Math 30b Orrison Logarithms, Exponentials, and Approximations Friday, October 2, 2015

18.{1.ii, 1.iv, 1.vi, 1.x, 5.ii, 5.iv, 5.vi, 8.b, 8.d, 8.f}, 20.{1.ii, 1.iv, 1.vi, 2.ii, 2.iv}

18.1.ii

Differentiate

$$f(x) = \log \left(1 + \log \left(1 + \log \left(1 + e^{1 + e^{1 + x}}\right)\right)\right).$$

18.1.iv

Differentiate

$$f(x) = e^{\left(\int_0^x e^{-t^2} dt\right)}.$$

18.1.vi

Differentiate

$$f(x) = \log_{e^x} \sin x.$$

18.1.x

Differentiate

$$f\left(x\right) =x^{x}.$$

18.5.ii

Find the following limit by l'Hopital's Rule.

$$\lim_{x \to 0} \frac{e^x - 1 - x - x^2/2 - x^3/6}{x^3}.$$

18.5.iv

Find the following limit by l'Hopital's Rule.

$$\lim_{x \to 0} \frac{\log(1+x) - x + x^2/2}{x^2}.$$

18.5.vi

Find the following limit by l'Hopital's Rule.

$$\lim_{x \to 0} \frac{\log(1+x) - x + x^2/2 - x^3/3}{x^3}.$$

18.8.b

Prove that

$$\tanh^2 + \frac{1}{\cosh^2} = 1.$$

18.8.d

Prove that

$$\cosh(x+y) = \cosh x \cosh y + \sinh x \sinh y.$$

18.8.f

Prove that

$$\cosh' = \sinh.$$

20.1.ii

Find the Taylor polynomials (of the indicated degree, at the indicated point) for

$$f(x) = e^{e^x}$$
; degree 3, at 0.

20.1.iv

Find the Taylor polynomials (of the indicated degree, at the indicated point) for \cos ; degree 2n, at π .

20.1.vi

Find the Taylor polynomials (of the indicated degree, at the indicated point) for \log ; degree n, at 2.

20.2.ii

Write the following polynomial in x as a polynomial in (x - 3):

$$x^4 - 12x^3 + 44x^2 + 2x + 1.$$

20.2.iv

Write the following polynomial in x as a polynomial in (x - 3):

$$a^2 + bx + c.$$