ICD EPSY 8251 Workshop

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31 August 2012

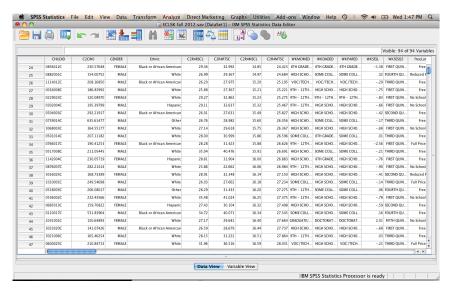
Overview

- Session 1 Introduction to SPSS
- Session 2 Exploratory Data Analysis
- 3 Session 3 Simple Linear Regression
- Session 4 Multiple Regression and ANOVA
- 5 Session 5 Student's t-test and Confidence Intervals

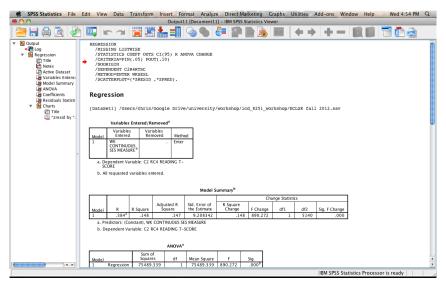
Introduction to SPSS

- Goals:
 - Understand the different elements of SPSS
 - Data Editor, Output Viewer, and Syntax Editor
 - Different menus
 - Be able to load data and create graphs

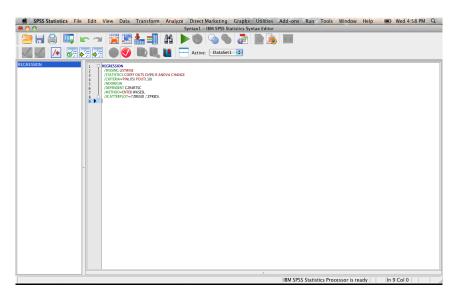
Data Editor



Output Viewer



Syntax Editor



File formats

- Data are saved in *.sav format.
- Output are saved in *.spv format.
- Syntax is saved in *.sps format
- You can directly save as Excel format or CSV
- For R, you can use the foreign library and the read.spss() function or save as a CSV and use the read.csv() command.

Variable View Fields

- Name and Label, descriptors of the variable.
- Values, value assigned to a level of the variable.
- Type, usually Numeric or String.
- Width and Decimals, affects the attributes of the cells in data view
- Missing, what is missing data coded as?
- Columns and Align, affects the attributes of the variable
- Measure
 - Scale Interval or ratio scale
 - Nominal Factor with no ordered levels
 - Ordinal Factor with ordered levels

Menus in Data View

- For descriptives, regression, ANOVA, t-test, look in the Analyze menu.
- For graphing, look in the Graphs and Analyze menu.
- For data manipulation, look in the Data menu.

Data

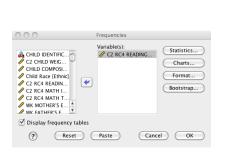
- The data used in this workshop (and throughout 8251) is from the Early Childhood Longitudinal Study, Kindergarten Class of 1998-99.
- The data focuses on children's early school experiences beginning with kindergarten and following children through middle school.
- The ECLS-K data provide descriptive information on children's status at entry to school, their transition into school, and their progression through 8th grade.
- The longitudinal nature of the ECLS-K data enables researchers to study how a wide range of family, school, community, and individual factors are associated with school performance.
- http://nces.ed.gov/ecls/kindergarten.asp

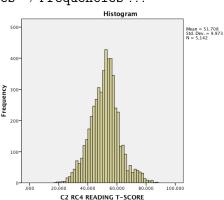
Graphs

- Histograms
- Stem-and-Leaf plot
- Boxplot
- Scatterplot

Histograms

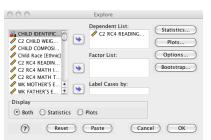
Analyze o Descriptive Statistics o Frequencies ...





Stem-and-Leaf plot

Analyze o Descriptive Statistics o Explore ...

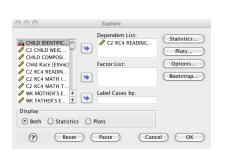


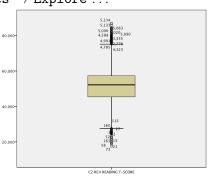
```
Stem & Leaf
Frequency
 10.00
 37.00
         0000111111
         22222223333333
 81.00
         4444445555555
 126.00
         6666666667777777777777
 166.00
         88888888888899999999999999
         000000000000000001111111111111111111
 212.00
 265.00
         311.00
         355.00
 355.00
         436.00
         513.00
         462.00
         468.00
 290.00
         261.00
         126.00
         222222222333333333333
 149.00
         4444444444444555555555555
 49.00
         66666777
 68.00
         ***********
 41.00
         0000111
 49.00
         22222333
 28.00
         44444
 105.00 Extremes
Sten width:
Each leaf:
       6 case(s)
```

& denotes fractional leaves.

Boxplot

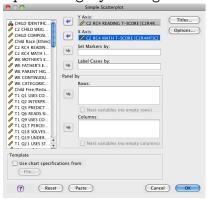
Analyze o Descriptive Statistics o Explore ...

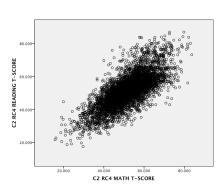




Scatterplot

$\mathtt{Graphs} o \mathtt{Legacy} \ \mathtt{Dialogs} o \mathtt{Scatter/Dot} \dots$





Graphing in SPSS

- Spend the next 10 minutes exploring the ECLSK data with graphs.
- See if you can recreate the graphs just presented.

EDA

Goals:

- To understand, to be able to calculate by hand, and to be able to have SPSS provide:
 - Measures of central tendency and variability
 - Understand how to calculate the expectation and variance of a RV
 - Covariance
 - Correlation
- To be able to connect the concepts of covariance and correlation

Measures of Central Tendency

- Mean, $\bar{x} = \sum_{i=n}^{n} \frac{y_i}{n}$
- Median, $\tilde{x} = P(X \le m) \ge \frac{1}{2}$ and $P(X \ge m) \ge \frac{1}{2}$
- Mode, most frequent value in a data set
- What is the mean, median, and mode?

 10	1	3	1	6
 10				

Measures of variability

- ullet Sample variance (unbiased), $s^2 = rac{\sum_i^n (y_i ar{y})^2}{n-1}$
- Standard deviation, $s = \sqrt{s^2}$
- What is s^2 and s?

У	7	7	9	2	1
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Expectation of a random variable

- Let X be a random variable (rv)
- The expectation of a X is defined as:
 - Discrete case, $EX = \sum_{x} xf(x)$
 - Continuous case, $EX = \int_{-\infty}^{\infty} xf(x)dx$
- The EX is also known as the mean of X or the mean of the distribution of X
- For a normal distribution, $EX = \mu$ and for a binomial distribution, EX = np.

Variance of a rv

- The variance of a rv, $Var(X) = E[(X EX)^2] = E[X^2] (EX)^2$
- The variance of the normal distribution, $Var(X) = \sigma^2$ and the variance of the binomial distribution is Var(X) = np(1-p).
- We can then describe the normal distribution as, $X \sim N(\mu, \sigma^2)$, where μ refers to the mean and σ^2 refers to the variance..

Properties of Expectations

- **Property 1**. If X = c and c is a constant rv, then E(c) = c and Var(c) = 0.
- **Property 2**. Let a, b be constants and Y = aX + b, then E(Y) = aE(X) + b and $Var(Y) = a^2 Var(X)$.
- **Property 3**. If X_1, X_2, \dots, X_n are independent rv, then $E[X_1, X_2, \dots, X_n] = EX_1 * EX_2 \dots EX_n$
- If the expectation of an estimator is equal to the population parameter of interest, then it is termed **unbiased**.
- Is the sample mean unbiased? note: $E(X_i) = \mu$ and X_i are independent and identically distributed.

$$E(\frac{\sum_{i=1}^{n}X_{i}}{n}) = \frac{1}{n}E(\sum_{i=1}^{n}X_{i}) = \frac{1}{n}\sum_{i=1}^{n}E(X_{i}) = \frac{1}{n}n\mu = \mu$$

• This is why we divide by n-1 to calculate obtain an unbiased estimate of variance.

Covariance and correlation

- Covariance, Cov(X, Y) = E[(X EX)]E[(Y EY)]
 - In 8251, you'll mostly use, $Cov(X,Y) = \frac{\sum_{i=1}^{n} (X_i \bar{X})(Y_i \bar{Y})}{n-1}$
- Correlation, $\rho = \frac{Cov(X,Y)}{\sqrt{Var(X)Var(Y)}}$
- What is Cov(X, Y) and ρ ?

X	7	18	2	12	3
У	12	14	5	19	1

EDA in SPSS

- Spend the next 10 minutes, exploring the ECLSK data
- Make sure you know how to find descriptive statistics, covariances, correlations, and can create simple plots!
 - ullet Analyze o Descriptive Statistics and Analyze o Correlate.
 - ullet Graphs o Chart Builder and Graphs o Legacy Dialogs.

SLR

- Goals:
 - To be able to relate correlation to SLR
 - To understand the assumptions of SLR
 - To be able to calculate the intercept and slope
 - To be able to calculate the coefficient of determination
 - To be able to run a SLR in SPSS and interpret the output

Simple Linear Regression Model

SLR model

$$y|x = \beta_0 + \beta_1 x + e|x$$

- $E[y|x] = \beta_0 + \beta_1 x$, because E[e|x] = 0.
- The residuals, e|x, are distributed $N(0, \sigma^2)$.
- $\bullet \ \beta_0 = \bar{y} \hat{\beta}_1 \bar{x}$
- $\beta_1 = \frac{SXY}{SXX} = \rho \frac{sd(y)}{sd(x)}$, where $SXY = \sum_{i}^{n} (x_i \bar{x})(y_i \bar{y})$ and $SXX = \sum_{i}^{n} (x_i \bar{x})^2$

Χ	7	18	2	12	3
у	12	14	5	19	1

What is β_0 ? What is β_1 ?

Assumptions of SLR

- Validity. The data you are analyzing should map to the research question you are trying to answer.
- The mean is a linear function of the predictor(s).
- Independence of residuals. That is that the residuals are uncorrelated with one another and are independent.
- Homogeneity of variance. Constant variance.
- Conditional distribution of y|x is normal. Alternatively, the residuals are normally distributed. This is the weakest assumption.

Coefficient of determination

R^2 - Coefficient of determination

$$1 - \frac{RSS}{SST}$$
, where $SST = \sum_{i=1}^{n} (y_i - \bar{y})^2$ and $RSS = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$

- Interpretation The proportion of variability in Y that is explained by conditioning on X (i.e. the model).
- This value ranges from 0 to 1
- In SLR, R^2 is equal to the square of the correlation between Y and X.

Coefficient of determination

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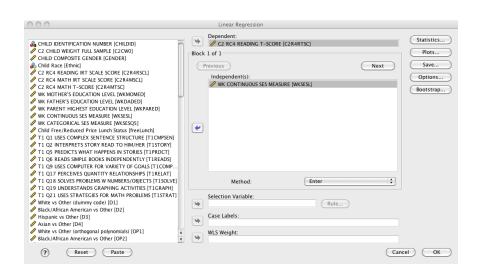
- Interpretation The proportion of variability in Y that is explained by X (i.e. the model).
- This value ranges from 0 to 1
- ullet In SLR, R^2 is equal to the square of the correlation between Y and X.
- What is SST, RSS, and R^2 ? What is $\sum_{i=1}^{n} y_i \bar{y}$?

Уi	22	23	26	35	31
ŷi	28.5	26.67	26.67	28.5	26.67
\bar{y}	27.4				

Example SLR from ECLSK

- Response (i.e. dependent or outcome variable) is the Reading T-score.
- Predictor (i.e. independent variable or covariate) is SES as a continuous measure.
- $E[Reading|SES] = \beta_0 + \beta_1[SES]$
- ullet Analyze o Regression o Linear...

Setting up the regression - SPSS



Output - SPSS

Regression

	Model Summary							
•	Model	R	R Square	Adjusted R Square	Std. Error of the Estimate			
	1	.384 ^a	.148	.147	9.208342			
	a. Predictors: (Constant), WK CONTINUOUS SES MEASURE							

ANOVA^a

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	75489.339	1	75489.339	890.272	.000b
	Residual	435838.915	5140	84.794		
	Total	511328.253	5141			

- a. Dependent Variable: C2 RC4 READING T-SCORE
- b. Predictors: (Constant), WK CONTINUOUS SES MEASURE

Coefficientsa

		Unstandardized Coefficients		Standardized Coefficients		
Model		В	Std. Error	Beta	t	Sig.
1	(Constant)	51.143	.130		394.002	.000
	WK CONTINUOUS SES MEASURE	5.173	.173	.384	29.837	.000

a. Dependent Variable: C2 RC4 READING T-SCORE

Regression and output - R

> m0=lm(C2R4RTSC~WKSESL,data=eclsk)

```
> summary(m0)
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 51.1431 0.1298 394.00 <2e-16 ***
WKSESI.
         5.1729 0.1734 29.84 <2e-16 ***
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 9.208 on 5140 degrees of freedom
Multiple R-squared: 0.1476, Adjusted R-squared: 0.1475
F-statistic: 890.3 on 1 and 5140 DF, p-value: < 2.2e-16
```

SLR in SPSS

- Spend the next 10 minutes, exploring the ECLSK data
- Run a SLR with a continuous outcome and one predictor.
 - Interpret the output

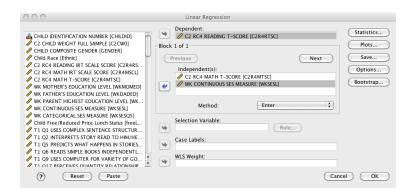
Regression and ANOVA

- Be able to run a multiple regression in SPSS and interpret the output
 - Using quantitative predictors and interactions.
 - Be able to check assumptions: Q-Q plot and residual plot
- Understand the relationship between ANOVA and MR
- Understand how to calculate a one-way ANOVA by hand
- Be able to run a one-way ANOVA in SPSS and interpret the output

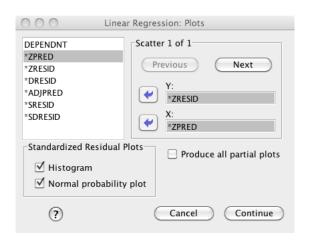
Multiple Regression in SPSS

- Running multiple regression in SPSS is done the same way as SLR.
- Solving for the β s is a little more difficult and most easily tackled with matrix algebra.
 - $Y = X\beta + e$
 - $\beta = (X^T X)^{-1} X^T Y$
 - You will not need to do this in 8251!
- Response (i.e. dependent or outcome variable) is the Reading T-score.
- Predictor (i.e. independent variable or covariate) is SES and Math T-score.
- $E[Reading|SES, MATH] = \beta_0 + \beta_1[SES] + \beta_2[MATH]$

Setting up the regression



Testing assumptions



Results

- [Reading|SES, MATH] = 13.864 + 1.410[SES] + .725[MATH]
- What does 13.864 correspond to?
- How do we interpret 1.410? 0.725?
- Do we meet assumptions?

Interaction model

- Create an interaction term
 - ullet Transfrom o Compute Variable...
- Refit model
- Is the interaction necessary?

Relationship between regression and ANOVA

- ANOVA (Analysis of Variance) examines whether groups differ in some outcome measure.
- The independent variable in an ANOVA is qualitative (categorical)
- A regression with a qualitative predictor with 2 levels will yield identical results to an ANOVA.
- \bullet Compare Geneal Linear Model \to Univariate...to Regression \to Linear...when using Reading T-Score as the DV and Gender as IV.
- So... ANOVA is a special case of regression.
- Using a predictor with more than 2 requires additional dummy variables.
- Also notice the relationship between T with 1 df and F.

Derivation of One-Way ANOVA

• See handout by Dr. Bob delMas

MR and ANOVA in SPSS

- Spend the next 10 minutes, exploring the ECLSK data
- Run a MR with two continuous outcomes and an interaction.
- Run a one-way ANOVA with Ethnic as the categorical predictor
- How many dummy variables would it take to make the regression output identical to the ANOVA output?

t-test and CIs

- Understand the relationship between a t-test to regression and ANOVA
- Be able to calculate the following t-test by hand and in SPSS
 - One-sample t-test
 - Two-sample t-test
 - Equal n and variance
 - Unequal n and equal variance
 - Be able to calculate by hand and in SPSS confidence intervals

Relationship between t-test and regression

- A one-sample t-test is equivalent to testing whether the intercept in a regression is equal to some value μ (often 0).
- A two-sample t-test is equivalent to testing whether the slope term in a regression for a qualitative variable is equal to some value μ (often 0).
- t-tests are used in regression to test whether parameters are significantly different than some value.
 - ullet In SPSS, t is, by default, calculated using a μ of 0.
 - The distribution of a parameter estimate in a regression model under the null hypothesis has a t-distribution and this is why we calculate a t-statistic.

One-sample t-test

- $T=rac{ar{X}-\mu}{s/\sqrt{n}}$, where s is the sample standard deviation, $ar{X}$ is the sample mean.
- ullet $H_O=\mu$, the population mean is equal to μ
- $H_A \neq \mu$, the population mean is not equal to μ
- df = n 1
- T ~ T(df)

Running a one-sample t-test

Suppose we have $X = \{2, 1, 2, 0, 2\}$ and we want to test whether μ is 0. What is H_O ? What is T? What is df?

Is there evidence against the null hypothesis if the critical value for significance is 2.776?

Two-sample t-test - equal n and variance

- ullet $\sqrt{rac{1}{2}(s_{X_1}^2+s_{X_2}^2)}$ is the pooled standard deviation
- $df = n_1 + n_2 2$
- If $X_1 = \{4, 2, 3, 5, 3\}, X_2 = \{2, 1, 2, 0, 2\}...$

Test $H_O: \mu_1 = \mu_2$ against $H_A: \mu_1 \neq \mu_2$.

Is there evidence against the null hypothesis if the critical value for significance is 2.306?

Two-sample t-test - unequal n

$$ullet$$
 $t=rac{ar{X}_1-ar{X}_2}{S_{X_1}X_2\sqrt{rac{1}{n_1}+rac{1}{n_2}}}$, where $S_{X_1X_2}=\sqrt{rac{(n_1-1)s_{X_1}^2+(n_2-1)s_{X_2}^2}{n_1+n_2-2}}$

- $df = n_1 + n_2 2$
- If $X_1 = \{5, 4, 4, 5\}$ and $X_2 = \{3, 2, 2, 3, 3\}...$

Test $H_O: \mu_1 = \mu_2$ against $H_A: \mu_1 \neq \mu_2$.

Is there evidence against the null hypothesis if the critical value for significance is 2.364?

Confidence Intervals

- Cls give identical information to hypothesis tests.
- ullet If CIs don't overlap with our test value, we know it is significant at lpha
- Typically construct 95% CI
- For a Z-statistic
 - $z \pm 1.96 * SE$
 - Critical value, 1.96, corresponds to the 97.5th quantile of a standard normal distribution
 - We use this when σ^2 is known. VERY UNCOMMON.
- For a t-statistic with a $(1 \alpha)\%$ CI
 - $\bar{X} \pm t_{\alpha/2} * SE$
 - Critical value, $t_{\alpha/2}$, corresponds to the $\alpha/2$ quantile of a t-distribution with df
 - Critical value found in books or R or let SPSS calculate it!

t-test and CI in SPSS

- Spend the next 10 minutes, exploring the ECLSK data
- Run a one-sample t-test and a two-sample t-test
- Make sure you request Cls.
- How are these calculated?

Wrap Up

- Today you learned . . .
 - SPSS
 - EDA
 - Simple Regression
 - Multiple Regression & ANOVA
 - T-tests and Confidence Intervals
 - Graphing & data management
 - Formulas
 - Measures of central tendency
 - Measures of variability & association
 - How to calculate a slope & intercept in SLR
 - How to perform a t-test and calculate confidence intervals

Now what?

- If this was a review, then relax and have a nice weekend
- If this was mostly a review, relax and have a nice weekend
- If this was all completely new, relax and have a nice weekend. But
 - The more basic stuff (t-tests, confidence intervals, measures of variability/association/central tendency, hypothesis testing) you should spend some time to learn.
 - Don't feel overwhelmed
 - Dr. Harwell will review these things again. Remember this is just a primer!
 - Spend some time focusing on stuff that was especially difficult

How to succeed in stat courses

- Work in groups and help one another out
- Don't wait too long, seek out help from Dr. Harwell, the TA, or other students
- You will learn R in 8252. Take some time over the semester, if you have time, to familiarize yourself with it.
- Stop by 164 ICD if you have questions.