

# Do End-to-end Stereo Algorithms Under-utilize Information?

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## Abstract

*Deep networks for stereo matching typically leverage 2D or 3D convolutional encoder-decoder architectures to aggregate cost and regularize the cost volume for accurate disparity estimation. Due to content-insensitive convolutions and down-sampling and up-sampling operations, these cost aggregation mechanisms do not take full advantage of the information available in the images. Disparity maps suffer from over-smoothing near occlusion boundaries, and erroneous predictions in thin structures. In this paper, we show how deep adaptive filtering and differentiable semi-global aggregation can be integrated in existing 2D and 3D convolutional networks for end-to-end stereo matching, leading to improved accuracy. The improvements are due to utilizing RGB information from the images as a signal to dynamically guide the matching process, in addition to being the signal we attempt to match across the images. We show extensive experimental results on the KITTI 2015 and Virtual KITTI 2 datasets comparing four stereo networks (DispNetC, GCNet, PSMNet and GANet) after integrating four adaptive filters (segmentation-aware bilateral filtering, dynamic filtering networks, pixel adaptive convolution and semi-global aggregation) into their architectures. Our code and models are available at <https://github.com/ccj5351/DAFStereoNets>.*

## 1. Introduction

Progress in learning based stereo matching has been rapid from early work that focused on aspects of the stereo matching pipeline [32], such as similarity computation [43], to recent end-to-end systems [7, 23, 29, 45]. What is remarkable is that the evolution of learning based stereo has largely mirrored that of conventional algorithms: initial end-to-end systems resembled winner-take-all stereo with the disparity of each pixel determined almost independently based on a small amount of local context, while GA-Net [45], arguably the most effective current algorithm, includes a differentiable form of the Semi-Global Matching (SGM) algorithm [20], which has been by far the most popular con-

vventional optimization technique for over a decade.

Despite their success, deep stereo networks seem to under-utilize information present in their inputs. Specifically, in this paper we demonstrate how many existing networks leverage RGB information from the images to extract features that facilitate matching, but leave additional information unexploited. We show that the accuracy of representative network architectures can be improved by integrating into them modules that are sensitive to pixel similarity, image edges or semantics and act like adaptive filters.

In our experiments, we have integrated four components that can be thought of as adaptive or guided filters into four existing networks for stereo matching. Specifically, we have experimented with segmentation-aware bilateral filtering (SABF) [17], dynamic filtering networks (DFN) [22], pixel adaptive convolution (PAC) [34] and semi-global aggregation (SGA) from GANet [45] integrated into DispNetC [29], GCNet [23], PSMNet [7], and GANet [45]. The set of filters is diverse: SABF, for example, is pre-trained to embed its input via a semantic segmentation loss, while SGA aggregates matching cost along rows and columns of cost volume slices. The backbone networks are also diverse, spanning 2D [29] and 3D [7, 23] convolutional networks and GANet that foregoes 3D convolutions in favor of the SGM-like aggregation mechanism. The number of parameters of the backbones ranges from 2.8 to 42.2 million.

The contributions of this paper are:

- Several novel deep architectures for stereo matching.
- Evidence that further progress in stereo matching is possible by leveraging image context as guidance for refinement, filtering and aggregation of the matching volume.
- A comparison of four filtering methods leading to the conclusion that SGA typically achieves the highest accuracy among them.

## 2. Related Work

We review deep learning based end-to-end stereo matching and content-guided or adaptive filtering in CNNs.

**End-to-end Stereo Matching.** End-to-end stereo matching methods can be generally grouped into two categories:

2D CNNs for correlation-based disparity estimation and 3D CNNs for cost volume based disparity regression.

A representative work in the first category is DispNetC [29]. It computes the correlations among features between stereo views at different disparity values, and regresses the disparity via an encoder-decoder 2D CNN architecture. Many other methods [26, 31, 33, 36, 41, 42, 44] extend this paradigm. CRL [31] employs a two-stage network for cascade disparity residual learning. Feature constancy is added in iResNet [26] to further refine the disparity. SegStereo [41], DSNet [44] and EdgeStereo [33] are multi-task learning approaches jointly optimizing stereo matching with semantic segmentation or edge detection.

State-of-the-art stereo networks [7, 16, 23, 45] largely fall in the second category. Different than the correlation based cost volume in 2D-CNN stereo networks, 3D-CNNs generate a 4D cost volume by concatenating the deep features from the Siamese branches along the channel dimension at each disparity level and each pixel position. GCNet [23] and PSMNet [7] apply 3D convolutional layers for cost aggregation, followed by a differentiable *soft-argmin* layer for disparity regression. GwcNet [16] leverages group-wise correlation of channel-split features to generate a hybrid cost volume that can be processed by a smaller 3D convolutional aggregation sub-network. GANet [45] includes local guided aggregation (LGA) and semi-global aggregation (SGA) layers for efficient cost aggregation which are complementary to 3D convolutional layers. LGA aggregates the cost volume locally to refine thin structures, while SGA is a differentiable counterpart of SGM [20].

**Content Guided and Adaptive Filtering in CNNs.** Existing content-adaptive CNNs fall into two general classes. In the first class, conventional image-adaptive filters (*e.g.* bilateral filters [1, 35], guided image filters [18] and non-local means [2, 4], among others) have been adapted to be differentiable and used as content-adaptive neural network layers [6, 8, 9, 14, 21, 24, 27, 28, 37, 38, 46]. Wu *et al.* [38] propose novel layers to perform guided filtering [18] inside CNNs. Wang *et al.* [37] present non-local neural networks to mimic non-local means [4] for capturing long-range dependencies. The bilateral inception module by Gadde *et al.* [14] can be inserted into existing CNN segmentation architectures for improved results. It performs bilateral filtering to propagate information between superpixels based on the spatial and color similarity. Harley *et al.* [17] integrate segmentation information in the CNN by firstly learning segmentation-aware embeddings, then generating local foreground attention masks, and combining the masking filters with convolutional filters to perform segmentation-aware convolution (see details in Sec. 3.2). Deformable convolutions [12, 47] produce spatially varying modifications to the convolutional filters, where the modifications are represented as offsets in favor of learning geometric-

invariant features. Pixel adaptive convolution (PAC) [34] mitigates the content-agnostic drawback of standard convolutions by multiplying the convolutional filter weights by a spatial kernel function. PAC has been applied in joint image upsampling networks [25] and in a learnable dense conditional random field (CRF) framework [9, 21, 24, 46]. See Sec. 3.2 for more details.

Another class of content-adaptive CNNs focuses on learning spatial position-aware filter weights using separate sub-networks. These approaches are called “Dynamic Filter Networks” (DFN) [22, 39, 40] or kernel prediction networks [3], which have been used in several computer vision tasks. Jia *et al.* [22] propose the first DFN where the convolutional filters are generated dynamically depending on input pixels. The filter weights, provided by a filter-generating network conditioned on an input, are applied to another input through the dynamic filtering layer (see details in Sec. 3.2). It is extended by Wu *et al.* [39] with an additional attention mechanism and a dynamic sampling strategy to allow the position-specific kernels to also learn from multiple neighboring regions.

### 3. Approach

In this section, we describe our approach for adapting state-of-the-art stereo matching networks [7, 23, 29, 45] by integrating deep filtering techniques to improve their accuracy. We show how four filtering techniques, segmentation-aware bilateral filtering (SABF) [17], dynamic filtering networks (DFN) [22], pixel adaptive convolution (PAC) [34] and semi-global aggregation (SGA) [45], can be used to filter the cost volume for accurate disparity estimation.

#### 3.1. Cost Volume in Stereo Matching

Given a rectified stereo pair  $\mathbf{I}_L$  and  $\mathbf{I}_R$  with dimensions  $H \times W$  ( $H$ : height,  $W$ : width), stereo matching finds the correspondence between a reference pixel  $\mathbf{p}_L$  in the left image  $\mathbf{I}_L$  and a target pixel  $\mathbf{p}_R$  in the right image  $\mathbf{I}_R$ . The cost volume (or matching volume)  $\mathcal{C}$  is defined as a 3D or 4D tensor with dimensions  $D \times H \times W$  or  $2F \times D \times H \times W$  ( $D$ : disparity range,  $F$ : feature dimensionality for each of the views), to represent the likelihood of a reference pixel  $\mathbf{p}_L(u, v)$  corresponding to a target pixel  $\mathbf{p}_R(u - d, v)$ , with disparity  $d \in [0, D]$ . Its construction is illustrated in Fig 1. Specifically, the extracted left feature vector  $\mathbf{f}_L(u, v) \in \mathbb{R}^F$  of the reference pixel  $\mathbf{p}_L(u, v)$  is either **correlated** (in 2D CNNs *e.g.* DispNetC [29] and iResNet [26]) or **concatenated** (in 3D CNNs *e.g.* GCNet [23], PSMNet [7] and GANet [45]) with the corresponding feature  $\mathbf{f}_R(u - d, v) \in \mathbb{R}^F$  of the target pixel  $\mathbf{p}_R(u - d, v)$ , for each disparity  $d \in \{0, \dots, D - 1\}$ . It is formulated in Eq. 1:

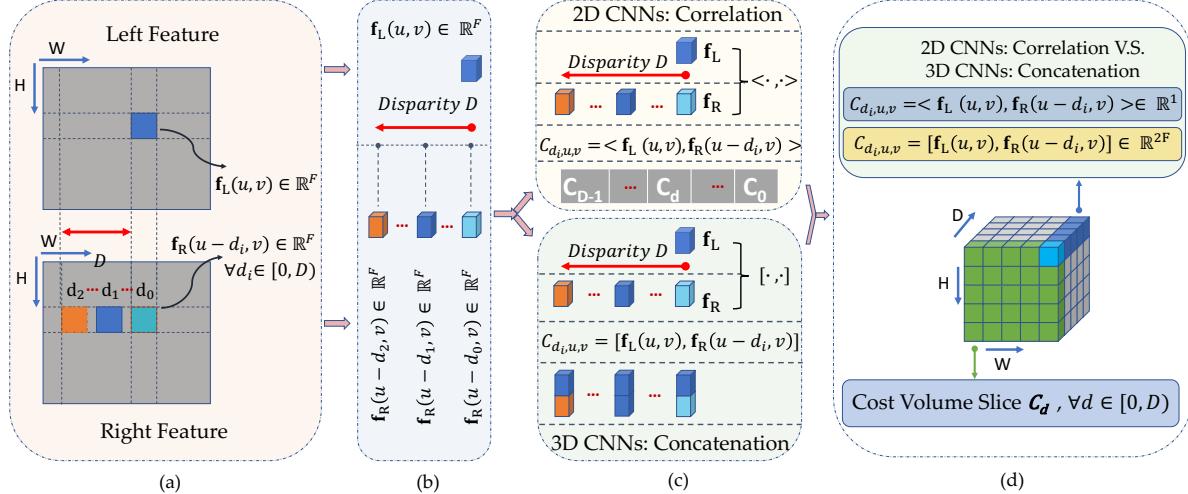


Figure 1: Cost volume in 2D and 3D CNNs for stereo matching. (a) Deep features are extracted for each view. (b) A left feature vector  $\mathbf{f}_L(u, v)$  and several counterparts  $\mathbf{f}_R(u - d_i, v)$ , at disparity  $d_i \in [0, D]$ . (c) The left feature vector is either correlated (top branch for 2D CNNs) or concatenated (bottom branch for 3D CNNs) with the corresponding right feature vectors. (d) The cost volume, including the highlighted cost volume slice  $\mathcal{C}_d$  (green), cost volume fiber  $\mathcal{C}_{u, v}$  (blue) and cost feature  $\mathcal{C}_{d, u, v}$  (light blue) that is a scalar for 2D CNNs or a vector for 3D CNNs.

$$\mathcal{C}_{d, u, v} = \begin{cases} \langle \mathbf{f}_L(u, v), \mathbf{f}_R(u - d, v) \rangle \in \mathbb{R}^1 & \text{2D CNNs} \\ [\mathbf{f}_L(u, v), \mathbf{f}_R(u - d, v)] \in \mathbb{R}^{2F} & \text{3D CNNs} \end{cases} \quad (1)$$

where  $\langle \cdot, \cdot \rangle$  denotes correlation,  $[\cdot, \cdot]$  indicates concatenation, resulting in a 3D or 4D tensor for 2D and 3D CNNs, respectively. We denote a **cost volume slice** at disparity  $d$  by  $\mathcal{C}_d$  (i.e.,  $\mathcal{C}_d = \mathcal{C}_{d, u, v}|_{u=1:W; v=1:H}$ ).

### 3.2. Content-Adaptive Filtering Modules

In this subsection, we present four content-adaptive filtering approaches which can be effectively incorporated as content-adaptive CNN layers in state-of-the-art networks for end-to-end stereo matching.

#### 3.2.1 Segmentation-aware Bilateral Filtering Module

Segmentation-aware bilateral filtering (SABF) [17] was proposed to enforce smoothness while preserving region boundaries or motion discontinuities in dense prediction tasks, such as semantic segmentation and optical flow estimation. As shown in Fig. 2, here we adapt the SABF to stereo matching to filter the cost volume  $\mathcal{C}$  (Sec. 3.1), by (i) learning to embed in a feature space where semantic dissimilarity between pixels can be measured by a distance function [10]; (ii) creating local foreground (relative to a given pixel) attention filters  $K^{sabf}$ ; (iii) filtering the cost volume  $\mathcal{C}$  so as to capture the relevant foreground and be robust to appearance variations in the background or occlusions.

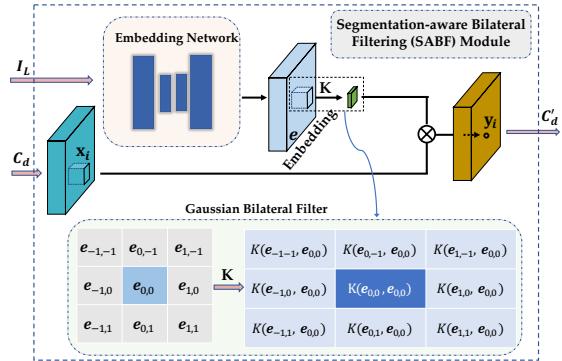


Figure 2: Integrating the segmentation-aware bilateral filtering (SABF) module. The upper branch shows the embedding  $e$  is learned by an *embedding network* from an input image  $I_L$ . Pairwise embedding distances are converted (Eq. 4) to SABF filter weights  $K$ , as shown at the bottom. The overall figure shows how SABF filters a cost volume slice  $\mathcal{C}_d$  to obtain a segmentation-aware filtered result  $\mathcal{C}'_d$ .

**Learning the Embedding.** Given an RGB image  $\mathbf{I}$ , consisting of  $N$  pixels  $\mathbf{q}$ , and its semantic segmentation label map  $\mathbf{l}$ , the embedding function is implemented as an *Embedding Network* that maps pixels into an embedding space as  $f : \mathbb{R}^3 \mapsto \mathbb{R}^{64}$ , or  $f(\mathbf{q}) = \mathbf{e}$ , where  $\mathbf{e} \in \mathbb{R}^{64}$  is the embedding for RGB pixel  $\mathbf{q}$ , with 64 as the dimension of the embedding space. See Fig. 2. The embeddings are learned via a loss function over pixel pairs sampled in a neighborhood around each pixel. Specifically, for any two pixels  $\mathbf{p}_i$

and  $\mathbf{p}_j$  and corresponding object class labels  $\mathbf{l}_i$  and  $\mathbf{l}_j$ , the pairwise loss is:

$$\ell_{i,j} = \begin{cases} \max(\|\mathbf{e}_i - \mathbf{e}_j\|_1 - \alpha, 0) & \text{if } \mathbf{l}_i = \mathbf{l}_j \\ \max(\beta - \|\mathbf{e}_i - \mathbf{e}_j\|_1, 0) & \text{if } \mathbf{l}_i \neq \mathbf{l}_j \end{cases} \quad (2)$$

where  $\|\cdot\|_1$  indicates the  $L_1$ -norm, and the thresholds are  $\alpha = 0.5$  and  $\beta = 2$ . Therefore, the total loss for all the pixels in the image  $\mathbf{I}$  is defined in Eq. 3:

$$\mathcal{L} = \sum_{i=0}^{N-1} \sum_{j \in \mathcal{N}_i} \ell_{i,j} \quad (3)$$

where  $j \in \mathcal{N}_i$  spans the spatial neighbors of index  $i$ . We follow the implementation of Harley *et al.* [17] where three overlapping  $3 \times 3$  neighborhoods with dilation rates of 1, 2, and 5 are used for a good trade-off between long-range pairwise connectivity and computational efficiency.

**Applying the SABF Layer.** Once the embedding is learned, the SABF filter weights are obtained by converting the pairwise distance between  $\mathbf{e}_i$  and  $\mathbf{e}_j$  into (unnormalized) probabilities using two Gaussian distributions as in Eq. 4:

$$K_{i,j}^{sabf} = \exp \left( -\frac{\|\mathbf{p}_i - \mathbf{p}_j\|^2}{2\sigma_s^2} - \frac{\|\mathbf{e}_i - \mathbf{e}_j\|^2}{2\sigma_r^2} \right) \quad (4)$$

where  $\sigma_s$  and  $\sigma_r$  are two predefined standard deviations. Then, given an input feature  $\mathbf{x}_i$ , we can efficiently compute a segmentation-aware filtered result  $\mathbf{y}_i$  via the SABF layer:

$$\mathbf{y}_i = \frac{\sum_{k \in \Omega(i)} \mathbf{x}_k K_{i,k}^{sabf}}{\sum_{k \in \Omega(i)} K_{i,k}^{sabf}} \quad (5)$$

where  $\Omega(\cdot)$  defines an  $s \times s$  (e.g.,  $5 \times 5$ ) filtering window. The input  $\mathbf{x}_i$  and output  $\mathbf{y}_i$  here are from a raw cost volume slice  $\mathcal{C}_d$  and the filtered slice  $\mathcal{C}'_d$ , respectively (Fig. 2).

### 3.2.2 Dynamic Filtering Networks (DFN) Module

Dynamic Filter Networks (DFN) [22] are a content-adaptive filtering technique. As shown in Fig. 4(b), the filters  $\mathcal{F}_\theta$  in the DFN are dynamically generated by a separate *filter-generating network* conditioned on an input  $\mathbf{x}_A$ . Then, they are applied to another input  $\mathbf{x}_B$  via the *dynamic filtering layer*. In our implementation,  $\mathbf{x}_A$  is the deep feature  $\mathbf{f}_L$  of the reference image  $\mathbf{I}_L$ , and  $\mathbf{x}_B$  is a cost volume slice  $\mathcal{C}_d$ .

**Filter-Generating Network.** Given an input  $\mathbf{x}_A \in \mathbb{R}^{H \times W \times C_A}$  ( $H$ : height,  $W$ : width,  $C_A$ : channel size of  $\mathbf{x}_A$ ), the filter-generating network generates dynamic filters  $\mathcal{F}_\theta$ , parameterized by  $\theta \in \mathbb{R}^{s \times s \times C_B \times n_F}$  ( $s$ : filter window size,  $C_B$ : channel size of  $\mathbf{x}_B$ ,  $n_F$ : the number of filters).

**Dynamic Local Filtering Layer.** The generated filters  $\mathcal{F}_\theta$  are applied to input images or feature maps  $\mathbf{x}_B \in \mathbb{R}^{H \times W \times C_B}$  via the *dynamic filtering layer* to output the filtered result  $G = \mathcal{F}_\theta(\mathbf{x}_B) \in \mathbb{R}^{H \times W}$ . Specifically, the dynamic filtering layer in the DFN [22] has two types of instances: *dynamic convolutional layer* (with  $n_F = 1$ ) and *dynamic local filtering layer* (with  $n_F = H \cdot W$ ). The latter is adopted in this paper because it guarantees content-adaptive filtering via applying a specific local filter  $\mathcal{F}_\theta^{(u,v)}$  to the neighborhood centered around each pixel coordinate  $(u, v)$  of the input  $\mathbf{x}_B$ :

$$G(u, v) = \mathcal{F}_\theta^{(u,v)}(\mathbf{x}_B(u, v)) \quad (6)$$

Therefore, the operations in Eq. 6 are not only input content specific but also spatial position specific.

### 3.2.3 Pixel Adaptive Convolutional (PAC) Module

Pixel adaptive convolution (PAC) proposed by Su *et al.* [34] is a new content-adaptive convolution, which can alleviate the drawback of standard convolution that ignores local image content, while retaining its favorable spatial sharing property compared with existing content-adaptive filters, *e.g.* the DFN [22]. As illustrated in Fig. 4(a), PAC modifies a conventional spatially invariant convolution filter  $\mathbf{W}$  at each position by multiplying it with a position-specific filter  $K^{pac}$ , the *adapting kernel*.  $K^{pac}$  has a pre-defined form, *e.g.* Gaussian:  $e^{-\frac{1}{2}\|\mathbf{f}_i - \mathbf{f}_j\|^2}$ , where  $\mathbf{f}_i$  and  $\mathbf{f}_j$  are the *adapting features*, corresponding to pixels  $\mathbf{p}_i$  and  $\mathbf{p}_j$ . The adapting features  $\mathbf{f}$  can be either hand-crafted (*e.g.* position and color features) or deep features. We use deep features extracted from the left image as the adapting features  $\mathbf{f}$ .

Given an input  $\mathbf{x}_i \in \mathbb{R}^{C_x}$  at pixel  $\mathbf{p}_i$ , the output  $\mathbf{y}_i \in \mathbb{R}^{C_y}$  filtered by PAC is defined as

$$\mathbf{y}_i = \sum_{j \in \Omega(i)} K^{pac}(\mathbf{f}_i, \mathbf{f}_j) \mathbf{W}[\mathbf{p}_i - \mathbf{p}_j] \mathbf{x}_i + \mathbf{b} \quad (7)$$

where  $C_x$  and  $C_y$  denote the feature dimension of  $\mathbf{x}_i$  and  $\mathbf{y}_i$ , respectively.  $\Omega(\cdot)$  defines an  $s \times s$  convolution window.  $\mathbf{W} \in \mathbb{R}^{C_y \times C_x \times s \times s}$  and  $\mathbf{b} \in \mathbb{R}^{C_y}$  indicate the convolution filter weights and biases. We adopt the notation  $[\mathbf{p}_i - \mathbf{p}_j]$  to spatially index filter weights  $\mathbf{W}$  with 2D spatial offsets. In our approach  $\mathbf{x}_i$  and  $\mathbf{y}_i$  are from the raw and filtered cost volume slices  $\mathcal{C}_d$  and  $\mathcal{C}'_d$ , respectively.

### 3.2.4 Semi-Global Aggregation Module

In contrast to the above filters that leverage local context, Semi-Global Aggregation (SGA) [45] is able to iteratively aggregate the cost volume considering both pixelwise costs and pairwise smoothness constraints in four directions. The constraints are originally defined and approximately solved

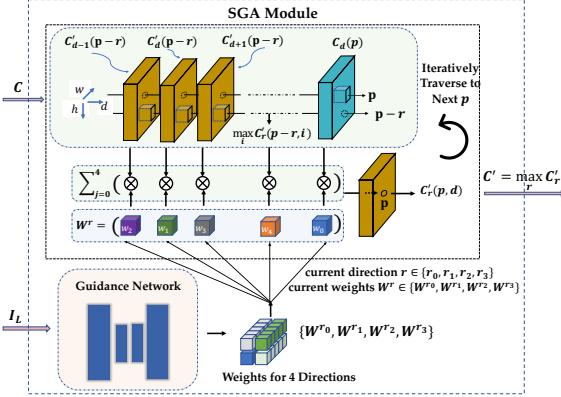


Figure 3: Integrating the SGA module. The bottom branch shows the guidance network which generates aggregation weights in four directions. The top branch illustrates SGA which iteratively aggregates the cost volume  $\mathcal{C}$  via traversing from pixel  $\mathbf{p} - \mathbf{r}$  to  $\mathbf{p}$  in a direction  $\mathbf{r}$ , over the entire image and each disparity  $d$ . The maximum response among the four directions is selected as the output  $\mathcal{C}'$ .

by Semi-Global Matching (SGM) [20] as an energy function of the disparity map. SGM learns to aggregate the cost volume  $\mathcal{C}$  to approximately minimize the energy, and also support backpropagation for end-to-end stereo matching as shown in Fig. 3. The aggregated cost volume  $\mathcal{C}'$  is recursively defined as:

$$\mathcal{C}'_{\mathbf{r}}(\mathbf{p}, d) = \text{sum} \begin{cases} \mathbf{w}_0(\mathbf{p}, \mathbf{r}) \cdot \mathcal{C}(\mathbf{p}, d) \\ \mathbf{w}_1(\mathbf{p}, \mathbf{r}) \cdot \mathcal{C}'_{\mathbf{r}}(\mathbf{p} - \mathbf{r}, d) \\ \mathbf{w}_2(\mathbf{p}, \mathbf{r}) \cdot \mathcal{C}'_{\mathbf{r}}(\mathbf{p} - \mathbf{r}, d - 1) \\ \mathbf{w}_3(\mathbf{p}, \mathbf{r}) \cdot \mathcal{C}'_{\mathbf{r}}(\mathbf{p} - \mathbf{r}, d + 1) \\ \mathbf{w}_4(\mathbf{p}, \mathbf{r}) \cdot \max_i \mathcal{C}'_{\mathbf{r}}(\mathbf{p} - \mathbf{r}, i) \end{cases} \quad (8)$$

where  $\mathbf{r}$  is a unit direction vector along which the cost  $\mathcal{C}'_{\mathbf{r}}(\mathbf{p}, d)$  of pixel  $\mathbf{p}$  at disparity  $d$  is aggregated. The weights  $\mathbf{w}_j$  are achieved and normalized (s.t.  $\sum_{j=0}^4 \mathbf{w}_j(\mathbf{p}, \mathbf{r}) = 1$ ) by a guidance sub-network to avoid very large accumulated values when traversing along the path. The final aggregated cost  $\mathcal{C}'_{\mathbf{r}}(\mathbf{p}, d)$  is obtained by picking the maximum among four directions, namely, left, right, up and down, i.e.,  $\mathbf{r} \in \{(-1, 0), (1, 0), (0, 1), (0, -1)\}$ , defined as:

$$\mathcal{C}'(\mathbf{p}, d) = \max_{\mathbf{r}} \mathcal{C}'_{\mathbf{r}}(\mathbf{p}, d) \quad (9)$$

### 3.3. Network Architecture

As illustrated in Fig. 4, our architecture takes as backbones four state-of-the-art 2D and 3D CNNs for stereo matching, i.e., DispNetC [29], GCNet [23], PSMNet [7] and GANet [45], and adapts SABF (Fig. 2), PAC (Fig.

4(a)), DFN (Fig. 4(b)) and SGA (Fig. 3), to aggregate the cost volume.

#### 3.3.1 Network Backbones

Given a rectified stereo pair, the backbone architectures described below include unary feature extraction from the images by a weight-sharing Siamese structure, cost volume computation and regularization, and disparity regression. Unary features are denoted by  $\mathbf{f}_u$ . 2D or 3D convolutional and transpose convolutional layers have  $3 \times 3$  or  $3 \times 3 \times 3$  kernels, unless otherwise specified.

**DispNetC Backbone.** DispNetC [29] is an encoder-decoder architecture with an explicit 1D correlation layer. The encoder downsamples the input images via convolution (stride = 2) by up to 1/64, while the decoder gradually upsamples the feature maps via transposed convolution (stride = 2) at 6 different scales ranging from 1/64 to 1/2. The input images are processed by a Siamese network (layers of conv1 and conv2) to generate  $\mathbf{f}_u$  ( $H/4 \times W/4 \times F$ ,  $F = 128$ ). Features  $\mathbf{f}_u$  are correlated by a 1D correlation layer [13] to form a 3D cost volume  $\mathcal{C}(D/4 \times H/4 \times W/4)$  with a maximum disparity of  $D/4$ . The volume is further contracted to 1/64 (layer conv6 and loss6) resolution and expanded by alternate transpose convolutions (upconv $N$ ), convolutions (iconv $N$ , pr $N$ ) and loss layers (loss $N$ ), where  $N = 5, 4, \dots, 1$ . There are six intermediate disparity maps which are all interpolated to the input resolution. The loss during training is computed on all six disparity maps, but only the last one is used as output.

**GCNet Backbone.** GCNet [23] is a 3D CNN architecture that explicitly reasons about geometry in stereo matching. We add a bilinear interpolation layer<sup>1</sup> to downsample the input stereo pair to half resolution. The images are then fed into a  $5 \times 5$  convolution layer and eight residual blocks [19] to extract  $\mathbf{f}_u$  ( $F \times H/4 \times W/4$ ,  $F = 32$ ). GCNet builds a 4D cost volume ( $D/4 \times 2F \times H/4 \times W/4$ ) by concatenating  $\mathbf{f}_u$  with its counterpart from the other view across each disparity level. The volume is downsampled by up to 1/16 via four encoding blocks (each has three convolutions with strides respectively 2, 1, 1) and upsampled by 32 via five decoding blocks (each has a skip-connection from the early layer and one transposed convolution with stride 2), resulting in an aggregated ( $D/2 \times H/2 \times W/2$ ) volume. It is interpolated to input resolution and regressed to predict the disparity map via the differentiable *soft argmin*:

$$\hat{\mathcal{D}} = \sum_{d=0}^{D-1} d \cdot \sigma(-\mathcal{C}_d) \quad (10)$$

where cost  $\mathcal{C}_d$  is first converted to a probability of each disparity value  $d$  via the *softmax* operation  $\sigma(\cdot)$ . The disparity

<sup>1</sup>It requires no parameters and helps reduce the computational burden.

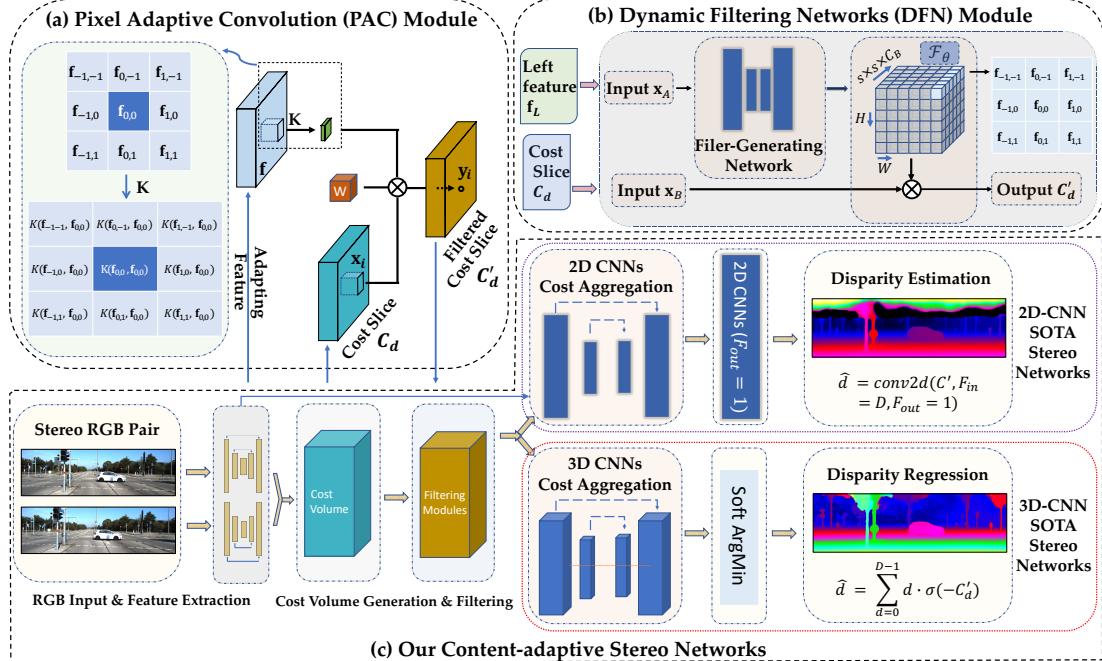


Figure 4: (a) PAC filters the cost volume slice  $C_d$  by multiplying it with a standard spatially invariant convolutional filter  $\mathbf{W}$  and a spatially varying filter  $K$  that depends on input pixel features  $\mathbf{f}$ . The output is the filtered slice  $C'_d$ . (b) DFN filters  $\mathcal{F}_\theta$  are dynamically generated by the *filter-generating network* conditioned on left pixel features  $\mathbf{f}_L$ .  $C_d$  is filtered by  $\mathcal{F}_\theta$  to output  $C'_d$ . (c) Overview of network architecture: a stereo pair is fed into a weight-sharing Siamese sub-network for feature learning; the extracted features of each view are correlated or concatenated to generate the cost volume  $\mathcal{C}$ ; content-adaptive filtering modules are applied to  $\mathcal{C}$  and output the filtered volume  $\mathcal{C}'_d$ , followed by state-of-the-art encoder-decoder cost aggregation and disparity regression, as shown in two branches for 2D and 3D convolutional architectures.

map  $\hat{\mathcal{D}}$  comprises the *expected* values of  $d$  for each pixel.

**PSMNet Backbone.** PSMNet [7] learns  $\mathbf{f}_u$  ( $F \times H/4 \times W/4$ ,  $F = 128$ ) via three convolution layers followed by four basic residual blocks [19]. To incorporate hierarchical global context, each  $\mathbf{f}_u$  is processed separately by spatial pyramid pooling (SPP) by a four-level average pooling block (with bin size equal to  $b \times b$ , where  $b = 64, 32, 16$ , and  $8$ ), followed by a  $1 \times 1$  convolution, bilinear interpolation and feature concatenation. This generates the SPP unary features ( $F \times H/4 \times W/4$ ,  $F = 32$ ), which are used to construct a 4D ( $D/4 \times 2F \times H/4 \times W/4$ ) cost volume. The volume is regularized by a stacked-hourglass architecture, built of three encoding-decoding blocks, each with four convolution layers (with strides 2, 1, 2 and 1), and two transposed convolution layers to restore the input resolution. Each hourglass generates a regularized volume, from which an intermediate disparity is obtained via the *soft argmin* (E.q. 10). The training loss is computed on all three intermediate disparities.

**GANet Backbone.** GANet [45] introduces local guided aggregation (LGA) and semi-global aggregation (SGA) layers which are complementary to 3D convolutional layers. The unary features  $\mathbf{f}_u$  ( $F \times H/3 \times W/3$ ,  $F = 32$ ) are extracted through a stacked hourglass CNN with skip con-

nnections. They are then used to construct a 4D cost volume ( $D/3 \times 2F \times H/3 \times W/3$ ), which is fed into a cost aggregation block (built of alternate 3D convolution and transpose convolution layers, SGA and LGA) for regularization, refinement and disparity regression via the *soft argmin* (E.q. 10). The guidance sub-network generates the weight matrices for SGA (Sec. 3.2) and LGA. The LGA layer is used before disparity regression and locally refines the 4D cost volume for several times. We adopt the GANet-deep version since it achieves the best accuracy among all variants (<https://github.com/feihuzhang/GANet>).

### 3.3.2 Network Capacity

Network capacities are listed in Table 1. The parameters of the four backbone networks (i.e., row W/O in gray, meaning no filters applied) increase in the order of GCNet < PSMNet < GANet < DispNetC. The order of the filtering modules (rows in skyblue) according to increasing number of parameters is PAC < DFN < SABF < SGA.

### 3.3.3 Loss Function

The loss is evaluated over the valid pixels which have ground truth disparity. We adopt the smooth  $L_1$  loss func-

Filters	Network Backbones							
	DispNetC		PSMNet		GANet		GCNet	
	No.	$\uparrow(\%)$	No.	$\uparrow(\%)$	No.	$\uparrow(\%)$	No.	$\uparrow(\%)$
W/O	42.2	-	5.2	-	6.6	-	2.8	-
SABF	44.0	4.2	7.0	34	<b>8.4</b>	<b>27</b>	4.6	62.4
DFN	42.6	0.8	5.6	6.4	6.9	5.1	3.2	11.8
PAC	42.3	0.1	5.3	2.0	6.7	1.6	2.9	3.6
SGA	<b>45.2</b>	<b>7.0</b>	<b>8.3</b>	<b>58.8</b>	-	-	<b>5.9</b>	<b>108</b>

Table 1: Network capacity. For each combination of the filtering techniques and network backbones, columns *No.* show the number of parameters in millions, and columns  $\uparrow(\%)$  are the relative increase in the number of parameter w.r.t. the backbone baselines. Largest values are in bold. Inapplicable entries are marked by “-”.

tion for end-to-end training:

$$L(d, \hat{d}) = \frac{1}{N} \sum_{i=1}^N l_s(||d_i - \hat{d}_i||_1)$$

and,  $l_s(x) = \begin{cases} 0.5x^2 & \text{if } |x| < 1 \\ |x| - 0.5 & \text{otherwise} \end{cases}$  (11)

where  $N$  counts the valid pixels,  $||d_i - \hat{d}_i||_1$  measures the absolute error of disparity prediction  $\hat{d}_i$  and ground truth  $d_i$ .

The GCNet backbone has one disparity output, while the other backbones produce multiple intermediate disparities on which the total loss is computed by weighted summation. Their loss weights are defined as 0.2, 0.6 and 1.0 for GANet and 0.5, 0.7 and 1.0 for PSMNet. DispNetC training starts on Scene Flow with weights of 0.05, 0.10, 0.14, 0.19, 0.24 and 0.29 for the six disparity estimates. In finetuning, only the final disparity is activated. When integrating SABF filters to the backbones, an embedding loss in Eq. 3 is added to the total loss with a weight of 0.06.

## 4. Experiments

### 4.1. Datasets

Our networks are trained from scratch on Scene Flow [29], then finetuned on Virtual KITTI 2 (VKT2) [5, 15] or KITTI 2015 (KT15) [30]. **Scene Flow** is a large scale synthetic dataset containing 35,454 training and 4,370 testing images with dense ground truth disparity maps. We exclude the pixels with disparities  $d > 192$  in training. **Virtual KITTI 2 (VKT2)** is a synthetic clone of the real KITTI dataset. It contains 5 sequence *clones* of Scene 01, 02, 06, 18 and 20, and nine variants with diverse weather conditions (e.g. fog, rain) or modified camera configurations (e.g. rotated by  $15^\circ$ ,  $30^\circ$ ). Since there is no designated validation set, we select (i) Scene06 (i.e., *VKT2-Val-S6* with 2,700 frames) and (ii) multiple blocks of consecutive frames from

Scene 01, 02, 18, 20 (i.e., *VKT2-Val-WoS6* with 2,620 frames), and use the remaining 15,940 images for training. The former scene remains unseen during training, while networks observe similar frames to the latter. We evaluate these settings separately. **KITTI 2015 (KT15)**: is a real dataset of street views. It contains 200 training stereo image pairs with sparsely labeled disparity from LiDAR data. We divided the training data into a training set (170 images) and a validation set (30 images) for our experiments.

**Metrics.** For KT15, we adopt the *bad-3* error (i.e., percentage of pixels with disparity error  $> 3\text{px}$  or  $\geq 5\%$  of the true disparity) counted over non-occluded (noc) or all pixels with ground truth. For VKT2, in addition to *bad-3*, we also use the endpoint error (EPE) and *bad-1* error ( $\geq 1\text{px}$  or  $\geq 5\%$ ) over all pixels.

### 4.2. Implementation Details

**Architecture details.** Our models are implemented with PyTorch. Each convolution layer is followed by batch normalization (BN) and ReLU unless otherwise specified. We use the official code of PSMNet and GANet, and implement DispNetC (no PyTorch version) and GCNet (no official code). Our implementations achieve similar or better results on the KT15 benchmark, i.e., bad-3 errors 4.48% (all) and 3.85% (noc) versus the authors’ 4.34% (all) and 4.05% (noc) for DispNetC, and 2.38% (all) and 2.07% (noc) versus the authors’ 2.87% (all) and 2.61% (noc) for GCNet. We use  $\sigma_s = 0.7$  and  $\sigma_r = 0.1$  in Eq. 4 for SABF. We investigate how the filter window  $s$  and dilation rate  $r$  affect the filtering output, and find that  $s = 5$  with  $r = 2$  achieve a good balance in accuracy, space requirements and runtime. Please see the supplementary material for ablation studies.

**Training details.** The SABF embedding network is pre-trained on Cityscapes [11]. For data augmentation we randomly crop  $256 \times 512$  image patches and do channel-wise standardization by subtracting the mean and dividing by the standard deviation. For fair comparison, we follow the baselines and set the maximum disparity to  $D = 192$ . We use the official pre-trained models on Scene Flow for GANet and PSMNet, and train DispNetC and GCNet on Scene Flow from scratch for 10 epochs with a learning rate (lr) of 0.001. Training is optimized with Adam ( $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ ), except for GCNet which uses RMSprop ( $\alpha = 0.9$ ). For KT15, our models and baselines are finetuned for 600 epochs (with lr= 0.001 for the first 300 epochs and lr= 0.0001 for the next 300 epochs). For VKT2, we finetune all algorithms for 20 epochs, with lr = 0.001 at first, then divided by 10 at epoch 5 and epoch 18.

### 4.3. Quantitative Results

All results are on the *validation sets* since we could not submit all combinations to the benchmarks. Due to page

Filters	DispNetC			PSMNet			GANet			GCNet		
	EPE(px)	$\geq 1$ px	$\geq 3$ px	EPE(px)	$\geq 1$ px	$\geq 3$ px	EPE(px)	$\geq 1$ px	$\geq 3$ px	EPE(px)	$\geq 1$ px	$\geq 3$ px
<i>Seen locations (i.e., Scene01, 02, 18 and 20) from VKT2 validation set <b>VKT2-Val-WoS6</b></i>												
W/O	0.68	11.54	3.72	0.45	7.08	2.21	<b>0.33</b>	<b>5.34</b>	<b>1.70</b>	0.62	9.71	3.18
SABF	0.65	10.86	3.48	<b>0.36</b>	<b>5.92</b>	<b>1.98</b>	0.34	5.50	1.76	0.60	9.89	3.19
DFN	<b>0.57</b>	9.85	3.26	0.42	6.45	2.17	0.37	6.23	1.99	0.60	9.20	3.11
PAC	0.58	9.92	3.39	0.52	7.81	2.61	0.40	7.01	2.20	0.75	12.98	4.02
SGA	<b>0.57</b>	<b>9.37</b>	<b>3.21</b>	0.40	6.08	2.14	-	-	-	<b>0.55</b>	<b>9.24</b>	<b>2.98</b>
<i>Totally unseen location (i.e., Scene06) from VKT2 validation set <b>VKT2-Val-S6</b></i>												
W/O	0.70	10.28	3.12	0.48	5.16	1.96	0.30	<b>3.09</b>	1.0563	0.59	7.48	2.25
SABF	0.69	9.75	3.00	0.44	4.47	1.73	<b>0.28</b>	3.16	<b>0.97</b>	0.56	7.51	2.23
DFN	<b>0.599</b>	8.54	<b>2.791</b>	<b>0.39</b>	4.83	<b>1.69</b>	0.29	3.54	1.0561	0.55	6.81	<b>2.14</b>
PAC	0.603	8.73	2.96	0.52	5.78	1.98	0.35	4.36	1.47	0.73	11.87	2.99
SGA	0.607	<b>8.02</b>	2.794	0.42	<b>4.34</b>	1.71	-	-	-	<b>0.53</b>	<b>7.45</b>	2.29

Table 2: Evaluation on VKT2 validation sets of VKT2-Val-WoS6 and VKT2-Val-S6. Results are shown in the entries of filters (rows in skyblue) and backbones (columns) w.r.t. the baselines (row W/O). Our improved results are highlighted in gray, and the best ones are in bold. GANet already contains SGA, resulting in blank entries “-”.

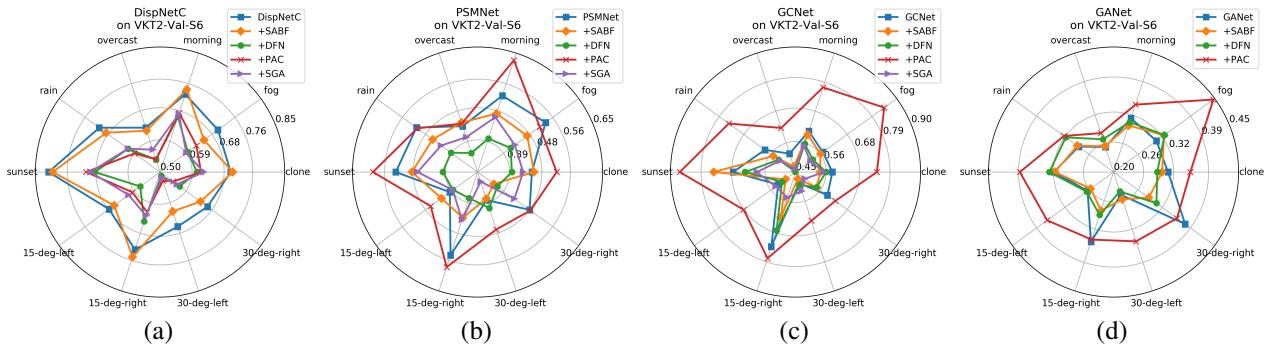


Figure 5: Results of (a) DispNetC, (b) PSMNet, (c) GCNet and (d) GANet on each category of validation set **VKT2-Val-S6**.

limits, qualitative results are available in the supplementary material.

**Virtual KITTI 2 Evaluation.** We finetune our models (the pre-trained backbones on Scene Flow after integrating the filters) on the VKT2 dataset. (*EPE*, *bad-1* and *bad-3*) on the **VKT2-Val-WoS6** and **VKT2-Val-S6** validation sets are listed in Table 2. In most cases, our models (rows in skyblue) achieve higher accuracy than the baselines (row W/O). The exception is standard GANet which performs well since it always includes SGA and LGA for global and local matching volume aggregation. Fig. 5 plots EPE errors on *individual* categories of **VKT2-Val-S6**. SABF, DFN and SGA boost 2D and 3D CNNs, while PAC improves 2D CNNs, but not 3D CNNs. When moving from familiar (**VKT2-Val-WoS6**) to unseen (**VKT2-Val-S6**) validation scenes, DFN achieves better adaptation than SGA, and the SABF and DFN variants outperform standard GANet.

**KITTI 2015 Evaluation.** The results on KT15 are shown in Table 3. Our networks obtain improved accuracy for all the backbones except for GANet. All the filters boost the backbones due to leveraging image context as guidance, and SGA achieves the highest accuracy among them.

## 5. Conclusions

We demonstrate how deep adaptive or guided filtering can be integrated into representative 2D and 3D CNNs for stereo matching with improved accuracy. Our extensive experimental results on Virtual KITTI 2 and KITTI 2015 highlight how our filtering modules effectively leverage the RGB information to dynamically guide the matching, resulting in further progress in stereo matching. SGA, a component of GANet, is the most effective filtering mechanism and improves all backbones. More broadly, our work shows

Filters	DispNetC		PSMNet		GANet		GCNet	
	noc	all	noc	all	noc	all	noc	all
W/O	2.59	3.02	1.46	1.60	<b>0.97</b>	<b>1.10</b>	2.06	2.64
SABF	2.26	2.63	1.28	1.40	1.07	1.17	1.76	2.10
DFN	2.37	2.78	1.23	1.34	0.99	1.11	1.70	2.08
PAC	2.38	2.72	1.29	1.48	1.13	1.23	1.71	2.03
SGA	<b>1.90</b>	<b>2.18</b>	<b>1.17</b>	<b>1.32</b>	-	-	<b>1.69</b>	<b>1.91</b>

Table 3: KITTI 2015 bad-3 validation results. Improved results are highlighted in gray, and best ones are in bold. GANet contains SGA, resulting in blank entries “-”.

that current state-of-the-art methods do not take full advantage of available information, with the exception of GANet which shows superior performance due to SGA and LGA, but has more parameters than GCNet and PSMNet. Integrating even the smaller filtering modules leads to decreases in error in the order of 10%.

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