

Example 1 27: As shown in Figure 3, in \triangle ABC, 0 is the center, and points E and F are on the large side BC. It is known that BF = BA, CE = CA. Prove: \angle $EOF = \angle B + \angle C$.

$$\frac{\frac{O-F}{O-E}}{\frac{B-A}{B-C}\frac{C-B}{C-A}} = \frac{\frac{O-F}{O-E}}{\left(\frac{A-F}{A-E}\right)^2} \frac{\frac{A-F}{A-B}}{\frac{F-B}{F-A}} \frac{\frac{A-C}{A-E}}{\frac{E-A}{E-C}} \frac{B-F}{E-C}.$$

Explanation: Note that O is the circumcenter of $\triangle AEF$, $2\angle EAF = \angle EOF$.