

X : Anzahl der Kinder pro Familie

$$\begin{aligned}
 a-) \quad \bar{x} &= \frac{1}{n} \sum_{i=1}^n x_i = \frac{1}{135} \left[5 \times 1 + 21 \times 2 + 46 \times 3 + 32 \times 4 + 11 \times 5 + 20 \times 6 \right] \cdot \frac{10^3}{10^3} \\
 &\quad \uparrow \\
 &\quad (16.5) \\
 &\quad 5.184 \\
 &= \frac{488}{135} \\
 \bar{x} &= 3,615
 \end{aligned}$$

$$b-) \text{ Stichprobenvarianz: } s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\begin{aligned}
 s^2 &= \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 \\
 &= \frac{1}{135 \cdot 10^3 - 1} \left[5(1 - \bar{x})^2 + 21(2 - \bar{x})^2 + 46(3 - \bar{x})^2 + 32(4 - \bar{x})^2 + 11(5 - \bar{x})^2 + 20(6 - \bar{x})^2 \right] \\
 &= \frac{1}{134,999} \cdot \frac{10^3}{10^3} \left[5(1 - \bar{x})^2 + 21(2 - \bar{x})^2 + 46(3 - \bar{x})^2 + 32(4 - \bar{x})^2 + 11(5 - \bar{x})^2 + 20(6 - \bar{x})^2 \right]
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{1}{134,999} (245,970) = 1,822 \\
 &\quad \uparrow \\
 &\quad \bar{x} = 3,615
 \end{aligned}$$

$$s^2 = 1,822$$