



Example 35 : As shown in Figure 1 , the known point M is the midpoint of the hypotenuse AB of $Rt \triangle ABC$, extend BC to point D , make $2 CD = AB$, connect MD , intersect the bisector of $\angle B$ at point E , and verify: $BE = ED$.

Proof: Suppose $C = 0$,

$$\left(\frac{\frac{B-0}{D-\frac{A+B}{2}}}{D-0} \right)^2 = 2 \frac{\frac{B-0}{B-E} \frac{\frac{A+B}{2}-D} {D-\frac{A+B}{2}} \frac{D}{A+B}}{\frac{B-A}{D-0} \frac{2}{B}}$$

[Certificate] Even MC , then $MC = MB$, so $\angle MCB = \angle MBC = 2 \angle EBD$.
 And $MC = CD$, so $\angle MCB = \angle CMD + \angle D = 2 \angle D$;
 So $\angle EBD = \angle D$, $BE = ED$. _