

$$\text{Subject parameter distribution: } \underbrace{\begin{bmatrix} \text{T0m_etal}_i \\ \text{cint}_i \\ \text{drift_etal}_i \\ \text{diff_etal}_i \\ \text{mvarYobs}_i \\ \text{T0var_etal}_i \end{bmatrix}}_{\phi(i)} \sim \text{tform} \left\{ \text{N} \left(\begin{bmatrix} \text{raw_T0m_etal} \\ \text{raw_cint} \\ \text{raw_drift_etal} \\ \text{raw_diff_etal} \\ \text{raw_mvarYobs} \\ \text{raw_T0var_etal} \end{bmatrix}, \begin{bmatrix} \text{rawPCov_1.1} & \text{rawPCov_2.1} & 0 & 0 & 0 & 0 \\ \text{rawPCov_2.1} & \text{rawPCov_2.2} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \right) + \underbrace{\begin{bmatrix} \text{raw_T0m_etal_Cohort2} & \text{raw_T0m_etal_Cohort3} & \text{raw_T0m_etal_Cohort4} \\ \text{raw_cint_Cohort2} & \text{raw_cint_Cohort3} & \text{raw_cint_Cohort4} \\ \text{raw_drift_etal_Cohort2} & \text{raw_drift_etal_Cohort3} & \text{raw_drift_etal_Cohort4} \\ \text{raw_diff_etal_Cohort2} & \text{raw_diff_etal_Cohort3} & \text{raw_diff_etal_Cohort4} \\ \text{raw_mvarYobs_Cohort2} & \text{raw_mvarYobs_Cohort3} & \text{raw_mvarYobs_Cohort4} \\ \text{raw_T0var_etal_Cohort2} & \text{raw_T0var_etal_Cohort3} & \text{raw_T0var_etal_Cohort4} \end{bmatrix}}_{\beta} \underbrace{\begin{bmatrix} \text{Cohort2} \\ \text{Cohort3} \\ \text{Cohort4} \end{bmatrix}}_{\mathbf{z}} \right\}$$

$$\text{Initial latent state: } \underbrace{[\text{etal}]}_{\boldsymbol{\eta}(t_0)}(t_0) \sim \text{N} \left(\underbrace{[\text{T0m_etal}]}_{\text{T0MEANS}}, \underbrace{U\text{corSDtoCov} \{ [0.001] \}}_{\text{Q}^*_{t_0} \text{ T0VAR}} \right)$$

$$\text{Deterministic change: } \text{d} \underbrace{[\text{etal}]}_{\text{d}\boldsymbol{\eta}(t)}(t) = \left(\underbrace{[\text{drift_etal}]}_{\mathbf{A} \text{ DRIFT}} \underbrace{[\text{etal}]}_{\boldsymbol{\eta}(t)}(t) + \underbrace{[\text{cint}]}_{\mathbf{b} \text{ CINT}} \right) \text{d}t +$$

$$\text{Random change: } \underbrace{U\text{corSDtoChol} \{ [\text{diff_etal}] \}}_{\mathbf{G} \text{ DIFFUSION}} \text{d} \underbrace{[W_1]}_{\text{d}\mathbf{W}(t)}(t)$$

$$\text{Observations: } \underbrace{[\text{Yobs}]}_{\mathbf{Y}(t)}(t) = \underbrace{[1]}_{\mathbf{\Lambda} \text{ LAMBDA}} \underbrace{[\text{etal}]}_{\boldsymbol{\eta}(t)}(t) + \underbrace{[0]}_{\boldsymbol{\tau} \text{ MANIFESTMEANS}} +$$

$$\text{Observation noise: } \underbrace{[\text{mvarYobs}]}_{\boldsymbol{\Theta} \text{ MANIFESTVAR}} \underbrace{[\epsilon_1]}_{\boldsymbol{\epsilon}(t)}(t)$$

$$\text{System noise distribution per time step: } \Delta[W_{j \in [1,1]}](t-u) \sim \text{N}(0, t-u) \quad \text{Observation noise distribution: } [\epsilon_{j \in [1,1]}](t) \sim \text{N}(0, 1)$$

Note: *UcorSDtoChol* converts lower tri matrix of standard deviations and unconstrained correlations to Cholesky factor, *UcorSDtoCov* = transposed cross product of *UcorSDtoChol*, to give covariance, See Driver & Voelkle (2018) p11.
Individual specific notation (subscript i) only shown for subject parameter distribution – pop. means shown elsewhere.