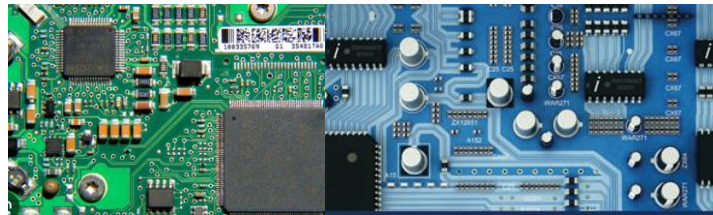





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# Circuit Analysis and Design

Academic year 2025/2026 – Lecture 4

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*“A good student never steal or cheat”*

# Agenda

## ☐ Revise Signal Functions

- Delta Function
- Step Function
- Ramp Function
- Exponential Functions
- Rectangular and Triangular Functions

## ☐ Revise Equivalent Resistance

## ☐ Voltage divider rule

## ☐ Current divider rule

## ☐ Summary

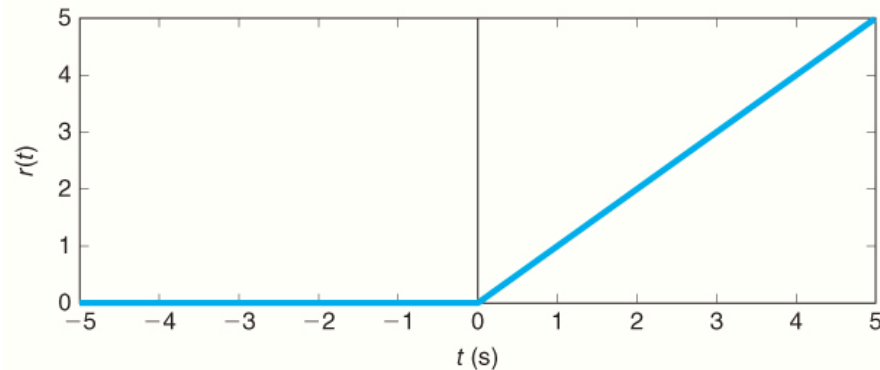


# Ramp Function

- ❑ A unit ramp function is defined by

$$r(t) = t u(t)$$

- ❑ Unit ramp function is shown here



- ❑ Unit ramp function is the integral of the unit step function:

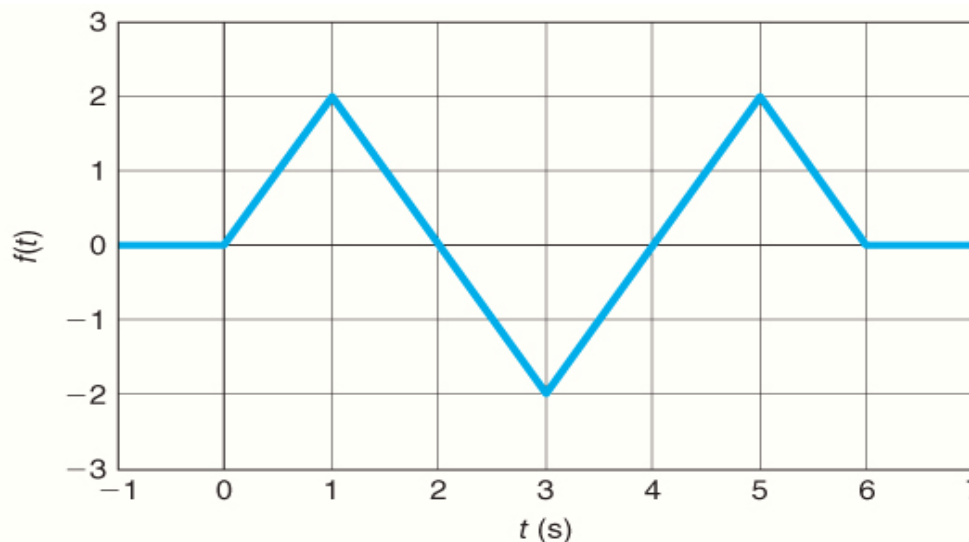
$$r(t) = \int_{-\infty}^t u(\lambda) d\lambda$$

- ❑ Derivative of unit ramp function is unit step function:

$$u(t) = \frac{dr(t)}{dt}$$

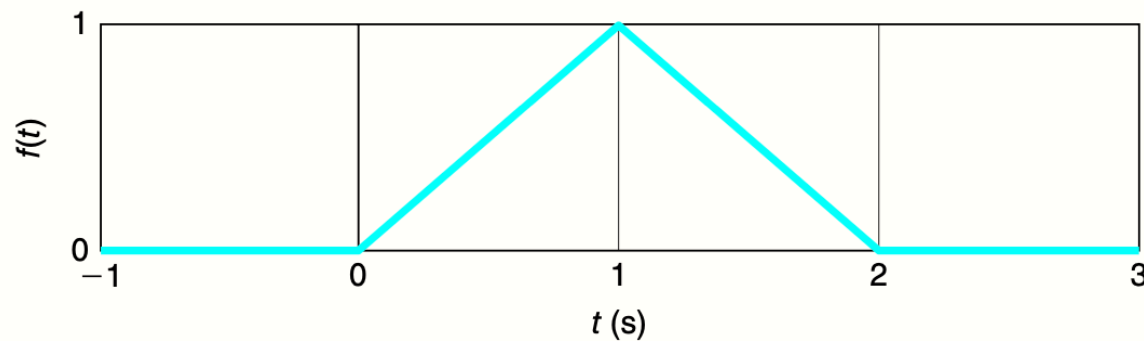
# EXAMPLE 1.9

- Plot  $f(t) = 2tu(t) - 4(t-1)u(t-1) + 4(t-3)u(t-3) - 4(t-5)u(t-5) + 2(t-6)u(t-6)$
- For  $t < 0$ ,  $f(t) = 0$ 
  - Step 1: For  $0 \leq t < 1$ ,  $f(t)$  is a linear line with slope of 2. (Slope = 2)
  - Step 2: For  $1 \leq t < 3$ ,  $f(t)$  is a linear line with slope of -2. (Slope =  $2 - 4 = -2$ )
  - Step 3: For  $3 \leq t < 5$ ,  $f(t)$  is a linear line with slope of 2. (Slope =  $-2 + 4 = 2$ )
  - Step 4: For  $5 \leq t < 6$ ,  $f(t)$  is a linear line with slope of -2. (Slope =  $2 - 4 = -2$ )
  - Step 5: For  $6 \leq t$ ,  $f(t) = 0$ . (Slope  $-2 + 2 = 0$ )



# Class work

Find the equation



## Options

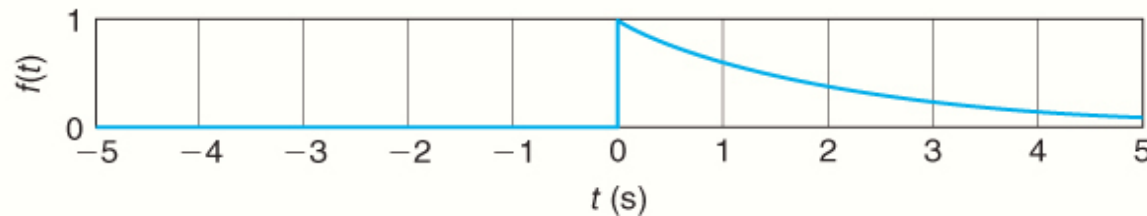
- A.  $tu(t) + 2(t - 1)u(t - 1) - (t - 2)u(t - 2)$
- B.  $tu(t) - 2(t - 1)u(t - 1) + (t - 2)u(t - 2)$
- C.  $tu(t) + (t - 2)u(t - 2)$

# Exponential Decay Functions

- A signal that decays exponentially can be written as

$$f(t) = e^{-at} u(t), a > 0.$$

- The signal  $f(t)$  for  $a = 0.5$  is shown in Figure 1.37.

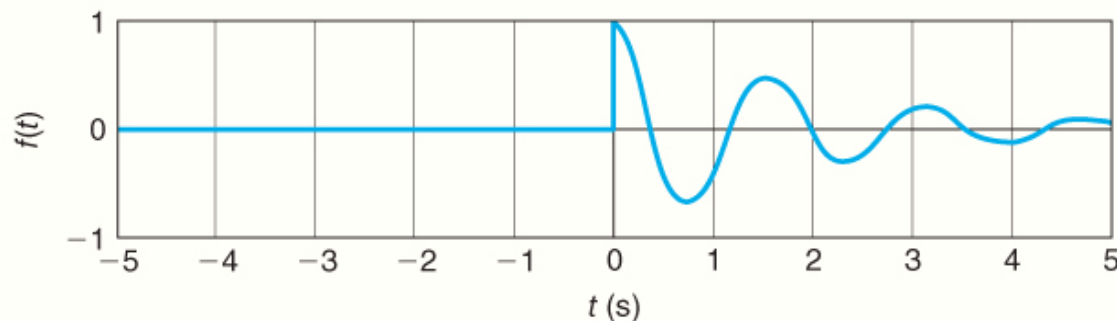


- Damped cosine and damped sine can be written respectively as

$$f(t) = e^{-at} \cos(bt) u(t), a > 0$$

$$f(t) = e^{-at} \sin(bt) u(t), a > 0$$

- Damped cosine signal is shown 1.38 for  $a = 0.5$  and  $b = 4$ .

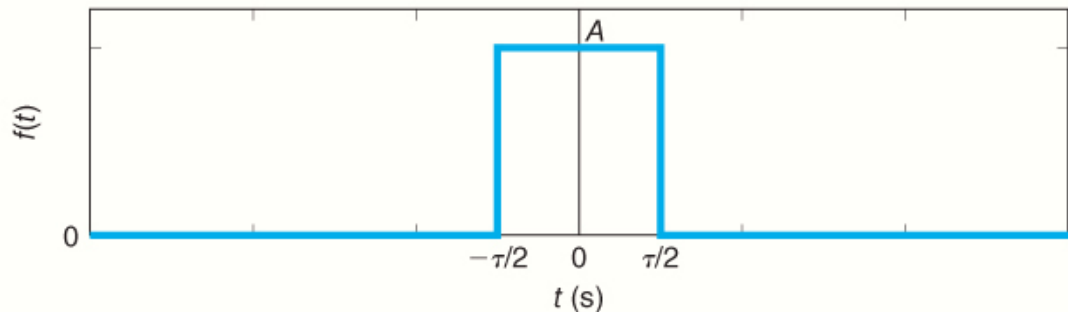


# Rectangular Pulse and Triangular Pulse

□ A **rectangular** pulse with amplitude  $A$  pulse width  $\tau$  is shown in Figure. Center of the pulse is at  $t = 0$ .

■ Rectangular pulse shown in is denoted by:

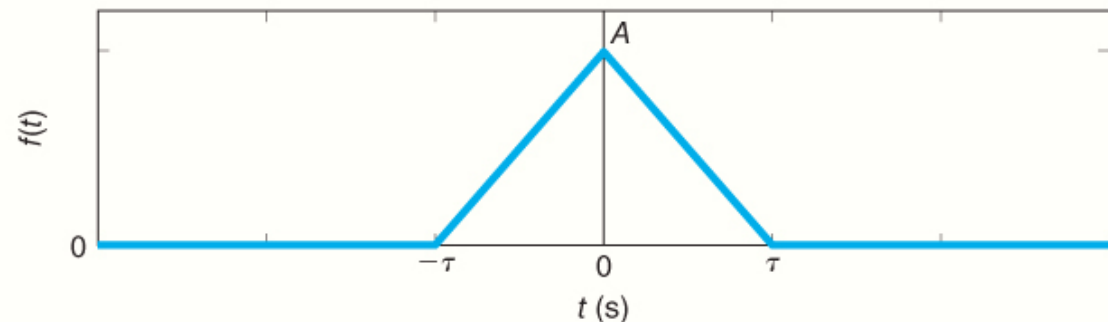
$$f(t) = A \operatorname{rect}\left(\frac{t}{\tau}\right)$$



□ A **triangular** pulse with amplitude  $A$  and base  $2\tau$  is shown in Figure. The center of the pulse is at  $t = 0$ .

■ Triangular pulse shown in Figure 1.42 is denoted by

$$f(t) = A \operatorname{tri}\left(\frac{t}{\tau}\right)$$

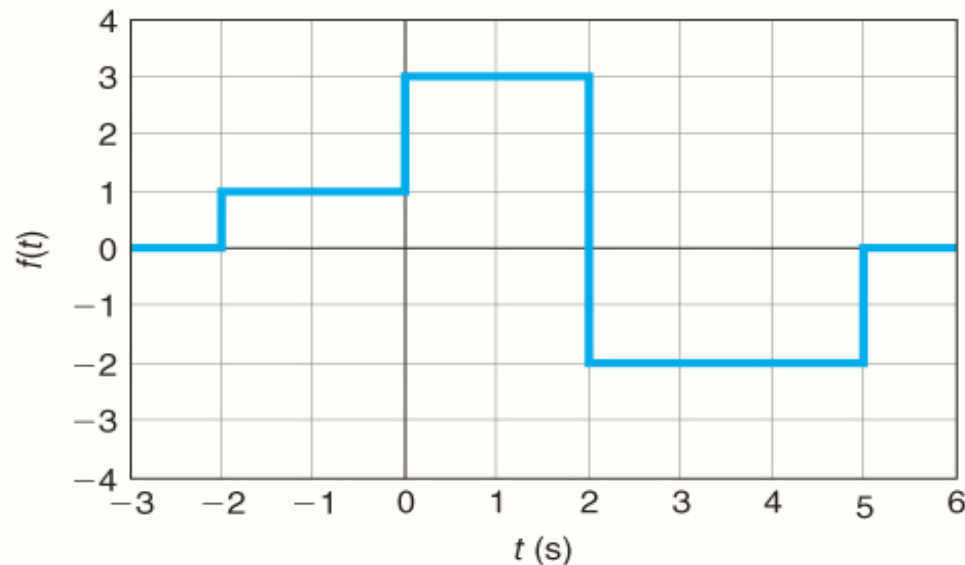


# EXAMPLE 1.11

□ Plot

$$f(t) = \text{rect}\left(\frac{t+1}{2}\right) + 3\text{rect}\left(\frac{t-1}{2}\right) - 2\text{rect}\left(\frac{t-3.5}{3}\right)$$

□ The first rectangle is centered at  $t = -1$  and has a height of 1 and width of 2. The second rectangle is centered at  $t = 1$  and has a height of 3 and width of 2. The third rectangle is centered at  $t = 3.5$  and has a height of  $-2$  and width of 3. The waveform  $f(t)$  is shown in Figure 1.40.



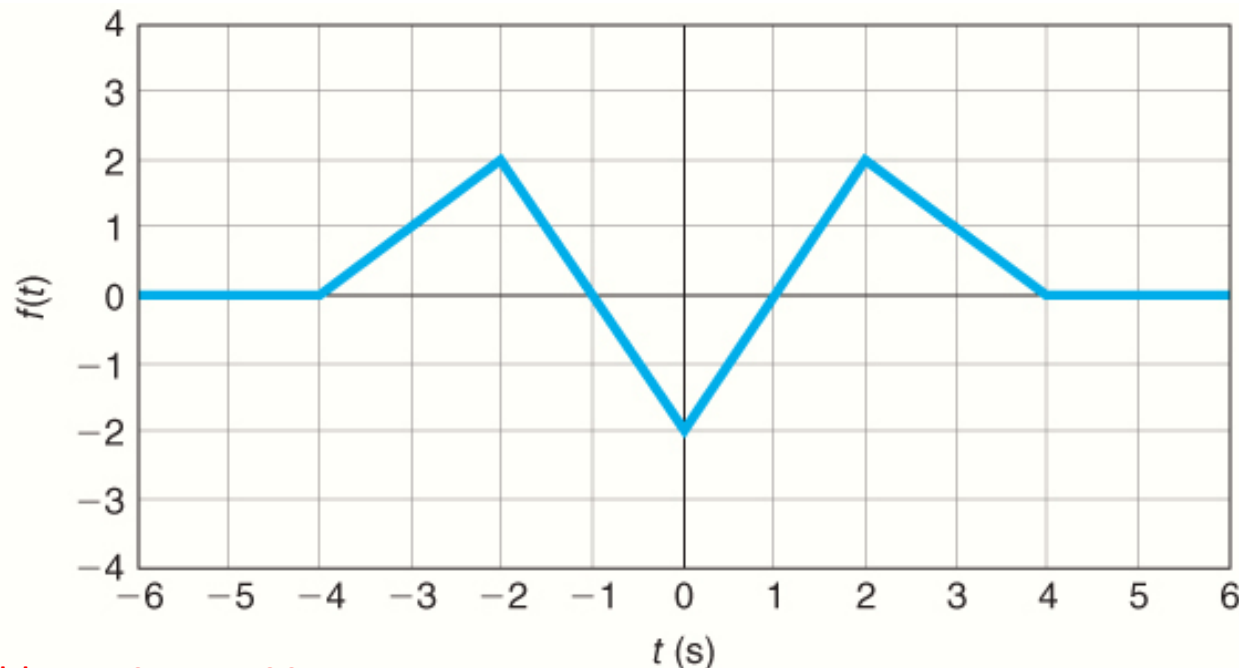


# EXAMPLE 1.12

□ Plot

$$f(t) = 2 \operatorname{tri}\left(\frac{t+2}{2}\right) - 2 \operatorname{tri}\left(\frac{t}{2}\right) + 2 \operatorname{tri}\left(\frac{t-2}{2}\right)$$

1. The first triangle is centered at  $t = -2$  and has a height of 2 and base of 4.
  2. The second triangle is centered at  $t = 0$  and has a height of -2 and base of 4.
  3. The third triangle is centered at  $t = 2$  and has a height of 2 and base of 4.
- The waveform  $f(t)$  is shown in Figure 1.43.



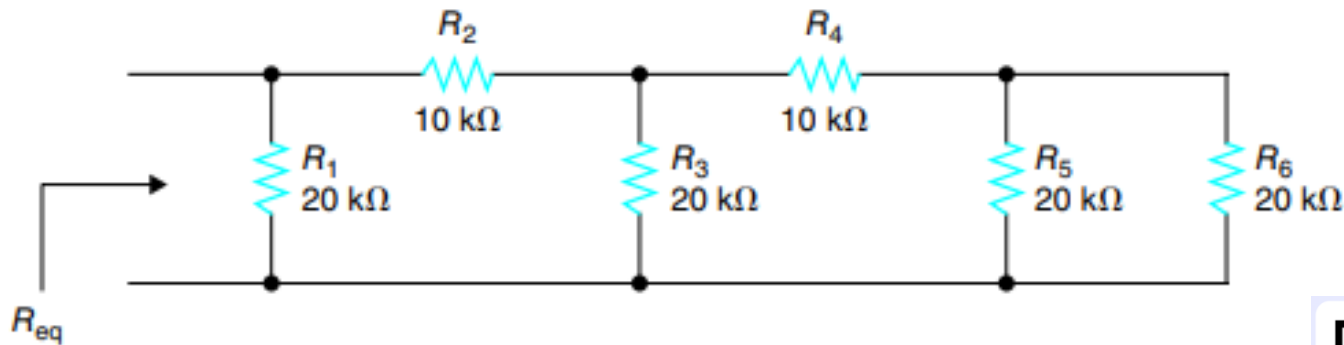
# Problem 2.39

Find the Equivalent Resistance



Fill in the Blanks

FIGURE P2.39



- What is the value of equivalent resistance -----  $k\Omega$

Solution will be provided in class



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## EXAMPLE 2.12

- Find the equivalent resistance seen from the voltage source. Also find  $I$ ,  $I_1$ ,  $I_2$ ,  $V_1$ ,  $V_2$ ,  $V_3$ , and power absorbed by resistors and power released by the voltage source.

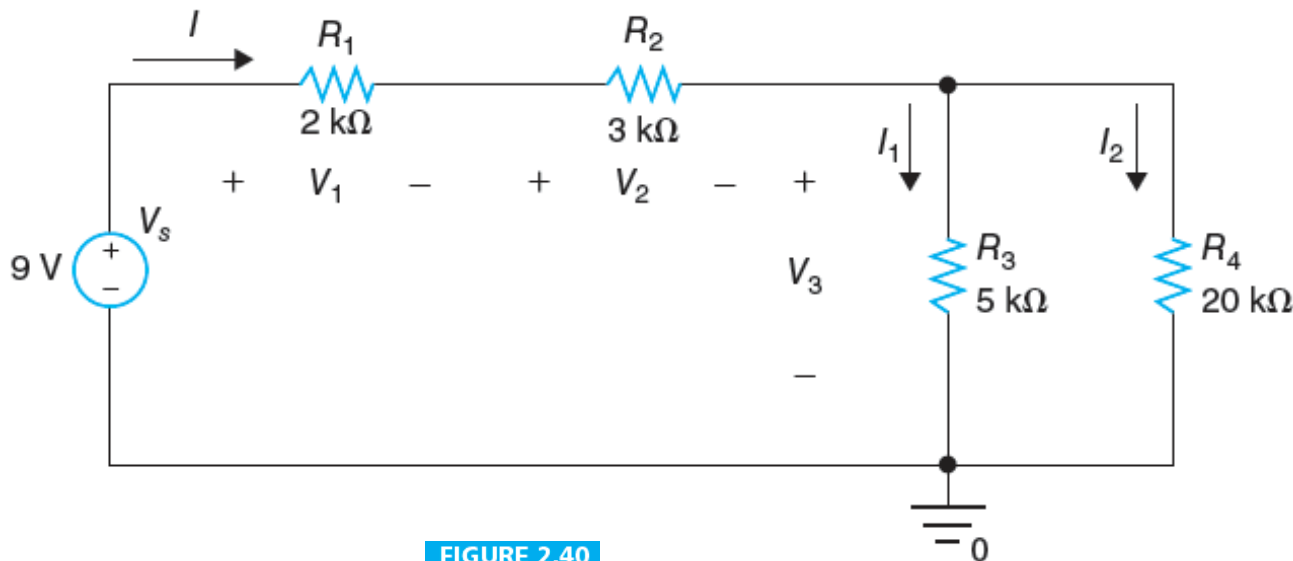


FIGURE 2.40

- The value of  $R_{eq}$
- A.  $9 \text{ k}\Omega$
- B.  $10 \text{ k}\Omega$

Solution will be provided in the class

## EXAMPLE 2.12

- Find the equivalent resistance seen from the voltage source. Also find  $I$ ,  $I_1$ ,  $I_2$ ,  $V_1$ ,  $V_2$ ,  $V_3$ , and power absorbed by resistors and power released by the voltage source.
- $R_a = R_3 \parallel R_4 = R_3 \times R_4 / (R_3 + R_4) = 100/25 \text{ k}\Omega = 4 \text{ k}\Omega$ ,  $R_{eq} = R_1 + R_2 + R_a = 9 \text{ k}\Omega$
  - $I = V_s / R_{eq} = 9/9000 \text{ A} = 1 \text{ mA}$
  - $V_1 = R_1 I = 2 \text{ V}$ ,  $V_2 = R_2 I = 3 \text{ V}$ ,  $V_3 = R_a I = 4 \text{ V}$
  - $I_1 = V_3 / R_3 = 0.8 \text{ mA}$ ,  $I_2 = V_3 / R_4 = 0.2 \text{ mA}$
  - $P_{R1} = I V_1 = 2 \text{ mW}$ ,  $P_{R2} = I V_2 = 3 \text{ mW}$ ,  $P_{R3} = I_1 V_3 = 3.2 \text{ mW}$ ,  $P_{R4} = I_2 V_3 = 0.8 \text{ mW}$
  - $P_{V_s} = -I V_s = -9 \text{ mW}$
  - Power absorbed by resistors = 9 mW
  - Power released by voltage source = 9 mW

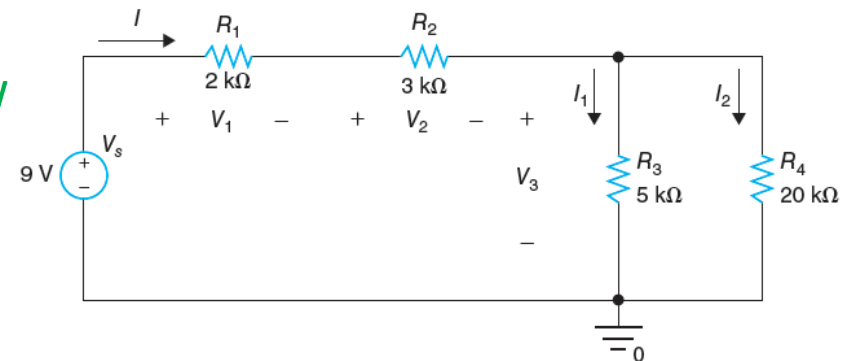
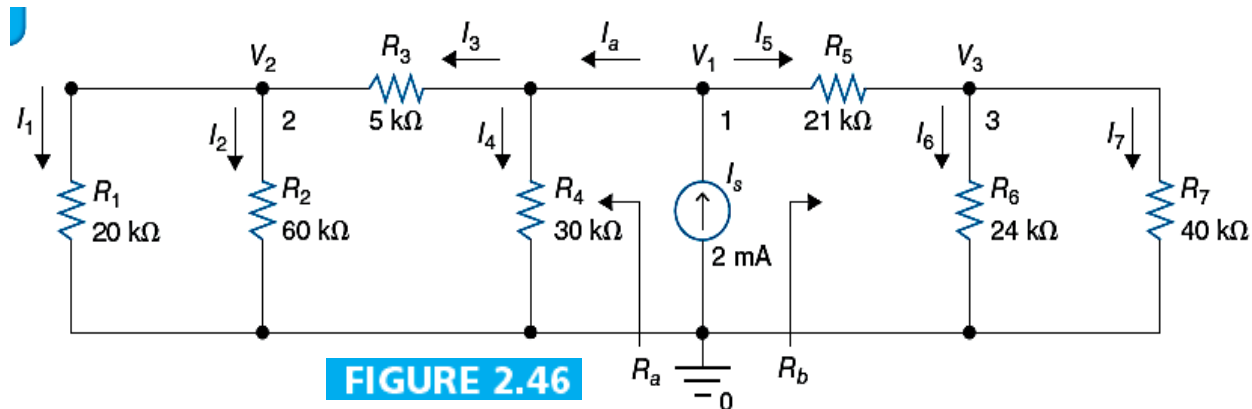


FIGURE 2.40

# Circuits with Parallel and Series Resistors

□ **Example 2.14:** Find the equivalent resistance seen from the current source. Also find  $I_a$ ,  $I_1$ ,  $I_2$ ,  $I_3$ ,  $I_4$ ,  $I_5$ ,  $I_6$ ,  $I_7$ ,  $V_1$ ,  $V_2$ ,  $V_3$  for the circuit shown in Figure 2.46.

- $R_8 = R_1 \parallel R_2 = R_1 \times R_2 / (R_1 + R_2) = 1200/80 \text{ k}\Omega = 15 \text{ k}\Omega$ ,  $R_9 = R_3 + R_8 = 20 \text{ k}\Omega$
- $R_a = R_4 \parallel R_9 = R_4 \times R_9 / (R_4 + R_9) = 600/50 \text{ k}\Omega = 12 \text{ k}\Omega$
- $R_{10} = R_6 \parallel R_7 = R_6 \times R_7 / (R_6 + R_7) = 960/64 \text{ k}\Omega = 15 \text{ k}\Omega$ ,  $R_b = R_5 + R_{10} = 36 \text{ k}\Omega$
- $R_{eq} = R_a \parallel R_b = R_a \times R_b / (R_a + R_b) = 432/48 \text{ k}\Omega = 9 \text{ k}\Omega$
- $V_1 = R_{eq} I_s = 9000 \times 0.002 = 18 \text{ V}$ ,  $I_a = V_1 / R_a = 18/12000 \text{ A} = 1.5 \text{ mA}$ ,  $I_5 = I_s - I_a = 0.5 \text{ mA}$
- $I_4 = V_1 / R_4 = 18/30000 \text{ A} = 0.6 \text{ mA}$ ,  $I_3 = I_a - I_4 = 0.9 \text{ mA}$ ,  $V_2 = V_1 - R_3 I_3 = 13.5 \text{ V}$
- $I_1 = V_2 / R_1 = 0.675 \text{ mA}$
- $I_2 = V_2 / R_2 = 0.225 \text{ mA}$
- $V_3 = V_1 - R_5 I_5 = 7.5 \text{ V}$
- $I_6 = V_3 / R_6 = 0.3125 \text{ mA}$
- $I_7 = V_3 / R_7 = 0.1875 \text{ mA}$



# Voltage Divider Rule for Two Resistors in Series

❑ A voltage source is connected to a series connection of resistors  $R_1$  and  $R_2$  as shown in Figure 2.49.

❑ Current through the resistors is given by  $\rightarrow I = \frac{V_s}{R_1 + R_2}$

❑ Voltage across  $R_1$  is given by

$$V_1 = I \times R_1 = \frac{V_s}{R_1 + R_2} \times R_1 = V_s \times \frac{R_1}{R_1 + R_2}$$

❑ Voltage across  $R_2$  is given by

$$V_2 = I \times R_2 = \frac{V_s}{R_1 + R_2} \times R_2 = V_s \times \frac{R_2}{R_1 + R_2}$$

❑ If two resistors are connected in Series, **Voltage from voltage source is divided between  $R_1$  and  $R_2$  in proportion to the resistance values.**

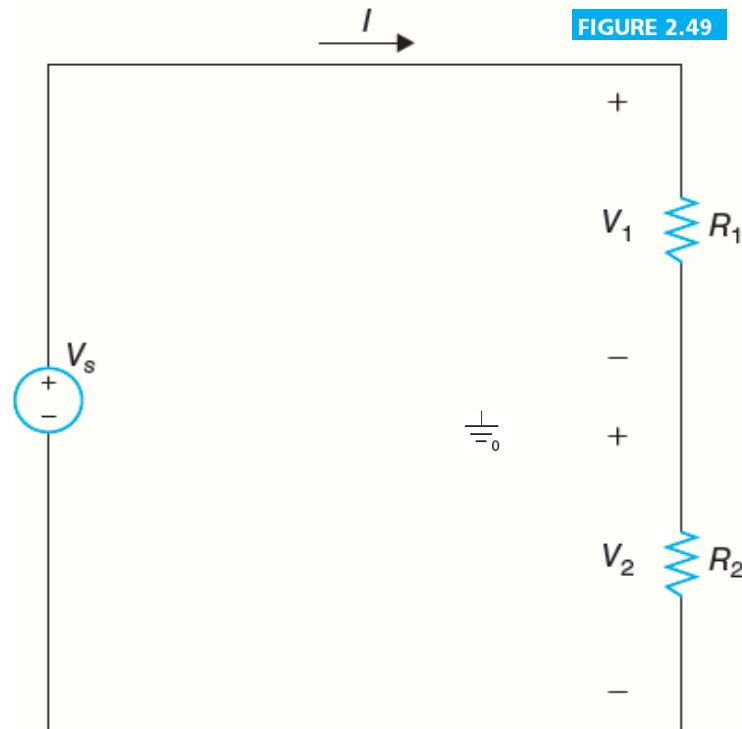


FIGURE 2.49

# Voltage Divider Rule for n Resistors

- ❑ A voltage source is connected to a series connection of n resistors  $R_1, R_2, \dots, R_n$ .
- ❑ The current through the resistors is given by

$$I = \frac{V_s}{R_1 + R_2 + \dots + R_n}$$

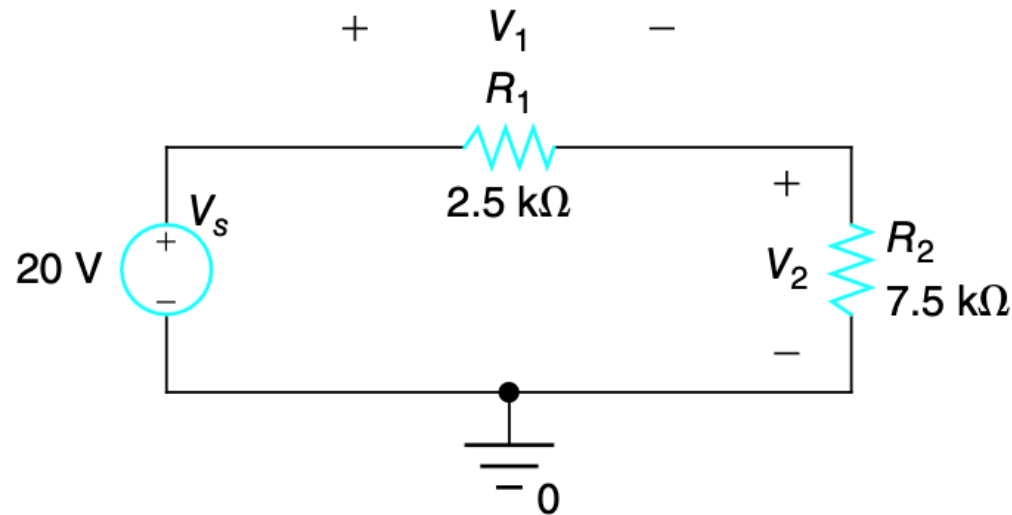
- ❑ The voltage across  $R_i$  is given by

$$V_i = I \times R_i = \frac{V_s}{R_1 + R_2 + \dots + R_n} \times R_i = V_s \times \frac{R_i}{R_1 + R_2 + \dots + R_n}$$

- ❑ The voltage from the voltage source is divided among n resistors in proportion to the resistance values.

## Problem 2.47

□ Use voltage divider rule to find voltage  $V_s$  and  $V_2$  in the circuit

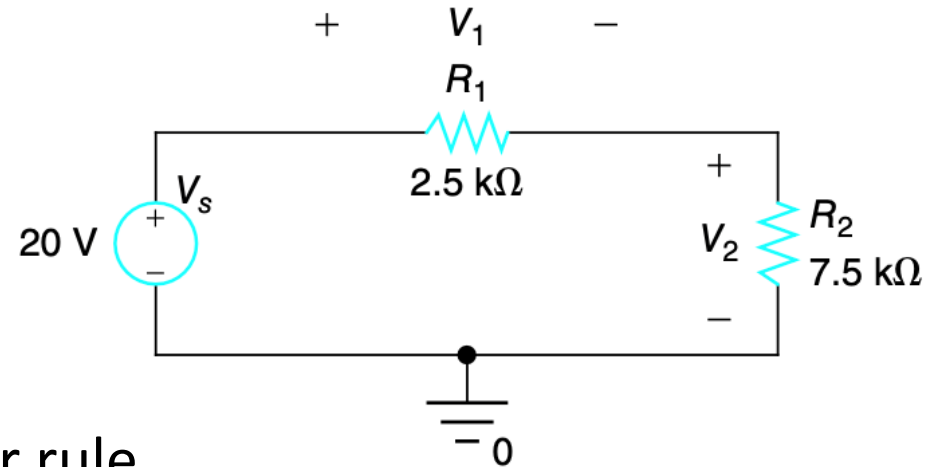


- Options
  - A.  $V_1 = 10, V_2 = 10$
  - B.  $V_1 = 4, V_2 = 16$
  - C.  $V_1 = 5, V_2 = 15$

Solutions will be provided in the class



# Problem 2.47 (Solution)

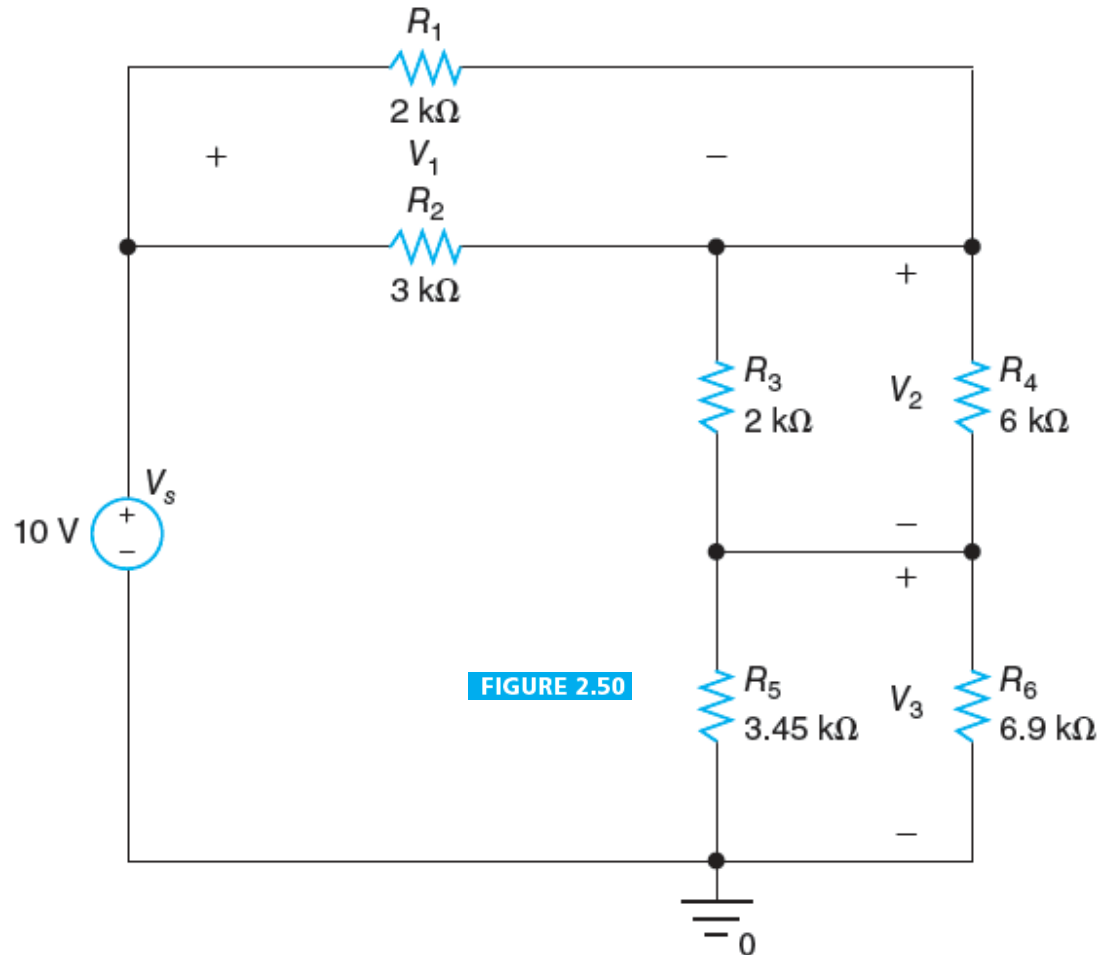


□ According to Voltage divider rule

- $V_1 = V_s \times \frac{R_1}{(R_1 + R_2)}$
- $V_1 = 20 \times \frac{2.5k}{2.5k + 7.5k} = 5V$
- $V_2 = V_s \times \frac{R_2}{(R_1 + R_2)}$
- $V_1 = 20 \times \frac{7.5k}{2.5k + 7.5k} = 15V$

# Circuit Analysis Using Voltage Divider Rule

□ We are interested in finding  $V_1$ ,  $V_2$ , and  $V_3$ .



# Circuit Analysis Using Voltage Divider Rule

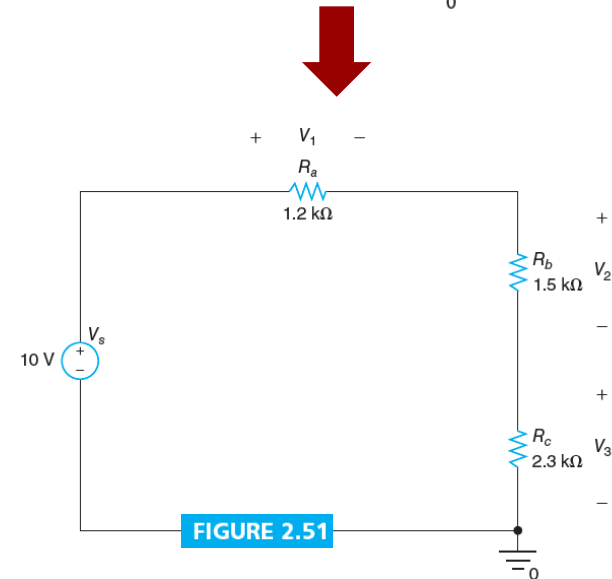
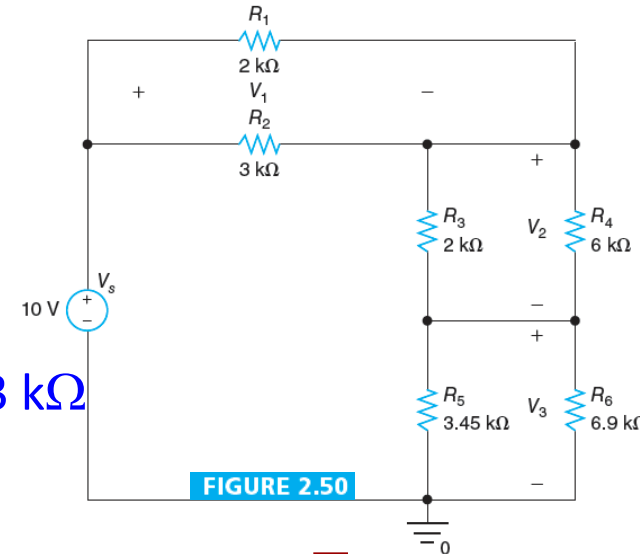
□ We are interested in finding  $V_1$ ,  $V_2$ , and  $V_3$ .

- $R_a = R_1 \parallel R_2 = R_1 \times R_2 / (R_1 + R_2) = 6/5 \text{ k}\Omega = 1.2 \text{ k}\Omega$
- $R_b = R_3 \parallel R_4 = R_3 \times R_4 / (R_3 + R_4) = 12/8 \text{ k}\Omega = 1.5 \text{ k}\Omega$
- $R_c = R_5 \parallel R_6 = R_5 \times R_6 / (R_5 + R_6) = 23.805/10.35 \text{ k}\Omega = 2.3 \text{ k}\Omega$

$$V_1 = V_s \times \frac{R_a}{R_a + R_b + R_c} = 10 \times \frac{1.2}{1.2 + 1.5 + 2.3} \text{ V} = 10 \times \frac{1.2}{5} \text{ V} = 2.4 \text{ V}$$

$$V_2 = V_s \times \frac{R_b}{R_a + R_b + R_c} = 10 \times \frac{1.5}{1.2 + 1.5 + 2.3} \text{ V} = 10 \times \frac{1.5}{5} \text{ V} = 3 \text{ V}$$

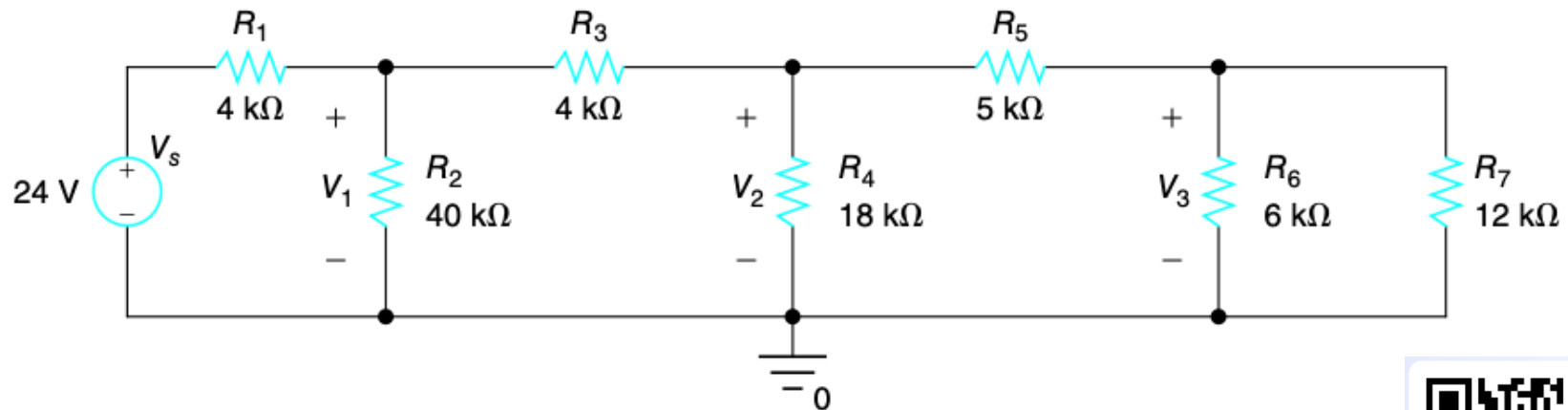
$$V_3 = V_s \times \frac{R_c}{R_a + R_b + R_c} = 10 \times \frac{2.3}{1.2 + 1.5 + 2.3} \text{ V} = 10 \times \frac{2.3}{5} \text{ V} = 4.6 \text{ V}$$



## Problem 2.52

□ Use the voltage divider rule to find voltages  $V_1$

★ Multiple Choice



### Options

- A.  $V_1 = 8 \text{ V}$
- B.  $V_1 = 12 \text{ V}$
- C.  $V_1 = 16 \text{ V}$



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# Problem 2.52 (Solution)

□ First find equivalent resistance

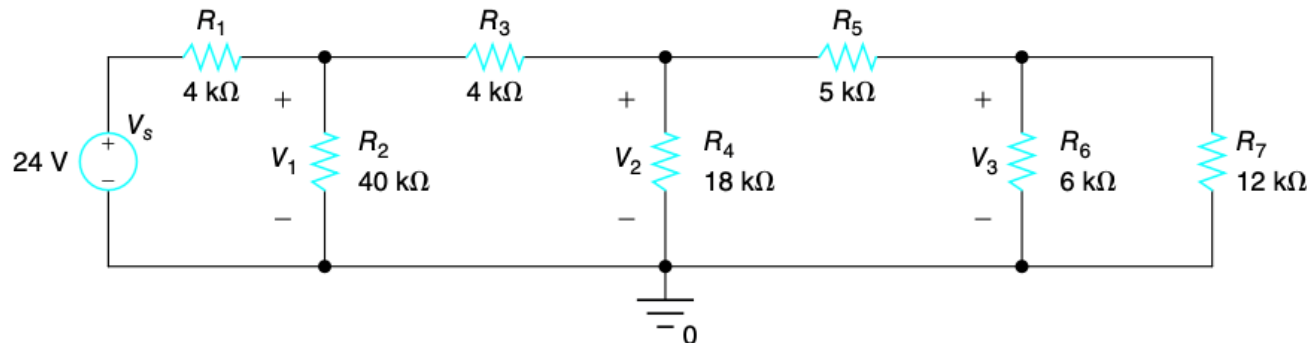
○  $R_a = R_7 || R_6 + R_5 = 6 || 12 + 5 = 9k\Omega$

○  $R_b = R_a || R_4 + R_3 = 9 || 18 + 4 = 10k\Omega$

○  $R_{eq} = R_b || R_2 + R_1 = 10 || 40 + 4 = 8 + 4 = 12k\Omega$

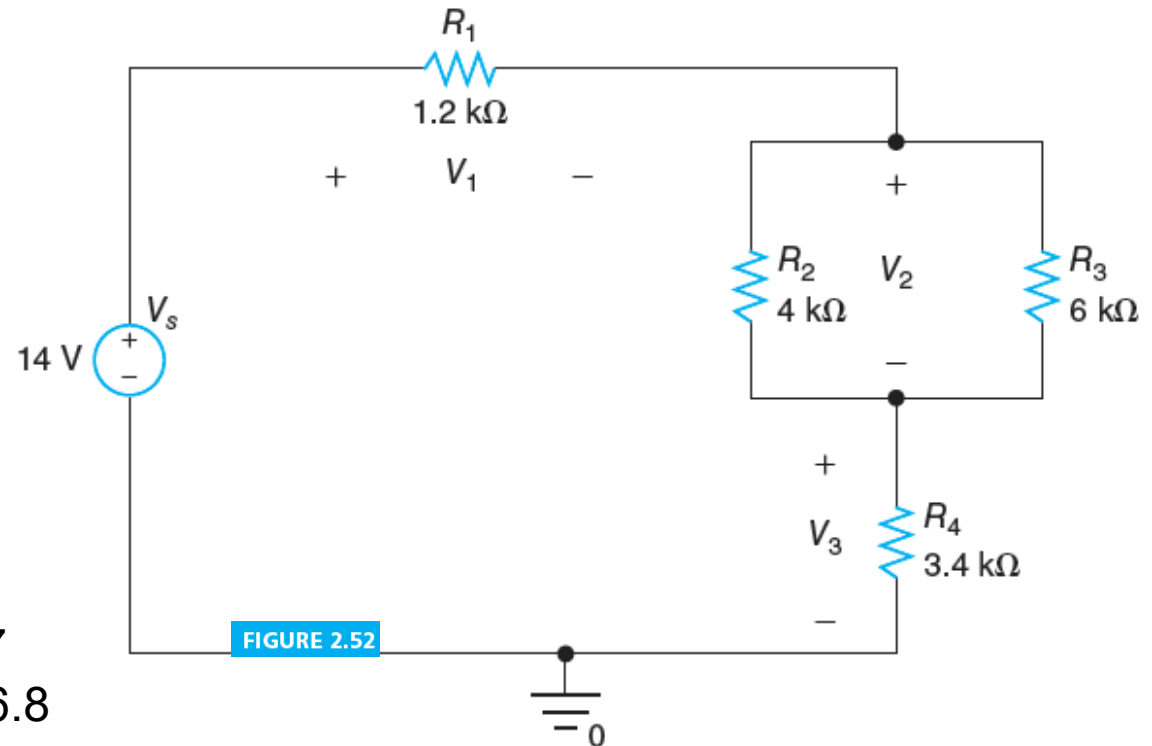
□ Calculate voltage using voltage divider

Solution will be provided in the class



## EXAMPLE 2.15

Find  $V_1$ ,  $V_2$ , and  $V_3$  in the circuit shown in Figure 2.52.



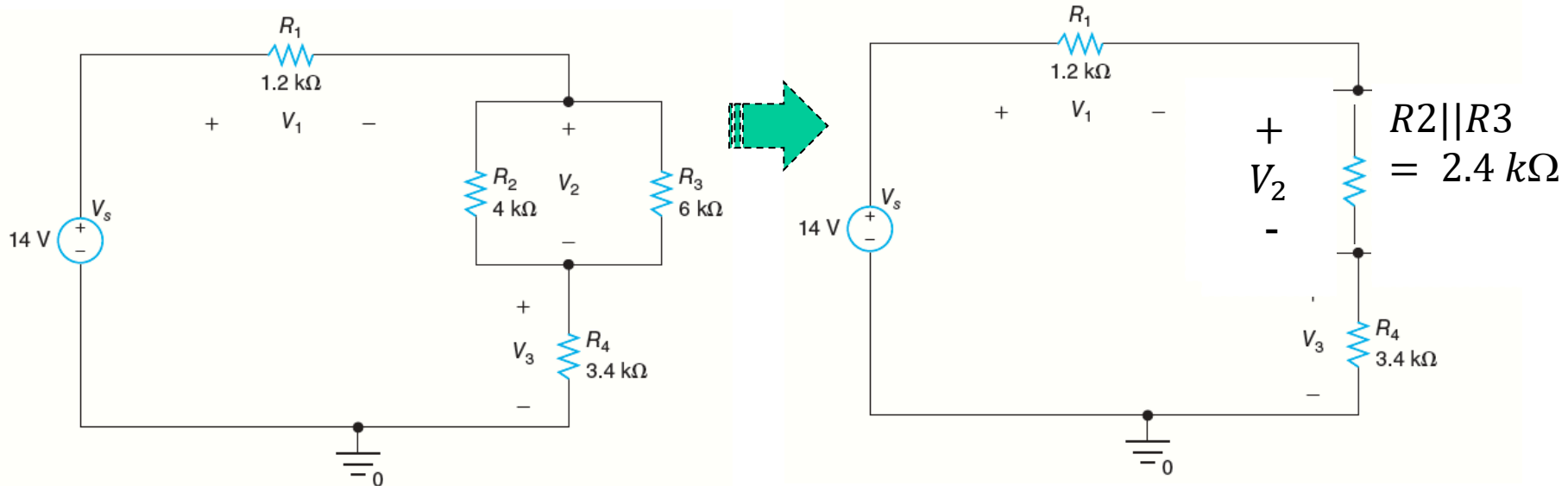
Options

- (A)  $V_1 = 2$ ,  $V_2 = 4$ ,  $V_3 = 8$
- (B)  $V_1 = 2.3$ ,  $V_2 = 4.7$ ,  $V_3 = 7$
- (C)  $V_1 = 2.4$ ,  $V_2 = 4.8$ ,  $V_3 = 6.8$

## EXAMPLE 2.15

Find  $V_1$ ,  $V_2$ , and  $V_3$  in the circuit shown in Figure 2.52.

○  $R_a = R_2 \parallel R_3 = R_2 \times R_3 / (R_2 + R_3) = 24/10 \text{ k}\Omega = 2.4 \text{ k}\Omega$



□ Apply  
Voltage  
divider rule

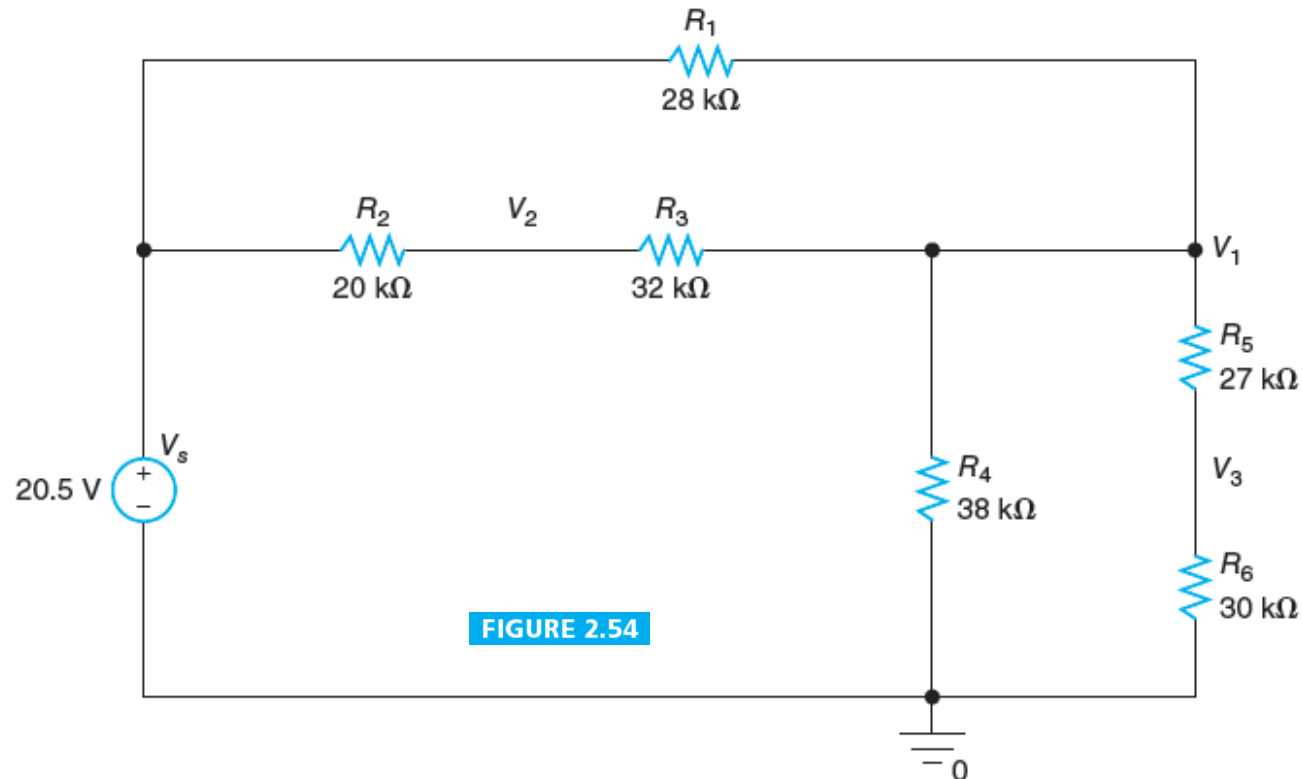
$$V_1 = V_s \times \frac{R_1}{R_1 + R_a + R_4} = 14 \times \frac{1.2}{1.2 + 2.4 + 3.4} \text{ V} = 14 \times \frac{1.2}{7} \text{ V} = 2.4 \text{ V}$$

$$V_2 = V_s \times \frac{R_a}{R_1 + R_a + R_4} = 14 \times \frac{2.4}{1.2 + 2.4 + 3.4} \text{ V} = 14 \times \frac{2.4}{7} \text{ V} = 4.8 \text{ V}$$

$$V_3 = V_s \times \frac{R_4}{R_1 + R_a + R_4} = 14 \times \frac{3.4}{1.2 + 2.4 + 3.4} \text{ V} = 14 \times \frac{3.4}{7} \text{ V} = 6.8 \text{ V}$$

## EXAMPLE 2.16

Find  $V_1$ ,  $V_2$ , and  $V_3$  in the circuit shown in Figure 2.54.





## EXAMPLE 2.16

- ❑ Find  $V_1$ ,  $V_2$ , and  $V_3$  in the circuit shown in Figure 2.54.
- ❑  $R_a = R_1 \parallel (R_2 + R_3) = 28 \times 52 / (28 + 52) \text{ k}\Omega = 18.2 \text{ k}\Omega$
- ❑  $R_b = R_4 \parallel (R_5 + R_6) = 38 \times 57 / (38 + 57) \text{ k}\Omega = 22.8 \text{ k}\Omega$

$$V_1 = V_s \times \frac{R_b}{R_a + R_b} = 20.5 \times \frac{22.8}{18.2 + 22.8} \text{ V} = 20.5 \times \frac{22.8}{41} \text{ V} = 11.4 \text{ V}$$

$$V_2 = V_1 + (V_s - V_1) \times \frac{R_3}{R_2 + R_3} = 11.4 \text{ V} + 9.1 \times \frac{32}{20 + 32} \text{ V} = 11.4 \text{ V} + 5.6 \text{ V} = 17 \text{ V}$$

$$V_3 = V_1 \times \frac{R_6}{R_5 + R_6} = 11.4 \times \frac{30}{27 + 30} \text{ V} = 6 \text{ V}$$

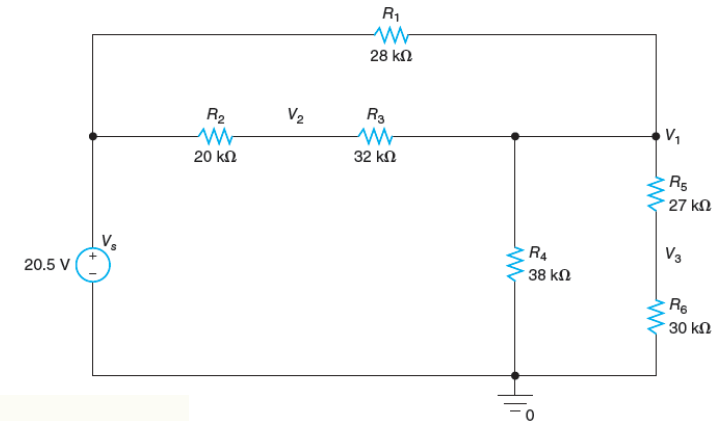


FIGURE 2.54

# Current Divider Rule for Two Resistors in Parallel

- Two resistors are connected in parallel to a current source (Fig.2.58).
- The equivalent resistance of  $R_1$  and  $R_2$  is given by

$$R = R_1 \parallel R_2 = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

- The voltage across  $R_1$  and  $R_2$  is given by

$$V = I_s R = I_s \times \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

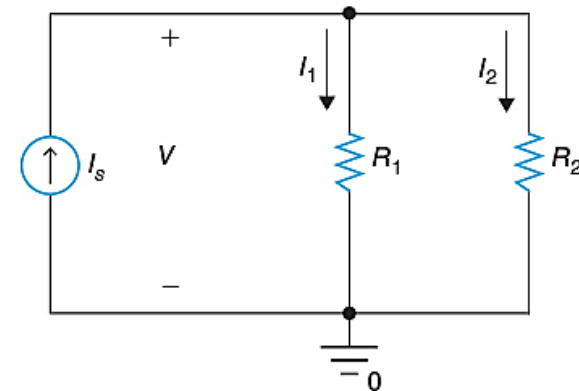
- The current through  $R_1$  and  $R_2$  are given respectively by

$$I_1 = \frac{V}{R_1} = I_s \times \frac{\frac{1}{R_1}}{\frac{1}{R_1} + \frac{1}{R_2}} = I_s \times \frac{G_1}{G_1 + G_2} = I_s \times \frac{R_2}{R_1 + R_2}, \quad I_2 = \frac{V}{R_2} = I_s \times \frac{\frac{1}{R_2}}{\frac{1}{R_1} + \frac{1}{R_2}} = I_s \times \frac{G_2}{G_1 + G_2} = I_s \times \frac{R_1}{R_1 + R_2}$$

- When resistors are in parallel, The current  $I_s$  from the current source is divided between  $R_1$  and  $R_2$  in proportion to the conductance (inverse of resistance) value. More current flows through smaller resistance.

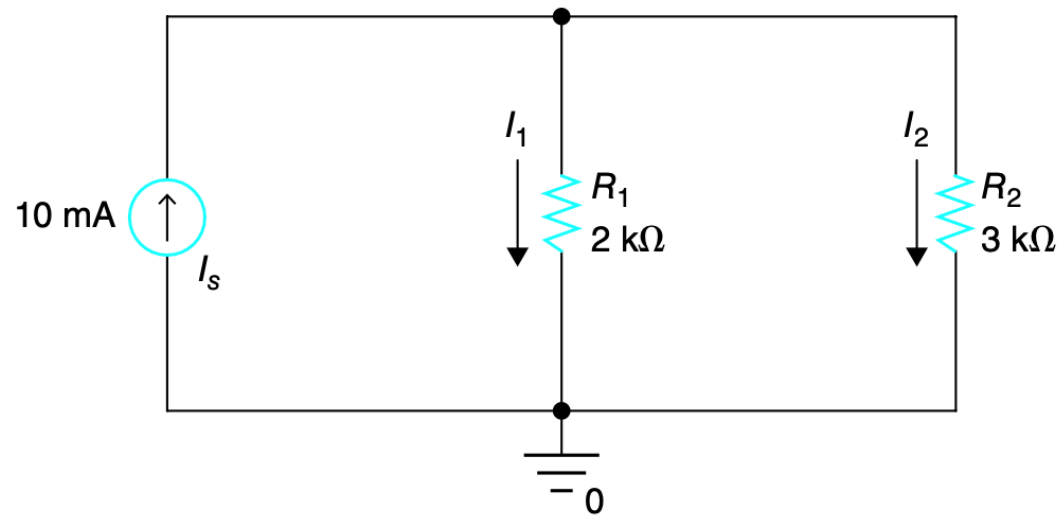
FIGURE 2.58

A circuit with two resistors in parallel.



# Problem 2.58

- Use the current divider rule to find currents  $I_1$  and
- $I_2$  in the circuit shown in the figure



$$\begin{aligned}
 \circ \quad I_1 &= I_s \times \frac{R_2}{R_1 + R_2} = 10 \times 10^{-3} \times \frac{3k}{5k} = 6mA \\
 \circ \quad I_2 &= I_s \times \frac{R_1}{R_1 + R_2} = 10 \times 10^{-3} \times \frac{2k}{5k} = 4mA
 \end{aligned}$$

# Current Divider Rule for n Resistors in Parallel

- n resistors are connected in parallel to a current source with current  $I_s$ .
- The equivalent resistance is given by

$$R = R_1 \parallel R_2 \parallel \dots \parallel R_n = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

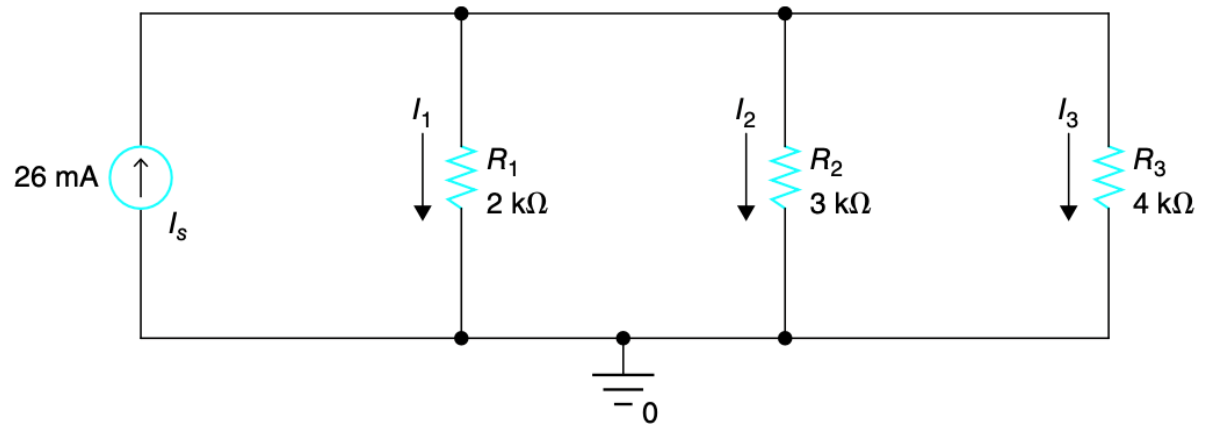
- The voltage across the resistors is given by  $\rightarrow V = I_s R = I_s \times \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$
- The current through the  $i$ th resistor  $R_i$  is

$$I_i = \frac{V}{R_i} = I_s \times \frac{\frac{1}{R_i}}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} = I_s \times \frac{G_i}{G_1 + G_2 + \dots + G_n}$$

- The current  $I_s$  from the current source is divided between resistors in proportion to the conductance (inverse of resistance) values.

# Problem 2.59

□ Use the current divider rule to find currents  $I_1$ ,  $I_2$  and  $I_3$  in the circuit



$$\circ I_1 = I_s \times \frac{\frac{1}{R_1}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = 26 \times 10^{-3} \times \frac{12k}{2k} \times \frac{1}{13} = 12mA$$

$$\circ I_2 = I_s \times \frac{\frac{1}{R_2}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = 26 \times 10^{-3} \times \frac{12k}{3k} \times \frac{1}{13} = 8mA$$

$$\circ I_3 = I_s \times \frac{\frac{1}{R_3}}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} = 26 \times 10^{-3} \times \frac{12k}{4k} \times \frac{1}{13} = 6mA$$

# Problem

□ Find  $I_1$ ,  $I_2$ ,  $I_3$  in the circuit shown in Figure 2.59.

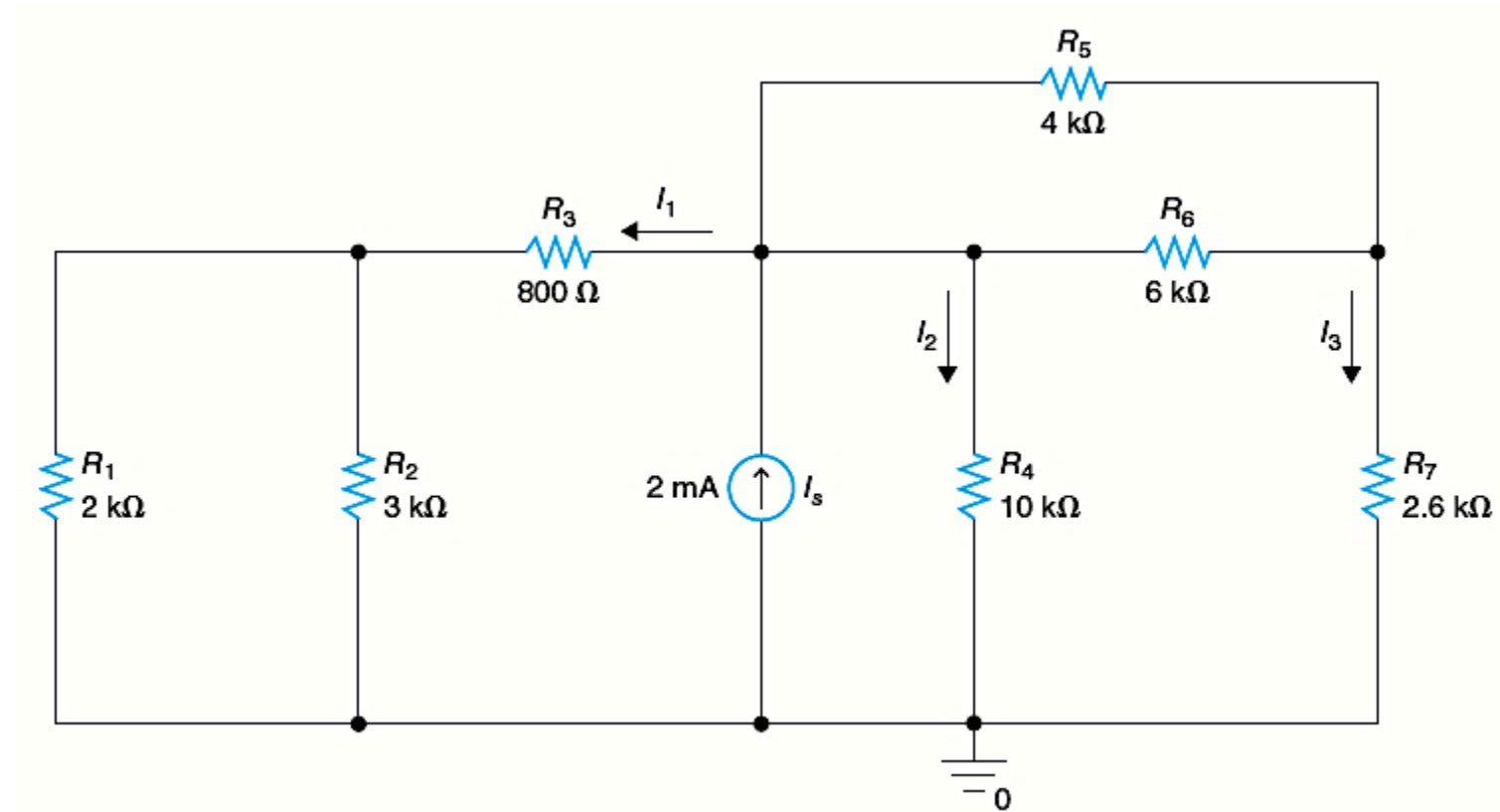


FIGURE 2.59

# Circuit Analysis Using Current Divider Rule

Find  $I_1$ ,  $I_2$ ,  $I_3$  in the circuit shown in Figure 2.59.

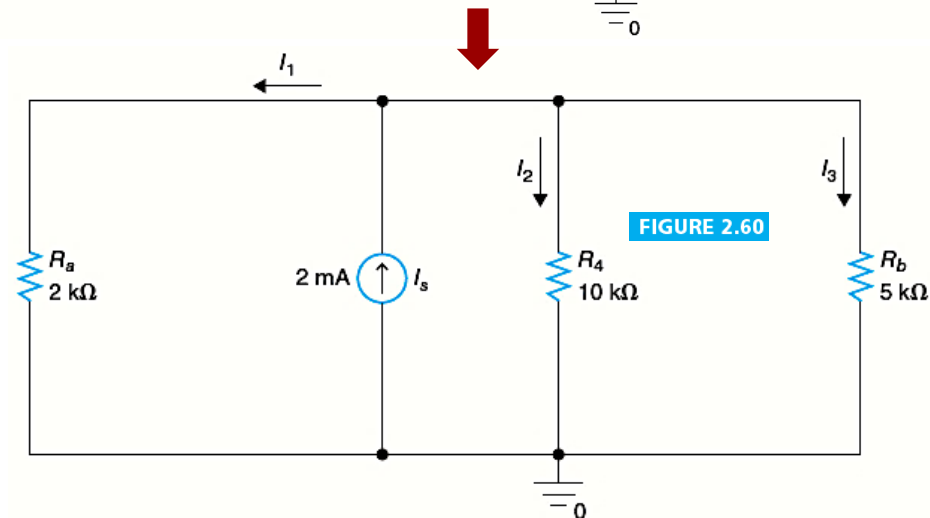
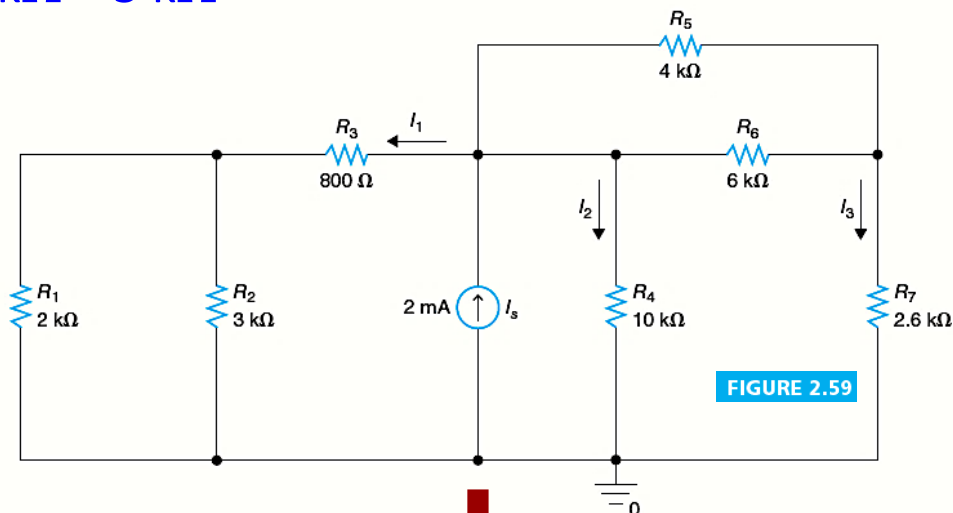
$R_a = R_3 + (R_1 \parallel R_2) = 0.8 \text{ k}\Omega + 1.2 \text{ k}\Omega = 2 \text{ k}\Omega$

$R_b = R_7 + (R_5 \parallel R_6) = 2.6 \text{ k}\Omega + 2.4 \text{ k}\Omega = 5 \text{ k}\Omega$

$$I_1 = I_s \times \frac{\frac{1}{R_a}}{\frac{1}{R_a} + \frac{1}{R_4} + \frac{1}{R_b}} = 2 \times \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{10} + \frac{1}{5}} \text{ mA} = 2 \times \frac{5}{8} \text{ mA} = 1.25 \text{ mA}$$

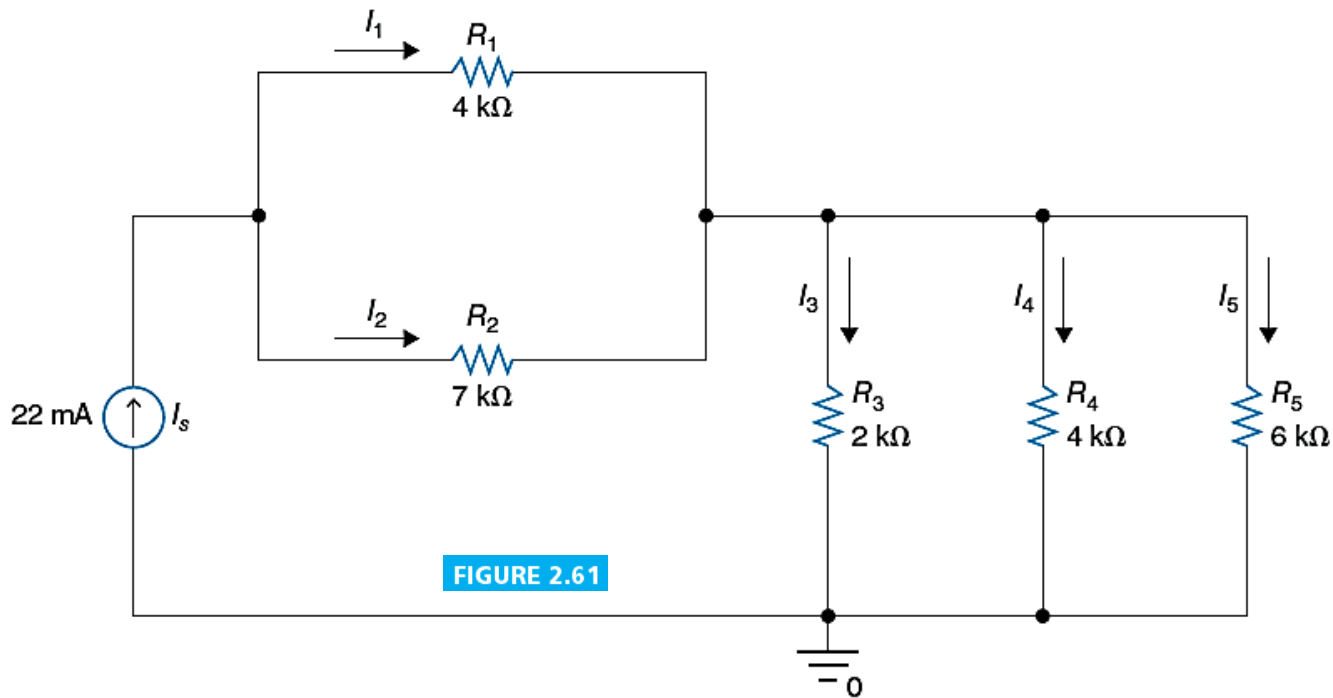
$$I_2 = I_s \times \frac{\frac{1}{R_4}}{\frac{1}{R_a} + \frac{1}{R_4} + \frac{1}{R_b}} = 2 \times \frac{\frac{1}{10}}{\frac{1}{2} + \frac{1}{10} + \frac{1}{5}} \text{ mA} = 2 \times \frac{1}{8} \text{ mA} = 0.25 \text{ mA}$$

$$I_3 = I_s \times \frac{\frac{1}{R_b}}{\frac{1}{R_a} + \frac{1}{R_4} + \frac{1}{R_b}} = 2 \times \frac{\frac{1}{5}}{\frac{1}{2} + \frac{1}{10} + \frac{1}{5}} \text{ mA} = 2 \times \frac{2}{8} \text{ mA} = 0.5 \text{ mA}$$



## EXAMPLE 2.17

□ In the circuit shown in Fig.2.61, use the current divider rule to find the currents  $I_1$ ,  $I_2$ ,  $I_3$ ,  $I_4$ ,  $I_5$ .



Find the value of  $I_5$ ?

(A) 4 mA  
 (B) 6 mA  
 (C) 12 mA



## EXAMPLE 2.17

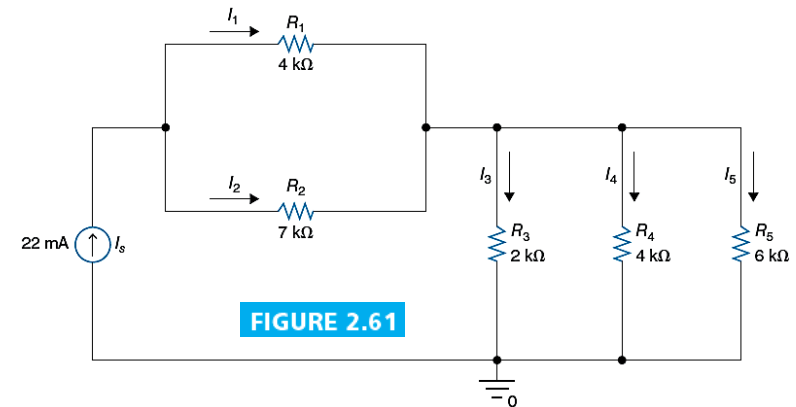
□ In the circuit shown in Fig.2.61, use the current divider rule to find the currents  $I_1$ ,  $I_2$ ,  $I_3$ ,  $I_4$ ,  $I_5$ .

$$I_1 = I_s \times \frac{R_2}{R_1 + R_2} = 22 \times \frac{7}{4 + 7} \text{ mA} = 22 \times \frac{7}{11} \text{ mA} = 14 \text{ mA} \quad I_2 = I_s \times \frac{R_1}{R_1 + R_2} = 22 \times \frac{4}{4 + 7} \text{ mA} = 22 \times \frac{4}{11} \text{ mA} = 8 \text{ mA}$$

$$I_3 = I_s \times \frac{\frac{1}{R_3}}{\frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5}} = 22 \times \frac{\frac{1}{2}}{\frac{1}{2} + \frac{1}{4} + \frac{1}{6}} \text{ mA} = 22 \times \frac{6}{11} \text{ mA} = 12 \text{ mA}$$

$$I_4 = I_s \times \frac{\frac{1}{R_4}}{\frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5}} = 22 \times \frac{\frac{1}{4}}{\frac{1}{2} + \frac{1}{4} + \frac{1}{6}} \text{ mA} = 22 \times \frac{3}{11} \text{ mA} = 6 \text{ mA}$$

$$I_5 = I_s \times \frac{\frac{1}{R_5}}{\frac{1}{R_3} + \frac{1}{R_4} + \frac{1}{R_5}} = 22 \times \frac{\frac{1}{6}}{\frac{1}{2} + \frac{1}{4} + \frac{1}{6}} \text{ mA} = 22 \times \frac{2}{11} \text{ mA} = 4 \text{ mA}$$



## EXAMPLE 2.18

- Find  $I_1, I_2, I_3, I_4, I_5, I_6, I_7, I_8, I_9$  in the circuit shown in Figure 2.63.
- $R_a = R_2 + (R_3 \parallel R_4) = 3 \text{ k}\Omega$
  - $R_b = (R_5 \parallel R_6) + (R_7 \parallel R_8) = 3 \text{ k}\Omega + 2 \text{ k}\Omega = 5 \text{ k}\Omega$
  - Application of current divider rule on  $R_1, R_a, R_b$ , we obtain

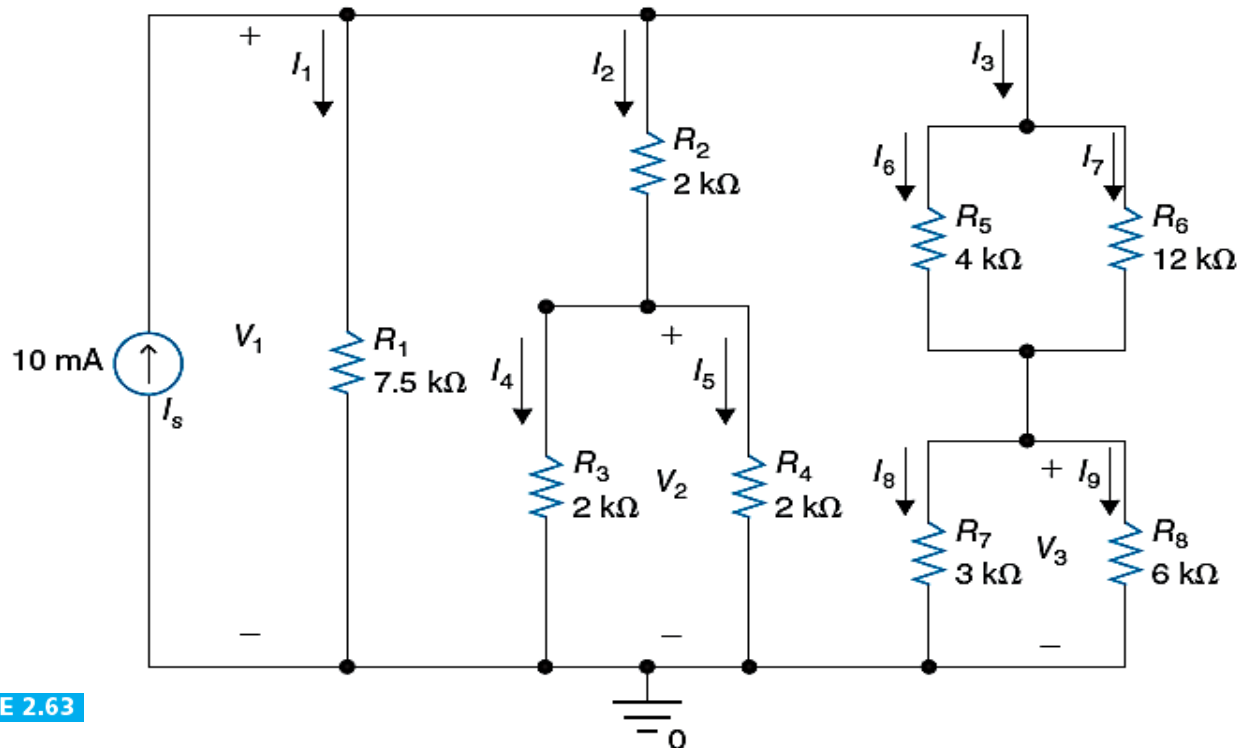


FIGURE 2.63

## EXAMPLE 2.18

Find  $I_1, I_2, I_3, I_4, I_5, I_6, I_7, I_8, I_9$  in the circuit shown in Figure 2.63.

- $R_a = R_2 + (R_3 \parallel R_4) = 3 \text{ k}\Omega$
- $R_b = (R_5 \parallel R_6) + (R_7 \parallel R_8) = 3 \text{ k}\Omega + 2 \text{ k}\Omega = 5 \text{ k}\Omega$
- Application of current divider rule on  $R_1, R_a, R_b$ , we obtain

$$I_1 = I_s \times \frac{\frac{1}{R_1}}{\frac{1}{R_1} + \frac{1}{R_a} + \frac{1}{R_b}} = 10 \times \frac{\frac{1}{7.5}}{\frac{1}{7.5} + \frac{1}{3} + \frac{1}{5}} \text{ mA} = 10 \times \frac{2}{10} \text{ mA} = 2 \text{ mA}$$

$$I_2 = I_s \times \frac{\frac{1}{R_a}}{\frac{1}{R_1} + \frac{1}{R_a} + \frac{1}{R_b}} = 10 \times \frac{\frac{1}{3}}{\frac{1}{7.5} + \frac{1}{3} + \frac{1}{5}} \text{ mA} = 10 \times \frac{5}{10} \text{ mA} = 5 \text{ mA}$$

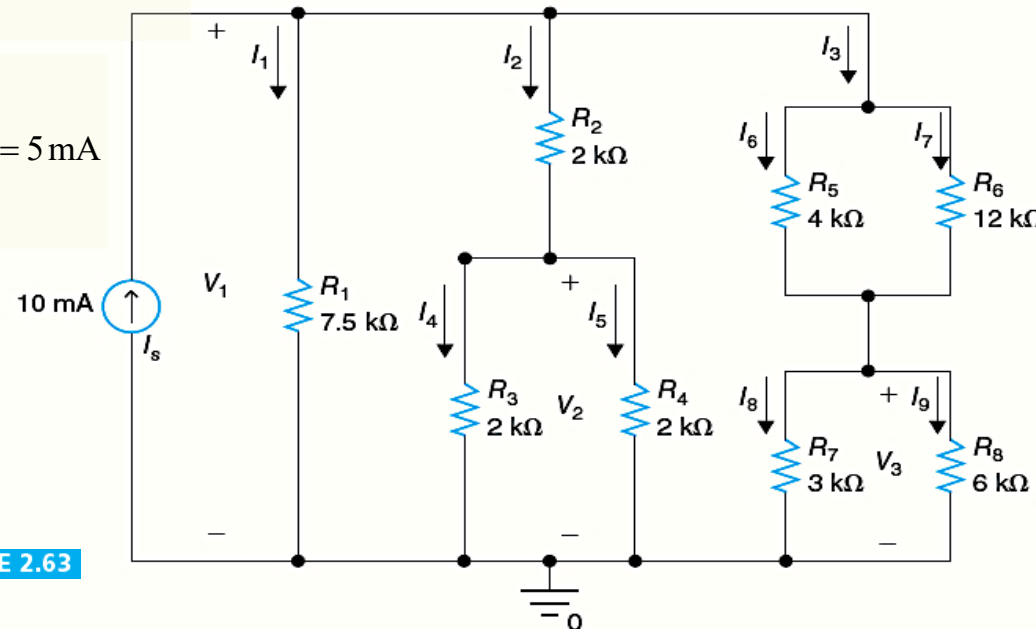
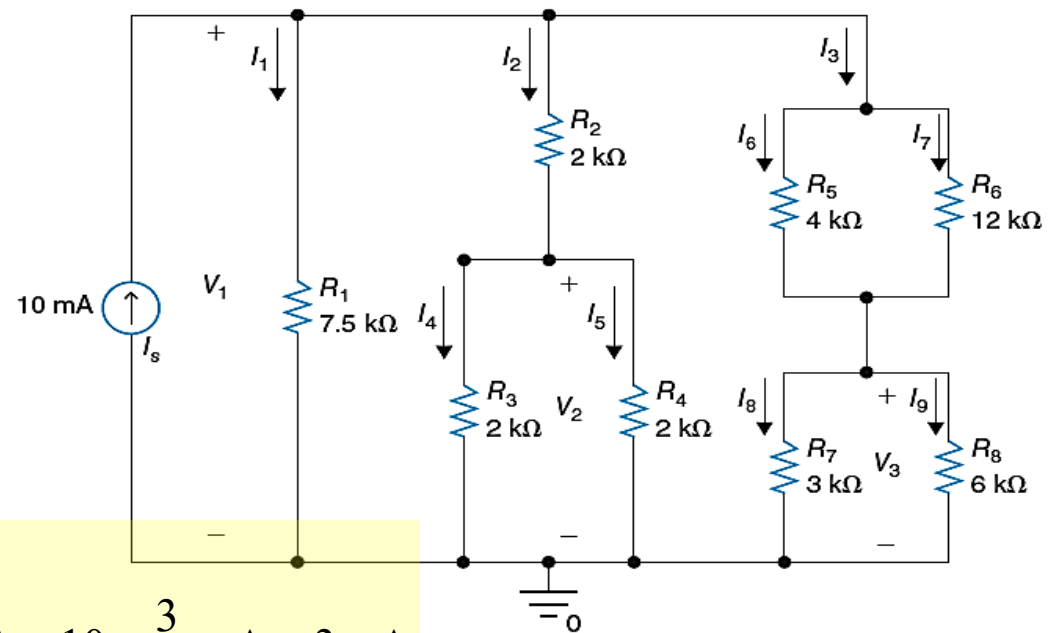


FIGURE 2.63

# EXAMPLE 2.18 (Continued)

FIGURE 2.63



$$I_3 = I_s \times \frac{\frac{1}{R_b}}{\frac{1}{R_1} + \frac{1}{R_a} + \frac{1}{R_b}} = 10 \times \frac{\frac{1}{5}}{\frac{1}{7.5} + \frac{1}{3} + \frac{1}{5}} \text{ mA} = 10 \times \frac{3}{10} \text{ mA} = 3 \text{ mA}$$

$$I_4 = I_2 \times \frac{R_4}{R_3 + R_4} = 2.5 \text{ mA} = I_5$$

$$I_6 = I_3 \times \frac{R_6}{R_5 + R_6} = 2.25 \text{ mA}, I_7 = 0.75 \text{ mA}$$

$$I_8 = I_3 \times \frac{R_8}{R_7 + R_8} = 2 \text{ mA}, I_9 = 1 \text{ mA}$$

Home work P2.58 to P2.67

# Summary of key concepts weeks 2-3

## □ Resistance (definition and physical meaning)

$$R = \frac{\ell}{\sigma A} = \frac{\ell \rho}{A}$$

## □ Ohm's law

$$V = RI, \quad I = \frac{V}{R}, \quad R = \frac{V}{I}$$

## □ KCL

The sum of currents entering a node equals the sum of currents leaving the same node.

The sum of currents leaving a node is zero.

The sum of currents entering a node is zero.

# Summary (Continued)

## □ KVL

The sum of voltage drops around a loop or mesh is equal to zero.

## □ Equivalent resistance of series connection of n resistors

$$R_{eq} = R_1 + R_2 + \dots + R_n$$

## □ Equivalent resistance of parallel connection of two resistors

$$R_{eq} = R_1 \parallel R_2 = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} = \frac{R_1 R_2}{R_1 + R_2}$$

# Summary (Continued)

- Equivalent resistance of parallel connection of n resistors

$$R_{eq} = R_1 \parallel R_2 \parallel \dots \parallel R_n = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$

- **Voltage divider** rule (two resistors are connected in series to a voltage source)

$$V_1 = V_s \times \frac{R_1}{R_1 + R_2}, \quad V_2 = V_s \times \frac{R_2}{R_1 + R_2}$$

- **Voltage divider** rule (n resistors are connected in series to a voltage source)

$$V_i = V_s \times \frac{R_i}{R_1 + R_2 + \dots + R_n}$$

## Summary (Continued)

❑ **Current divider** rule (two resistors are connected in parallel to a current source)

$$I_1 = I_s \times \frac{\frac{1}{R_1}}{\frac{1}{R_1} + \frac{1}{R_2}} = I_s \times \frac{R_2}{R_1 + R_2}, \quad I_2 = I_s \times \frac{\frac{1}{R_2}}{\frac{1}{R_1} + \frac{1}{R_2}} = I_s \times \frac{R_1}{R_1 + R_2}$$

❑ **Current divider** rule (n resistors are connected in parallel to a current source)

$$I_i = I_s \times \frac{\frac{1}{R_i}}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}}$$



# Summary (Continued)

□ What will we study in next lecture.