

Example 1 64: As shown in Figure 1, the known point I is $\triangle ABC$ the center of , and the extension line of AI intersects with DBC, $IG \perp BC$, G which is the vertical foot. Prove: $\angle BID = \angle CIG$.

$$-\left(\frac{I-G}{B-C}\right)^{2} \frac{\frac{I-D}{A-B}}{\frac{A-C}{I-D}} \frac{\frac{B-A}{B-I}}{\frac{B-I}{C-I}} \frac{C-B}{C-I} = \left(\frac{\frac{I-D}{I-B}}{\frac{I-C}{I-G}}\right)^{2},$$

Proof: $\angle CIG = 90^{\circ} - \frac{1}{2} \angle ACB = \frac{1}{2} (180^{\circ} - \angle ACB) = \frac{1}{2} (\angle CAB + \angle ABC) = \angle BID$.