```
#1a
library(dplyr)
library(stringr)
library(zoo)
library(ggplot2)
library(devtools)
#install urbnmapr
##devtools::install_github("UrbanInstitute/urbnmapr")
library(urbnmapr)
install_github("Stat", force=TRUE)
##some functions we wrote for the analysis
source(file = "data_and_functions/functions_covid19.R")
##get the data from JHU CSSE, which contain the death and confirmed cases at county-level
base =
'https://raw.githubusercontent.com/CSSEGISandData/COVID-19/master/csse_covid_19_data/csse_covid_19_time_series/
death = 'time_series_covid19_deaths_'
confirm = 'time_series_covid19_confirmed_'
###up-to-date US death and confirmed cases
us_death = read.csv(paste0(base,death,"US.csv"))
us confirm = read.csv(paste0(base,confirm,"US.csv"))
##dimension
dim(us_death)
dim(us_confirm)
##get the column names of the data
col names = colnames(us death)
all\_dates = as.Date(paste0(str\_sub(col\_names[13:dim(us\_death)[2]], 2, -1), "20"), tryFormats = c("\%m.\%d.\%Y"))
##these are the dates from the data set
all_dates
##this site provide the confirmed state-level total test from which you can get the positive rate
covid19 project url = "https://api.covidtracking.com/v1/states/daily.csv"
covid_19_project = read.csv(covid19_project_url)
covid 19 project$date = as.Date(as.character(covid 19 project$date), "%Y %m %d")
##note that this date starts from the current day
covid_19_project$date
##nation level analysis
##nation level daily confirmed cases, plot and
nation_death = us_death %>%
 dplyr::filter(Country_Region == "US")
###observed confirmed cases
nation confirmed = us confirm %>%
 dplyr::filter(Country_Region == "US")
###the first row of the state death data set and you can see the format
nation_death[1,]
###get the cumulative death toll and confirmed cases
nation death sum = apply(nation death[,12:dim(nation death)[2]], 2, sum)
nation_confirmed_sum = apply(nation_confirmed[,12:dim(nation_confirmed)[2]], 2, sum)
##get dates you want to analyze
start_date = as.Date("2020-4-01")
```

```
end_date = as.Date("2020-12-01")
##the deaths and confirmed cases for the state on the selected dates
nation_death_selected = nation_death_sum[1 + which(all_dates %in% seq.Date(start_date, end_date, by=1))]
nation_confirmed_selected = nation_confirmed_sum[which(all_dates %in% seq.Date(start_date, end_date, by=1))]
nation_death_selected=as.numeric(nation_death_selected)
nation_confirmed_selected=as.numeric(nation_confirmed_selected)
##plot cumulative confirmed cases and death
date_selected=seq.Date(start_date, end_date, by=1)
par(mfrow=c(1,2))
plot(date selected,nation confirmed selected,xlab='date',ylab='cumulative observed confirmed cases',type='l')
plot(date_selected,nation_death_selected,xlab='date',ylab='cumulative death toll',type='l')
##close it
##daily increase between each date
daily_date_selected=date_selected[2:length(date_selected)]
##let's get the daily confirmed cases
nation_confirmed_selected_daily=nation_confirmed_selected[2:length(nation_confirmed_selected)]-nation_confirmed_selected[1:
(length(nation_confirmed_selected)-1)]
##create a data frame
daily_confirmed_nation_df = data.frame(date = daily_date_selected, value = nation_confirmed_selected_daily)
##let's get the daily death cases
nation death selected daily=nation death selected[2:length(nation death selected)]-nation death selected[1:(length(nation d
eath selected)-1)]
##create a data frame
daily_death_nation_df = data.frame(date = daily_date_selected, value = nation_death_selected_daily)
###daily confirmed cases in US
daily_confirmed_nation_df %>%
 ggplot(aes(x=date, y=value)) +
 geom_bar(stat = 'identity', color="white", fill="#ff8540", width = 1) +
 ylab("Daily confirmed cases in US")+
 xlab("Date")+
 theme(text = element_text(size = 20),
    legend title = element text(size = 15),
    legend.text = element_text(size = 15),
    legend.key.width=unit(1,"cm"),
    axis.text.y = element text(angle=90, hjust=1))
###daily death in US
daily_death_nation_df %>%
 ggplot(aes(x=date, y=value)) +
 geom_bar(stat = 'identity', color="white", fill="#0000FF", width = 1) +
 ylab("Daily Death cases in US")+
 xlab("Date")+
 theme(text = element text(size = 20),
    legend.title = element_text(size = 15),
    legend.text = element_text(size = 15),
    legend.key.width=unit(1,"cm"),
    axis.text.y = element text(angle=90, hjust=1))
##let's obtain a seven-day average of the smoothed version of the confirmed cases and deaths
nation confirmed selected daily avg = data seven day smoothing(nation confirmed selected daily)
daily_confirmed_nation_smoothed_df = data.frame(date = daily_date_selected, value = nation_confirmed_selected_daily_avg)
nation_death_selected_daily_avg = data_seven_day_smoothing(nation_death_selected_daily)
daily_death_nation_smoothed_df = data.frame(date = daily_date_selected, value = nation_death_selected_daily_avg)
##plot the smoothed version
###daily confirmed cases in US
daily_confirmed_nation_smoothed_df %>%
```

```
ggplot(aes(x=date, y=value)) +
 geom_bar(stat = 'identity', color="white", fill="#ff8540", width = 1) +
 ylab("7-day averaged daily confirmed cases in US")+
 xlab("Date")+
 theme(text = element text(size = 20),
    legend.title = element_text(size = 15),
    legend.text = element_text(size = 15),
    legend.key.width=unit(1,"cm"),
    axis text y = element text(angle=90, hjust=1))
###daily death in US
daily_death_nation_smoothed_df %>%
 ggplot(aes(x=date, y=value)) +
 geom_bar(stat = 'identity', color="white", fill="#0000FF", width = 1) +
 ylab("7-day averaged daily death cases in US")+
 xlab("Date")+
 theme(text = element text(size = 20),
    legend.title = element_text(size = 15),
    legend.text = element_text(size = 15),
    legend.key.width=unit(1,"cm"),
    axis.text.y = element text(angle=90, hjust=1))
##get the test positive rates
##########this is state-level positive rate
###deal with positive rate
nation_test = covid_19_project %>%
 dplyr::select(date, state,totalTestResultsIncrease, positiveIncrease)
nation_test_aggregated = nation_test %>%
 group_by(date) %>%
 summarise_each(funs(sum), positiveIncrease, totalTestResultsIncrease)
nation_test_aggregated$positiveIncrease_7_day_avg = data_seven_day_smoothing(nation_test_aggregated$positiveIncrease)
nation test aggregated$totalTestResultsIncrease 7 day avg =
data seven day smoothing(nation test aggregated$totalTestResultsIncrease)
nation_test_aggregated$positive_rate = nation_test_aggregated$positiveIncrease_7_day_avg /
nation test aggregated$totalTestResultsIncrease 7 day avg
# ##reverse the sequence because it start from the current date
# nation daily test selected=rev(us test PositiveRateus test PositiveRate[nation test aggregated$date>=(start date) &
nation_test_aggregated$date<=end_date])
###let's smooth it and get the seven day average
us test daily test smoothed = data seven day smoothing(nation test aggregated$totalTestResultsIncrease)
us_test_daily_positive_smoothed = data_seven_day_smoothing(nation_test_aggregated$positiveIncrease)
##note that the following sequences start from the latest day
us_test_PositiveRate_smoothed = us_test_daily_positive_smoothed / us_test_daily_test_smoothed
us_test_PositiveRate_smoothed_selected=us_test_PositiveRate_smoothed[nation_test_aggregated$date>=(start_date) &
nation_test_aggregated$date<=end_date]
###plot the smoothed positive rates
plot(date_selected, us_test_PositiveRate_smoothed_selected,type="I",xlab='date',ylab='7-day avg daily positive rate')
```

```
(Changing the "end date" for each graph)
end date = as.Date("2020-10-30")
###Let's see whether we can make a map for CA about the confirmed cases over county popultation
### at a particular date
# set the date for map the end date you selected before
date_for_map = end_date
##cleaning
us_confirm_death_clean = clean_JHU_data_for_map(us_confirm, us_death)
us confirm clean = us confirm death clean[[1]]
us_death_clean = us_confirm_death_clean[[2]]
# calculate the daily confirmed cases for all US counties
us daily confirm clean = us confirm clean
us_daily_confirm_clean[,12] = NA
us_daily_confirm_clean[,13:dim(us_confirm_clean)[2]] = t(apply(us_confirm_clean[12:dim(us_confirm_clean)[2]], 1, diff))
##vou can make the confirmed cases to be zero if it is smaller than zero
#us_daily_confirm_clean[(us_daily_confirm_clean)<0] = 0
# calculate the daily death toll for all US counties
us_daily_death_clean = us_death_clean
us_daily_death_clean[,13] = NA
us daily death clean[,14:dim(us death clean)[2]] = t(apply(us death clean[13:dim(us death clean)[2]], 1, diff))
##you can make the daily death cases to be zero if it is smaller than zero
#us_daily_death_clean[us_daily_death_clean<0] = 0
# select the daily confirm cases for CA counties
state daily confirm = us daily confirm clean%>%
 filter(Province_State == state_name)
# This shape file contains the coordinates for county boundaries
state shape data = counties %>%
 filter(state_name == state_name)
# get the population for CA counties
state_population = us_daily_death_clean %>%
 filter(Province_State == state_name)%>%
 dplyr::select(Population)
state_population = as.numeric(state_population$Population)
# extract the daily confirmed cases on the selected date date for map
state_daily_confirm_selected = state_daily_confirm[, c(1:11, 11+ which(all_dates == date_for_map))]
# the Ratio = daily confirmed cases / population
state_daily_confirm_rate_selected = state_daily_confirm_selected
state_daily_confirm_rate_selected[,12] = state_daily_confirm_selected[,12]/state_population
state_daily_confirm_rate_selected[,12][state_daily_confirm_rate_selected[,12]==0]=NA
colnames(state_daily_confirm_rate_selected)[12] = "Ratio"
##This is the county and rate
state_daily_confirm_rate_selected[,c(11,12)]
# joint the daily confirmed cases with the shape file
state_daily_confirm_rate_selected_joint <- left_join(state_daily_confirm_rate_selected, state_shape_data, by = "county_fips")
# find the lower and upper limits of the ratio
range(state_daily_confirm_rate_selected$Ratio*100, na.rm = T)
state_daily_confirm_rate_selected_joint %>%
 ggplot(aes(long, lat, group = group, fill = Ratio*100)) +
 scale_fill_gradient(low = "yellow", high = "red", na.value = "grey90")+
 geom_polygon(col = "black") +
 coord_map(projection = "albers", lat0 = 10, lat1 = 45) +
 labs(fill = expression("Ratio (%)")) +
```

```
ggtitle(paste0("Daily confirmed cases / population in ", state_name, ", ", date_for_map))+
 xlab("lon") +ylab("lat")
##close it
#limits
###Let's look at 7-day daily average versus county population
# calculate the 7-day averaged daily confirm cases
state daily confirm avg = state daily confirm
state_daily_confirm_avg[, 13:dim(state_daily_confirm)[2]] = t(apply(state_daily_confirm[,13:dim(state_daily_confirm)[2]], 1,
data_seven_day_smoothing))
# extract the averaged daily confirmed cases on the selected date
state_daily_confirm_avg_selected = state_daily_confirm_avg[, c(1:11, 11+ which(all_dates == date_for_map))]
# the Ratio = averaged daily confirmed cases / population
state_daily_confirm_rate_avg_selected = state_daily_confirm_avg_selected
state_daily_confirm_rate_avg_selected[, 12] = state_daily_confirm_avg_selected[, 12]/state_population
state_daily_confirm_rate_avg_selected[,12][state_daily_confirm_rate_avg_selected[,12]==0]=NA
colnames(state_daily_confirm_rate_avg_selected)[12] = "Ratio"
## county and rate
state daily confirm rate avg selected[,c(11,12)]
index_largest=which(state_daily_confirm_rate_avg_selected[,c(12)]==max(state_daily_confirm_rate_avg_selected[,c(12)],na.rm=
state daily confirm rate avg selected[index largest,c(11,12)]
# joint the averaged daily confirmed cases with the shape file
state_daily_confirm_rate_avg_selected_joint <- left_join(state_daily_confirm_rate_avg_selected, state_shape_data, by =
"county_fips")
# find the lower and upper limits of the ratio
range(state_daily_confirm_rate_avg_selected$Ratio*100, na.rm = T)
state_daily_confirm_rate_avg_selected_joint %>%
 ggplot(aes(long, lat, group = group, fill = Ratio*100)) +
 scale fill gradient(low = "yellow", high = "red", na.value = "grey90")+
 geom_polygon(col = "black") +
 coord_map(projection = "albers", lat0 = 10, lat1 = 45) +
 labs(fill = expression("Ratio (%)")) +
 ggtitle(paste0("7-day averaged daily confirmed cases / population in ", state name, ", ", date for map))+
 xlab("lon") +ylab("lat")
##close it
```

#2a

```
start_date_Mi = as.Date("2020-7-1")
end_date_Mi = as.Date("2020-11-1")

date_selected=seq.Date(start_date_Mi, end_date_Mi, by=1)

Mi_confirmed = us_confirm %>%
filter(Province_State == "Michigan") %>%
select(starts_with("x"))

Mi_confirmed_sum = apply(Mi_confirmed, 2, sum)

Mi_confirmed_selected = Mi_confirmed_sum[which(all_dates %in% seq.Date(start_date_Mi, end_date_Mi, by=1))]

Mi_confirmed_selected=as.numeric(Mi_confirmed_selected)

Mi_confirmed_selected_daily=Mi_confirmed_selected[2:length(Mi_confirmed_selected)]-Mi_confirmed_selected[1:(length(Mi_confirmed_selected)])

daily_date_selected=date_selected[2:length(date_selected)]
```

```
daily_date_selected=date_selected[2:length(date_selected)]
# 7-day average of daily cases
Mi confirmed selected daily avg = data seven day smoothing(Mi confirmed selected daily)
daily_confirmed_Mi_avg_df = data.frame(date = daily_date_selected, value = Mi_confirmed_selected_daily_avg)
# Michigan, 7-day avg confirmed cases
daily confirmed Mi avg df %>%
 ggplot(aes(x=date, y=value)) +
 geom_bar(stat = 'identity', color="white", fill="#ff8540", width = 1) +
 ylab("7-day Averaged Daily Confirmed Cases in Michigan")+
 xlab("Date")+
 theme(text = element_text(size = 20),
    legend.title = element text(size = 15),
    legend.text = element_text(size = 15),
    legend.key.width=unit(1,"cm"),
    axis.text.y = element_text(angle=90, hjust=1))
Mi_test = covid_19_project %>%
 dplyr::select(date, state, totalTestResultsIncrease, positiveIncrease) %>%
 filter(state == "MI")
Mi_test_aggregated = Mi_test %>%
 group_by(date) %>%
 summarise_each(funs(sum), positiveIncrease, totalTestResultsIncrease)
Mi_test_aggregated$positiveIncrease_7_day_avg = data_seven_day_smoothing(Mi_test_aggregated$positiveIncrease)
Mi test aggregated$totalTestResultsIncrease_7_day_avg =
data_seven_day_smoothing(Mi_test_aggregated$totalTestResultsIncrease)
Mi_test_aggregated$positive_rate = Mi_test_aggregated$positiveIncrease_7_day_avg /
Mi test aggregated$totalTestResultsIncrease 7 day avg
###let's smooth it and get the seven day average
Mi_test_daily_test_smoothed = data_seven_day_smoothing(Mi_test_aggregated$totalTestResultsIncrease)
Mi test daily positive smoothed = data seven day smoothing(Mi test aggregated$positiveIncrease)
##note that the following sequences start from the latest day
Mi test PositiveRate smoothed = Mi test daily positive smoothed / Mi test daily test smoothed
Mi_test_PositiveRate_smoothed_selected=Mi_test_PositiveRate_smoothed[Mi_test_aggregated$date>=(start_date_Mi) &
Mi_test_aggregated$date<=end_date_Mi]
###plot the smoothed positive rates
plot(date_selected, Mi_test_PositiveRate_smoothed_selected,type="l',xlab='date',ylab='7-day averaged daily positive rate for MI')
#2bc
###Let's see whether we can make a map for CA about the confirmed cases over county population
### at a particular date
# set the date for map the end date you selected before
date_for_map = end_date
us confirm death clean = clean JHU data for map(us confirm, us death)
us confirm_clean = us_confirm_death_clean[[1]]
us death clean = us confirm death clean[[2]]
# calculate the daily confirmed cases for all US counties
```

us_daily_confirm_clean = us_confirm_clean

```
us daily confirm clean[,12] = NA
us_daily_confirm_clean[,13:dim(us_confirm_clean)[2]] = t(apply(us_confirm_clean[12:dim(us_confirm_clean)[2]], 1, diff))
##you can make the confirmed cases to be zero if it is smaller than zero
#us_daily_confirm_clean[(us_daily_confirm_clean)<0] = 0
# calculate the daily death toll for all US counties
us daily death clean = us death clean
us daily death clean[.13] = NA
us_daily_death_clean[,14:dim(us_death_clean)[2]] = t(apply(us_death_clean[13:dim(us_death_clean)[2]], 1, diff))
##you can make the daily death cases to be zero if it is smaller than zero
#us daily death clean[us daily death clean<0] = 0
# select the daily confirm cases for CA counties
state_daily_confirm = us_daily_confirm_clean%>%
 filter(Province State == state name)
# This shape file contains the coordinates for county boundaries
state shape data = counties %>%
 filter(state name == state name)
# get the population for CA counties
state_population = us_daily_death_clean %>%
 filter(Province State == state name)%>%
 dplyr::select(Population)
state population = as.numeric(state population$Population)
# extract the daily confirmed cases on the selected date date_for_map
state_daily_confirm_selected = state_daily_confirm[, c(1:11, 11+ which(all_dates == date_for_map))]
# the Ratio = daily confirmed cases / population
state_daily_confirm_rate_selected = state_daily_confirm_selected
state_daily_confirm_rate_selected[,12] = state_daily_confirm_selected[,12]/state_population
state_daily_confirm_rate_selected[,12][state_daily_confirm_rate_selected[,12]==0]=NA
colnames(state_daily_confirm_rate_selected)[12] = "Ratio"
##This is the county and rate
state_daily_confirm_rate_selected[,c(11,12)]
# joint the daily confirmed cases with the shape file
state daily confirm rate selected joint <- left join(state daily confirm rate selected, state shape data, by = "county fips")
# find the lower and upper limits of the ratio
range(state_daily_confirm_rate_selected$Ratio*100, na.rm = T)
state_daily_confirm_rate_selected_joint %>%
 ggplot(aes(long, lat, group = group, fill = Ratio*100)) +
 scale fill gradient(low = "yellow", high = "red", na.value = "grey90")+
 geom_polygon(col = "black") +
 coord_map(projection = "albers", lat0 = 10, lat1 = 45) +
 labs(fill = expression("Ratio (%)")) +
 ggtitle(paste0("Daily confirmed cases / population in ", state_name, ", ", date_for_map))+
 xlab("lon") +ylab("lat")
##close it
#limits
###Let's look at 7-day daily average versus county population
# calculate the 7-day averaged daily confirm cases
state daily confirm avg = state daily confirm
state_daily_confirm_avg[, 13:dim(state_daily_confirm)[2]] = t(apply(state_daily_confirm[,13:dim(state_daily_confirm)[2]], 1,
data_seven_day_smoothing))
# extract the averaged daily confirmed cases on the selected date
state_daily_confirm_avg_selected = state_daily_confirm_avg[, c(1:11, 11+ which(all_dates == date_for_map))]
# the Ratio = averaged daily confirmed cases / population
state_daily_confirm_rate_avg_selected = state_daily_confirm_avg_selected
```

```
state_daily_confirm_rate_avg_selected[, 12] = state_daily_confirm_avg_selected[, 12]/state_population
state daily confirm rate avg selected[,12][state daily confirm rate avg selected[,12]==0]=NA
colnames(state_daily_confirm_rate_avg_selected)[12] = "Ratio"
## county and rate
state_daily_confirm_rate_avg_selected[,c(11,12)]
index_largest=which(state_daily_confirm_rate_avg_selected[,c(12)]==max(state_daily_confirm_rate_avg_selected[,c(12)],na.rm=
state_daily_confirm_rate_avg_selected[index_largest,c(11,12)]
# joint the averaged daily confirmed cases with the shape file
state_daily_confirm_rate_avg_selected_joint <- left_join(state_daily_confirm_rate_avg_selected, state_shape_data, by =
"county_fips")
# find the lower and upper limits of the ratio
range(state_daily_confirm_rate_avg_selected$Ratio*100, na.rm = T)
state_daily_confirm_rate_avg_selected_joint %>%
 ggplot(aes(long, lat, group = group, fill = Ratio*100)) +
 scale_fill_gradient(low = "yellow", high = "red", na.value = "grey90")+
 geom_polygon(col = "black") +
 coord map(projection = "albers", lat0 = 10, lat1 = 45) +
 labs(fill = expression("Ratio (%)")) +
 ggtitle(paste0("7-day averaged daily confirmed cases / population in ", state_name, ", ", date_for_map))+
 xlab("lon") +ylab("lat")
##close it
##FL level analysis
##FL level daily confirmed cases, plot and
FL death = us death %>%
 filter(Province_State == "Florida") %>%
 select(starts with("x"))
###observed confirmed cases
FL confirmed = us confirm %>%
 filter(Province State == "Florida") %>%
 select(starts_with("x"))
###the first row of the state death data set and you can see the format
FL_death[1,]
###get the cumulative death toll and confirmed cases
FL_death_sum = apply(FL_death[,12:dim(FL_death)[2]], 2, sum)
FL_confirmed_sum = apply(FL_confirmed[,12:dim(FL_confirmed)[2]], 2, sum)
##get dates you want to analyze
start date = as.Date("2020-7-01")
end_date = as.Date("2020-11-01")
##the deaths and confirmed cases for the state on the selected dates
FL_death_selected = FL_death_sum[1 + which(all_dates %in% seq.Date(start_date, end_date, by=1))]
FL confirmed selected = FL confirmed sum[which(all dates %in% seq.Date(start date, end date, by=1))]
FL death selected=as.numeric(FL death selected)
FL_confirmed_selected=as.numeric(FL_confirmed_selected)
##plot cumulative confirmed cases and death
```

```
date_selected=seq.Date(start_date, end_date, by=1)
par(mfrow=c(1,2))
plot(date_selected,FL_confirmed_selected,xlab='date',ylab='cumulative observed confirmed cases',type='l')
plot(date_selected,FL_death_selected,xlab='date',ylab='cumulative death toll',type='l')
##close it
```

#3b (refer to #2bc- change state to 'Florida')

#4a (refer to #3a- change state to 'California')

#4c (refer to #2bc- change state to 'California' and the end_date)

#4d

date_seq = seq.Date(start_date, end_date, by=1)

 $plot(N-param_record_approx_for_beta[1,] \sim date_seq, type="l", col="blue", xlab = "Date", ylab = "Infective Cases", main = paste0(county_names[each_index], ", population=", round(N/10^6,2),"M", ", Ratio = ", round(ratio_real,3))) lines(confirm_selected \sim date_seq, type="l", col="red") legend("topleft", legend = c("Estimated Confirmed Cases", "Observed Confirmed Cases"), lty = c(1,1), col = c("red", "blue"))$

#4e

#4gh

(part g: gamma new is 1/4.75 for 5% reduction, part h: 1/4.5 for 10% reduction)

```
###work on some simulation if the infectious period decreases
gamma_new = 1/ 4.75 ###suppose it changes from 5 day to 4.75 days

param_record_approx_for_beta_new = matrix(0, 5, n) # 5 rows: S_t, I_t, R_t, D_t, C_t
param_record_approx_for_beta_new[,1] = init_for_beta
param_record_approx_for_beta_new[1,] = S_t_seq

# record the value of transmission rate
# approx_beta_seq_new = rep(0, n-1)
# we should fix the beta when we change the gamma parameter

# iterative approach for calculating the seq of compartments in SIRDC

for (i in 1:(n-1)){
    S_t_1 = param_record_approx_for_beta_new[1,i]
    I_t_1 = param_record_approx_for_beta_new[2,i]
    R_t_1 = param_record_approx_for_beta_new[3,i]
```

```
D_t_1 = param_record_approx_for_beta_new[4,i]
    C_t_1 = param_record_approx_for_beta_new[5,i]
   beta_t_1_2 = approx_beta_seq[i]
   if(I_t_1<1<1)
     l_{\underline{t}} = 1
    S_t_2 = uniroot(find_root_S_t_2, c(0, N), tol = 0.0001, param = c(S_t_1, beta_t_1_2, l_t_1), N = N, gamma=gamma_new)
    \begin{array}{l} I = I = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 + S t 2*root)/(2*N) - gamma_new) \\ R = I - 1 * exp(beta t 1 2*(S t 1 2*(S
   D_t^2 = D_t^1 + delta*theta*(R_t^1+R_t^2)/2
   C_t_2 = C_t_1 + (1-delta)*theta*(R_t_1+R_t_2)/2
  param_record_approx_for_beta_new[, i+1] = c(S_t_2)root, I_t_2, R_t_2, D_t_2, C_t_2)
 # calculate the smoothed transmission rate using 7 day average
# approx_beta_seq_smoothed_new = rollapply(approx_beta_seq_new, width = 7, by = 1, FUN = mean, align = "left")
###plot the simulated death
 plot(param_record_approx_for_beta_new[4,]~date_seq,ylim = ylimit_death, type="l", col="blue", xlab = "Date", ylab = "Death
 Cases", main = paste0(county_names[each_index], ", population=", round(N/10^6,2),"M", ", Ratio = ", round(ratio_real,3)))
 lines(death_selected~date_seq, col = "red")
 legend("topleft", legend = c("Observed death toll", "Simulated death toll"), lty = c(1,1), col = c("red", "blue"))
```