## Tutorial 6 (Week 13, 30.6.2020) Microfluidics

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## Capillarity

Find the expression for the Young–Laplace pressure drop across a liquid/gas interface with surface tension coefficient  $\gamma$  inside a flat and very wide rectangular channel of height h, where the contact angle for the bottom and top plate are given by  $\theta_1$  and  $\theta_2$ , respectively.

## **Two-Phase Flow**

- 1. Derive the expressions for  $h_1$  and  $h_2$  for the two-phase Poiseuille flow in Chapter Two-Phase Flows (Two Phase Flows.ipynb). Discuss the limits of  $\mu_1 \to 0$  and  $\mu_2 \to \infty$  if they make sense.
- 2. The dispersion relation  $\omega(k)$  for gravity waves is given by Eq. (20) in Chapter Two-Phase Flows](Two Phase Flows.ipynb). Discuss the physical interpretation of this expression for  $\rho_1 > \rho_2$  and for  $\rho_1 < \rho_2$ . Does the finding relate with your experiences, if yes give examles. Hint: consider the time evolution using the complex notation  $e^{-i\omega t}$  for the time dependence.

## **Electrosmotic Flow**

Plot the electric potential and the flow profile for the electric osmotic flow in a infinitely long flow channel as a function of z. Start with the program in Chapter <u>Electrosomotic flow (Electrosomotic flow.ipynb</u>). Derive from Eq. (27) in Chapter <u>Electrosomotic flow (Electrosomotic flow.ipynb</u>) the flow rate Q through the thin channel.