All Power Analyses are Wrong, How to be More Right

Christopher David Desjardins

Research Methodology Consulting Center

5/1/19

Materials

Slides: https://bit.ly/2Y2kMBz

R code: https://bit.ly/2GLMKdO

Why are you here? Why do you care power?

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ADMINISTRATIVE POLICY

Doctoral Degree: Completion

Responsible University Officer(s):	Policy Owner(s):	Policy contact(s):	Date Revised
 Executive Vice President and Provost 	 Vice Provost and Dean of Graduate Education 	 Karen Starry 	Jun 19, 2017
			Effective Date

POLICY STATEMENT

This policy sets the standards for the doctoral final oral examination and the submission of the final copy of the doctoral dissertation for the completion of the doctoral degree.

I The Doctoral Final Oral Evamination

- a. The doctoral final oral committee must consist of at least four members, including the advisor(s), All members of the committee and the candidate must participate in the final oral examination. Committee members and/or the student may participate remotely as long as all conditions for remote participation in the examination are met.
 - i. At least three members (including the advisor) must be from the student's major field.
 - ii. At least one member must represent a field outside the major. If the student has declared a minor, the outside member, or one of the outside members, must represent the minor field.
 - iii. Members cannot satisfy the requirement with respect to more than one field.
 - iv. The chair of the committee must not be the candidate's advisor or co-advisor.
 - v. At least two members of the committee must be tenured or tenure-track University faculty members who hold earned doctorate degrees or designated equivalents in appropriate fields from an accredited institution. At least one of the committee members must be a tenured University faculty member.
 - vi. Collegiate deans or their designated representatives at the collegiate level must verify eligibility and approve the members of the final oral examination committee

Jul 15, 2012

Jump to:

Procedures Forms Appendices FAO

IES RFA - Goal 1

1. Exploration (Goal One)

a) Purpose

The Exploration goal supports projects that will identify <u>malleable factors</u> associated with <u>student education outcomes</u> and/or the factors and conditions that <u>mediate</u> or <u>moderate</u> that relationship. Exploration projects are intended to build and inform theoretical foundations to support future applied research efforts such as (1) the development of <u>interventions</u> or the evaluation of these interventions or (2) the development and <u>validation</u> of <u>assessments</u>.

Recommendations for a Strong Application: In order to address the above requirements, the Institute recommends that you include the following in your Research Plan section to strengthen the methodological rigor of the proposed exploratory work.

 For all quantitative inferential analyses, demonstrate that the sample provides sufficient power to address your research aims.

IES RFA - Goal 3

- 3. Efficacy and Follow-up (Goal Three)
- b. Research Plan The purpose of this section is to describe the evaluation of the intervention.

Requirements: In order to be responsive and sent forward for scientific peer review, **all** applications under the Efficacy and Follow-up goal **must** describe

(ii) The power analysis; and

IES RFA - Goal 4

- 4. Replication: Efficacy and Effectiveness (Goal Four)
- b. Research Plan The purpose of this section is to describe the evaluation of the intervention.

Requirements: In order to be responsive and sent forward for scientific peer review, **all** applications under Goal Four **must** describe:

- (i) The research design;
- (ii) The power analysis; and

Quick digression: What this talk isn't about

I am not interested in post-hoc or observed power and you shouldn't be either.

If p $> \alpha$, then you are either underpowered and committed a Type II error or you are correct there was no effect.

However, you might be interested in knowing your power given a specific effect size and sample size.

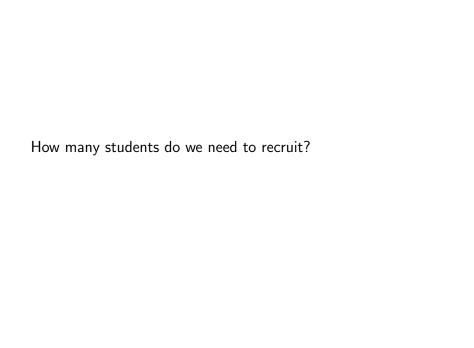
This blog clearly articulates the problem.

Motivating research question

Do low-income high school students receiving *TutorNow* have higher composite ACT scores than low-income high school students not receiving *TutorNow*?

Possible outcomes

- 1. Students in *TutorNow* have higher ACT composite scores than students not in *TutorNow*.
- 2. Students in *TutorNow* have lower ACT composite scores than students not in *TutorNow* (paradoxical effect).
- 3. There are no differences in ACT composite scores between students in *TutorNow* and students not in *TutorNow*.



► Anticipated size of effect

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- Attrition

Which effect size?

In our *TutorNow* example, there are lots of potential effect sizes one could consider.

- 1. Cohen's d
- 2. Point-biserial correlation
- $3. R^2$
- 4. Unstandardized regression coefficient

Cohen's d

Given that we have two independent samples, most likely consider Cohen's d.

$$d = \frac{\bar{X}_{Trt} - \bar{X}_{Ctrl}}{s}$$

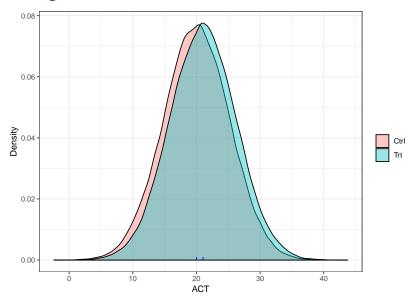
Benefits:

Units are in standard deviations Criteria for small (0.2), medium (0.5), and large (0.8) effects

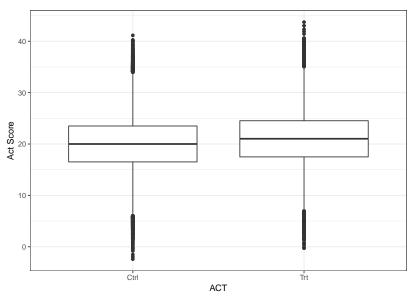
Drawbacks:

Units are in standard deviations Criteria for small (0.2), medium (0.5), and large (0.8) effects

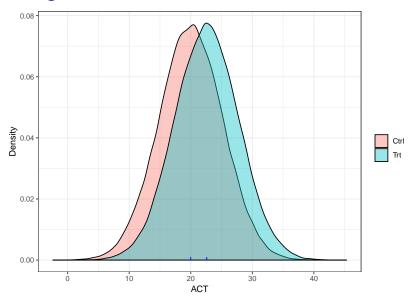
What might a Cohen's d of 0.2 look like for the ACT?



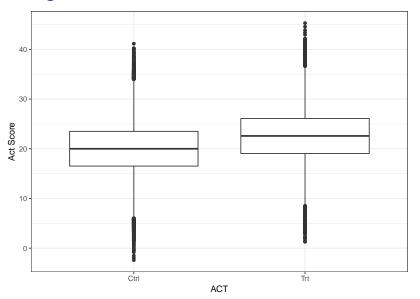
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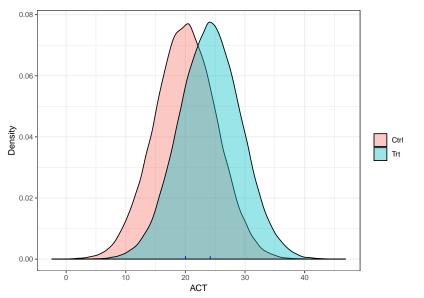
What might a Cohen's d of 0.5 look like for the ACT?



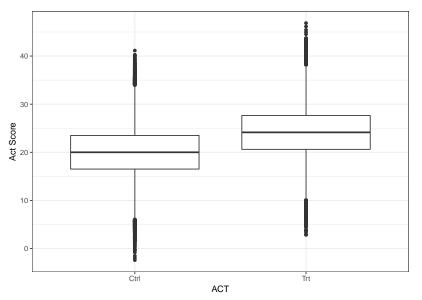
What might a Cohen's d of 0.5 look like for the ACT?



What might an a Cohen's d of 0.8 look like for the ACT?



What does a Cohen's d of 0.8 look like for the ACT?



Interpreting these effect sizes

Assuming a standard deviation of 5.2

- ▶ Cohen's d of 0.2 would correspond to a difference in means of 1.04.
- ▶ Cohen's d of 0.5 would correspond to a difference in means of 2.6.
- ▶ Cohen's d of 0.8 would correspond to a difference in means of 4.16.

The standard error of measurement is 0.93 (according to the ACT Technical Manual), half of the width of a 95% confidence interval would be:

$$(1.96 * 0.93) = 1.8228$$

This "half" width is larger than the mean difference that resulted in a Cohen's d of 0.2, but not a Cohen's d of 0.5. (Apples to Oranges)

A better approach - MMES

- What is a minimum meaningful effect size (MMES)?
 - A theoretically-driven effect size that if detected in the study is clinically/educationally/economically meaningful. Anything smaller, is trivial.
 - ► IES calls this **practical significance**.
 - Differs from minimum detectable effect size (MDES) because MDES is a statistical artifact.
- How to work with the MMES?
 - 1. Consult literature and determine effect sizes reported.
 - Discuss with practitioners what is a meaningful effect size for your application.
 - 3. Articulate why this is meaningful to colleagues.
 - 4. Articulate it in a meaningful and understandable unit.
 - Approach RMCC folks with a MMES and ask them to run a power analysis.

Statistical Inference

Compare the students receiving TutorNow with students not receiving TutorNow using a two-sample t-test:

$$t = \frac{\bar{X}_{Trt} - \bar{X}_{Ctrl}}{\sqrt{\frac{s_{Trt}^2 + s_{Ctrl}^2}{2}} \sqrt{\frac{2}{N}}}$$

Assumes that

- 1. Samples are from normally distributed populations
- 2. Sample sizes are equal
- 3. Groups have the same variance

Hypothesis testing

We're principally interested in testing the difference between the means

$$H_0$$
: $\mu_{Trt} - \mu_{Ctrl} = 0$
 H_1 : $\mu_{Trt} - \mu_{Ctrl} \neq 0$

But aren't we really interested in?

$$H_0$$
: $\mu_{Trt} - \mu_{Ctrl} = MMES$
 H_1 : $\mu_{Trt} - \mu_{Ctrl} > MMES$

There's no reason we have to test the first one.

Errors in hypothesis testing

Let H_0 represent a null hypothesis.

	H_0 True	H_0 False
Fail to Reject H_0	Correct Decision	Type II Error
	(True Negative, $1-lpha$)	(False Negative, β)
Reject H ₀	Type I Error	Correct Decision
	(False positive, α)	(True Positive, $1-\beta$)

Errors in hypothesis testing

$$H_0$$
: $\mu_{Trt} - \mu_{Ctrl} = MMES$
 H_1 : $\mu_{Trt} - \mu_{Ctrl} > MMES$

		Truth		
		Not a meaningfully	A meaningfully im-	
		improvement	provement	
Conclusion	Doesn't work	Correct Decision	Type II	
	Works	Type I	Correct Decision	

Power is our ability to conclude that *TutorNow* represents a meaningful (and significant) improvement on the ACT for low-income students compared to low-income students not receiving *TutorNow* when in fact *TutorNow* actually is an improvement.

Consequences

- ▶ Type I error (α)
 - Conclude that TutorNow has a significant, and meaningful, improvement on the ACT over students not receiving tutoring when it does not.
 - Waste resources (time, money)
 - Program's effectiveness isn't reproducible.
- ▶ Type II error (β)
 - Conclude that TutorNow does not have a significant, and meaningful, improvement over students not receiving tutoring when in fact it does.
 - Withhold a treatment that could improve student outcomes
 - Program is no longer developed

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 - Withhold a treatment that could improve student outcomes
 - Program is no longer developed
- Which one is the worse error?

Quick digression - Ecological example

- RQ: Does timber harvesting affect the presence of river otters in a watershed?
- ► *H*₀: Timber harvesting has no effect on the presence of river otters in a watershed.
- H₁: Timber harvesting negatively affects the presence of river otters in a watershed.

Quick digression - Ecological example

- ▶ Type I error (α)
 - Conclude that timber harvesting negatively affects the presence of river otters use of a watershed when it does not.
 - ► Local economic impact
 - Timber harvested halted regionally, nationally.
- ▶ Type II error (1β)
 - Conclude that timber harvesting has no effect on the presence of river otters use of a watershed when it does.
 - River otters go locally extinct (extirpated)
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 - ▶ River otters go extinct where ever timber harvesting occurs
- ▶ Which one is the worse error?

Power Analysis

What do we need?

- ► A statistical model/test
- ► An effect size estimate
- ▶ A Type I error (α)
- ▶ A Type II error (β) or power (1β)
- Sample size

How do we perform an actual power analysis?

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- ▶ Identify the statistical test you wish to perform.
- ▶ For basic tests, power calculators exist
 - Must meet assumptions of the test.
 - This is why many power analyses are wrong.
- ► For complex models, power is mostly simulation-based.
 - Every parameter in the model must have a value.

1. Can reproduce power analysis calculators.

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- 2. Real data rarely conform exactly to modeling assumptions.
- 3. Understand the extent that violations could impact findings.
- 4. Want to play with scenarios.

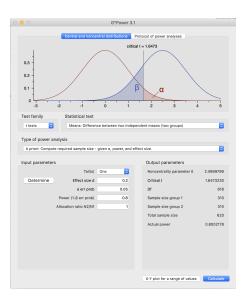
Power analysis for ACT

In R:

Given an effect size (Cohen's d) of 0.2 (aka MDES), $\alpha=.05$, power = .80, and two-sample t-test with a one-sided alternative hypothesis.

```
pwr::pwr.t.test(d = 0.2, sig.level = .05, power = .80,
                type = "two.sample", alternative = "greater")
##
##
        Two-sample t test power calculation
##
##
                 n = 309.8065
##
                 d = 0.2
##
         sig.level = 0.05
             power = 0.8
##
       alternative = greater
##
##
## NOTE: n is number in *each* group
```

In G-Power:



How do we do a power analysis via simulation?

- Specify the data-generating mechanism, α , and sample size or effect size.
- Assuming sample size (N) and effect size are provided,
 - Randomly generate data of size N a large number of times (e.g., 2000 or 5000 replicates)
 - Perform the desired statistical test and save the p-value.
 - An empirical estimate of power is the number of times out of the 2000 or 5000 replicates where p $< \alpha$,
- Trying to obtain a desired sample/effect size,
 - Randomly generate data a large number of times (e.g., 2000 or 5000 replicates) but vary either sample size or effect size.
 - Perform the desired statistical test, save the p-value and, record the estimated power.
 - ► The smallest sample size size/MDES is where power is .80 or greater.

Power analysis of t-test via simulation

```
H_0: \mu_{Trt} - \mu_{Ctrl} = 0
H_1: \mu_{Trt} - \mu_{Ctrl} > 0
```

```
set.seed(512019)
run_sim <- replicate(5000, expr = {</pre>
trt \leftarrow rnorm(310, mean = 21.04, sd = 5.2)
ctrl \leftarrow rnorm(310, mean = 20, sd = 5.2)
test <- t.test(trt. ctrl. var.equal = FALSE, alternative = "greater")
d <- cohen.d(trt, ctrl)</pre>
c(test$p.value, d)
run_sim <- data.frame(t(run_sim))</pre>
colnames(run_sim) <- c("p.value", "d")</pre>
mean(run_sim$d) # effect size
## [1] 0.2004489
mean(run_sim$p.value < .05) # empirical power</pre>
## [1] 0.7958
```

Power analysis of simple linear regression via simulation

```
ACT | Trt \sim N(\beta_0 + \beta_1 \text{Trt}, \sigma^2)

H_0: \beta_1 = 0

H_1: \beta_1 > 0
```

```
set.seed(512019)
run_sim <- replicate(5000, expr = {
   trt <- rnorm(310, mean = 21.04, sd = 5.2)
   ctrl <- rnorm(310, mean = 20, sd = 5.2)
   y <- c(trt, ctrl)
   x <- rep(c("Trt", "Ctrl"), each = 310)
   mod <- lm(y ~ x)
   pt(summary(mod)$coef[2, 3], df = 618, lower.tail = FALSE)
})
   mean(run_sim < .05) # empirical power
## [1] 0.7958</pre>
```

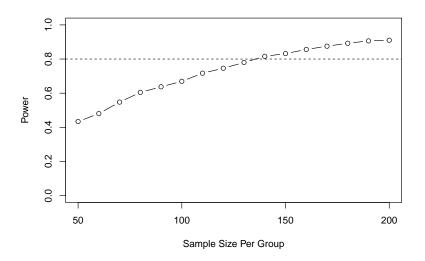
A more interesting power analysis

Let's say you've determined the MMES is a Cohen's d of 0.2. Anything less than 0.2 is not of practical interest. You expect a medium size effect of 0.5. You want to know the **minimum sample size** to detect an effect greater than 0.2 assuming you have an effect of 0.5 with a power of 0.8. Also, we'll relax our assumption about equal variance for the t-test.

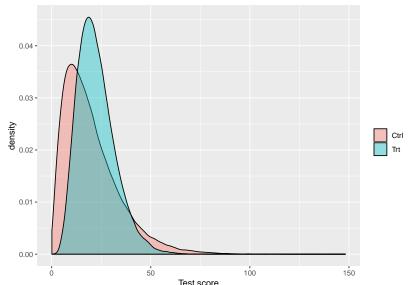
$$H_0: \mu_{Trt} - \mu_{Ctrl} = 1.04$$

 $H_1: \mu_{Trt} - \mu_{Ctrl} > 1.04$

Power curve



Let's play with the assumptions now Instead of the two groups coming from two normal populations, what happens if they come from two skewed distributions but still have the same mean difference in the population?

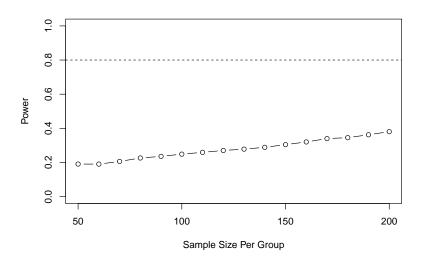


Treatment: mean = 22.6, sd = 9.51

tmp <- replicate(5000, calc_p(samp))
power <- c(power, mean(tmp < .05))</pre>

power <- NULL
for(samp in n){</pre>

Power curve



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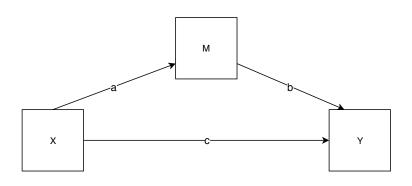
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- 7. SPSS can't do it.

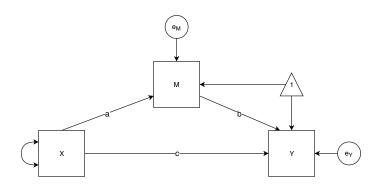
Good news?

- ▶ If you can write your model, it is very easy to simulate power in R.
 - Can use base functions to simulate mixed effects model, SEM, regressions, etc.
 - Can use functions in MASS and lavaan for simulating from multivariate normal and SEM models.
- ► If you use Mplus, https://www.statmodel.com/usersguide/chapter12.shtml

Power analysis - Mediation



Power analysis - Mediation (explicit)



Equations

1. M regressed on X

$$M|X \sim N(\beta_m + aX, \sigma_m^2)$$

2. Y regressed on M and X

$$Y|X, M \sim N(\beta_y + bM + cX, \sigma_y^2)$$

We are interested in the indirect effect, ab.

What we need for the power analysis if interest is in the indirect effect, ab

- \triangleright β_m and β_y the intercepts. Could set to zero if variables are mean-centered.
- ▶ a, b, and c the slope terms. The effect of X on M, the effect of M on Y holding X constant, and the effect of X on Y holding M constant.
- $ightharpoonup \sigma_m^2$ and σ_y^2 residual variance
- X needs a distribution.
 - Should it be continuous or discrete?
- ▶ **Need to provide 8 parameters** and to find power of ab could vary a, b, or both.
- ▶ What type of effect size to use? Several proposed ...
 - Standardized indirect effect squared (v) (Lachowicz, Preacher, & Kelley, 2018)
 - The variance in Y accounted for jointly by M and X adjusting for the ordering of variables.
 - Could use Cohen's criteria for R² (.02, .15, .25)

How to proceed

First, what do we want? A sample size given a MMES or do we know the sample size and need to know our MDES? Let's assume the former and let's assume a MMES of .10 and want to know our sample size given a power of .80 and an α of .05.

Second, we need to set the parameters.

- ▶ We'll standardize X and make M and Y standardized, too.
- ▶ No need for β_m and β_y .
- We know we need to constrain $ab^2 = .10$, so how do to decide what value to use for a and b?
- ► Can set each standardized regression weights (beta) to .562 as long as ab = .316.
- If using Baron & Kenny framework, probably the above approach is best.
- ▶ We'll set c to .14 (a small effect).

Third, let's assume we can recruit (or afford) between 50 - 120 participants, but would prefer the least amount possible.

Fourth, we'll run 2,000 replications of each condition.

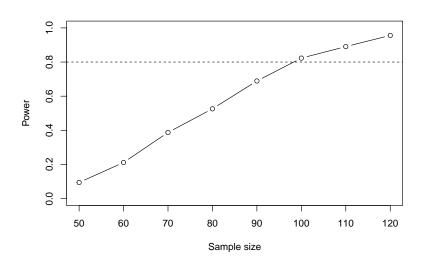
Setting up the model

```
set.seed(05012019)
library(lavaan)
\# relationship between X and M, M and Y, and X and Y
a < -.562
b <- .562
c < - .14
# Fit the model
mod <- '
M ~ a*X
         # M regressed onto X
Y ~ b*M + c*X # Y regressed onto M and X
v := (a*b)*(a*b) # indirect effect squared
# How many observations should we generate.
n < -100
\# Generate X to be a random normal variable, M, and Y
X \leftarrow rnorm(n = n, mean = 0, sd = 1)
M \leftarrow a*X + rnorm(n, mean = 0, sd = sqrt(1 - a^2))
Y \leftarrow b*M + c*X + rnorm(n, mean = 0, sd = sqrt(1 - (b^2 + c^2 + 2*b*c*a)))
dat <- data.frame(Y, X, M)
# Fit the model
fit <- sem(model = mod, data = dat)
# Extract the relevant information
param <- parameterEstimates(fit)</pre>
subset(param, label == "v", pvalue)
```

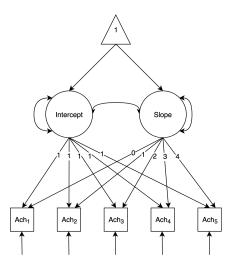
Running the simulation

```
sample_size \leftarrow seq(50, 120, by = 10)
alpha <- .05
run sim <- function(N){
  # How many observations should we generate.
 n <- N
 # Generate X to be a random normal variable, M, and Y
 X \leftarrow rnorm(n = n, mean = 0, sd = 1)
 M \leftarrow a*X + rnorm(n, mean = 0, sd = sqrt(1 - a^2))
 Y \leftarrow b*M + c*X + rnorm(n, mean = 0, sd = sqrt(1 - (b^2 + c^2 + 2*b*c*a)))
  dat <- data.frame(Y, X, M)
  # Fit the model
 fit <- sem(model = mod, data = dat)
  # Extract the relevant information
  param <- parameterEstimates(fit)</pre>
  subset(param, label == "v", pvalue, drop = TRUE)
set.seed(05012019)
power <- NULL
for(samp in sample_size){
  p_values <- replicate(2000, run_sim(samp))</pre>
 power <- c(power, mean(p_values < alpha))</pre>
```

Power curve for mediation analysis



Linear (latent) growth curve model



Let's say we're interested in detecting the minimum unstandardized parameter coefficient for the mean of the slope (i.e., change in achievement over time) assuming we have a sample size of 100.

Generating data in R

```
nobs <- 100
ran effs \leftarrow c(5, .5)
cor_mat \leftarrow matrix(c(1, -.2, -.2, 1), nrow = 2)
cov mat <- cor2cov(cor mat, ran effs)</pre>
int_mean <- 20
slope_mean <- 1.5 # this is our parameter of interest!</pre>
fact_scores <- MASS::mvrnorm(n = nobs, mu = c(int_mean, slope_mean), Sigma = cov_mat)</pre>
ach1 <- 1*fact_scores[, 1] + 0*fact_scores[, 2] + rnorm(nobs, sd = .5)
ach2 <- 1*fact scores[, 1] + 1*fact scores[, 2] + rnorm(nobs, sd = .5)
ach3 <- 1*fact_scores[, 1] + 2*fact_scores[, 2] + rnorm(nobs, sd = .5)
ach4 <- 1*fact_scores[, 1] + 3*fact_scores[, 2] + rnorm(nobs, sd = .5)
ach5 <- 1*fact scores[, 1] + 4*fact scores[, 2] + rnorm(nobs, sd = .5)
dat <- data.frame(id = 1:nobs, ach1, ach2, ach3, ach4, ach5)
dat_1 <- reshape(dat, direction = "long", varying = 2:6,</pre>
                 timevar = "year", v.names = "score", times = 0:4)
```

Fitting the model in R

```
mod <- "
int = 1*ach1 + 1*ach2 + 1*ach3 + 1*ach4 + 1*ach5
slope = 0*ach1 + 1*ach2 + 2*ach3 + 3*ach4 + 4*ach5

int ~ 1
slope ~ eff*1

int ~ int + slope
slope ~~ slope

ach1 ~~ e*ach1
ach2 ~~ e*ach2
ach3 ~~ e*ach3
ach4 ~~ e*ach4
ach5 ~~ e*ach5
"</pre>
```

Equivalent models

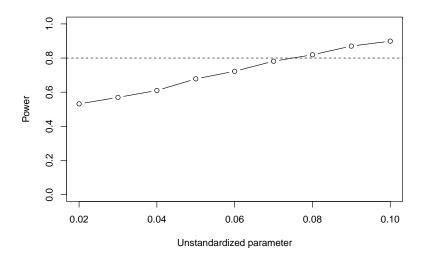
```
# as a latent growth curve model
lgcm.fit <- growth(mod, data = dat)
summary(lgcm.fit)

# as a mixed effects model
me.fit <- lme4::lmer(score ~ 1 + year + (1 + year | id), data = dat_l)
summary(me.fit)</pre>
```

```
alpha <- .5
nobs <- 100
ran_effs \leftarrow c(5, .5)
cor_mat \leftarrow matrix(c(1, -.2, -.2, 1), nrow = 2)
cov_mat <- cor2cov(cor_mat, ran_effs)</pre>
int mean <- 20
eff sizes \leftarrow seq(.02, .1, by = .01)
run_sim <- function(param){</pre>
  slope_mean <- param # this is our parameter of interest!</pre>
 fact_scores <- MASS::mvrnorm(n = nobs, mu = c(int_mean, slope_mean), Sigma = cov_mat)</pre>
  ach1 <- 1*fact_scores[, 1] + 0*fact_scores[, 2] + rnorm(nobs, sd = .5)
  ach2 <- 1*fact_scores[, 1] + 1*fact_scores[, 2] + rnorm(nobs, sd = .5)
  ach3 <- 1*fact scores[. 1] + 2*fact scores[. 2] + rnorm(nobs, sd = .5)
  ach4 <- 1*fact_scores[, 1] + 3*fact_scores[, 2] + rnorm(nobs, sd = .5)
  ach5 <- 1*fact_scores[, 1] + 4*fact_scores[, 2] + rnorm(nobs, sd = .5)
  dat <- data.frame(id = 1:nobs, ach1, ach2, ach3, ach4, ach5)
  lgcm.fit <- growth(mod, data = dat)</pre>
  params <- parameterEstimates(lgcm.fit)</pre>
 subset(params, label == "eff", pvalue, drop = TRUE)
set.seed(05012019)
power <- NULL
for(param in eff sizes){
```

p_values <- replicate(2000, run_sim(param))
power <- c(power, mean(p_values < alpha))</pre>

Power curve for LGCM



Why should we promote a culture of simulation-based power analyses?

- ▶ All power analyses can be performed via simulation.
- Simulation requires deeper thought about research questions and models that will be examined a priori.
- Deepens our understanding of power and statistical concepts (more generally)

How can we promote a culture of simulation-based power analyses in CEHD?

- 1. Work with RMCC and involve us early.
- 2. Make sure students exiting PhD-level statistics courses know how to write their models and know the assumptions.
 - If they know the models and the assumptions, then they can test them and understand what to expect if they don't meet their assumptions.
- 3. Avoid thinking about power as a binary concept.
- 4. Involve simulation, as much as possible, in the classroom.
- 5. Just teach R.