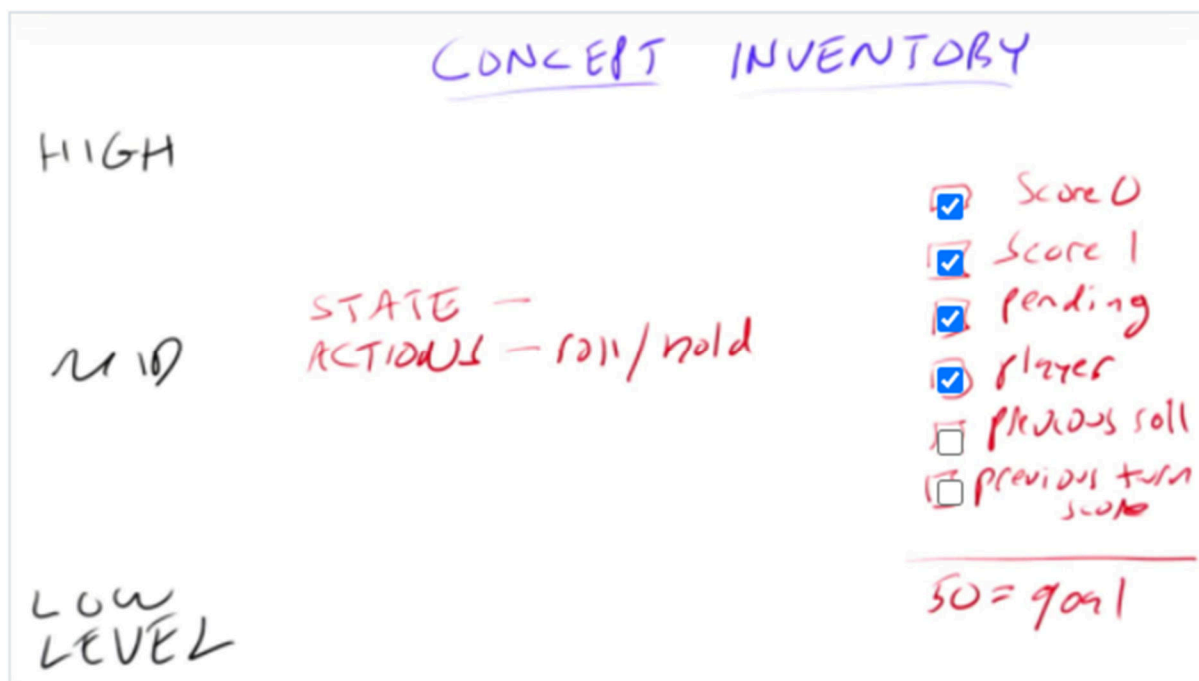


The State Of Pig



Hold And Roll

```
13
14 def hold(state):
15     """Apply the hold action to a state to yield a new state:
16     Reap the 'pending' points and it becomes the other player's turn."""
17     (p, me, you, pending) = state
18     return (other[p], you, me + pending, 0)
19
20 def roll(state, d):
21     """Apply the roll action to a state (and a die roll d) to yield a new state:
22     If d is 1, get 1 point (losing any accumulated 'pending' points),
23     and it is the other player's turn. If d > 1, add d to 'pending' points."""
24     (p, me, you, pending) = state
25     if d == 1:
26         return (other[p], you, me + 1, 0)
27     else:
28         return (p, me, you, pending + d)
29
30 other = {1: 0, 0: 1}
31
```

Clueless

```
possible_moves = ['roll', 'hold']

def clueless(state):
    """A strategy that ignores the state and chooses at random from possible moves"""
    return random.choice(possible_moves)
```

Hold At Strategy

```
9
0 ▾ def hold_at(x):
1     """Return a strategy that holds if and only if
2     pending >= x or player reaches goal."""
3     def strategy(state):
4         (p, me, you, pending) = state
5         return 'hold' if (pending >= x or me + pending >= goal) else 'roll'
6     strategy.__name__ = 'hold_at(%d)' % x
7     return strategy
8
9 goal = 50
0 ▾ def test():
1     assert hold_at(30)((1, 29, 15, 20)) == 'roll'
2     assert hold_at(30)((1, 29, 15, 21)) == 'hold'
3     assert hold_at(15)((0, 2, 30, 10)) == 'roll'
4     assert hold_at(15)((0, 2, 30, 15)) == 'hold'
5     return 'tests pass'
6
7 print test()
8
```

Play Pig

```
def play_pig(A, B):
    """Play a game of pig between two players, represented
    Each time through the main loop we ask the current player
    which must be 'hold' or 'roll', and we update the state
    When one player's score exceeds the goal, return that player's name
    strategies=[A,B]
    state=(0,0,0,0)
    while True:
        (p,me,you,pending)=state
        if me >=goal:
            return strategies[p]
        elif you >= goal:
            return strategies[other[p]]
        elif strategies[p](state)=='hold':
            state=hold(state)
        else:
            state=roll(state,random.randint(1,6))
```

Loading The Dice

```
def play_pig(A, B, dierolls=dierolls()):
    """Play a game of pig between two players, represented
    Each time through the main loop we ask the current player
    which must be 'hold' or 'roll', and we update the state
    When one player's score exceeds the goal, return that player's name
    strategies = [A, B]
    state = (0, 0, 0, 0)
    while True:
        (p, me, you, pending) = state
        if me >= goal:
            return strategies[p]
        elif you >= goal:
            return strategies[other[p]]
        elif strategies[p](state) == 'hold':
            state = hold(state)
        else:
            state = roll(state, next(dierolls))

goal=50

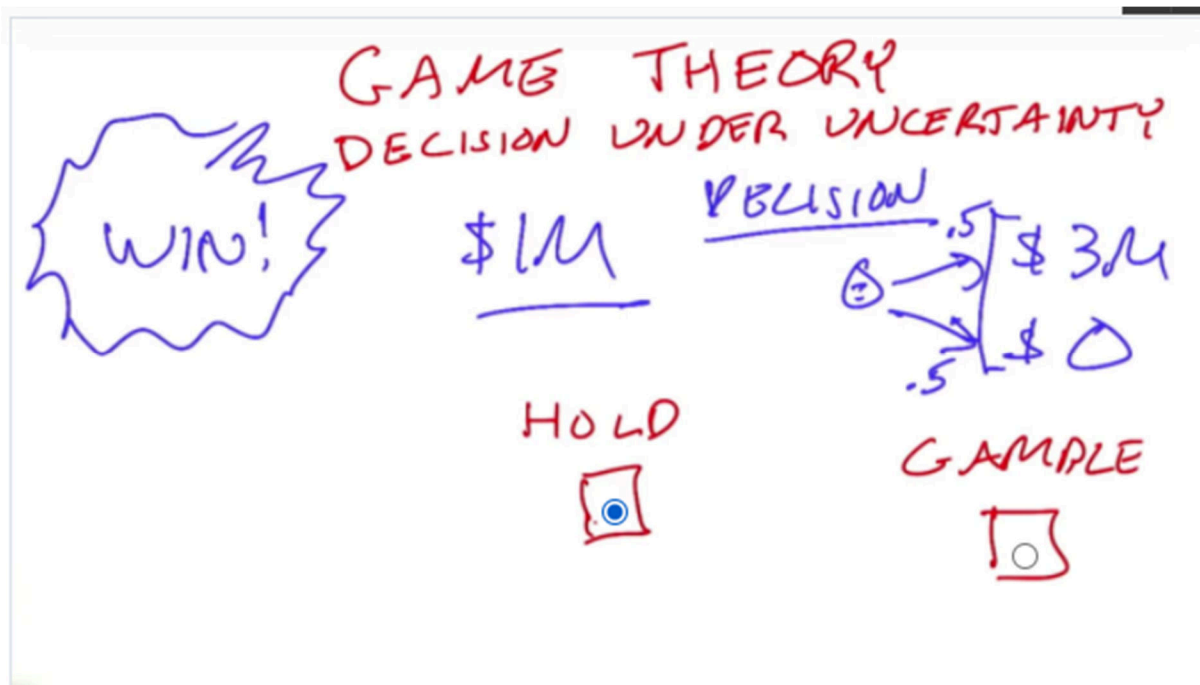
def test():
    A, B = hold_at(50), clueless
    rolls = iter([6,6,6,6,6,6,6,6,2]) # <-- Your
    assert play_pig(A, B, rolls) == A
    return 'test passes'

print test()
```

Optimizing Strategy



Game Theory



Break Even Point

```
1
2
3 million = 1000000
4
5 def Q(state, action, U):
6     "The expected value of taking action in state, according to utility U."
7     if action == 'hold':
8         return U(state + 1*million)
9     if action == 'gamble':
10        return U(state + 3*million) * .5 + U(state) * .5
11
12
13 U = math.log10
14 ## what is c such that: Q(c, 'gamble', U) == Q(c, 'hold', U)
15
16
17 ## c = [ 1 ] million
18
19
20
21
22
23
24
```

RUN

Press 'Run' to see your result

Whats Your Crossover

```
6     "The expected value of taking action in state, according to utility U."
7     if action == 'hold':
8         return U(state + 1*million)
9     if action == 'gamble':
10        return U(state + 3*million) * .5 + U(state) * .5
11
12
13 U = math.log10
14 ## what is c such that: Q(c, 'gamble', U) == Q(c, 'hold', U)
15
16
17 ## c = [ 1 ] million
18
19 c = 1*million
20 Q(c, 'gamble', math.log10), Q(c, 'hold', math.log10)
21 (6.301029995663981, 6.301029995663981)
22
23
24 # What's your crossover? c = [ ]
25
26
27
28
29
30
```

RUN

Press 'Run' to see your result

Maxwins

```
36 def max_wins(state):
37     """The optimal pig strategy chooses an action with the highest
38     return best_action(state, pig_actions, Q_pig, Pwin)
```

Maximizing Differential


```
3 def max_diffs(state):
9     """A strategy that maximizes the expected difference between
9     and my opponent's."""
1 return best_action(state, pig_actions, Q_pig, win_diff)
2
```

Legal Actions

```
def play_pig(A, B, dierolls=dierolls()):
    """Play a game of pig between two players, represented by
    Each time through the main loop we ask the current player
    which must be 'hold' or 'roll', and we update the state ac
    When one player's score exceeds the goal, return that play
    strategies = [A, B]
    state = (0, 0, 0, 0)
    while True:
        (p, me, you, pending) = state
        if me >= goal:
            return strategies[p]
        elif you >= goal:
            return strategies[other[p]]
        else:
            action = strategies[p](state)
            if action == 'hold':
                state=hold(state)
            elif action == 'roll':
                state=roll(state,next(dierolls))
            else:
                return strategies[other[p]]
```

Simulation Vs Enumeration

SIMULATION vs ENUMERATION

 .5 B, .5 G

$\frac{1}{3} = P(2 \text{ boys} \mid \text{at least 1 boy and 2 children total}) = P(A \mid B)$

Tuesday

```
32 what is the probability of two boys?
33 """
34 day = 'SMTWtFs'
35
36 two_kids_bday = product(sex, day, sex, day)
37
38 boy_tuesday = [s for s in two_kids_bday if 'BT' in s]
39
40 print condP(two_boys, boy_tuesday)
41
42 ## Enter as a fraction [ 13 ] / [ 27 ]
43
44
45
46
```