2019 Boston College Summer School of Theoretical Condensed Matter Physics

Xiaodong Hu*
Department of Physics, Boston College
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In this paper I list a group of topics I am interested in and summarize related materials worth reading (still under construction). It plays a role of summer study plan to prevent myself from deviation of the main thread. Hopefully I can cover most of them after three months's study.

山无数, 乱红如雨, 不记来时路。

---- 秦观「点绛唇·桃源」

o 2D CFT

- ★ OPE to Renormalization Group (Wilson-Fisher and XY Model) [1, 2]
- \star Anomaly and Central Charge [3–5]
- ★ Kac-Moody Algebra and Edge Modes of FQHE [6]

$\circ \ \mathbf{Quantum} \ \mathbf{Transport} \ \mathbf{Theory}$

- \star Bloch Theorem [4, 7, 8]
- * Luttinger's Gravitational Formulation on Thermal Transports [9, 10]
- ★ Low-energy Newton Cartan theory of Quantum Transports [11–14]
- * Lattice Theory of Quantum Transport [15]
- \star Topological Origin of Thermal Hall Effects [14–16]
- ★ Discussion on Energy Magnetization [10, 17, 18]
- * Semi-classical Treatment of Nonlinear Hall Response [19]
- * Magnon Thermal Hall Effect [20, 21]

o Lieb-Schulz-Mattis Theorem

- \star LSM theorem in (1+1)D [22]
- ★ LSM theorem in higher dimensions [23–25]

o Realization of Kitaev Model

- * Kitaev's Honeycomb Model [26]
- \star Honeycomb Iridates [27, 28]
- * Anyons and Unitary Modular Tensor Categories [26, 29]

o Advanced FQHE

- ★ Dirac Theory of Composite Fermions [30]
- ★ Hall Viscosity [31]
- ★ Low-energy Newton Cartan theory of FQHE [13, 32]

o Duality

- * Kramers-Wannier Duality and XY Duality [33–37]
- * Bosonic Particle-Vortex Duality [38, 39]
- ★ Fermionic Particle-Vortex Duality [30, 40–43]

^{*}Electronic address: xiaodong.hu@bc.edu

o Topological Insulators and Topological Superconductors

- \star Haldane Model [44–46]
- ★ Chern Insulators in Higher Dimensions [45]
- $\star \mathbb{Z}_2$ Invariant and Kane-Mele Model [44–46]
- ★ Vortex and Majorana Fermions [47, 48]
- * Topological Periodic Table [49, 50]

o Quantum Evalution

- * Lieb-Robinson Bounds [51, 52]
- ★ Equal-time Correlation [53]
- * Insensitivity to Twisted Boundary Conditions [54]

o Quantum Phase Transition

* Deconfined Quantum Critical Point [39, 55]

\circ TQFT

- ★ Chern-Simons Gauge Fields and K-matrix Theory of FQHE [56, 57]
- ★ Non-linear Sigma Model and WZW Model [58, 59]
- * Braiding Statistics [56, 60]

• Others Topics Discussed in Journal Club

* Paradox in Defining Bulk Quadrupole Moment [61]

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