



Pass through the right angle vertex C of the isosceles right angle $\triangle ABC$ to draw a parallel line to AB , and take a point D on it, make $AB = AD$, let AD and BC intersect at point E , and verify: $BD = BE$, $2CD = AE$, $2S_{\triangle ABC} = S_{\triangle ABE}$, $2\angle CAD = \angle DAB$.

Example 1 61 : As shown in Figure 1, there is a point D in $\triangle ABC$, $\angle CAB$, so that $AD = AB$, $2\angle CAD = \angle DAB$, AD and BC intersect at point E , to prove: **The necessary and sufficient condition of $CA \perp CB$ is $BD = BE$.**

$$\frac{\frac{D-B}{D-A} \left(\frac{C-B}{C-A} \right)^2 \left(\frac{A-D}{C-B} \right)^2 \left(\frac{A-C}{A-D} \right)^2}{\frac{B-A}{B-D} \left(\frac{C-A}{D-A} \right) \frac{A-D}{A-B}} = -1,$$