



Example 25 : As shown in Figure 1, let P and Q be two fixed points on line segment BC , and $BP = CQ$, A is a moving point outside BC , when point A moves to make $\angle BAP = \angle CAQ$, determine the shape of $\triangle ABC$, and justify your conclusions.

Proof: Suppose $A = 0$, $P = tB + (1-t)C$, $Q = B + C - P$, $(1-t)t \frac{\frac{C-B}{B}}{\frac{B-C}{Q}} + \frac{\frac{P}{C}}{\frac{B}{Q}} = 1$.