



**Example 1 86 :** As shown in Figure 1, quadrilateral  $ABCD$ ,  $AC$  intersects  $BD$  at  $P$ , and  $AB$  intersects  $DC$  at  $E$ . Prove that the necessary and sufficient condition for the four points  $A$ ,  $B$ ,  $C$ , and  $D$  to be in a circle is the angle bisector of  $\angle APD$  and  $\angle AED$  parallel.

$$\left(\frac{L_2}{L_1}\right)^2 \frac{A-C}{D-C} \frac{L_1}{C-A} \frac{B-A}{C-D} = 1,$$

$$u = \pi - \angle A - \frac{\pi - \angle A - \angle D}{2} = \frac{\pi - \angle A + \angle D}{2},$$

$$v = \frac{\pi - \angle DAC - \angle BDA}{2} + \angle BDA = \frac{\pi - \angle DAC + \angle BDA}{2},$$

$$u = v \Leftrightarrow -\angle A + \angle D = -\angle DAC + \angle BDA.$$