



**Example 1 92 :** As shown in Figure 1 , point  $P$  on the  $\triangle ABC$  plane ,  $P$  ,  $P_1$  is symmetric about  $AB$ ,  $P$  , is symmetric  $P_2$  about  $BC$  ,  $P$  , is symmetric  $P_3$  about  $CA$  , prove that the circumscribed circles of  $\triangle ABP_1$  ,  $\triangle BCP_2$  ,  $\triangle CAP_3$  intersect at one point.

Proof: Assuming that the circumscribed circle of  $\triangle ABP_1$  ,  $\triangle BCP_2$  intersects at  $Q$  , it is only necessary to prove *that*  $\angle AQC = \angle APC$  .

$$\text{Proof: } \frac{\frac{Q-C}{Q-A}}{\frac{P-A}{P-C}} = \frac{\frac{Q-B}{Q-A}}{\frac{B-P_1}{P_1-A}} \frac{\frac{P-B}{P-A}}{\frac{P_2-C}{P_2-B}} \frac{\frac{Q-C}{Q-B}}{\frac{P_2-C}{P_2-B}} \frac{\frac{P-C}{P-B}}{\frac{P_2-C}{P_2-B}} .$$