



**Example 46 :** As shown in the figure, in the quadrilateral  $ABCD$ ,  $AB$  intersects  $CD$  at  $P$ ,  $AD$  intersects  $BC$  at  $Q$ ,  $BD$  and  $AC$  intersect straight line  $PQ$  at  $S$  and  $T$  respectively, and the point  $O$  is outside the straight line  $PQ$ . The necessary and sufficient condition for proving  $OS \perp OT$  is  $\angle POT = \angle QOT$ . \_

Proof: Suppose  $O = 0$ ,  $D = \frac{xA + yB + zC}{x + y + z}$ ,  $P = \frac{xA + yB}{x + y}$ ,  $Q = \frac{yB + zC}{y + z}$ ,

$$S = \frac{xA + 2yB + zC}{x + 2y + z}, \quad T = \frac{xA - zC}{x - z},$$

$$(x + 2y + z)^2 \left( \frac{S}{T} \right)^2 - 4(x + y)(y + z) \frac{T}{Q} = (x - z)^2.$$

$O$  in the condition has a certain degree of activity, some special positions can be selected for compilation.