

Example 1 94: As shown in Figure 1, it is known that $AB \perp CD$, AB intersects CD at P, and M is the midpoint of BC. Prove: The necessary and sufficient condition for $PM \perp AD$ is that A, C, B, and D share a circle.

Proof:
$$\frac{P-M}{D-A} = \frac{\frac{P-M}{P-C}}{\frac{C-D}{C-B}} \frac{C-D}{\frac{A-D}{A-B}} \frac{C-P}{A-B},$$