



Example 41 : In the parallelogram $ABCD$, the rays AM and AD are symmetrical about AC , BM and BC are symmetrical about D , and O is the intersection of diagonals AC and BD . Prove: $\angle OMA = \angle BMO$.

Proof: Suppose $O = 0$, $M = xA + yB$, $T = \frac{M-0}{M-A}$, $t_1 = \frac{A-0}{A+B}$, $t_2 = \frac{B-0}{B-M}$,

$$T = \frac{x+y+1-t_1-t_2+(t_1-t_2)(x-y)}{x+y-1},$$

Explanation: Note $x+y-1 \neq 0$ that it is equivalent to that M is not on the straight line AB .

If M is on the straight line AB , the conclusion does not hold. Therefore, this question requires an additional condition $AB \neq BC$ to ensure that M is on the straight line AB .