

Example 89: As shown in Figure 3, circle A intersects circle B at two points P and I, and $PA \perp PB$, D is a point on circle A, D and E are symmetrical about A, DI intersects circle B at F, and EI intersects circle B at G, if G is on FB, then $FG \perp DE$.

$$\frac{F-G}{E-D} = \frac{G-I}{I-D} \frac{F-G}{B-G} \left(\frac{I-B}{G-I} / \frac{G-I}{G-B} \right) \frac{I-G}{E-I} \frac{A-D}{E-D} \left(\frac{I-A}{I-B} \frac{I-E}{I-D} \right) \left(\frac{D-I}{D-A} / \frac{I-A}{D-I} \right).$$