

E-411 PRMA

LECTURE 9 & 10 - ITEM RESPONSE THEORY

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ITEM ANALYSIS

ISSUES IN TEST DEVELOPMENT

ALTERNATIVES TO ITEM ANALYSIS

TEST REVISION

STANDARDIZATION

REVISING OLD TESTS

CROSS- AND CO- VALIDATION

TODAY

Item Response Theory

REVIEW

Classical Test Theory

CRITIQUES OF CTT

- Person are measured on number correct
- Score dependent on number of items on a test and their difficulty
- Scores are limited to fixed values
- Scores are interpretable on a within-group normative basis
- SEM is group dependent and constant for a group
- Item and person fit evaluation difficult
- Test development different depending on type of test

ITEM RESPONSE THEORY RATIONALE

WHAT IS ITEM RESPONSE THEORY?

A measurement perspective

GENERALIZED ANXIETY DISORDER

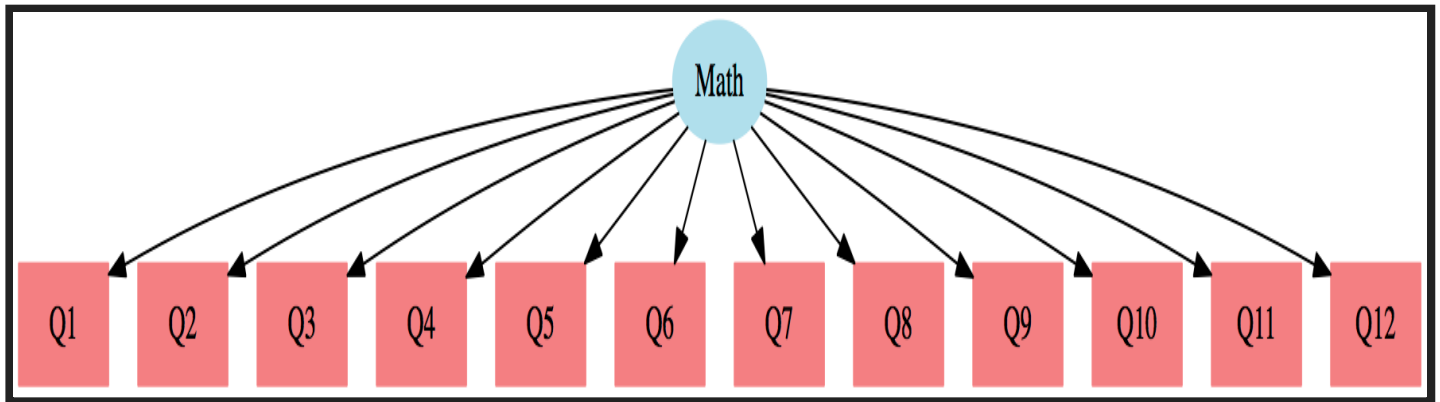
- Anxiety could be loosely defined as feelings that range from general uneasiness to incapacitating attacks of terror
- Is anxiety latent and is it continuous, categorical, or both?

HOW TO MEASURE GENERALIZED ANXIETY?

- Used observed (i.e. **manifest variables**) that provide a proxy of generalized anxiety
- These provide our **operationalized definition** of generalized anxiety
- But how do we put these observed measures onto the generalized anxiety scale?

PROPERTIES OF IRT

ASSUMPTIONS OF IRT

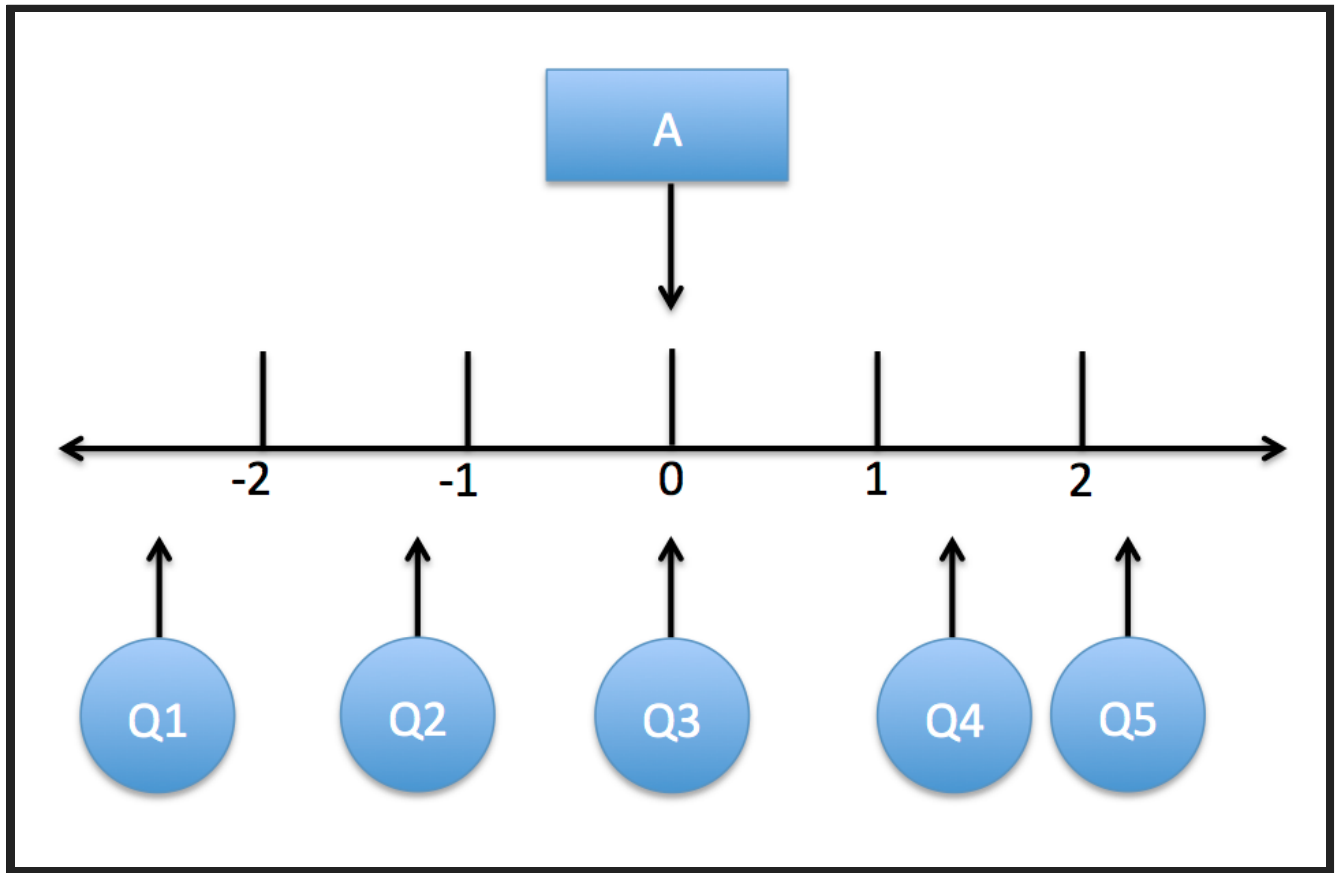


ITEM PARAMETERS

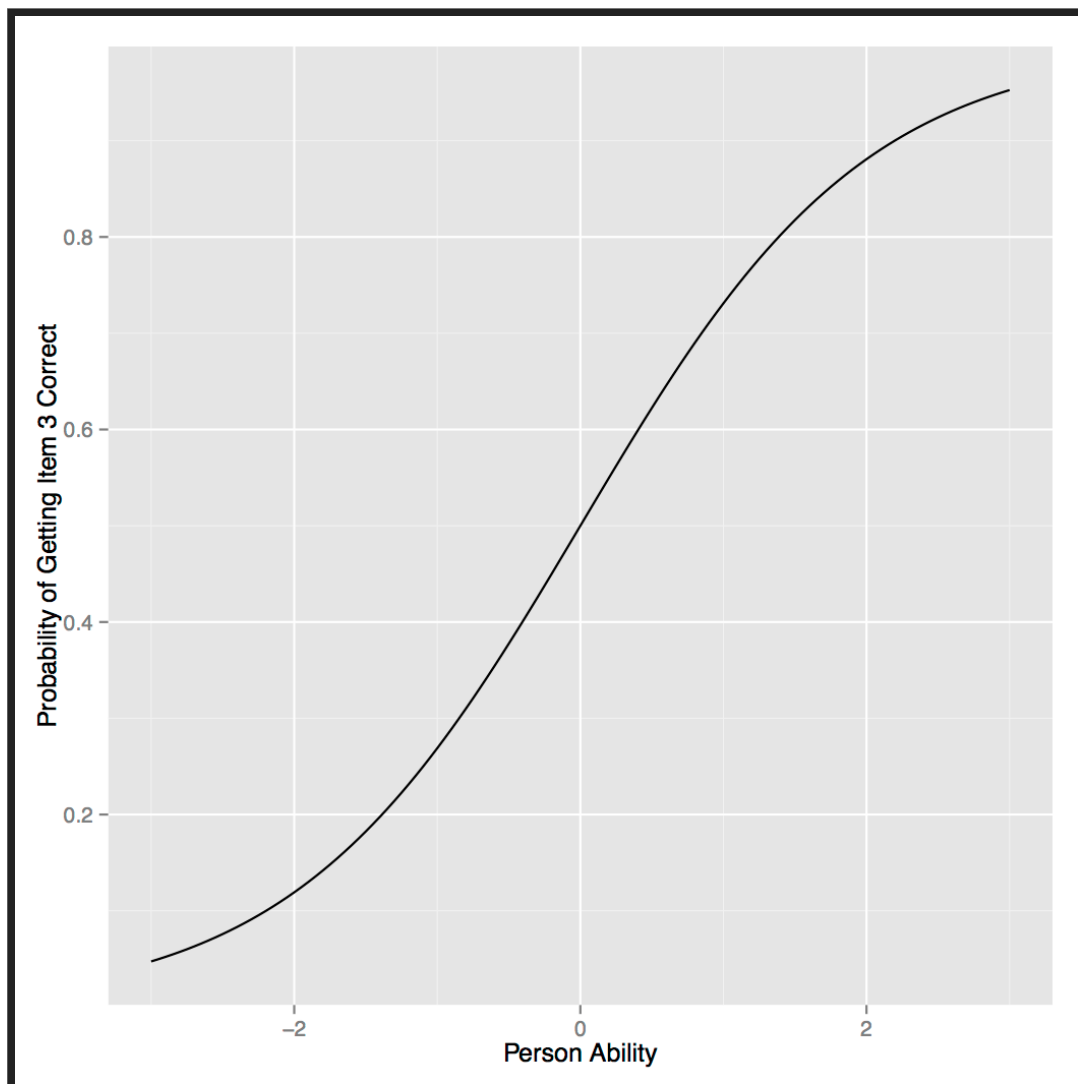
OTHER TRAITS OF IRT

- Use test information function for designing a test
- Has methods for examining item fit for identifying items that misfit
- Has methods for examining person fit for identifying persons that misfit
- Adaptive testing can be implemented (e.g. CAT)
- IRT is a family of models for various response types and could be used with multidimensional data.

IRT CONCEPTUALLY



ITEM RESPONSE FUNCTION (IRF)



THE RASCH MODEL

WHAT DOES $\theta - b_j$ MEAN

```
rasch <- function(person, item) {  
  exp(person - item) / (1 + exp(person - item))  
}  
rasch(person = 1, item = 1.5)  
# [1] 0.3775407  
  
rasch(person = 1, item = 1)  
# [1] 0.5
```


<https://lundinn.shinyapps.io/rasch>

shinyapps.io

<https://lundinn.shinyapps.io/twoopl>

shinyapps.io

<https://lundinn.shinyapps.io/threepl>

shinyapps.io

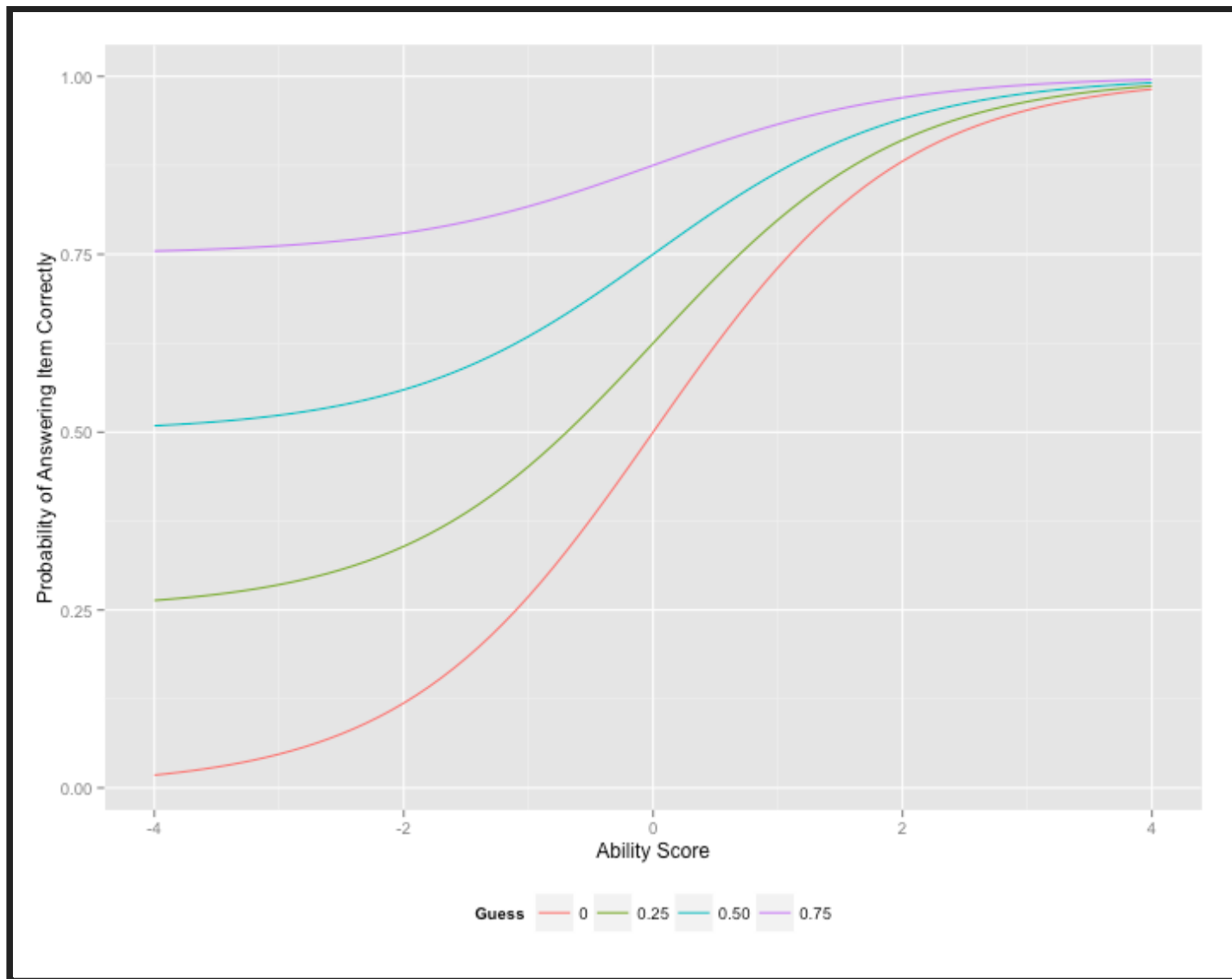
GETTING ITEM CORRECT RECAP

For the 1-PL and the Rasch, the probability of getting an item correct is a function of the distance an item is located from a person.

For the 2-PL, this is also a function of how well the item differentiates among people at different locations.

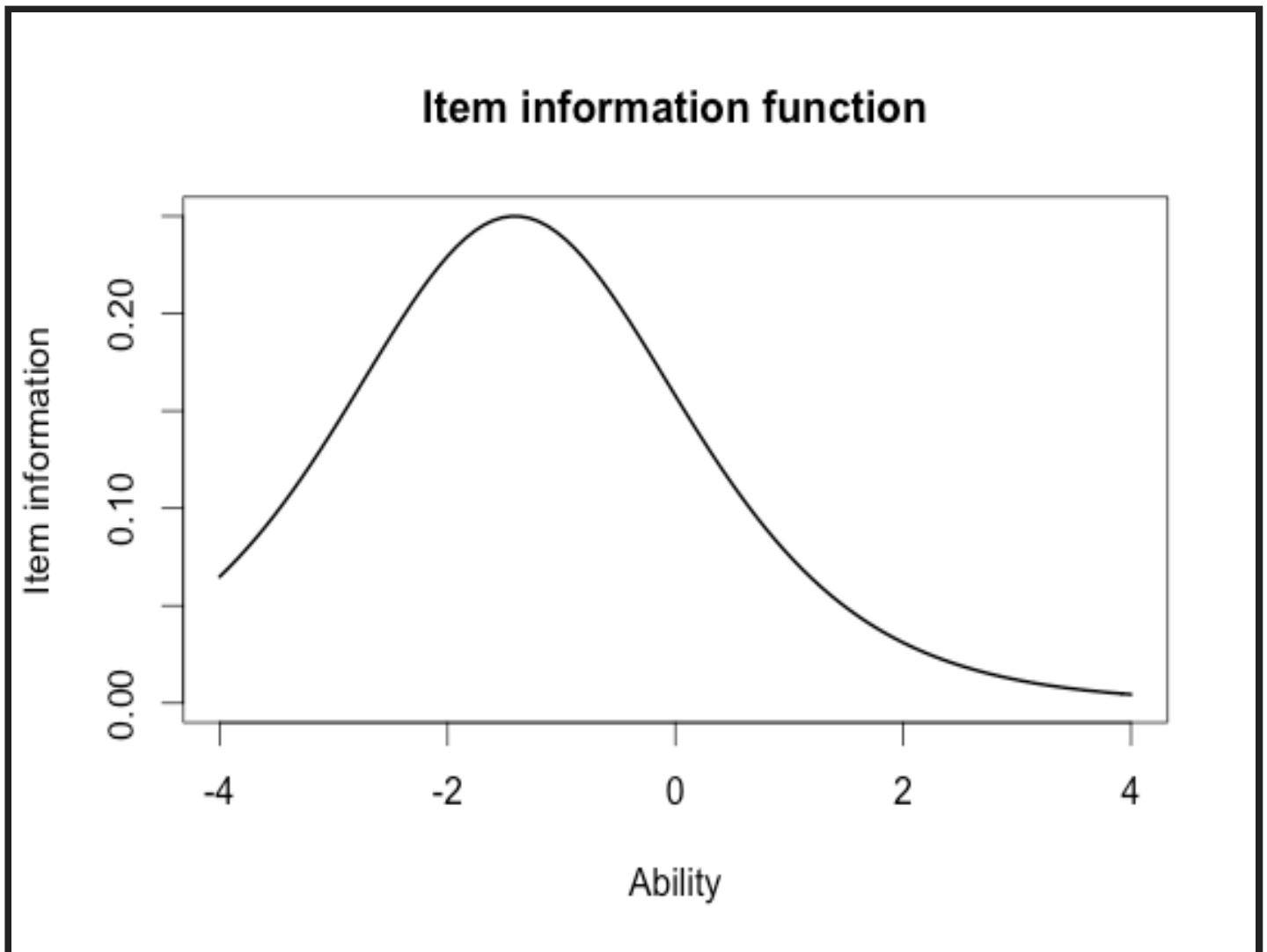
For the 3-PL, include item difficulty, item discrimination, and guessing

GUESSING PARAMETER



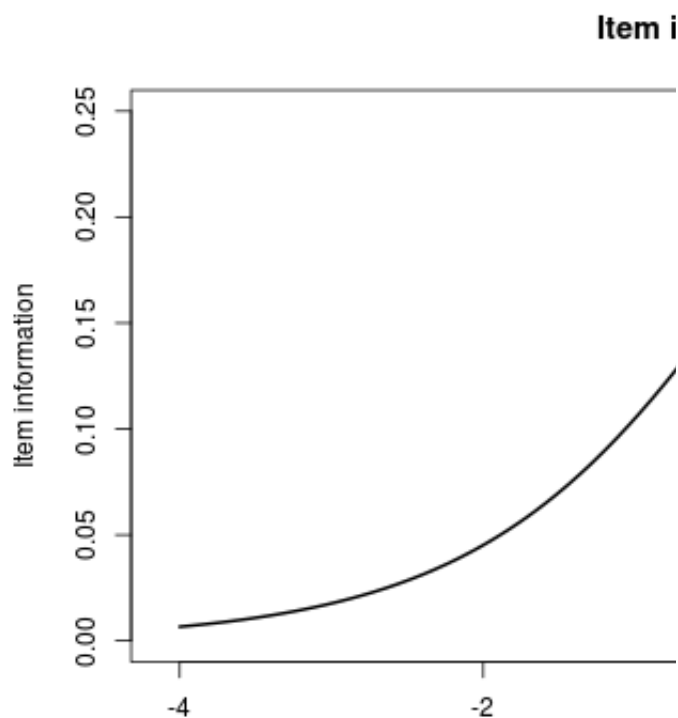
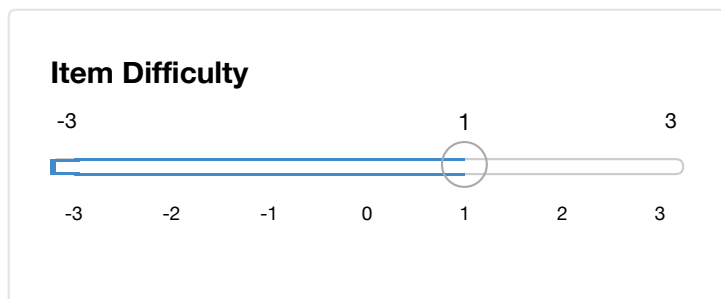
STANDARD ERROR OF ESTIMATE AND INFORMATION

ITEM INFORMATION FUNCTION



http://130.208.71.121:3838/rasch_informati

Rasch Information



http://130.208.71.121:3838/twoopl_informati

2PL IRT information

Item Difficulty

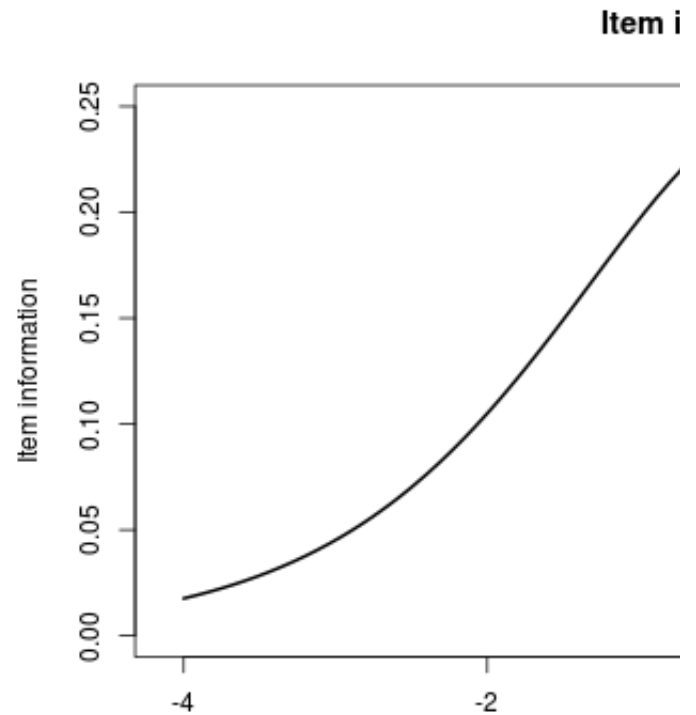
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Item Discrimination

1

3

1 1.2 1.4 1.6 1.8 2 2.2 2.4 2.6 2.8 3



http://130.208.71.121:3838/threepl_informa

3PL IRT model

Item Difficulty

0 ▼

Item Discrimination

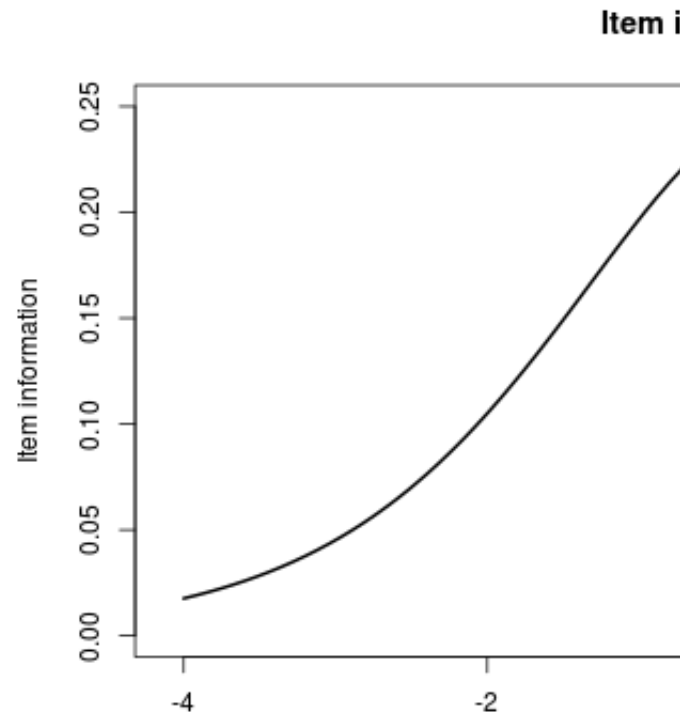
1 3

1 1.2 1.4 1.6 1.8 2 2.2 2.4 2.6 2.8 3

Guessing

0 1

0 0.25 0.5 0.75 1



TEST INFORMATION FUNCTION

