

Example 1 98 : As shown in Figure 1 , there are A, B, C, and D on circle O, and AB intersects CD with E. Prove: $2 \angle CEB = \angle COB + \angle DOA$.

Proof:
$$\frac{\left(\frac{D-C}{A-B}\right)^2}{\frac{O-C}{O-B}\frac{O-D}{O-A}} = \frac{\frac{D-C}{D-O}}{\frac{C-O}{C-D}} \frac{\frac{A-O}{A-B}}{\frac{B-A}{B-O}},$$

Explanation: The identities use directed angles. If a conventional angle is used, as shown in Figure 1, $2\angle$ $CEB = \angle$ $COB + \angle$ DOA. As shown in Figure 2 , $2\angle$ $CEB = \angle COB - \angle DOA$.