

Subject parameter distribution: $\underbrace{\begin{bmatrix} \text{T0m_eta1}_i \\ \text{slope}_i \end{bmatrix}}_{\phi(i)} \sim \text{tform} \left\{ \text{N} \left(\begin{bmatrix} \text{raw_T0m_eta1} \\ \text{raw_slope} \end{bmatrix}, \begin{bmatrix} \text{raw_PCov_1.1} & \text{raw_PCov_2.1} \\ \text{raw_PCov_2.1} & \text{raw_PCov_2.2} \end{bmatrix} \right) \right\}$

Initial latent states: $\underbrace{[\text{eta1}]}_{\eta(t_0)}(t_0) \sim \text{N} \left(\underbrace{[\text{T0m_eta1}]}_{\text{T0MEANS}}, \underbrace{\text{covsdcor} \{ [\text{Pcorsqrt_1.1}] \}}_{\underbrace{\mathbf{Q}^*_{t_0}}_{\text{T0VAR}}} \right)$

Deterministic change: $\underbrace{d[\text{eta1}]}_{d\eta(t)}(t) = \begin{pmatrix} \underbrace{[0]}_{\underbrace{\mathbf{A}}_{\text{DRIFT}}} \underbrace{[\text{eta1}]}_{\eta(t)}(t) + \underbrace{[\text{slope}]}_{\underbrace{\mathbf{b}}_{\text{CINT}}} \end{pmatrix} dt +$

Random change: $\underbrace{\text{cholsdcor} \{ [0] \}}_{\underbrace{\mathbf{G}}_{\text{DIFFUSION}}} d \underbrace{[W_1]}_{d\mathbf{W}(t)}(t)$

Observations: $\underbrace{[y1]}_{\mathbf{Y}(t)}(t) = \underbrace{[1]}_{\underbrace{\mathbf{\Lambda}}_{\text{LAMBDA}}} \underbrace{[\text{eta1}]}_{\eta(t)}(t) + \underbrace{[0]}_{\underbrace{\boldsymbol{\tau}}_{\text{MANIFESTMEANS}}} + \underbrace{[\log 1p(\exp(\text{errorsd.intercept} + \text{errorsd.byeta1} * \text{eta1}))]}_{\underbrace{\boldsymbol{\Theta}}_{\text{MANIFESTVAR}}} \underbrace{[\epsilon_1]}_{\epsilon(t)}(t)$

Latent noise per time step : $\Delta[W_{j \in [1,1]}](t-u) \sim \text{N}(0, t-u)$ Observation noise: $[\epsilon_{j \in [1,1]}](t) \sim \text{N}(0, 1)$

cholsdcor converts lower tri matrix of std dev and unconstrained correlation to Cholesky factor covariance.

covsdcor = transposed cross product of *cholsdcor*, to give covariance.

See Driver & Voelke (2018) p11.