

L1—wtr

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April 2019

1 Introduction to Machine Learning

Brief Introduction to Machine Learning

Machine learning algorithms are used in a wide variety of applications, such as email filtering, and computer vision, where it is *infeasible to develop an algorithm of specific instructions for performing the task*.

classification for discrete data

regression for continuous data

Basic Terminology

Attribute = Attribute value such as color shape weight

Samples data set such as melon1 melon2 and so on

Feature vector such as a melon with green color , big shape , high weight

Hold-out

We divide the whole sample set into two parts, training set and testing set.

Method 1 Cross validation

1 Divide the dataset into k subsets(mutually exclusive)

2 Each time, the combination of (k - 1) subsets is used as the training set, the last one as the testing set

3 K-fold cross validation

4 LOO (leave one out) (in which $k == m$; number of samples)

5 $K = 10$ (usually)

Method 2 Bootstrapping

1 Dataset D (m samples) -> generate D'

2 For i in range (m)

3 Randomly select a sample s, and place its copy into D'

4 End

5 About 36.8 percent of samples don't appear in D'

Bias-variance

Expectation of the learning algorithm

$$f^*(x) = E_D[f(x; D)]$$

Variance

$$var(x) = E_D[(f(x; D) - f^*(x))^2]$$

Noise

$$e^2 = E_D[(y_d - y)^2]$$

Bias(difference between expected output and actual label)

$$bias^2 = (f^*(x) - y)^2$$

Conclusion

$$E(f; D) = bias^2 + var(x) + e^2$$

DecisionTree

A decision tree = root node + internal node + leaf node

Node set - leaf node - Each node corresponds to an attribute test

Leaf Node set - Each node corresponds to an output

Input: Training data set $D = \{x_1, y_1, x_2, y_2, \dots, x_n, y_n\}$

Attribute set $A = \{a_1, a_2, a_3, \dots\}$

Function : $Generate_Tree(D, A)$

generatenode

if(all samples in D are in the same class C) **then**

label node as C node **return**

end if

if A is empty **OR** all samples in D have same attributes in A **then**

label node as a leaf node, classify it as a class with the most samples in D

end if

select the best attribute in A (how to select it will be introduced later)

for every a^* **do** create a branch for node ; make D_v represent for sample set

where $a^* = a_v^*$

if D_v is empty **then**

label it as leaf node ; label the class which receives most samples **return**

else $Generate_Tree(D_v, A - a_n)$

end if

end for

Information Entropy

We use this to evaluate the gain of information, in order to decide which attribute fits best.

$$Gain(D, a) = Ent(D) - \sum_{v=1}^V Ent(D^v) \cdot |D_v| / |D|$$

Among those attributes, we chose the attribute with the largest $Gain(D, a)$.

Pruning

Pruning is mainly divided into two kinds, prepruning and postpruning.

The purpose is to improve the generalizing ability of decision trees.

We need to find a balance between low learning rate and high learning rate.

If the learning rate is too low, the model is not effective enough.

If the learning rate is too high, the model will mistaken some special attributes as general attributes,

