

Example 1 90 : As shown in Figure 1 , the quadrilateral ABCD, AC intersects BD at O, and the feet of O on the four sides of BC, CD, DA, and AB are E, F, G, and H. Prove: The necessary and sufficient condition for $AC \perp BD$ is E, F, G, H are four points in a circle.

Proof:
$$\frac{\frac{G-F}{G-H}}{\frac{E-F}{E-H}} = \left(\frac{A-C}{B-D}\right)^{2} \frac{\frac{G-O}{G-H}}{\frac{A-C}{A-B}} \frac{\frac{G-F}{G-O}}{\frac{B-O}{D-B}} \frac{\frac{E-H}{E-O}}{\frac{E-O}{C-D}} \frac{\frac{E-F}{C-A}}{\frac{C-A}{C-D}}.$$