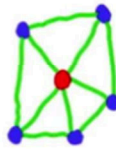
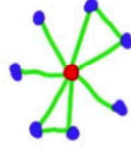
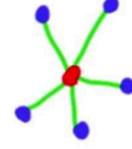
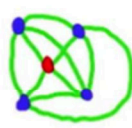
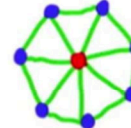
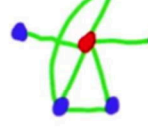


Clustering Coefficient

Clustering Coefficient

a)  b)  c) 

d)  e)  f) 

Order by clustering coefficient of the **red** node of each graph - lowest to highest

cbfead

Bipartite I

Bipartite Graphs

Consider a bipartite graph, B , that has five nodes in one group and three in the other

LEFT RIGHT

• •
• •
• •
• •
• •

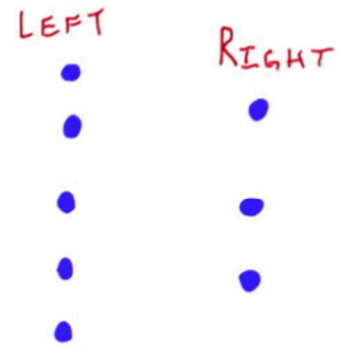
i) What is the smallest number of edges needed to make B have a single reachable component consisting of all the nodes?

7

Bipartite II

Bipartite Graphs

Consider a bipartite graph, B , that has five nodes in one group and three in the other

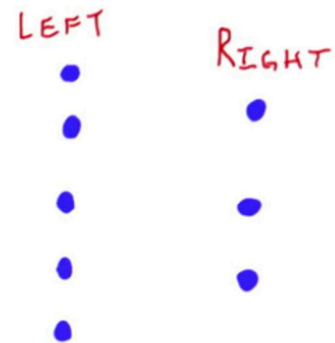


- 1) What is the smallest number of edges needed to make B have a single reachable component consisting of all the edges?
- 2) What is the maximum number of edges B can have?

Bipartite III

Bipartite Graphs

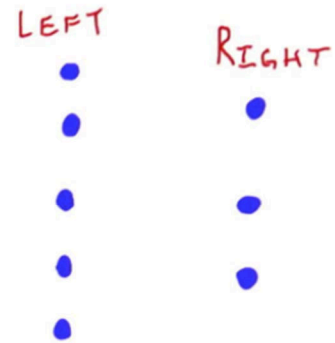
Consider a bipartite graph, B , that has five nodes in one group and three in the other



- 3) What is the maximum possible path length in B ?

Bipartite Graphs

Consider a bipartite graph, B , that has five nodes in one group and three in the other



3) What is the maximum possible path length in B ?

4) What is the maximum possible clustering coefficient for a node in B ?

ONLY CONSIDER
NODES DEGREE ≥ 2 .

Mark Component

```

5
6 def mark_component(G, node, marked):
7     open_list = [node]
8     total_marked = 1
9     marked[node] = True
10    while len(open_list) > 0:
11        node = open_list.pop()
12        for neighbor in G[node]:
13            if neighbor not in marked:
14                open_list.append(neighbor)
15                marked[neighbor] = True
16                total_marked += 1
17    return total_marked
18

```

Centrality

```
6 def centrality_max(G, v):
7     distance_from_start = {}
8     open_list = [v]
9     distance_from_start[v] = 0
10    while len(open_list) > 0:
11        current = open_list[0]
12        del open_list[0]
13        for neighbor in G[current].keys():
14            if neighbor not in distance_from_start:
15                distance_from_start[neighbor] = distance_from_start[current] + 1
16                open_list.append(neighbor)
17    return max(distance_from_start.values())
18
```

Bridge Edges

```
1 #
2 # First some utility functions
3 #
4
5 def make_link(G, node1, node2, r_or_g):
6     # modified make_link to apply
7     # a color to the edge instead of just 1
8     if node1 not in G:
9         G[node1] = {}
10    (G[node1])[node2] = r_or_g
11    if node2 not in G:
12        G[node2] = {}
13    (G[node2])[node1] = r_or_g
14    return G
15
16 def get_children(S, root, parent):
17     """returns the children from following the
18     green edges"""
19     return [n for n, e in S[root].items()
20             if ((not n == parent) and
21                 (e == 'green'))]
22
23 def get_children_all(S, root, parent):
24     """returns the children from following
25     green edges and the children from following
26     red edges"""
27     green = []
28     red = []
29     for n, e in S[root].items():
30         if e == 'green':
```