



Example 1 88 : As shown in Figure 1, quadrilateral $ABCD$, AB intersects DC at E , I_1 , I_2 are respectively the inner centers of $\triangle I_1I_2ABC$ and $\triangle DBC$, intersects AB at I_1' , intersects at $I_2'DC$, to prove: A, B, C, D four points cocircle The necessary and sufficient condition is $EI_1' = EI_2'$.

$$\left(\frac{B-I_1}{B-I_2} \right)^2 \frac{A-C}{A-B} \frac{C-B}{C-I_2} \frac{B-A}{B-I_1} \frac{C-I_1}{C-A} \frac{B-I_2}{B-C} = 1,$$

$$\left(\frac{C-I_1}{C-I_2} \right) \frac{D-C}{D-B} \frac{C-B}{C-D} \frac{B-I_1}{B-C} \frac{C-I_1}{C-I_1} \frac{B-I_2}{B-I_2} = 1,$$

$$\frac{D-C}{I_2-I_1} \frac{I_1-I_2}{I_1-C} \frac{A-C}{A-B} \frac{C-B}{C-I_1} \frac{C-I_1}{C-A} \frac{B-I_2}{B-C} = 1,$$

$$\frac{I_1-I_2}{A-B} \frac{B-I_2}{B-C} \frac{D-C}{D-B} \frac{I_2-B}{I_2-I_1} \frac{C-B}{C-I_1} \frac{B-I_2}{B-I_2} = 1,$$

Explanation: To prove $EI_1' = EI_2'$, it is necessary to introduce a straight line $I_1'I_2'$, which is inconvenient to eliminate. It needs to be divided into two steps, first prove that the four points B, I_1, I_2 , and C are in a circle, and then prove it $EI_1' = EI_2'$. But because of this, it will cause trouble for the push back. The following proof may be more appropriate.