

$$\text{Subject parameter distribution: } \underbrace{\begin{bmatrix} \text{T0m_eta1}_i \\ \text{slope}_i \end{bmatrix}}_{\phi(i)} \sim \text{tform} \left\{ \text{N} \left(\begin{bmatrix} \text{raw_T0m_eta1} \\ \text{raw_slope} \end{bmatrix}, \begin{bmatrix} \text{rawPCov.1.1} & \text{rawPCov.2.1} \\ \text{rawPCov.2.1} & \text{rawPCov.2.2} \end{bmatrix} \right) \right\}$$

$$\text{Initial latent state: } \underbrace{\begin{bmatrix} \text{eta1} \end{bmatrix} (t_0)}_{\eta(t_0)} \sim \text{N} \left(\underbrace{\begin{bmatrix} \text{T0m_eta1} \end{bmatrix}}_{\text{T0MEANS}}, \underbrace{\text{covsdcor} \{ \begin{bmatrix} \text{Pcorsqrt.1.1} \end{bmatrix} \}}_{\underbrace{\mathbf{Q}^*}_{\text{T0VAR}}}_{t_0} \right)$$

$$\text{Deterministic change: } \underbrace{\text{d} \begin{bmatrix} \text{eta1} \end{bmatrix} (t)}_{\text{d}\eta(t)} = \left(\underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{\mathbf{A}_{\text{DRIFT}}} \underbrace{\begin{bmatrix} \text{eta1} \end{bmatrix} (t)}_{\eta(t)} + \underbrace{\begin{bmatrix} \text{slope} \end{bmatrix}}_{\mathbf{b}_{\text{CINT}}} \right) \text{d}t +$$

$$\text{Random change: } \underbrace{\text{cholsdcor} \{ \begin{bmatrix} 0 \end{bmatrix} \}}_{\mathbf{G}_{\text{DIFFUSION}}} \underbrace{\text{d} \begin{bmatrix} W_1 \end{bmatrix} (t)}_{\text{d}\mathbf{W}(t)}$$

$$\text{Observations: } \underbrace{\begin{bmatrix} y1 \end{bmatrix} (t)}_{\mathbf{Y}(t)} = \underbrace{\begin{bmatrix} 1 \end{bmatrix}}_{\mathbf{\Lambda}_{\text{LAMBDA}}} \underbrace{\begin{bmatrix} \text{eta1} \end{bmatrix} (t)}_{\eta(t)} + \underbrace{\begin{bmatrix} 0 \end{bmatrix}}_{\boldsymbol{\tau}_{\text{MANIFESTMEANS}}} + \underbrace{\left[\log 1\text{p_exp}(\text{errorsd_intercept} + \text{errorsd_byeta1} * \text{eta1}) \right]}_{\boldsymbol{\Theta}_{\text{MANIFESTVAR}}} \underbrace{\begin{bmatrix} \epsilon_1 \end{bmatrix} (t)}_{\boldsymbol{\epsilon}(t)}$$

$$\text{Latent noise per time step: } \Delta[W_{j \in [1,1]}](t-u) \sim \text{N}(0, t-u)$$

$$\text{Observation noise: } [\epsilon_{j \in [1,1]}](t) \sim \text{N}(0, 1)$$

cholsdcor converts lower tri matrix of std dev and unconstrained correlation to Cholesky factor covariance.

covsdcor = transposed cross product of *cholsdcor*, to give covariance.

See Driver & Voelkle (2018) p11.