

# Ion-Matter itneractions

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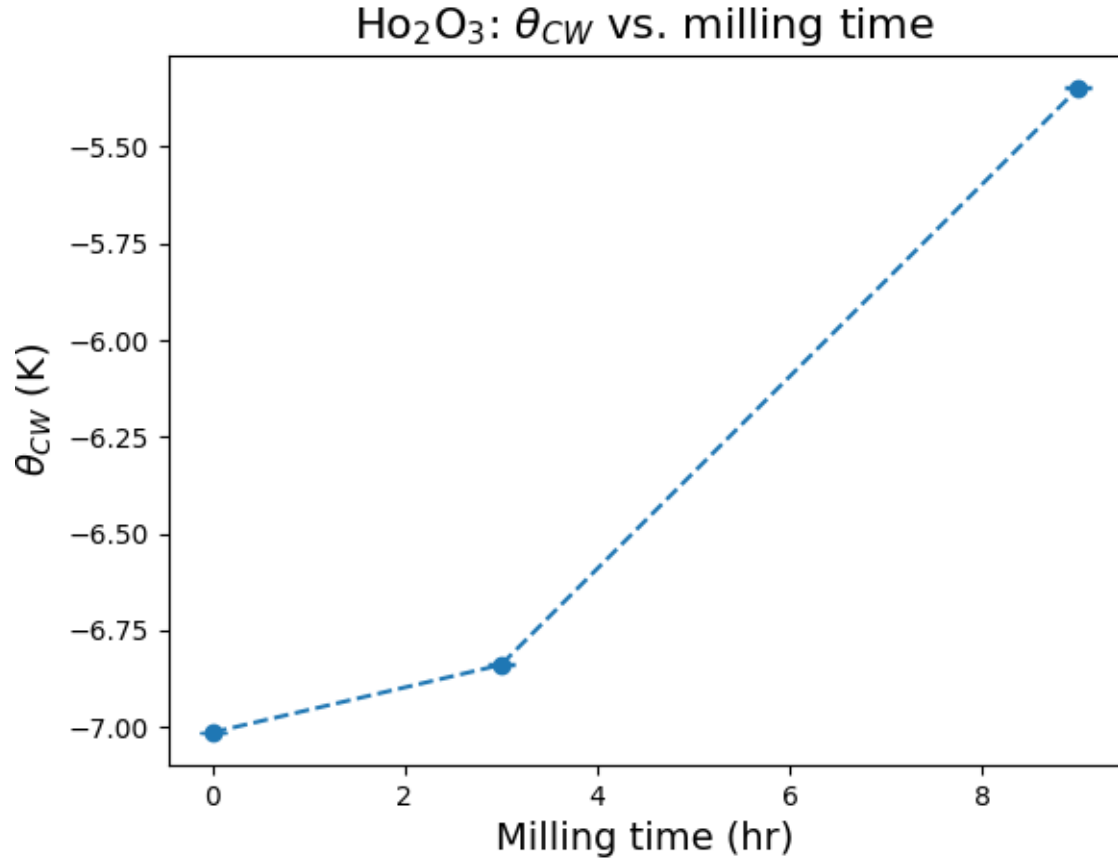


Figure 1: asd

$$S_c = 4\pi r_0^2 m_e c^2 \left(\frac{z^2}{\beta^2}\right) \left(\frac{N_A \rho Z}{M_m}\right) \left\{ \ln\left(\frac{2m_e c^2 \gamma^2 \beta^2}{I}\right) - \beta^2 \right\}$$

$$\alpha \rightarrow T/A = 200 \text{ MeV}, T = 800 \text{ MeV}$$

$$r_0 = 2.818 \times 10^{-13} \text{ cm}$$

$$m_e c^2 = 0.511 \text{ MeV}$$

$$z^2 = 4$$

$$E_\alpha = T_\alpha + m_\alpha c^2 = \gamma(m_\alpha c^2)$$

$$T_\alpha = (\gamma - 1)m_\alpha c^2$$

Calculate mass of alpha:

$$m_\alpha = (4 * 931.494 \text{ MeV}) + \delta - 2m_e = 3727.379$$

$$\gamma = 1.215$$

$$\gamma^2 = \frac{1}{1 - \beta^2}$$

$$\beta^2 = 1 - \frac{1}{\gamma^2} = 0.323$$

$$\beta^2 \gamma^2 = \gamma^2 - 1$$

$$n_e = \frac{N_A \rho Z}{M_m}$$

$$I_{Al} = 166 \text{ eV}$$

Plug into massive equation. Check units

$$S_c = 37.908 \text{ (MeV/cm from star database)}$$

$$S_c = 37.879 \text{ MeV/cm from Python calc}$$

## Calculating densities

- Use NIST values

– Air:

- \*  $Z = 6, 7, 8, 18$

- \*  $\rho = 1.20479 \times 10^{-2} \text{ g/cm}^3$

- \* Mean excitation energy = 86.7 eV

$$\rho_A = \frac{N_A}{M_m} \rho$$

$$\rho_A = \frac{N_A}{mw} \rho n_i$$

$$mw = \sum_{i=1}^N n_i A_i$$

$$f_i = \frac{n_i A_i}{\sum_{i=1}^N n_i A_i} = \frac{n_i A_i}{mw}$$

$$\rho_{A_i} = N_A / (mw) \rho \frac{f_i mw_i}{A_i}$$

$$\rho_{A_i} = N_A \rho \frac{f_i}{A_i}$$

or

$$\rho_{A_i} = \frac{N_a \rho f_i}{A_i}$$

Electron density

$$n_e = \sum_{i=1}^N \frac{N_a \rho f_i}{A_i} Z_i$$

- Don't need molar weight of molecule

- Electron density of water

$$A_O = 16$$

$$A_H = 1$$

$$Z_O = 8$$

$$Z_H = 1$$

$$f_H = 2/18$$

$$f_O = 16/18$$

$$n_e = N_A \rho \left[ \frac{f_H}{A_H} Z_H + \frac{f_O}{A_O} Z_O \right]$$

$$n_e = 3.35 \times 10^{23} [e^- / cm^3]$$