

1. {a,b,c}, 2. {a,b,c}, 3. {a,b,c}, 4, 5

1.a

Find the matrix Df of partial derivatives for the following function:

$$f(x, y) = \langle e^x, e^y, e^{\cos x} \rangle$$

■

1.b

Find the matrix Df of partial derivatives for the following function:

$$f(x, y, z) = \langle x^2 e^{x+y}, \cos(x-y) \rangle$$

■

1.c

Find the matrix Df of partial derivatives for the following function:

$$f(x, y, z) = \left\langle xy, \frac{x}{1+y^2}, e^{xy} \right\rangle$$

■

2.a

Find $\frac{\partial f}{\partial s}$ and $\frac{\partial f}{\partial t}$ for the following function in two ways: first use substitution, then use the chain rule:

$$f(x, y) = \sin(xy) \text{ where } x = s + t \text{ and } y = s^2 + t^2$$

■

2.b

Find $\frac{\partial f}{\partial s}$ and $\frac{\partial f}{\partial t}$ for the following function in two ways: first use substitution, then use the chain rule:

$$f(x, y) = e^{xy} \text{ where } x = \sin t \text{ and } y = e^{st}$$

2.c

Find $\frac{\partial f}{\partial s}$ and $\frac{\partial f}{\partial t}$ for the following function in two ways: first use substitution, then use the chain rule:

$$f(x, y, z) = \cos(xyz) \text{ where } x = st, y = st^2 \text{ and } z = st^3$$

3.a

Calculate $D(f \circ g)$ in two ways: first use substitution, then use the chain rule:

$$f(x, y) = x^2 - 7y^2 \text{ and } g(s, t) = \langle st^2, se^t \rangle$$

3.b

Calculate $D(f \circ g)$ in two ways: first use substitution, then use the chain rule:

$$f(x, y) = \langle xy - y^2, \cos x \rangle \text{ and } g(s, t) = \langle \frac{s}{t}, st \rangle$$

3.c

Calculate $D(f \circ g)$ in two ways: first use substitution, then use the chain rule:

$$f(x, y, z) = \langle e^x, e^{x+y}, e^{x+y+z} \rangle \text{ and } g(s, t) = \langle e^s, e^t, e^{s-t} \rangle$$

4

Suppose an insect flies along a helical curve $x = 2 \cos t$, $y = 2 \sin t$, $z = 3t$. If the barometric pressure is varying from point to point as $P(x, y, z) = 6x^2z/y$ atm, then use the chain rule to determine how the pressure is changing at the insects location when $t = \pi/4$ min.

5

Suppose $w = f\left(\frac{y-x}{xy}, \frac{z-x}{xz}\right)$ is a differentiable function of $u = \frac{y-x}{xy}$ and $v = \frac{z-x}{xz}$. Show that

$$x^2 \frac{\partial w}{\partial x} + y^2 \frac{\partial w}{\partial y} + z^2 \frac{\partial w}{\partial z} = 0.$$