



Example 182 : As shown in Figure 1 , let M be a point inside $\triangle ABC$ Δ , the inscribed circle of ABC and side BC , the tangent points of CA, AB are D, E, F respectively , the Δ inscribed circle of MBC and sides BC, CM , the tangent points of MB are D, H, G , and prove that the four points E, F, G , and H share a circle.

$$\left(\frac{F-E}{G-H} \right)^2 \frac{B-A}{C-A} \frac{B-M}{C-M} \frac{F-G}{G-F} \frac{H-E}{E-H} = 1,$$

Explanation: This question looks complicated, but you only need to convert $AF = AE$, $MG = MH$, $BF = BD = BG$, $CD = CE = CH$, and these line segment relationships into angle representations.