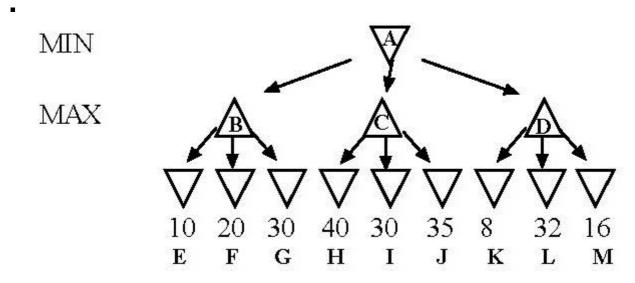
• 練習 minimax with alpha-beta pruning (AIMA Sec. 5.3) 考慮以下 game tree

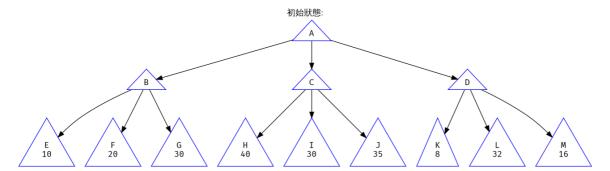


- 注意:這一棵 game tree 和 AIMA 圖5.2雖然類似・但是有不少差異
- 提示:注意 AIMA Sec. 5.3.1 所講的 move ordering 問題
- 假設我們在執行 AIMA 圖 5.7 演算法中 for each a in Action(state) do 的時候,都是從上面 game tree 左邊的節點開始、逐次往右搜尋的話,則上述哪一些 subtree 可以被忽略?說明原因。
- 假設我們在執行 AIMA 圖 5.7 演算法中 for each a in Action(state) do 的時候,都是從上面 game tree 右邊的節點開始、逐次往左搜尋的話,則上述哪一些 subtree 可以被忽略?說明原因

第一小題,從左邊節點往右

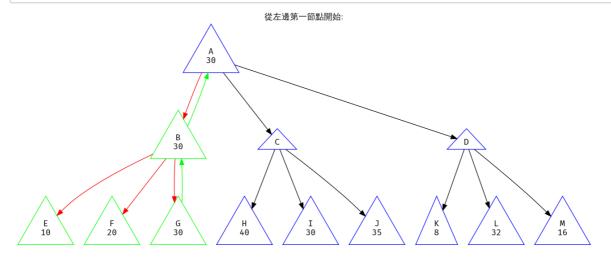
In [48]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "初始狀態:"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A", color=blue]
    B[shape=triangle, label="B", color=blue]
    C[shape=triangle, label="C", color=blue]
    D[shape=triangle, label="D", color=blue]
    A -> B
    A->C
    A->D
    E[shape=triangle, label="E\n10", color=blue]
    F[shape=triangle, label="F\n20", color=blue]
G[shape=triangle, label="G\n30", color=blue]
    H[shape=triangle, label="H\n40", color=blue]
    I[shape=triangle, label="I\n30", color=blue]
    J[shape=triangle, label="J\n35", color=blue]
    K[shape=triangle, label="K\n8", color=blue]
    L[shape=triangle, label="L\n32", color=blue]
    M[shape=triangle, label="M\n16", color=blue]
    B->E
    B->F
    B->G
    C->H
    C->I
    C->J
    D->K
    D->L
    D->M
}
```



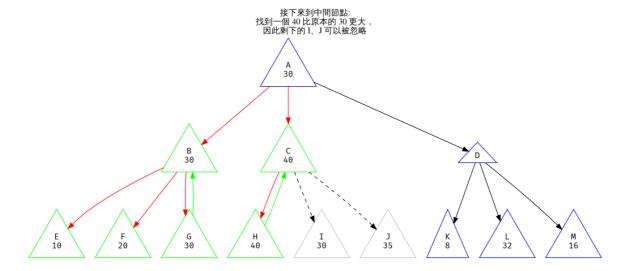
In [56]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "從左邊第一節點開始:"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n30", color=blue]
    B[shape=triangle, label="B\n30", color=green]
    C[shape=triangle, label="C", color=blue]
    D[shape=triangle, label="D", color=blue]
    A->B[color=red]
    B->A[color=green]
    A->C
    A->D
    E[shape=triangle, label="E\n10", color=green]
    F[shape=triangle, label="F\n20", color=green]
    G[shape=triangle, label="G\n30", color=green]
    H[shape=triangle, label="H\n40", color=blue]
    I[shape=triangle, label="I\n30", color=blue]
J[shape=triangle, label="J\n35", color=blue]
    K[shape=triangle, label="K\n8", color=blue]
    L[shape=triangle, label="L\n32", color=blue]
    M[shape=triangle, label="M\n16", color=blue]
    B->E[color=red]
    B->F[color=red]
    B->G[color=red]
    G->B[color=green]
    C->H
    C->I
    C->J
    D->K
    D->L
    D->M
}
```



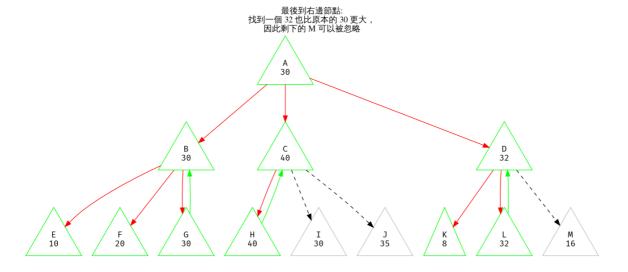
In [70]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "接下來到中間節點:\n找到一個 40 比原本的 30 更大,\n因此剩下的 I、J 可以被忽略"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n30", color=blue]
    B[shape=triangle, label="B\n30", color=green]
    C[shape=triangle, label="C\n40", color=green]
    D[shape=triangle, label="D", color=blue]
    A->B[color=red]
    A->C[color=red]
    A->D
    E[shape=triangle, label="E\n10", color=green]
    F[shape=triangle, label="F\n20", color=green]
G[shape=triangle, label="G\n30", color=green]
    H[shape=triangle, label="H\n40", color=green]
    I[shape=triangle, label="I\n30", color=gray]
    J[shape=triangle, label="J\n35", color=gray]
    K[shape=triangle, label="K\n8", color=blue]
    L[shape=triangle, label="L\n32", color=blue]
    M[shape=triangle, label="M\n16", color=blue]
    B->E[color=red]
    B->F[color=red]
    B->G[color=red]
    G->B[color=green]
    C->H[color=red]
    H->C[color=green]
    C->I[style=dashed]
    C->J[style=dashed]
    D->K
    D->L
    D->M
}
```



In [71]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "最後到右邊節點:\n找到一個 32 也比原本的 30 更大,\n因此剩下的 M 可以被忽略"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n30", color=green]
    B[shape=triangle, label="B\n30", color=green]
    C[shape=triangle, label="C\n40", color=green]
    D[shape=triangle, label="D\n32", color=green]
    A->B[color=red]
    A->C[color=red]
    A->D[color=red]
    E[shape=triangle, label="E\n10", color=green]
    F[shape=triangle, label="F\n20", color=green]
G[shape=triangle, label="G\n30", color=green]
    H[shape=triangle, label="H\n40", color=green]
    I[shape=triangle, label="I\n30", color=gray]
    J[shape=triangle, label="J\n35", color=gray]
    K[shape=triangle, label="K\n8", color=green]
    L[shape=triangle, label="L\n32", color=green]
    M[shape=triangle, label="M\n16", color=gray]
    B->E[color=red]
    B->F[color=red]
    B->G[color=red]
    G->B[color=green]
    C->H[color=red]
    H->C[color=green]
    C->I[style=dashed]
    C->J[style=dashed]
    D->K[color=red]
    D->L[color=red]
    L->D[color=green]
    D->M[style=dashed]
}
```

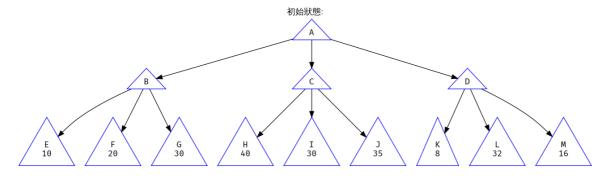


得出若從左邊開始,會找到 B,值為 30 的結果

第二小題,從右至左

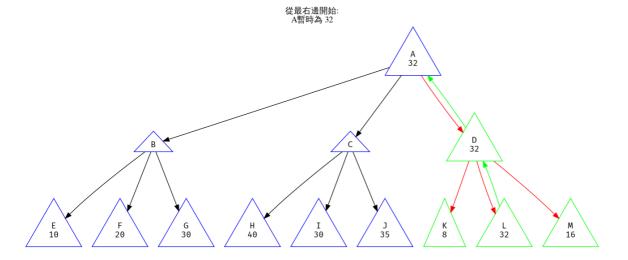
In [53]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "初始狀態:"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A", color=blue]
    B[shape=triangle, label="B", color=blue]
    C[shape=triangle, label="C", color=blue]
    D[shape=triangle, label="D", color=blue]
    A->B
    A->C
    A->D
    E[shape=triangle, label="E\n10", color=blue]
    F[shape=triangle, label="F\n20", color=blue]
    G[shape=triangle, label="G\n30", color=blue]
    H[shape=triangle, label="H\n40", color=blue] I[shape=triangle, label="I\n30", color=blue]
    J[shape=triangle, label="J\n35", color=blue]
    K[shape=triangle, label="K\n8", color=blue]
    L[shape=triangle, label="L\n32", color=blue]
    M[shape=triangle, label="M\n16", color=blue]
    B->E
    B->F
    B->G
    C->H
    C->I
    C->J
    D->K
    D->L
    D->M
}
```



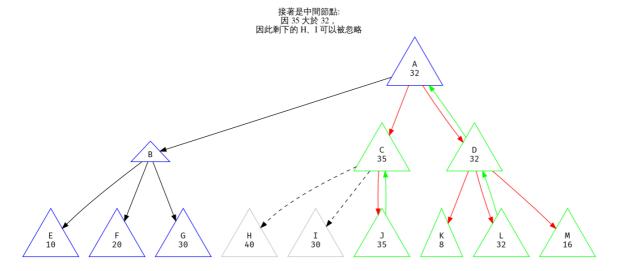
In [61]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "從最右邊開始:\nA暫時為 32"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n32", color=blue]
    B[shape=triangle, label="B", color=blue]
    C[shape=triangle, label="C", color=blue]
    D[shape=triangle, label="D\n32", color=green]
    A -> B
    A->C
    A->D[color=red]
    D->A[color=green]
    E[shape=triangle, label="E\n10", color=blue]
F[shape=triangle, label="F\n20", color=blue]
    G[shape=triangle, label="G\n30", color=blue]
    H[shape=triangle, label="H\n40", color=blue]
    I[shape=triangle, label="I\n30", color=blue]
J[shape=triangle, label="J\n35", color=blue]
    K[shape=triangle, label="K\n8", color=green]
    L[shape=triangle, label="L\n32", color=green]
    M[shape=triangle, label="M\n16", color=green]
    B->E
    B->F
    B->G
    C->H
    C->I
    C->J
    D->K[color=red]
    D->L[color=red]
    L->D[color=green]
    D->M[color=red]
}
```



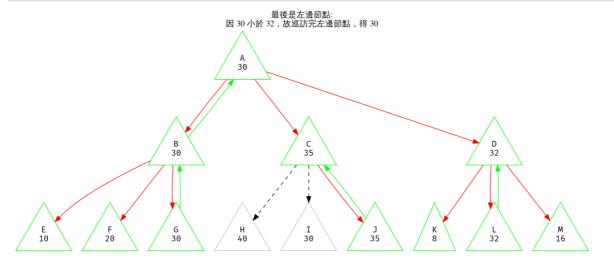
In [72]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "接著是中間節點:\n因 35 大於 32, \n因此剩下的 H、I 可以被忽略"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n32", color=blue]
    B[shape=triangle, label="B", color=blue]
    C[shape=triangle, label="C\n35", color=green]
    D[shape=triangle, label="D\n32", color=green]
    A -> B
    A->C[color=red]
    A->D[color=red]
    D->A[color=green]
    E[shape=triangle, label="E\n10", color=blue]
    F[shape=triangle, label="F\n20", color=blue]
    G[shape=triangle, label="G\n30", color=blue]
    H[shape=triangle, label="H\n40", color=gray]
    I[shape=triangle, label="I\n30", color=gray]
J[shape=triangle, label="J\n35", color=green]
    K[shape=triangle, label="K\n8", color=green]
    L[shape=triangle, label="L\n32", color=green]
    M[shape=triangle, label="M\n16", color=green]
    B->E
    B->F
    B->G
    C->H[style=dashed]
    C->I[style=dashed]
    C->J[color=red]
    J->C[color=green]
    D->K[color=red]
    D->L[color=red]
    L->D[color=green]
    D->M[color=red]
}
```



In [67]:

```
digraph {
    labelloc = "t"
    labelfontname = "文泉驛微米黑"
    label = "最後是左邊節點:\n因 30 小於 32·故巡訪完左邊節點·得 30"
    node [fontname="Fira Mono"]
    A[shape=triangle, label="A\n30", color=green]
    B[shape=triangle, label="B\n30", color=green]
    C[shape=triangle, label="C\n35", color=green]
    D[shape=triangle, label="D\n32", color=green]
    A->B[color=red]
    B->A[color=green]
    A->C[color=red]
    A->D[color=red]
    E[shape=triangle, label="E\n10", color=green]
    F[shape=triangle, label="F\n20", color=green]
    G[shape=triangle, label="G\n30", color=green]
   H[shape=triangle, label="H\n40", color=gray]
    I[shape=triangle, label="I\n30", color=gray]
    J[shape=triangle, label="J\n35", color=green]
    K[shape=triangle, label="K\n8", color=green]
    L[shape=triangle, label="L\n32", color=green]
    M[shape=triangle, label="M\n16", color=green]
    B->E[color=red]
    B->F[color=red]
    B->G[color=red]
    G->B[color=green]
    C->H[style=dashed]
    C->I[style=dashed]
    C->J[color=red]
    J->C[color=green]
    D->K[color=red]
    D->L[color=red]
    L->D[color=green]
    D->M[color=red]
}
```



• 模仿上課時以真值表證明 $P\Rightarrow Q\equiv \neg Q\Rightarrow \neg P$ 的方式 (在白板上寫的證明),證明以下關係

$$P \Rightarrow Q \equiv \neg P \lor Q$$

依下列 truth table 之推導,可得

$$P\Rightarrow Q\equiv \neg P\vee Q$$

$$P \quad Q \quad \neg P \quad P \quad \neg P \\ \Rightarrow Q \quad \lor Q$$

$$T \quad T \quad F \quad T \quad T$$

$$T \quad F \quad F \quad F \quad F$$

- 模仿 simple.proof.pdf 證明 $P_{2,2}$ 不成立 $(P_{2,2}=False)$ 的程序,利用以下的 logic sentences,證明 $W_{2,2}$ 也不成立。
 - 参考 Al.logical.agents.pdf 第18頁上的說明·或者 AlMA Sec. 7.4.3 (p. 247) 的內容·我們使用 W 和 S 的符號

1. R1:
$$W_{1,3} \Rightarrow S_{1,2} \wedge S_{2,3} \wedge S_{1,4}$$

2. R2:
$$S_{1,2} \Rightarrow W_{1,1} ee W_{2,2} ee W_{1,3}$$

3. R3:
$$W_{2,2} \Rightarrow S_{1,2} \wedge S_{3,2} \wedge S_{2,1} \wedge S_{2,3}$$

4. R4:
$$S_{2.1} \Rightarrow W_{1.1} \lor W_{2.2} \lor W_{3.1}$$

5. F1:
$$\neg S_{1,1}$$

6. F2:
$$S_{1,2}$$

7. F3:
$$\neg S_{2,1}$$

8. F4:
$$\neg W_{1,1}$$

1. 先用 implication elimination 推導 3:

• R5:
$$W_{2,2} \Rightarrow S_{1,2} \wedge S_{3,2} \wedge S_{2,1} \wedge S_{2,3} \equiv \neg W_{2,2} ee (S_{1,2} \wedge S_{3,2} \wedge S_{2,1} \wedge S_{2,3})$$

- 2. 再以 F3,推導出:
 - R6: $S_{1,2} \wedge S_{3,2} \wedge S_{2,1} \wedge S_{2,3}$ 為 false 當給定 $\neg S_{2,1}$ 為 true
- 3. 而當 $S_{1,2} \wedge S_{3,2} \wedge S_{2,1} \wedge S_{2,3}$ 為 false · 且上述 R5 為 true 成立時 · 只有一個情況:
 - R7: ¬W_{2.2} 為 true
- 4. 故得證:
 - R8: $W_{2,2}$ 為 false