

Example 33: According to the above identity, different interpretations can be made for different graphics, so the following conclusions can be obtained.

As shown in the figure, the tangent lines AP and AQ of O pass through point A, and the tangent lines CM and CN of O pass through point C. AP and CM intersect at point B, and AQ and CN intersect at point D. Then the following identities hold:

$$\frac{AO^2}{DA \cdot AB} = \frac{CO^2}{BC \cdot CD}, \quad \frac{BO^2}{AB \cdot BC} = \frac{DO^2}{CD \cdot DA},$$

$$\frac{AO^2}{DA \cdot AB} - \frac{BO^2}{AB \cdot BC} = 1, \quad \frac{BO^2}{AB \cdot BC} - \frac{CO^2}{BC \cdot CD} = -1,$$

$$\frac{CO^2}{BC \cdot CD} - \frac{DO^2}{CD \cdot DA} = 1, \quad \frac{DO^2}{CD \cdot DA} - \frac{AO^2}{DA \cdot AB} = -1.$$