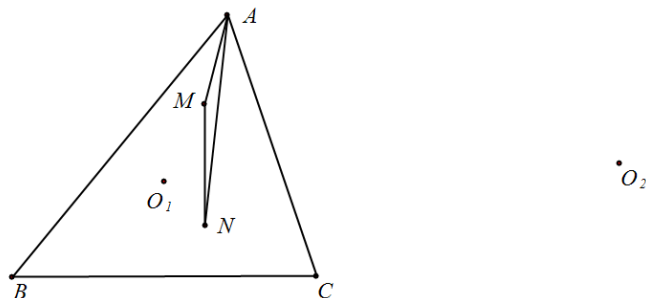


figure 1

Example 99 : As shown in Figure 1 , in the acute angle $\triangle ABC$, $AB > AC$, M, N are two different points on the side of BC , so that $\angle BAM = \angle CAN$. Let the circumcenters of $\triangle ABC$ and $\triangle AMN$ be O_1, O_2 respectively , to prove: O_1, O_2, A three points are collinear. (Additional test questions for the 2012 National High School Mathematics League)

$$\frac{A - O_1}{A - O_2} = \frac{A - C}{A - B} \left(\frac{C - B}{C - A} \frac{A - O_1}{A - B} \right) / \left(\frac{N - M}{N - A} \frac{A - O_2}{A - M} \right) \frac{M - N}{B - C},$$



As shown in Figure 2 , in the acute angle $\triangle ABC$, $AB > AC$, M, N are two points inside $\triangle ABC$, so that $\angle BAM = \angle CAN$ and $MN \perp BC$. Let the circumcenters of $\triangle ABC$ and $\triangle AMN$ be O_1, O_2 respectively , Prove: $AO_1 \perp AO_2$.

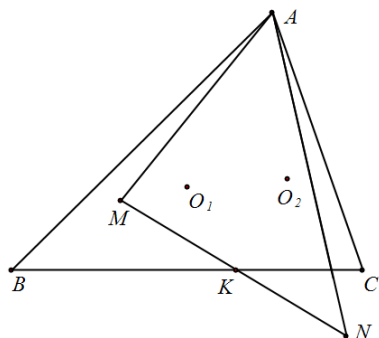


Figure 3