



Example 1 93 : As shown in Figure 1 , *point* M in $\triangle ABC$, extend AM to AA_1 , make $AM = A_1M$, extend BM to BB_1 , make $BM = B_1M$, extend CM to CC_1 , make $CM = C_1M$, to prove: the circumscribed circles of $\triangle ABC_1$, $\triangle A_1BC$, $\triangle AB_1C$ intersect at point D .

Proof: Assume that the circumscribed circles of $\triangle ABC_1$ and $\triangle A_1BC$ intersect at point D , and then prove that D is on the circumscribed circle of $\triangle AB_1C$.

$$\text{Proof: } \frac{\frac{D-A}{D-C}}{\frac{B_1-A}{B_1-C}} = \frac{\frac{A_1-B}{B_1-A} \frac{C_1-A}{A_1-C} \frac{B_1-C}{C_1-B}}{\frac{B-D}{A_1-C} \frac{D-A}{C_1-B}},$$