

$$\text{Initial latent states: } \underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t_0)} (t_0) \sim \text{N} \left( \underbrace{\begin{bmatrix} \text{T0m\_ss\_level} \\ \text{T0m\_ss\_velocity} \end{bmatrix}}_{\text{T0MEANS}}, \underbrace{\text{covsdcor} \left\{ \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \right\}}_{\substack{\mathbf{Q}^*_{t_0} \\ \text{T0VAR}}} \right)$$

$$\text{Deterministic change: } \underbrace{\text{d} \begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\text{d}\boldsymbol{\eta}(t)} (t) = \left( \underbrace{\begin{bmatrix} 0 & 1 \\ \text{a21} & \text{a22} \end{bmatrix}}_{\substack{\mathbf{A} \\ \text{DRIFT}}} \underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)} (t) + \underbrace{\begin{bmatrix} 0 \\ 0 \end{bmatrix}}_{\substack{\mathbf{b} \\ \text{CINT}}} \right) dt +$$

$$\text{Random change: } \underbrace{\text{cholsdcor} \left\{ \begin{bmatrix} 0 & 0 \\ 0 & \text{diffusion} \end{bmatrix} \right\}}_{\substack{\mathbf{G} \\ \text{DIFFUSION}}} \underbrace{\text{d} \begin{bmatrix} W_1 \\ W_2 \end{bmatrix}}_{\text{d}\mathbf{W}(t)} (t)$$

$$\text{Observations: } \underbrace{\begin{bmatrix} \text{sunspots} \end{bmatrix}}_{\mathbf{Y}(t)} (t) = \underbrace{\begin{bmatrix} 1 & 0 \end{bmatrix}}_{\substack{\mathbf{\Lambda} \\ \text{LAMBDA}}} \underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)} (t) + \underbrace{\begin{bmatrix} \text{m1} \end{bmatrix}}_{\substack{\boldsymbol{\tau} \\ \text{MANIFESTMEANS}}} + \underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{\substack{\boldsymbol{\Theta} \\ \text{MANIFESTVAR}}} \underbrace{\begin{bmatrix} \epsilon_1 \end{bmatrix}}_{\boldsymbol{\epsilon}(t)} (t)$$

Latent noise per time step :  $\Delta[W_{j \in [1,2]}](t-u) \sim \text{N}(0, t-u)$  Observation noise:  $[\epsilon_{j \in [1,2]}](t) \sim \text{N}(0, 1)$

*cholsdcor* converts lower tri matrix of std dev and unconstrained correlation to Cholesky factor covariance.

*covsdcor* = transposed cross product of *cholsdcor*, to give covariance.

See Driver & Voelke (2018) p11.