



Example 65 : As shown in Figure 1, $\triangle ABC$, there are points D and E on BA and BC respectively, and $BD = BE$, points F and G on CA and on the extension line of CB respectively, and $CF = CG$, and DE intersects FG at P , then $\angle DPF = \frac{1}{2} \angle A$.

$$\frac{\left(\frac{P-F}{P-D} \right)^2}{\frac{A-C}{A-B}} = \frac{\frac{B-A}{D-P} \frac{F-P}{B-C}}{\frac{C-A}{F-P}}$$