Math 30b Orrison Double and Triple Integrals Tuesday, October 13, 2015

 $1.\{a,b\}, 2.\{a,b\}, 3.\{a,b\}, 4.\{a,b\}, 5\{a,b\}$

1.a

Evaluate the following:

$$\int_0^1 \int_{\sqrt{x}}^1 24x^2y \, dy \, dx$$

1.b

Evaluate the following:

$$\int_0^\pi \int_0^y \sin(x) \, dx \, dy$$

2.a

Evaluate the following:

 $\iint_{R} (6x + 24y) \, dA$, where *R* is the region bounded by y = x/2, y = 0, and x = 2.

2.b

Evaluate the following:

 $\iint_R 4x \, dA$, where *R* is the region bounded by $y = \ln x$, y = 0, and x = 2.

3.a

Use double integrals to find the area of the following regions:

the region bounded by $x = y - y^2$ and x + y = 0

.

3.b

Use double integrals to find the area of the following regions:

the region in the first quadrant bounded by y = 2x - 4 and $8y = 16 + x^2$

4.a

Express the following as iterated double integrals with the opposite order of integration and then evaluate:

$$\int_0^4 \int_{x/2}^2 e^{y^2} \, dy \, dx$$

4.b

Express the following as iterated double integrals with the opposite order of integration and then evaluate:

$$\int_0^2 \int_{x^2}^{2x} xy \, dy \, dx$$

5.a

Use triple integrals to find the following: the mass of the solid in the first octant that is bounded by

$$z = y/2$$
, $x = 3$, $y = 4$ where the density is given by $\rho(x, y, z) = 4y$

5.b

Use triple integrals to find the following: the mass of the solid in the first octant that is bounded by

$$z = 2 - y$$
, $x = 3$ where the density is given by $\rho(x, y, z) = z$