

Initial
latent
state:

$$\underbrace{\begin{bmatrix} \text{ss_level} \\ \text{ss_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t_0)}(t_0) \sim \text{N} \left(\underbrace{\begin{bmatrix} -44.507 \\ 0.383 \end{bmatrix}}_{\text{TOMEANS}}, \underbrace{UcorSDtoCov \left\{ \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \right\}}_{\mathbf{Q}^*_{t0}} \right)$$

Deterministic
change:

$$\text{d} \underbrace{\begin{bmatrix} \text{ss_level} \\ \text{ss_velocity} \end{bmatrix}}_{\text{d}\boldsymbol{\eta}(t)}(t) = \left(\underbrace{\begin{bmatrix} 0 & 1 \\ -0.456 & -0.676 \end{bmatrix}}_{\mathbf{A}_{\text{DRIFT}}} \underbrace{\begin{bmatrix} \text{ss_level} \\ \text{ss_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)}(t) + \underbrace{\begin{bmatrix} 0 \\ 0 \end{bmatrix}}_{\mathbf{b}_{\text{CINT}}} \right) \text{d}t +$$

Random
change:

$$\underbrace{UcorSDtoChol \left\{ \begin{bmatrix} 0 & 0 \\ 0 & 31.233 \end{bmatrix} \right\}}_{\mathbf{G}_{\text{DIFFUSION}}} \text{d} \underbrace{\begin{bmatrix} W_1 \\ W_2 \end{bmatrix}}_{\text{d}\mathbf{W}(t)}(t)$$

Observations:

$$\underbrace{[\text{sunspots}]}_{\mathbf{Y}(t)}(t) = \underbrace{\begin{bmatrix} 1 & 0 \end{bmatrix}}_{\mathbf{\Lambda}_{\text{LAMBDA}}} \underbrace{\begin{bmatrix} \text{ss_level} \\ \text{ss_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)}(t) + \underbrace{[49.55]}_{\boldsymbol{\tau}_{\text{MANIFESTMEANS}}} +$$

Observation
noise:

$$\underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{\boldsymbol{\Theta}_{\text{MANIFESTVAR}}} + \underbrace{\begin{bmatrix} \epsilon_1 \end{bmatrix}}_{\boldsymbol{\epsilon}(t)}(t)$$

System noise
distribution per time
step: $\Delta[W_{j \in [1,2]}](t-u) \sim \text{N}(0, t-u)$

Observation noise
distribution: $[\epsilon_{j \in [1,2]}](t) \sim \text{N}(0, 1)$

Note: *UcorSDtoChol* converts lower tri matrix of standard deviations and unconstrained correlations to Cholesky factor, *UcorSDtoCov* = transposed cross product of UcorSDtoChol, to give covariance, See Driver & Voelkle (2018) p11.