

Example 157: As shown in Figure 3, in $\triangle ABC$, I is the center, extend BI and CI to intersect the circle with BC as the diameter at M and N, and prove: AI \perp MN.

$$\left(\frac{A-I}{M-N}\right)^{2} \frac{\frac{C-N}{C-A}}{\frac{C-B}{C-N}} \left(\frac{\frac{M-N}{M-B}}{\frac{C-N}{C-B}}\right)^{2} \frac{\left(\frac{M-B}{I-A}\right)^{2}}{\frac{C-B}{C-A}} = 1,$$