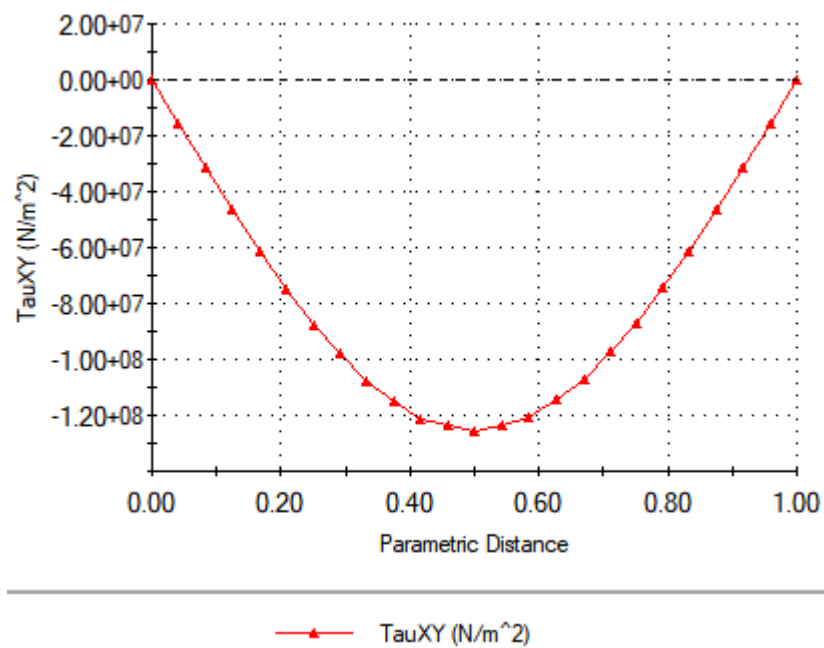
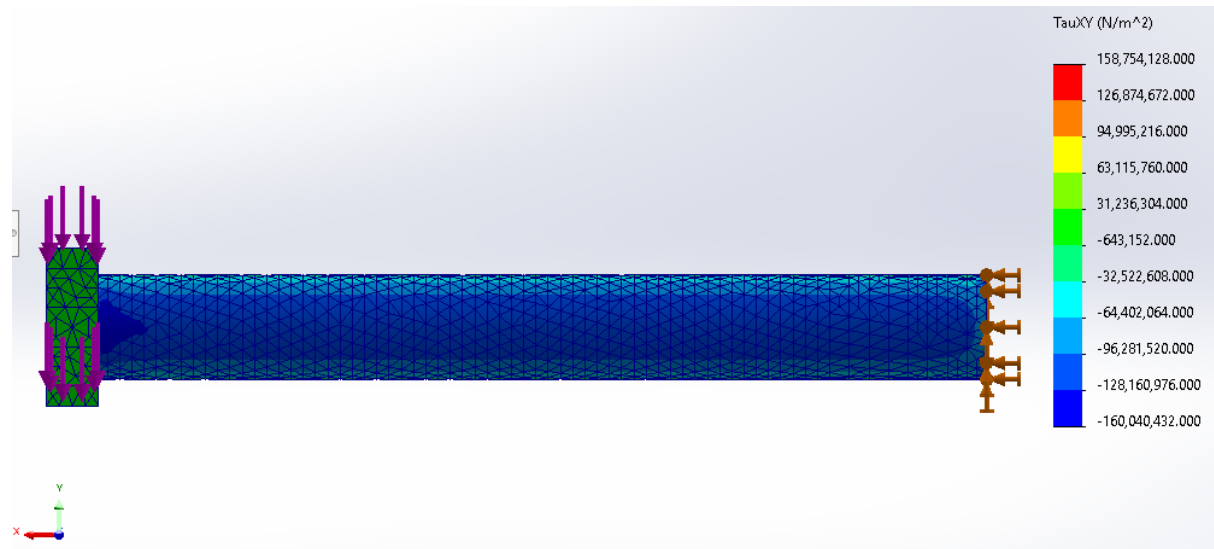


XY plot of shear stress τ_{xy} at section Z-Z using the probe feature, front side:

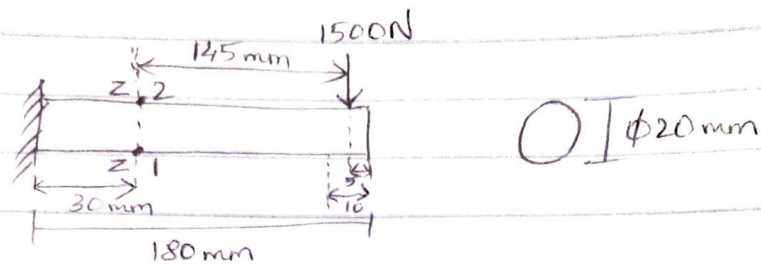


XY plot of shear stress τ_{xy} at section Z-Z using the probe feature:

Back side,



Q.2.d.



Bending moment at z-z:

$$M = 1500 \times 0.145 = 217.5 \text{ Nm}$$

$$y_{\max} = 10 \text{ mm} = 0.01 \text{ m}$$

$$I_{zz} = \frac{\pi D^4}{64} = \frac{\pi (0.02)^4}{64} = 7.854 \times 10^{-9} \text{ m}^4$$

$$\sigma_{\max/\min} = \pm \frac{M y_{\max}}{I_{zz}} = \pm \frac{217.5 \times 0.01}{7.854 \times 10^{-9}} = 276928953 \text{ N/m}^2$$

$$= 0.27693 \times 10^9 \text{ Pa}$$

$$= 0.27693 \text{ GPa}$$

Bending stress at top,

$$\sigma_2 = \sigma_{\max} = + 276928953 \text{ N/m}^2$$

Bending stress at bottom,

$$\sigma_1 = \sigma_{\min} = - 276928953 \text{ N/m}^2$$

Q2.e. Comparing bending stress between FEA & classical:

At bottom,

Classical: $\sigma_1 = -276,928,953 \text{ N/m}^2$

FEA: $\sigma_1 = -277,810,912 \text{ N/m}^2$

Difference w.r.t. classical: 0.3%

At top,

Classical: $\sigma_2 = 276,928,953 \text{ N/m}^2$

FEA: $\sigma_2 = 277,666,752 \text{ N/m}^2$

Difference w.r.t. classical: 0.3%

Conclusion: The FEA results are within 0.5% of the classical values for bending stress where we consider assumptions of 2D, uniform cross-section, neutral axis at centre. We can say that the results closely align as the geometry is simple and our assumptions are sufficiently considering the actual loading condition. Nonetheless, considering a factor of safety of 1.2 or above for safe design is good practice.