

Initial  
latent  
state:

$$\underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t_0)}(t_0) \sim \text{N} \left( \underbrace{\begin{bmatrix} -44.799 \\ 1.034 \end{bmatrix}}_{\text{TOMEANS}}, \underbrace{\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}}_{\text{Q}^*_{t_0} \text{ TOVAR}} \right)$$

Deterministic  
change:

$$\underbrace{d \begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{d\boldsymbol{\eta}(t)}(t) = \left( \underbrace{\begin{bmatrix} 0 & 1 \\ -0.456 & -0.68 \end{bmatrix}}_{\mathbf{A} \text{ DRIFT}} \underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)}(t) + \underbrace{\begin{bmatrix} 0 \\ 0 \end{bmatrix}}_{\mathbf{b} \text{ CINT}} \right) dt +$$

Random  
change:

$$\underbrace{\text{cholstdcor} \left\{ \begin{bmatrix} 0 & 0 \\ 0 & 31.349 \end{bmatrix} \right\}}_{\mathbf{G} \text{ DIFFUSION}} d \underbrace{\begin{bmatrix} W_1 \\ W_2 \end{bmatrix}}_{d\mathbf{W}(t)}(t)$$

Observations:

$$\underbrace{\begin{bmatrix} \text{sunspots} \end{bmatrix}}_{\mathbf{Y}(t)}(t) = \underbrace{\begin{bmatrix} 1 & 0 \end{bmatrix}}_{\mathbf{\Lambda} \text{ LAMBDA}} \underbrace{\begin{bmatrix} \text{ss\_level} \\ \text{ss\_velocity} \end{bmatrix}}_{\boldsymbol{\eta}(t)}(t) + \underbrace{\begin{bmatrix} 49.759 \end{bmatrix}}_{\boldsymbol{\tau} \text{ MANIFESTMEANS}} + \underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{\boldsymbol{\Theta} \text{ MANIFESTVAR}} + \underbrace{\begin{bmatrix} \epsilon_1 \end{bmatrix}}_{\boldsymbol{\epsilon}(t)}(t)$$

Latent noise  
per time step:

$$\Delta[W_{j \in [1,2]}](t-u) \sim \text{N}(0, t-u)$$

Observation  
noise:

$$[\epsilon_{j \in [1,2]}](t) \sim \text{N}(0, 1)$$

*cholstdcor* converts lower tri matrix of std dev and unconstrained correlation to Cholesky factor covariance.

*covstdcor* = transposed cross product of *cholstdcor*, to give covariance.

See Driver & Voelkle (2018) p11.