Machine Learning Lab

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Candidate Elimination Algorithm

Terms Used:

- 1. Concept learning: Concept learning is basically learning task of the machine (Learn by Train data)
- 2. **General Hypothesis**: Not Specifying features to learn the machine.
- 3. $G = \{??, ??,??,??...\}$: Number of attributes
- 4. **Specific Hypothesis**: Specifying features to learn machine (Specific feature)
- 5. **S**= {'pi', 'pi', 'pi'...}: Number of pi depends on number of attributes.
- 6. **Version Space**: It is intermediate of general hypothesis and Specific hypothesis. It not only just written one hypothesis but a set of all possible hypothesis based on training data-set.

Algorithm:

```
In [1]: #import usful packages
        import numpy as np
        import pandas as pd
In [2]: |#read data set
        df = pd.read csv('data/ce.csv')
In [3]: #preview dataset
Out[3]:
                  airtemp humidity
                                   wind water forcast enjoysport
              sky
                            normal strong
                                                            Yes
         0 sunny
                    warm
                                         warm
                                                same
                                                            Yes
         1 sunny
                    warm
                             high strong
                                         warm
                                                same
         2
             rainy
                     cold
                             high
                                  strong
                                         warm change
                                                            No
         3 sunny
                                                            Yes
                    warm
                             high strong
                                          cool change
In [4]: |#defining algorithm
        def candidate_elimination(con,tar):
             for i,val in enumerate(tar):
                 if val == 'Yes':
                     specific_h = con[i].copy()
                     break
             general_h = [["?" for i in range(len(specific_h))] for i in range(len(specific_h))
             for i, val in enumerate(con):
                 if tar[i] == "Yes":
                     for j in range(len(specific h)):
                         if val[j]!= specific_h[j]:
                              specific h[i] ='?'
                             general_h[j][j] ='?'
                 if tar[i] == "No":
                     for j in range(len(specific h)):
                         if val[j]!= specific h[j]:
                              general h[j][j] = specific h[j]
                         else:
                              general_h[j][j] = '?'
             return specific h,general h
In [5]: #run algorithm
        con = np.array(df)[:,:-1]
```

```
In [5]: #run algorithm
    con = np.array(df)[:,:-1]
    tar = np.array(df)[:,-1]
    spe_h,gen_h = candidate_elimination(con,tar)
```

Find-S algorithm:

Important Representation:

- 1. ? indicates that any value is acceptable for the attribute.
- 2. specify a single required value (e.g., Cold) for the attribute.
- 3. φ indicates that no value is acceptable.
- 4. The most general hypothesis is represented by: {?, ?, ?, ?, ?}
- 5. The most specific hypothesis is represented by : $\{\phi, \phi, \phi, \phi, \phi, \phi\}$

Algorithm:

- 1. Initialize h to the most specific hypothesis in H
- 2. For each positive training instance x For each attribute constraint a, in h

```
If the constraint a, is satisfied by \mathbf{x} Then do nothing Else replace a, in h by the next more general constraint that is satisfied by \mathbf{x}
```

3. Output hypothesis h

```
In [7]: #import usful packages

import numpy as np
import pandas as pd
```

```
In [8]: #read data set
         df = pd.read csv('data/fs.csv')
 In [9]: #preview dataset
          df
 Out[9]:
              Color Toughness Fungus Appearance Poisonous
              Green
                          Hard
                                   No
                                          Wrinkled
                                                        Yes
          1
                          Hard
                                  Yes
                                          Smooth
              Green
                                                        No
                                          Wrinkled
          2
              Brown
                          Soft
                                   No
                                                        No
          3 Orange
                          Hard
                                   No
                                          Wrinkled
                                                        Yes
              Green
                          Hard
                                  Yes
                                          Wrinkled
                                                        Yes
          5 Orange
                          Hard
                                   No
                                          Wrinkled
                                                        Yes
In [10]: | # find s algo
          def find_s(con,tar):
              for i,val in enumerate(tar):
                  if val == 'Yes':
                      specific_h = con[i].copy()
                      break
              for i,val in enumerate(con):
                  if tar[i] == 'Yes':
                      for j,feat in enumerate(val):
                           if specific_h[j] != feat:
                               specific_h[j] = '?'
                      print(specific_h)
              return specific_h
In [11]: #run algorithm
          con = np.array(df)[:,:-1]
         tar = np.array(df)[:,-1]
          gen_h = find_s(con,tar)
          ['Green' 'Hard' 'No' 'Wrinkled']
          ['?' 'Hard' 'No' 'Wrinkled']
          ['?' 'Hard' '?' 'Wrinkled']
          ['?' 'Hard' '?' 'Wrinkled']
In [12]: #see result
         gen h
Out[12]: array(['?', 'Hard', '?', 'Wrinkled'], dtype=object)
```

A. Simple Linear Analysis (From Scratch)

```
In [1]: #import package
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

Suppose the required regression line equation is :

$$y = m. x + b$$

There are two equations called normal equation from which we can find m and b:

$$\Sigma XY = b. \Sigma X + m. \Sigma X^{2} \qquad \dots (1)$$

$$\Sigma Y = n. b + m. \Sigma X \qquad \dots (2)$$

Or we can solve the two equation for m and b as:

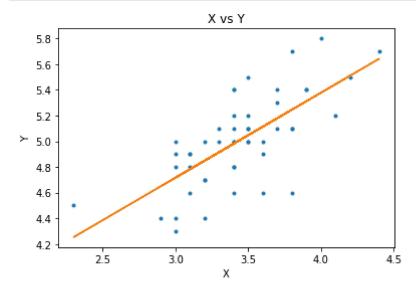
$$m = \frac{n. \Sigma xy - \Sigma x. \Sigma y}{n. \Sigma x^2 - (\Sigma x)^2}$$
$$b = \overline{y} - m. \overline{x}$$

```
In [3]: #Calculate m and b for y = mx+b
X = np.array(df['X'])
Y = np.array(df['Y'])

m = ((len(X)*sum(X*Y)) - sum(X)*sum(Y))/((len(X)*sum(X**2)) - (sum(X)**2))
b = np.mean(Y)- m*np.mean(X)
```

```
In [4]: # append calculated y column in df
df['Y_h'] = m*X + b
```

```
In [5]: #plot data points and y=mx+b line
plt.plot(df['X'],df['Y'],'.')
plt.plot(df['X'],df['Y_h'],'-')
plt.xlabel("X");
plt.ylabel("Y");
plt.title("X vs Y");
```



B. Multiple Linear Regression (From Scratch)

```
In [6]: df1 = pd.read_csv("data/mlr.csv")
    df1.head()
```

Out[6]:

	X1	X2	Х3	X4	X5
0	6.8	225	0.442	0.672	9.2
1	6.3	180	0.435	0.797	11.7
2	6.4	190	0.456	0.761	15.8
3	6.2	180	0.416	0.651	8.6
4	6.9	205	0.449	0.900	23.2

Data Description

```
The following data (X1, X2, X3, X4, X5) are for each player.

X1 = height in feet

X2 = weight in pounds

X3 = percent of successful field goals (out of 100 attempted)

X4 = percent of successful free throws (out of 100 attempted)

X5 = average points scored per game

X = np.array(df1.drop('X5',axis = 1))
```

$$y = b_0 + x_1b_1 + x_2b_2 + \cdots$$
$$Y = Xb$$

$$\mathbf{X} = \begin{bmatrix} 1 & X_1 & X_2 & \cdots \\ 1 & \cdots & \cdots & \cdot \\ \vdots & \vdots & \ddots & \vdots \\ 1 & \cdots & \cdots & \cdots \end{bmatrix}$$

$$\mathbf{Y} = \begin{bmatrix} Y_1 \\ Y_2 \\ \vdots \\ Y_n \end{bmatrix}$$

$$\mathbf{B} = \begin{bmatrix} b_0 & b_1 & b_2 \cdots \end{bmatrix}$$

```
In [8]: b = np.linalg.inv(X.T@X)@X.T@Y
Out[8]: array([ 4.14870671e+00, -3.69049908e+00, 9.45845788e-03, 4.79401992e+01,
                1.13710193e+01])
In [9]: | Y_pred = X@b
        Y_pred
Out[9]: array([10.01235894, 12.51777389, 12.84069605, 10.3157912 , 12.38231366,
               12.18928646, 14.76231003, 12.2882684 , 11.06248103, 13.80102549,
               12.92521215, 13.24396498, 8.64006433, 12.60525851, 12.92430257,
               15.2545908 , 15.58138272 , 5.09650334 , 9.94940424 , 12.49696124 ,
                9.05637536, 10.25083143, 8.06191203, 10.07255781, 14.74963484,
               12.07610898, 13.95300287, 8.71473239, 11.3419041 , 14.40707455,
               15.27283126, 10.4123043 , 13.64991307, 10.25083143, 8.97445925,
               14.70763753, 14.90726563, 13.253166 , 7.32888666, 6.6597904 ,
                8.95334041, 5.83073166, 13.82675288, 16.36627839, 12.00928465,
               10.11871685, 17.63471509, 9.70871125, 8.95738083, 14.73644788,
               15.93275941, 12.25972646, 11.34188054, 10.03210379])
```

$$R^{2} = \frac{\Sigma (\hat{Y} - \overline{Y})^{2}}{\Sigma (Y - \overline{Y})^{2}}$$

```
In [10]: Y_mean = np.mean(Y)

R2 = (np.sum((Y_pred-Y_mean)**2))/(np.sum((Y-Y_mean)**2))
    print(f"R^2 value is {R2}")
```

R^2 value is 0.22225063130014133

Linear Regression Using SKLearn

1. Read Data

n	ud	- 1	- 1	1	- 1	
v	u	u				
			-		-	

	age	sex	bmi	children	smoker	region	charges
0	19	0	27.900	0	1	3	16884.92400
1	18	1	33.770	1	0	2	1725.55230
2	28	1	33.000	3	0	2	4449.46200
3	33	1	22.705	0	0	1	21984.47061
4	32	1	28.880	0	0	1	3866.85520

```
In [12]: df_3.info()
```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 348 entries, 0 to 347
Data columns (total 7 columns):

#	Column	Non-Null Count	Dtype
0	age	348 non-null	int64
1	sex	348 non-null	int64
2	bmi	348 non-null	float64
3	children	348 non-null	int64
4	smoker	348 non-null	int64
5	region	348 non-null	int64
6	charges	348 non-null	float64

dtypes: float64(2), int64(5)

memory usage: 19.2 KB

2. Import Linear Regressor and Split Data Set

```
In [13]: | from sklearn.linear_model import LinearRegression
         from sklearn.model selection import train test split
In [14]: | X = df_3.drop('charges', axis = 1)
         Y = df 3['charges']
In [15]: X_train,X_test,Y_train,Y_test = train_test_split(X,Y, test_size = 0.3)
         3. Train Linear Regrression Model
In [16]: |lr_model = LinearRegression()
In [17]: |lr_model.fit(X_train,Y_train)
Out[17]: LinearRegression()
         4. Predict and check Model
In [18]: |loc = 10
         x = X_test.iloc[loc]
         y = Y_test.iloc[loc]
         y_pred = lr_model.predict([x])
In [19]: | print(f'x = {x.values}\ny = {y}\nPredicted Value = {y_pred[0]}')
                    0. 28.9 0.
                                   0. 3.]
         x = [19.
         y = 1743.214
         Predicted Value = 1913.0976139823597
In [20]: print(f'Score of Model = {Ir model.score(X test,Y test)}')
         Score of Model = 0.7750219073416568
```

Locally Weight Regression (From Scretch)

```
In [1]: # import useful module
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

Algorithm

Locally weighted Regression is a non parametric Regression Algorithms in which we need data every time we calculate matrix.

Cost Function in Linear Regression:

$$\mathbf{costfn} = \Sigma (y_i - \theta x_i)^2$$

Cost Function for Locally Weighted Regression:

$$\mathbf{costfn} = \Sigma w_i (y_i - \theta x_i)^2$$

where x_i , y_i is the $i^t h$ example and w_i is weight. Generally

$$w_i = e^{-\frac{(x_i - x)^2}{2\tau^2}}$$

by minimize costfn for θ and solving expression we get

$$\theta = (X^T W X)^{-1} (X^T W Y)$$

And prediction is $y = X\theta$.

```
In [2]: def w_i(point,X,tau):
    m,n = X.shape
    w = np.mat(np.eye(m))

    for j in range(m):
        diff = X[j]-point
        w[j, j] = np.exp(diff * diff.T / (-2.0 * tau**2))
    return w
```

```
In [3]: def theta(X,Y,point,tau):
    W = w_i(point,X,tau)
    th_x = X.T@W@X
    th_y = X.T@W@Y.T
    th = th_x.I@th_y
    return th
```

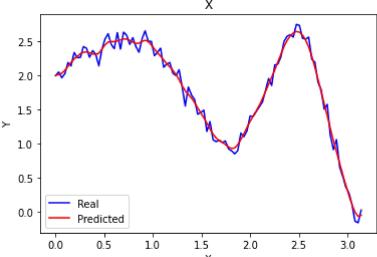
```
In [4]: def predict(X,Y,tau):
    m,n = np.shape(X)
    ypred = np.zeros(m)

for i in range(m):
        ypred[i] = X[i] * theta( X, Y, X[i],tau)
    return ypred
```

. ---- .

Generate X and Y and apply

```
In [5]:
        n = 100
        xs = np.linspace(0, np.pi, n)
        ys = 1 + np.sin(xs) + np.cos(xs**2) + np.random.normal(0, 0.1, n)
In [6]: X = np.mat(xs)
        Y = np.mat(ys)
        #add 1 with each entry in X
        m = X.shape[1]
        one = np.ones((1,m))
        X = np.hstack((one.T,X.T))
        print(X[:5])
        [[1.
                      0.
         [1.
                      0.03173326]
         [1.
                      0.06346652]
         [1.
                      0.09519978]
         [1.
                      0.12693304]]
In [7]: Y_prediction_05 = predict(X,Y,0.05)
In [8]: X_1 = xs
        Y_1 = ys
        Y_p = Y_prediction_05
        plt.plot(X_1,Y_1,'b-')
        plt.plot(X_1,Y_p,'r-')
        plt.xlabel('X')
        plt.ylabel('Y')
        plt.title('X')
        plt.legend(['Real','Predicted'])
Out[8]: <matplotlib.legend.Legend at 0x2202eeed070>
                                    Х
           2.5
```



Part 2

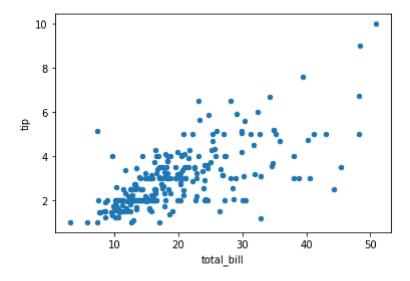
Use on DataSet

```
In [9]: # Read Data and make DataFrame
df = pd.read_csv('data/tips.csv')
df.head()
```

Out[9]:		total_bill	tip	sex	smoker	day	time	size
	0	16.99	1.01	Female	No	Sun	Dinner	2
	1	10.34	1.66	Male	No	Sun	Dinner	3
	2	21.01	3.50	Male	No	Sun	Dinner	3
	3	23.68	3.31	Male	No	Sun	Dinner	2
	4	24.59	3.61	Female	No	Sun	Dinner	4

```
In [10]: #plot total_bill vs tip
df.plot(x = 'total_bill',y = 'tip',kind = 'scatter')
```

Out[10]: <AxesSubplot:xlabel='total_bill', ylabel='tip'>



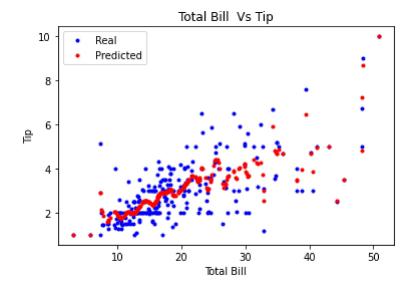
```
In [11]: # select columns regression
         X = np.mat(df['total_bill'])
         Y = np.mat(df['tip'])
         #add 1 with each entry in X
         m = X.shape[1]
         one = np.ones((1,m))
         X = np.hstack((one.T,X.T))
         print(X[:5])
                  16.99]
         [[ 1.
          [ 1.
                  10.34]
          [ 1.
                  21.01]
                  23.68]
          [ 1.
          [ 1.
                  24.59]]
In [12]: Y_prediction = predict(X,Y,0.4)
```

Plot the predicted result

```
In [13]: X_l = df['total_bill']
Y_l = df['tip']
Y_p = Y_prediction

plt.plot(X_l,Y_l,'b.')
plt.plot(X_l,Y_p,'r.')
plt.xlabel('Total Bill')
plt.ylabel('Tip')
plt.title('Total Bill Vs Tip')
plt.legend(['Real','Predicted'])
```

Out[13]: <matplotlib.legend.Legend at 0x2202f37ef70>



Decision Tree

```
In [1]: #import useful package
        import pandas as pd
        from sklearn.model selection import train test split
        from sklearn.tree import DecisionTreeClassifier, plot tree
        import matplotlib.pyplot as plt
        from sklearn.metrics import confusion matrix,accuracy score
In [2]: #read data
        df = pd.read_csv('data/Iris.csv')
        df.head()
Out[2]:
            Id SepalLengthCm SepalWidthCm PetalLengthCm PetalWidthCm
                                                                       Species
                         5.1
                                                                 0.2 Iris-setosa
         0
            1
                                       3.5
                                                    1.4
            2
                                                                  0.2 Iris-setosa
         1
                         4.9
                                       3.0
                                                    1.4
         2
            3
                         4.7
                                       3.2
                                                    1.3
                                                                 0.2 Iris-setosa
         3
           4
                         4.6
                                       3.1
                                                    1.5
                                                                 0.2 Iris-setosa
         4 5
                         5.0
                                       3.6
                                                    1.4
                                                                 0.2 Iris-setosa
In [3]: df.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 150 entries, 0 to 149
        Data columns (total 6 columns):
          #
             Column
                             Non-Null Count Dtype
          0
                             150 non-null
                                              int64
                                              float64
          1
             SepalLengthCm 150 non-null
          2
             SepalWidthCm
                             150 non-null
                                              float64
          3
             PetalLengthCm 150 non-null
                                              float64
          4
             PetalWidthCm
                             150 non-null
                                              float64
                             150 non-null
          5
             Species
                                              object
        dtypes: float64(4), int64(1), object(1)
        memory usage: 7.2+ KB
In [4]: | #Splitting data in to train and test part
        X = df.drop(['Species','Id'],axis=1)
        class name = list(df.Species.unique())
        feat_name = list(X.columns)
        Y = df.Species.apply(lambda x: class name.index(x))
        #Y = df.Species
In [5]: x_train,x_test,y_train,y_test = train_test_split(X,Y,test_size = 0.3)
```

Train Model:-ID3

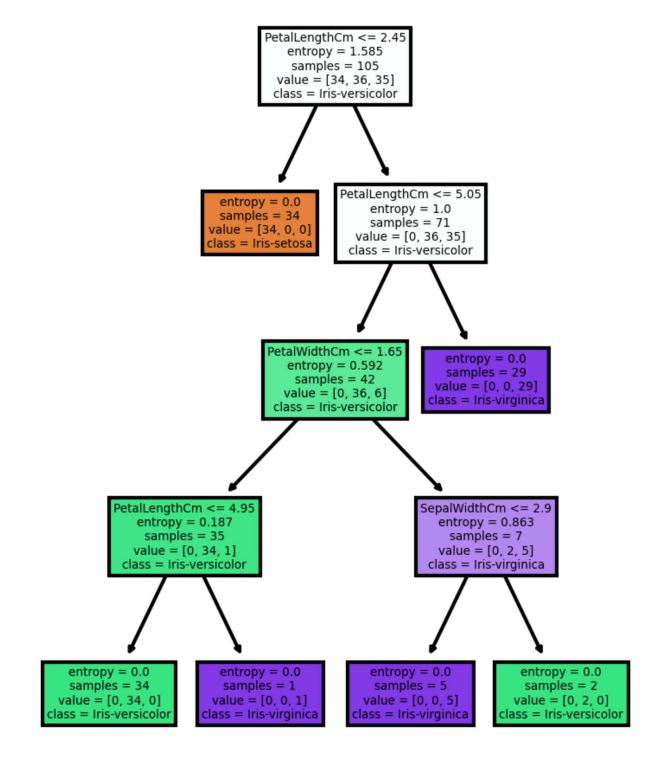
In [6]: | cd3 = DecisionTreeClassifier(criterion='entropy')

Out[6]: DecisionTreeClassifier(criterion='entropy')

cd3.fit(x_train,y_train)

Algorithm

```
ID3 (Examples, Target Attribute, Attributes)
        Create a root node for the tree
        If all examples are positive, Return the single-node tree Root, with labe
   1 = +.
        If all examples are negative, Return the single-node tree Root, with labe
   1 = -.
        If number of predicting attributes is empty, then Return the single node
    tree Root,
        with label = most common value of the target attribute in the examples.
        Otherwise Begin
            A ← The Attribute that best classifies examples.
            Decision Tree attribute for Root = A.
            For each possible value, vi, of A,
                Add a new tree branch below Root, corresponding to the test A = v
   i.
                Let Examples(vi) be the subset of examples that have the value vi
   for A
                If Examples(vi) is empty
                    Then below this new branch add a leaf node with label = most
    common target value in the examples
                Else below this new branch add the subtree ID3 (Examples(vi), Tar
   get Attribute, Attributes - {A})
        End
        Return Root
ID3 algorithm is based on entropy and information gain calculation.
Entropy is calculated as
                               Entropy = -\Sigma p(X) \log p(X)
Where p(X) is a Fraction of example in given class
and information gain is calculated as-
                          GAIN = Entropy(p) - \sum_{i=1}^{n_i} Entropy(i)
```



```
In [8]: #check accurecy
      y pred = cd3.predict(x test)
      print(f'Accuracy Score of model is : {accuracy_score(y_test,y_pred)}')
       In [9]: print('Confusion Metrics :')
      print(confusion_matrix(y_test,y_pred))
       Confusion Metrics:
       [[16 0 0]
       [ 0 13 1]
       [ 0 2 13]]
```

Train Model:-CART

Algorithm

```
Step 1: Start at the root node with all training instances
Step 2: Select an attribute on the basis of splitting criteria
Step 3: Partition instances according to selected attribute recursively
```

ID3 algorithm is based on GINI Impurity.

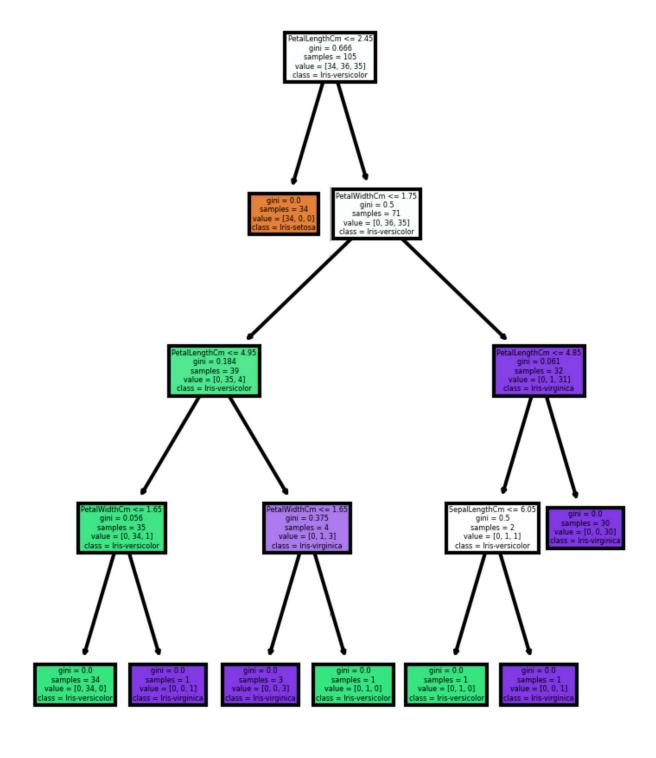
GINI is calculated as

GINI =
$$1 - \Sigma(p_i)^2$$

Where p_i is the probability that a tuple in D belongs to the class C

```
In [10]: | cart = DecisionTreeClassifier(criterion='gini')
         cart.fit(x_train,y_train)
```

Out[10]: DecisionTreeClassifier()



Logestic Regression

Logistic Regression is a Machine Learning algorithm which is used for the classification problems, it is a predictive analysis algorithm and based on the concept of probability.

For Logestic Regression Output Function:

$$\sigma(z) = \mathbf{sigmoid}(z)$$

Where

$$z = \beta_0 + \beta_1 x + \cdots$$

And

$$sigmoid(z) = \frac{1}{1 + e^{-z}} = \frac{1}{1 + e^{-\beta_0 + \beta_1 x + \dots}}$$

 $\sigma(z)$ gives values between 0 and 1.

and Cost Function is:

$$J(\theta) = -\frac{1}{m} \sum \left[y \log \sigma(z) + (1 - y) \log (1 - \sigma(z)) \right]$$

To minimise our cost Function we use Gradient Descent.

$$\theta_j := \theta_j - \alpha \sum_{i=1}^m (\sigma(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

```
In [10]: #import useful package
         import pandas as pd
         from sklearn.model selection import train test split
         from sklearn.linear_model import LogisticRegression
         import matplotlib.pyplot as plt
         from sklearn.metrics import confusion matrix,accuracy score
In [11]: | df = pd.read csv('data/Social Network Ads.csv')
         df.head()
Out[11]:
              User ID Gender Age EstimatedSalary Purchased
          0 15624510
                                         19000
                       Male
                              19
                                                       0
          1 15810944
                       Male
                              35
                                         20000
                                                      0
          2 15668575 Female
                              26
                                         43000
                                                      0
          3 15603246 Female
                              27
                                         57000
                                                       0
          4 15804002
                                         76000
                                                      0
                       Male
                              19
In [12]: | df.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 400 entries, 0 to 399
         Data columns (total 5 columns):
              Column
                               Non-Null Count Dtype
              -----
                                _____
          _ _ _
              User ID
                               400 non-null
          0
                                                int64
          1
              Gender
                               400 non-null
                                                object
          2
              Age
                               400 non-null
                                                int64
          3
              EstimatedSalary 400 non-null
                                                int64
          4
              Purchased
                               400 non-null
                                                int64
         dtypes: int64(4), object(1)
         memory usage: 15.8+ KB
In [13]: #convert class feature in numerical
         g list = ['Male','Female']
         df.Gender = df.Gender.apply(lambda x: g list.index(x))
In [15]: #Splitting Data in train and test
         X = df.drop(['User ID', 'Purchased'], axis = 1)
         Y = df['Purchased']
         x_train,x_test,y_train,y_test = train_test_split(X,Y,test_size = 0.3)
In [16]: #Training Logestic Regression Model
         LogReg = LogisticRegression()
         LogReg.fit(X,Y)
Out[16]: LogisticRegression()
```

```
In [26]: print("Coefficient for Regression:")
    print(*LogReg.coef_[0],sep = '\n')

    Coefficient for Regression:
        -9.322295567048426e-11
        -2.1041517809748262e-09
        -2.693014040541572e-06

In [28]: #Test accurecy
    y_pred = LogReg.predict(x_test)
    print(f'Accurecy = {accuracy_score(y_test,y_pred)}')

    Accurecy = 0.64166666666666667
```